

## CS345 Fall 2012 - Homework Assignment # 1

Due Thursday, September 13, 2012 by 5:00 pm. Use turnin to submit your homework (i.e., turnin –submit [MW use swati, TTh use bs2827] cs345\_hw1 lambda.pdf)

1. [2 Points] In Section 22 of DeLong (pages 152 - 160), Howard defines multiplication recursively in a manner similar to what was shown in class for addition. Write this definition of multiplication in relation notation and show that  $2 \times 3 = 6$  using this relation notation. (You can use the Pd function (DeLong, page 158) in your answer if it is useful).

Evaluate (beta-reduce) the  $\lambda$  expressions in problems 2 and 3 in a manner similar to the following example:

```
((λx.λy.(y x) λp.λq.p) λi.i)
(λy.(y λp.λq.p) λi.i)
(λi.i λp.λq.p)
λp.λq.p
```

2. [2 Points]  $((\lambda x.\lambda y.\lambda z.((x\ y)\ z)\ \lambda f.\lambda a.(f\ a))\ \lambda i.i)\ \lambda j.j)$
3. [2 Points]  $(\lambda h.((\lambda a.\lambda f.(f\ a)\ h)\ h)\ \lambda f.(f\ f))$
4. [2 Points] Use  $\alpha$  conversion to ensure unique names in the following expression:  $\lambda x.\lambda y.(\lambda x.y\ \lambda y.x)$

$X$	$Y$	$X \text{ implies } Y$
False	False	True
False	True	True
True	False	False
True	True	True

5. [2 Points] Define a  $\lambda$  calculus representation for *implies*. You should be able to reduce your answer down so that it's in terms of  $x$ , and  $y$  and maybe true, and/or false. Notice, when  $X$  is true, *Implies* is the same as  $Y$  and when  $X$  is False, *Implies* is True.