STA207 homework3

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23.13

```
transform_function <- function(x) {
  log10(x + 1)
}
kidney$Days <- transform_function(as.numeric(as.character(kidney$Days)))
kidney <- subset(kidney, Duration != 2 | Weight != 1) # empty y_21 cell</pre>
```

(a)

The full model is:

$$Y_{ijk} = \mu_{..} + \alpha_1 * X_{ij1} + \beta_1 * X_{ij2} + \beta_2 * X_{ij3} + \epsilon_{ijk}$$

The reduced model for testing for factor A main effects is:

$$Y_{ijk} = \mu_{..} + \beta_1 * X_{ij2} + \beta_2 * X_{ij3} + \epsilon_{ijk}$$

The reduced model for testing for factor B main effects is:

$$Y_{ijk} = \mu_{..} + \alpha_1 * X_{ij1} + \epsilon_{ijk}$$

Where:

$$X_{ij1} = \begin{cases} 1, & \text{if case from level 1 for factor A} \\ -1, & \text{if case from level 2 for factor A} \end{cases}$$

$$X_{ij2} = \begin{cases} 1, & \text{if case from level 1 for factor B} \\ -1, & \text{if case from level 3 for factor B} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij3} = \begin{cases} 1, & \text{if case from level 2 for factor B} \\ -1, & \text{if case from level 3 for factor B} \\ 0, & \text{otherwise} \end{cases}$$

(b)

```
kidney$X1 = ifelse(kidney$Duration == 1, 1, -1)
kidney$X2 = ifelse(kidney$Weight == 1,1, ifelse(kidney$Weight == 3, -1, 0))
kidney$X3 = ifelse(kidney$Weight == 2,1, ifelse(kidney$Weight == 3, -1, 0))
fullModel = with(kidney, lm(Days~X1+X2+X3))
fullModel
```

```
##
## Call:
## lm(formula = Days ~ X1 + X2 + X3)
##
## Coefficients:
## (Intercept)
                          X1
                                        Х2
                                                       ХЗ
       0.66939
                     0.11733
                                  -0.34323
                                                 0.02608
sse.full = anova(fullModel)[4,2]
sse.full
## [1] 4.489821
reducedModelTestA = with(kidney, lm(Days~X2+X3))
reducedModelTestA
##
## Call:
## lm(formula = Days ~ X2 + X3)
##
## Coefficients:
## (Intercept)
                          Х2
                                         ХЗ
                   -0.26502
                                  -0.01303
       0.70850
sse.reduceA = anova(reducedModelTestA)[3,2]
sse.reduceA
## [1] 5.040447
reducedModelTestB = with(kidney, lm(Days~X1))
reducedModelTestB
##
## Call:
## lm(formula = Days ~ X1)
##
## Coefficients:
## (Intercept)
                          Х1
       0.75520
                     0.03152
sse.reduceB = anova(reducedModelTestB)[2,2]
sse.reduceB
## [1] 7.10425
From R output above, we can fit the full model as:
\hat{Y} = 0.66939 + 0.11733 * X_{ij1} - 0.34323 * X_{ij2} + 0.02608 * X_{ij3}
And the SSE of full model is 4.4898209.
The reduced model for testing A main effects is:
```

$$\hat{Y} = 0.70850 - 0.26502 * X_{ij2} - 0.01303 * X_{ij3}$$

The corresponding SSE is 5.0404474.

The reduced model for testing B main effects is:

$$\hat{Y} = 0.75520 + 0.03152 * X_{ij1}$$

The corresponding SSE is 7.1042504.

TESTING A MAIN EFFECTS:

$$H_0: \alpha_1 = 0$$

$$H_1:\alpha_1\neq 0$$

$$F^* = \frac{(5.0404474 - 4.4898209)/1}{(4.4898209)/46} = 0.5506265/0.0976048 = 5.6414$$

$$F(0.95, 1, 46) = 4.0517$$

$$p - val = 0.02176$$

The decision rule is: if F^* is greater that 4.0517, then reject H_0 , otherwise, accept H_1 . Here, $5.6414 \ge 4.0517$, so we reject H_0 , concluding that factor A main effects are present. The p-value is 0.02176, which is less than 0.05, leading to the same conclusion.

