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### Homework 3

1. (5 points) A 2D triangle has vertices (0,0), (2,1), (1,1). What are the barycentric coordinates of the point (0.8,0.7)?

# Answer:

Let  $(\lambda_1, \lambda_2, \lambda_3)$  be the barycentric coordinate of the point (0.8, 0.7).

Then we have:

$$\lambda_1 * 0 + \lambda_2 * 2 + \lambda_3 * -1 = 0.8 \leftrightarrow \lambda_2 * 2 + \lambda_3 * -1 = 0.8$$

$$\lambda_1 * 0 + \lambda_2 * 1 + \lambda_3 * 1 = 0.7 \leftrightarrow \lambda_2 * 1 + \lambda_3 * 1 = 0.7$$

Solving this system of equations, we get:

$$\lambda_2 = 0.5$$

$$\lambda_3 = 0.2$$

Since 
$$\lambda_1 + \lambda_2 + \lambda_3 = 1$$
,  $\lambda_1 = 0.3$ 

The final answer is: (0.3, 0.5, 0.2)

2. (5 points) Suppose a triangle has the following RGB colors at its vertices: c0 = (1,0,0), c1 = (1,0.8,0.4), c2 = (0.6,0.3,0.9). Given a point with barycentric coordinates (0.2,0.5,0.3), what will the color be at that point using linear interpolation?

## Answer:

For RGB color, we can linearly interpolate the value of each component by weighing the value of the same component at each vertex by the corresponding barycentric coordinate.

In other words, at the point (0.2, 0.5, 0.3), we have:

$$R = 0.2 * 1 + 0.5 * 1 + 0.3 * 0.6 = 0.88$$

$$G = 0.2 * 0 + 0.5 * 0.8 + 0.3 * 0.3 = 0.49$$

$$B = 0.2 * 0 + 0.5 * 0.4 + 0.3 * 0.9 = 0.47$$

The final answer is: (0.88, 0.49, 0.47)

3. (5 points) Suppose a triangle has the following vertex normals: n0 = (1,0,0), c1 = (0,1,1), c2 = (2,1,0). Given a point with barycentric coordinates (0.2,0.5,0.3), what will the normal be at that point using linear interpolation?

#### Answer:

First we normalize the unnormalized normals:

$$n1 = c1/\sqrt{2} = (0, 1/\sqrt{2}, 1/\sqrt{2})$$

$$n2 = c2/\sqrt{5} = (2/\sqrt{5}, 1/\sqrt{5}, 0)$$

After that we weigh each normalized normal by each corresponding barycentric coordinate to get the normal at the point of interest.

Doing the weighing component-wise, the calculation is as follow:

$$x = 0.2 * 1 + 0.5 * 0 + 0.3 * 2/\sqrt{5} = 0.4683$$
$$y = 0.2 * 0 + 0.5 * 1/\sqrt{2} + 0.3 * 1/\sqrt{5} = 0.4877$$
$$z = 0.2 * 0 + 0.5 * 1/\sqrt{2} + 0.3 * 0 = 0.3536$$

The final answer is: (0.4683, 0.4877, 0.3536)

4. A light source located at (0,0,10) emits white light for specular, diffuse and ambient reflections. A triangle has vertices v0 = (0,0,0), v1 = (1,0,0), v2 = (1/2,1,0). Each vertex has an associated normal, which are n0 = (0,0,1), n1 = (0,0,1),  $n2 = (0,\sqrt{2}/2,\sqrt{2}/2)$ . The triangle has material properties kd = [1,0,0]', ks = [0,1,0]' and a specular coefficient of 10. A point p is located at barycentric coordinates (0.2,0.6,0.2) with respect to the triangle. The viewers eye is at (5,0,10).

Using the Phong reflection model and assuming no distance attenuation, answer the following questions. You may write code to solve the equations if you wish, but you must show all steps, including the values of the relevant vectors. Be sure to always normalize your vectors!

- (a) (5 points) What is the diffuse reflection term at vertex v1?
- (b) (5 points) What is the specular reflection term at vertex v1?
- (c) (5 points) Assuming phong reflection, what is the diffuse reflection term at point p?
- (d) (5 points) Assuming phong reflection, what is the specular reflection term at point p?
- (e) (5 points) If we move the light source very slightly up along the positive y axis, what will happen to the diffuse and specular terms for vertex v1? Why? You don't need to do the calculations, just describe what will happen.

#### Answer:

- 5. (5 points) Consider a texture that is square and is a smooth, linear gradient from red to green moving left to right. That is, all pixels (0, y) are red, all pixels (w1, y) are green (where w is the width of the texture), and all pixels in-between vary linearly in color. Give the color in RGB for the following texture coordinates.
  - (a) (0, 0.5)
  - (b) (0.5, 0.5)
  - (c) (0.75, 0.5)
  - (d) (0.75, 0.75)
- 6. (5 points) Consider the texture from the previous question. Let a triangle have vertices that have texture coordinates vt0 = (0,0), vt1 = (1,0), vt2 = (0.5,1). Let point p be at barycentric coordinates (0.5, 0.5, 0) with respect to the triangle. What is the color at p?