

Your Name: Key

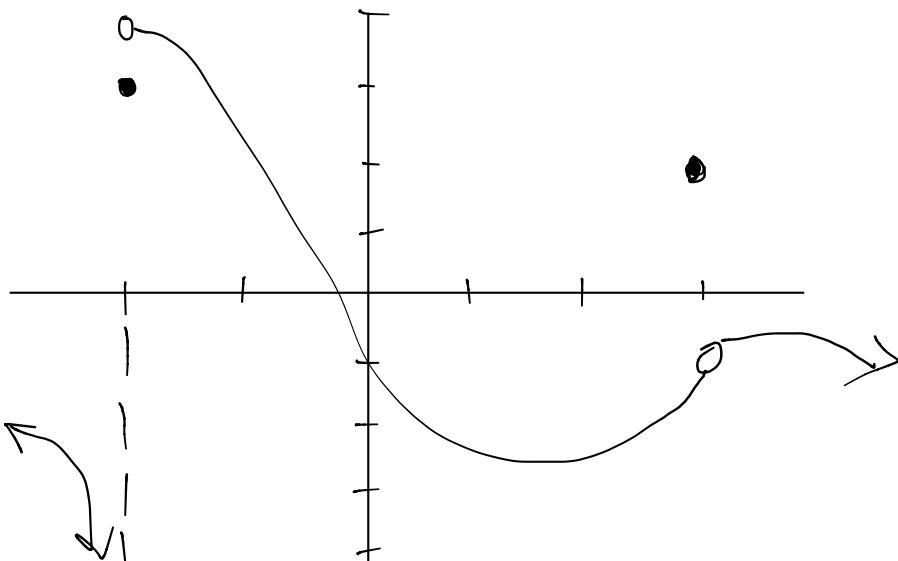
Calculus I, Math 151-06, Quiz #1

1. [11 points total]

- (a) [7 points] Sketch a graph of a function $f(x)$ which has all of the following properties:

$$\lim_{x \rightarrow -2^-} f(x) = -\infty \quad \lim_{x \rightarrow -2^+} f(x) = 4 \quad f(-2) = 3$$

$$\lim_{x \rightarrow 3^-} f(x) = -1 \quad \lim_{x \rightarrow 3^+} f(x) = -1 \quad f(3) = 2$$



- (b) [4 points] Evaluate $\lim_{x \rightarrow -2} f(x)$ and $\lim_{x \rightarrow 3} f(x)$.

$$\lim_{x \rightarrow -2} f(x) \text{ DNE}.$$

$$\lim_{x \rightarrow 3} f(x) = -1.$$

2. [14 points total] Evaluate the following limits.

$$\begin{aligned}
 \text{(a) [6 points]} \quad & \lim_{t \rightarrow -1} \frac{\sqrt{3-t} - 2}{t+1} = \frac{\sqrt{4} - 2}{-1+1} = \frac{0}{0} \\
 & = \lim_{t \rightarrow -1} \frac{(\sqrt{3-t} - 2)(\sqrt{3-t} + 2)}{(t+1)(\sqrt{3-t} + 2)} = \lim_{t \rightarrow -1} \frac{3-t-4}{(t+1)(\sqrt{3-t} + 2)} = \lim_{t \rightarrow -1} \frac{-t-1}{(t+1)(\sqrt{3-t} + 2)} \\
 & = \lim_{t \rightarrow -1} \frac{-1(t+1)}{(t+1)(\sqrt{3-t} + 2)} = \lim_{t \rightarrow -1} \frac{-1}{\sqrt{3-t} + 2} = \frac{-1}{\sqrt{4} + 2} = \boxed{\frac{-1}{4}}
 \end{aligned}$$

$$\text{(b) [8 points]} \quad \lim_{h \rightarrow 0} \frac{f(4+h) - f(4)}{h}, \text{ where } f(x) = \frac{2}{x}.$$

$$\begin{aligned}
 & = \lim_{h \rightarrow 0} \frac{\frac{2}{4+h} - \frac{2}{4}}{h} = \frac{\frac{2}{4} - \frac{2}{4}}{0} = \frac{0}{0} \\
 & = \lim_{h \rightarrow 0} \frac{\frac{2(4)}{(4+h)(4)} - \frac{2(4+h)}{(4+h)(4)}}{h} = \lim_{h \rightarrow 0} \frac{\frac{8}{4h+16} - \frac{8+2h}{4h+16}}{h} = \lim_{h \rightarrow 0} \frac{\frac{-2h}{4h+16}}{h/1} \\
 & = \lim_{h \rightarrow 0} \frac{-2h}{4h+16} \cdot \frac{1}{h} = \lim_{h \rightarrow 0} \frac{-2}{4h+16} = \frac{-2}{16} = \boxed{\frac{-1}{8}}
 \end{aligned}$$