TESTING B MAIN EFFECTS:

$$H_0: \beta_1 = \beta_2 = 0$$

 $H_1: notall\beta equal to 0$

$$F^* = \frac{(7.1042504 - 4.4898209)/2}{(4.4898209)/46} = 1.307215/0.0976048 = 13.39294$$

$$F(0.95, 2, 46) = 3.1996$$

$$p - val = 2.608231e - 05$$

The decision rule is: if F^* is greater that 3.1996, then reject H_0 , otherwise, accept H_1 . Here, $13.39294 \ge 4.0517$, so we reject H_0 , concluding that factor B main effects are present. The p-value is almost zero, which is less than 0.05, leading to the same conclusion.

23.19

(a)

The ANOVA model is:

$$Y_{ij} = \mu_{..} + \rho_i + \tau_j + \epsilon_{ij}$$
, Where $i = 1, 2, ..., 5, j = 1, 2, 3$

The corresponding regression model is:

$$Y_{ij} = \mu_{..} + \rho_1 * X_{ij1} + \rho_2 * X_{ij2} + \rho_3 * X_{ij3} + \rho_4 * X_{ij4} + \tau_1 * X_{ij5} + \tau_2 * X_{ij6} + \epsilon_{ij}$$

Where:

$$X_{ij1} = \begin{cases} 1, & \text{if case from block 1} \\ -1, & \text{if case from block 5} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij2} = \begin{cases} 1, & \text{if case from block 2} \\ -1, & \text{if case from block 5} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij3} = \begin{cases} 1, & \text{if case from block 3} \\ -1, & \text{if case from block 5} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij4} = \begin{cases} 1, & \text{if case from block 4} \\ -1, & \text{if case from block 5} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij5} = \begin{cases} 1, & \text{if case from treatment 1} \\ -1, & \text{if case from treatment 3} \\ 0, & \text{otherwise} \end{cases}$$

$$X_{ij6} = \begin{cases} 1, & \text{if case from treatment 2} \\ -1, & \text{if case from treatment 2} \\ 0, & \text{otherwise} \end{cases}$$

(b)

The reduced model for testing for differences in the mean reductions in lipid level for treatment is:

$$Y_{ij} = \mu_{..} + \rho_1 * X_{ij1} + \rho_2 * X_{ij2} + \rho_3 * X_{ij3} + \rho_4 * X_{ij4} + \epsilon_{ij}$$

