

A Universal Optimal Sizing for Hybrid Energy Storage System of Electric Vehicles

Appendix: Sizing result

1. Full-active configuration

| No. | n_{bat_s} | n_{bat_p} | n_{sc_s} | n_{sc_p} | RMS_{cell} [A] | Cost [USD] | HESS mass [kg] | HESS volume [m ³] |
|-----|--------------|--------------|-------------|-------------|---------------------|---------------|-------------------|----------------------------------|
| 1 | 58 | 57 | 64 | 1 | 0.774940 | 10846.2 | 250.2931 | 0.089988 |
| 2 | 65 | 51 | 61 | 1 | 0.774944 | 10780.5 | 250.6812 | 0.089984 |
| 3 | 62 | 54 | 50 | 1 | 0.776662 | 10539.6 | 252.1042 | 0.089969 |
| 4 | 62 | 53 | 50 | 1 | 0.789403 | 10372.2 | 247.5211 | 0.088376 |
| 5 | 60 | 54 | 50 | 1 | 0.798688 | 10248 | 244.1208 | 0.087193 |
| 6 | 60 | 53 | 55 | 1 | 0.807297 | 10236 | 240.1476 | 0.086043 |
| 7 | 57 | 55 | 54 | 1 | 0.817767 | 10084.5 | 236.7288 | 0.084808 |
| 8 | 70 | 45 | 50 | 1 | 0.818533 | 10005 | 237.4680 | 0.084880 |
| 9 | 61 | 51 | 49 | 1 | 0.827325 | 9869.7 | 234.4927 | 0.083800 |
| 10 | 60 | 51 | 50 | 1 | 0.838461 | 9762 | 230.8152 | 0.082567 |
| 11 | 57 | 53 | 49 | 1 | 0.848875 | 9626.7 | 227.8399 | 0.081486 |
| 12 | 62 | 48 | 49 | 1 | 0.859616 | 9505.2 | 224.5135 | 0.080330 |
| 13 | 61 | 48 | 49 | 1 | 0.871578 | 9375.6 | 220.9654 | 0.079096 |
| 14 | 59 | 49 | 49 | 1 | 0.881659 | 9275.7 | 218.2303 | 0.078145 |
| 15 | 74 | 38 | 53 | 1 | 0.899346 | 9182.4 | 212.7602 | 0.076429 |
| 16 | 60 | 47 | 48 | 1 | 0.901514 | 9054 | 212.8896 | 0.076242 |
| 17 | 59 | 47 | 48 | 1 | 0.915672 | 8927.1 | 209.4154 | 0.075034 |
| 18 | 62 | 44 | 48 | 1 | 0.928598 | 8805.6 | 206.0890 | 0.073878 |
| 19 | 61 | 44 | 48 | 1 | 0.941498 | 8686.8 | 202.8365 | 0.072747 |
| 20 | 56 | 47 | 48 | 1 | 0.957745 | 8546.4 | 198.9926 | 0.071410 |
| 21 | 58 | 45 | 48 | 1 | 0.965818 | 8487 | 197.3664 | 0.070845 |
| 22 | 56 | 46 | 47 | 1 | 0.977137 | 8365.2 | 194.7607 | 0.069892 |
| 23 | 62 | 41 | 47 | 1 | 0.989206 | 8273.4 | 192.2474 | 0.069019 |
| 24 | 64 | 39 | 47 | 1 | 1.004947 | 8149.2 | 188.8471 | 0.067836 |
| 25 | 56 | 44 | 47 | 1 | 1.016729 | 8062.8 | 186.4817 | 0.067014 |
| 26 | 60 | 40 | 47 | 1 | 1.041262 | 7890 | 181.7508 | 0.065369 |
| 27 | 67 | 35 | 51 | 1 | 1.058261 | 7861.5 | 178.0548 | 0.064269 |
| 28 | 66 | 35 | 51 | 1 | 1.072955 | 7767 | 175.4676 | 0.063370 |
| 29 | 57 | 40 | 51 | 1 | 1.085713 | 7686 | 173.2500 | 0.062599 |
| 30 | 61 | 37 | 51 | 1 | 1.095408 | 7623.9 | 171.5498 | 0.062007 |
| 31 | 61 | 37 | 46 | 1 | 1.101325 | 7473.9 | 171.0878 | 0.061615 |
| 32 | 62 | 35 | 53 | 1 | 1.133233 | 7449 | 165.3036 | 0.059928 |
| 33 | 58 | 37 | 53 | 1 | 1.144468 | 7384.2 | 163.5295 | 0.059312 |
| 34 | 56 | 37 | 58 | 1 | 1.175207 | 7334.4 | 158.5214 | 0.057802 |
| 35 | 57 | 36 | 57 | 1 | 1.186308 | 7250.4 | 156.9506 | 0.057209 |
| 36 | 63 | 32 | 60 | 1 | 1.202326 | 7243.2 | 154.5667 | 0.056519 |
| 37 | 60 | 33 | 58 | 1 | 1.225187 | 7086 | 151.7208 | 0.055437 |
| 38 | 60 | 33 | 50 | 1 | 1.233167 | 6846 | 150.9816 | 0.054810 |
| 39 | 64 | 31 | 45 | 1 | 1.237042 | 6706.8 | 150.8153 | 0.054520 |
| 40 | 56 | 35 | 45 | 1 | 1.252189 | 6642 | 149.0412 | 0.053904 |

