

# 1.1 Reglas de Derivación e Integración

| INTEGRALES INMEDIATAS   |                                |  | REGLAS DE DERIVACIÓN   |                                       |  |   |
|---|--------------------------------|--|--|---------------------------------------|--|---|
| 1. $\int du = u + C$<br>2. $\int u^n du = \frac{u^{n+1}}{n+1} + C, n \neq -1$<br>3. $\int u^{-1} du = \int \frac{du}{u} = \ln u  + C$<br>4. $\int a^u du = \frac{a^u}{\ln a} + C$<br>5. $\int e^u du = e^u + C$<br>6. $\int \sin u du = -\cos u + C$<br>7. $\int \cos u du = \sin u + C$<br>8. $\int \tan u du = \ln \sec u  + C$<br>9. $\int \sec^2 u du = \tan u + C$<br>10. $\int \csc^2 u du = -\cot u + C$<br>11. $\int \sec u \tan u du = \sec u + C$<br>12. $\int \csc u \cot u du = -\csc u + C$<br>13. $\int \cot u du = \ln \sin u  + C$<br>14. $\int \sec u du = \ln \sec u + \tan u  + C$<br>15. $\int \csc u du = \ln \csc u - \cot u  + C$<br>16. $\int \frac{du}{u^2 + a^2} = \frac{1}{a} \arctan \frac{u}{a} + C$<br>17. $\int \frac{du}{u^2 - a^2} = \frac{1}{2a} \ln \left  \frac{u-a}{u+a} \right  + C$<br>18. $\int \frac{du}{a^2 - u^2} = \frac{1}{2a} \ln \left  \frac{a+u}{a-u} \right  + C$ |                                |  | 1. $d(\ln u) = \frac{du}{u}$<br>2. $d(\log_a u) = \frac{du}{u \ln a}$<br>3. $d(e^u) = e^u du$<br>4. $d(a^u) = a^u \ln a du$<br>5. $d(\sin u) = \cos u du$<br>6. $d(\cos u) = -\sin u du$<br>7. $d(\tan u) = \sec^2 u du$<br>8. $d(\cot u) = -\csc^2 u du$<br>9. $d(\sec u) = \sec u \tan u du$<br>10. $d(\csc u) = -\csc u \cot u du$<br>11. $d(\arcsin u) = \frac{du}{\sqrt{1-u^2}}$<br>12. $d(\arccos u) = -\frac{du}{\sqrt{1-u^2}}$<br>13. $d(\arctan u) = \frac{du}{1+u^2}$<br>14. $d(\operatorname{arccot} u) = -\frac{du}{1+u^2}$<br>15. $d(\operatorname{arcsec} u) = \frac{du}{u\sqrt{u^2-1}}$<br>16. $d(\operatorname{arccsc} u) = -\frac{du}{u\sqrt{u^2-1}}$ |                                       |  |   |
| LEYES DE LOS EXPONENTES   |                                |  | IDENTIDADES TRIGONOMÉTRICAS  |                                       |  |   |
| $a^m \cdot a^n = a^{m+n}$   |                                |  | $\cos^2 x = 1 - \sin^2 x$  |                                       | $\sin^2 x = 1 - \cos^2 x$                      |   |
| $\frac{a^m}{a^n} = a^{m-n}$   | $(a^m)^n = a^{mn}$             | $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$ | $\sin^2 x = \frac{1}{2} - \frac{1}{2} \cos 2x$   |                                       | $\cos^2 x = \frac{1}{2} + \frac{1}{2} \cos 2x$ |   |
| $a^{-n} = \frac{1}{a^n}$  |                                | $\sqrt[n]{a^m} = a^{m/n}$                      | $\sin^2 x + \cos^2 x = 1$  |                                       | $\sin x \cos x = \frac{1}{2} \sin 2x$          |   |
| TRIGONOMETRÍA   |                                |  | $\sin 2x = 2 \sin x \cos x$  |                                       | $\cos 2x = 2 \cos^2 x - 1$                     |   |
| $\sin \theta = \frac{C.O.}{H}$  | $\cos \theta = \frac{C.A.}{H}$ | $\tan \theta = \frac{C.O.}{C.A.}$              | $\sec^2 \theta = 1 + \tan^2 \theta$  |                                       | $\tan^2 \theta = \sec^2 \theta - 1$            |   |
| $\csc \theta = \frac{H}{C.O.}$  | $\sec \theta = \frac{H}{C.A.}$ | $\cot \theta = \frac{C.A.}{C.O.}$              | $\cot^2 \theta = \csc^2 \theta - 1$  |                                       | $\csc^2 \theta = \cot^2 \theta + 1$            |   |
| $\int u dv = uv - \int v du$<br>(“Un día ví una vaca sin cola vestida de uniforme”)   |                                |  | $\csc \theta = \frac{1}{\sin \theta}$  | $\sec \theta = \frac{1}{\cos \theta}$ | $\cot \theta = \frac{1}{\tan \theta}$          | $\tan \theta = \frac{\sin \theta}{\cos \theta}$ |