2. Semi-active configuration

| No. | n_{bat_s} | n_{bat_p} | n_{sc_s} | n_{sc_p} | RMS_{cell} [A] | Cost [USD] | HESS mass [kg] | HESS volume [m ³] |
|-----|--------------|--------------|-------------|-------------|---------------------|---------------|-------------------|----------------------------------|
| 1 | 91 | 40 | 62 | 1 | 0.697780 | 11688 | 231.97 | 0.093280 |
| 2 | 91 | 40 | 56 | 1 | 0.701709 | 11508 | 231.50 | 0.092834 |
| 3 | 91 | 40 | 52 | 1 | 0.704308 | 11388 | 231.19 | 0.092537 |
| 4 | 91 | 38 | 54 | 1 | 0.734383 | 10956.6 | 219.99 | 0.088252 |
| 5 | 91 | 37 | 58 | 1 | 0.748922 | 10830.9 | 214.62 | 0.086333 |
| 6 | 91 | 37 | 55 | 1 | 0.750770 | 10740.9 | 214.39 | 0.086110 |
| 7 | 91 | 36 | 58 | 1 | 0.766907 | 10585.2 | 208.95 | 0.084116 |
| 8 | 91 | 36 | 53 | 1 | 0.770380 | 10435.2 | 208.56 | 0.083744 |
| 9 | 91 | 35 | 58 | 1 | 0.786967 | 10339.5 | 203.27 | 0.081899 |
| 10 | 91 | 35 | 51 | 1 | 0.790950 | 10129.5 | 202.72 | 0.081379 |
| 11 | 91 | 34 | 53 | 1 | 0.810505 | 9943.8 | 197.20 | 0.079311 |
| 12 | 91 | 34 | 51 | 1 | 0.812211 | 9883.8 | 197.04 | 0.079162 |
| 13 | 91 | 33 | 57 | 1 | 0.829496 | 9818.1 | 191.83 | 0.077391 |
| 14 | 91 | 33 | 54 | 1 | 0.831246 | 9728.1 | 191.60 | 0.077168 |
| 15 | 91 | 32 | 58 | 1 | 0.851431 | 9602.4 | 186.23 | 0.075249 |
| 16 | 91 | 32 | 52 | 1 | 0.855863 | 9422.4 | 185.76 | 0.074803 |
| 17 | 91 | 31 | 56 | 1 | 0.877083 | 9296.7 | 180.40 | 0.072883 |
| 18 | 91 | 31 | 53 | 1 | 0.879338 | 9206.7 | 180.16 | 0.072660 |
| 19 | 91 | 30 | 57 | 1 | 0.902023 | 9081 | 174.80 | 0.070741 |
| 20 | 91 | 30 | 53 | 1 | 0.905259 | 8961 | 174.49 | 0.070443 |
| 21 | 91 | 29 | 55 | 1 | 0.931423 | 8775.3 | 168.96 | 0.068375 |
| 22 | 91 | 28 | 62 | 1 | 0.956015 | 8739.6 | 163.83 | 0.066679 |
| 23 | 91 | 28 | 60 | 1 | 0.957952 | 8679.6 | 163.68 | 0.066530 |
| 24 | 91 | 28 | 53 | 1 | 0.964262 | 8469.6 | 163.13 | 0.066010 |
| 25 | 91 | 27 | 61 | 1 | 0.988579 | 8463.9 | 158.07 | 0.064388 |
| 26 | 91 | 27 | 59 | 1 | 0.990392 | 8403.9 | 157.92 | 0.064239 |
| 27 | 91 | 26 | 66 | 1 | 1.018069 | 8368.2 | 152.79 | 0.062543 |
| 28 | 91 | 26 | 53 | 1 | 1.030630 | 7978.2 | 151.77 | 0.061576 |
| 29 | 91 | 25 | 60 | 1 | 1.060490 | 7942.5 | 146.64 | 0.059880 |
| 30 | 91 | 25 | 55 | 1 | 1.065593 | 7792.5 | 146.25 | 0.059508 |
| 31 | 91 | 24 | 61 | 1 | 1.101345 | 7726.8 | 141.04 | 0.057737 |
| 32 | 91 | 24 | 57 | 1 | 1.103889 | 7606.8 | 140.73 | 0.057440 |
| 33 | 91 | 24 | 51 | 1 | 1.110066 | 7426.8 | 140.26 | 0.056994 |
| 34 | 91 | 24 | 50 | 1 | 1.111230 | 7396.8 | 140.18 | 0.056920 |
| 35 | 91 | 23 | 56 | 1 | 1.148763 | 7331.1 | 134.97 | 0.055149 |
| 36 | 91 | 23 | 53 | 1 | 1.152083 | 7241.1 | 134.74 | 0.054926 |
| 37 | 91 | 23 | 48 | 1 | 1.157319 | 7091.1 | 134.35 | 0.054554 |
| 38 | 91 | 22 | 56 | 1 | 1.197918 | 7085.4 | 129.29 | 0.052932 |
| 39 | 91 | 22 | 55 | 1 | 1.199126 | 7055.4 | 129.21 | 0.052858 |
| 40 | 91 | 22 | 47 | 1 | 1.206593 | 6815.4 | 128.59 | 0.052263 |

3. Passive configuration

| No. | n_{bat_s} | n_{bat_p} | n_{sc_s} | n_{sc_p} | RMS_{cell} [A] | Cost [USD] | HESS mass [kg] | HESS volume [m ³] |
|-----|--------------|--------------|-------------|-------------|---------------------|---------------|-------------------|----------------------------------|
| 1 | 91 | 38 | 135 | 1 | 0.779428 | 13386.6 | 200.197 | 0.089084 |
| 2 | 91 | 37 | 135 | 1 | 0.798493 | 13140.9 | 195.173 | 0.086989 |
| 3 | 91 | 36 | 135 | 1 | 0.817619 | 12895.2 | 190.150 | 0.084894 |
| 4 | 91 | 35 | 135 | 1 | 0.838859 | 12649.5 | 185.127 | 0.082800 |
| 5 | 91 | 34 | 135 | 1 | 0.860289 | 12403.8 | 180.104 | 0.080705 |
| 6 | 91 | 33 | 135 | 1 | 0.884105 | 12158.1 | 175.081 | 0.078610 |
| 7 | 91 | 32 | 135 | 1 | 0.908287 | 11912.4 | 170.057 | 0.076515 |
| 8 | 91 | 31 | 135 | 1 | 0.935184 | 11666.7 | 165.034 | 0.074420 |
| 9 | 91 | 30 | 135 | 1 | 0.962676 | 11421 | 160.011 | 0.072326 |
| 10 | 91 | 29 | 135 | 1 | 0.992058 | 11175.3 | 154.988 | 0.070231 |
| 11 | 91 | 28 | 135 | 1 | 1.024807 | 10929.6 | 149.965 | 0.068136 |
| 12 | 91 | 27 | 135 | 1 | 1.058648 | 10683.9 | 144.941 | 0.066041 |
| 13 | 91 | 26 | 135 | 1 | 1.096462 | 10438.2 | 139.918 | 0.063947 |
| 14 | 91 | 25 | 135 | 1 | 1.135863 | 10192.5 | 134.895 | 0.061852 |
| 15 | 91 | 24 | 135 | 1 | 1.180018 | 9946.8 | 129.872 | 0.059757 |
| 16 | 91 | 23 | 135 | 1 | 1.226452 | 9701.1 | 124.849 | 0.057662 |
| 17 | 91 | 22 | 135 | 1 | 1.278711 | 9455.4 | 119.825 | 0.055568 |
| 18 | 91 | 21 | 135 | 1 | 1.334219 | 9209.7 | 114.802 | 0.053473 |

With:

- n_{bat_s} : number of battery cells connected in series
- n_{bat_p} : number of battery branches connected in parallel
- n_{sc_s} : number of supercapacitor modules connected in series
- n_{sc_p} : number of supercapacitor branches connected in parallel
- RMS_{cell} : root-mean-square value of the battery cell current
- $Cost$: the price of the energy storage system