(c)

```
Yij = c(0.73, 0.67, 0.15, 0.86, 0.75, 0.21, 0.94, 0.81, 0.26, 1.4, 1.32, 0.75, 1.62, 1.41, 0.78)
obs = data.frame(matrix(Yij, 5,3,2))
rownames(obs) = c("block1", "block2", "block3", "block4", "block5")
names(obs) = c("treatment1", "treatment2", "treatment3")
obs[1,3] = NA
obs[5,1] = NA
obs
          treatment1 treatment2 treatment3
##
## block1
                0.73
                           0.67
## block2
                0.86
                           0.75
                                       0.21
## block3
                0.94
                           0.81
                                       0.26
## block4
                1.40
                           1.32
                                       0.75
## block5
                NA
                           1.41
                                      0.78
Y = c(0.73, 0.67, 0.86, 0.75, 0.21, 0.94, 0.81, 0.26, 1.4, 1.32, 0.75, 1.41, 0.78)
X1 = c(1,1,0,0,0,0,0,0,0,0,0,-1,-1)
X2 = c(0,0,1,1,1,0,0,0,0,0,0,-1,-1)
X3 = c(0,0,0,0,0,1,1,1,0,0,0,-1,-1)
X4 = c(0,0,0,0,0,0,0,0,1,1,1,-1,-1)
X5 = c(1,0,1,0,-1,1,0,-1,1,0,-1,0,-1)
X6 = c(0,1,0,1,-1,0,1,-1,0,1,-1,1,-1)
df = cbind(Y, X1, X2, X3, X4, X5,X6)
df = data.frame(df)
```

```
fullModel2 = with(df, lm(Y~X1+X2+X3+X4+X5+X6))
fullModel2
##
## Call:
## lm(formula = Y \sim X1 + X2 + X3 + X4 + X5 + X6)
## Coefficients:
         (Intercept)
                                                                               X1
                                                                                                                                                                   ХЗ
                                                                                                                                                                                                            Х4
                         0.8294
                                                               -0.3361
                                                                                                          -0.2227
                                                                                                                                                                                                0.3273
##
                                                                                                                                                   -0.1594
##
                                      Х5
                                                                               Х6
##
                         0.2508
                                                                   0.1626
sse.full2 = anova(fullModel2)[7,2]
sse.full2
## [1] 0.00350582
reducedModel2 = with(df, lm(Y~X1+X2+X3+X4))
reducedModel2
##
## Call:
## lm(formula = Y \sim X1 + X2 + X3 + X4)
## Coefficients:
##
        (Intercept)
                                                                               X1
                                                                                                                         X2
                                                                                                                                                                   ХЗ
                                                                                                                                                                                                            X4
                         0.8457
                                                               -0.1457
                                                                                                          -0.2390
                                                                                                                                                   -0.1757
                                                                                                                                                                                                0.3110
sse.reduce2 = anova(reducedModel2)[5,2]
sse.reduce2
## [1] 0.9541833
From R output above, we can fit the full model as:
\hat{Y} = 0.8294 - 0.3361 * X_1 - 0.2227 * X_2 - 0.1594 * X_3 + 0.3273 * X_4 + 0.2508 * X_5 + 0.1626 * X_6 + 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0000 * 0.0
And the SSE of full model is 0.0035058.
The reduced model for testing differences in the treatment is:
\hat{Y} = 0.8457 - 0.1457 * X_1 - 0.2390 * X_2 - 0.1757 * X_3 + 0.311 * X_4
The corresponding SSE is 0.9541833.
TESTING TREATMENT EFFECTS:
H_0: \tau_1 = \tau_2 = 0
H_1: notallequal to zero
F^* = \frac{(0.9541833 - 0.0035058)/2}{(0.0025058)/6} = 0.4753/0.00058 = 819.48
                            \frac{(0.0035058)/6}{}
F(0.95, 2, 6) = 5.1433
```

The decision rule is: if F^* is greater that 5.1433, then reject H_0 , otherwise, accept H_1 . Here, $819.48 \ge 4.0517$, so we reject H_0 , concluding that the mean reductions in lipid level differ for the three diets. The result is the same as obtained in Problem 23.17d.

(d)

vcov(fullModel2)

```
##
                                                   (Intercept)
                                                                                                                      Х1
                                                                                                                                                                X2
                                                                                                                                                                                                          Х3
## (Intercept) 4.760990e-05 1.298452e-05 -8.656346e-06 -8.656346e-06
## X1
                                               1.298452e-05 2.448509e-04 -5.193808e-05 -5.193808e-05
## X2
                                            -8.656346e-06 -5.193808e-05 1.644706e-04 -3.029721e-05
## X3
                                            -8.656346e-06 -5.193808e-05 -3.029721e-05 1.644706e-04
## X4
                                            -8.656346e-06 -5.193808e-05 -3.029721e-05 -3.029721e-05
## X5
                                               4.328173e-06 -3.524369e-05 -4.328173e-06 -4.328173e-06
                                            -8.656346e-06 -1.298452e-05 8.656346e-06
                                                                                                                                                                           8.656346e-06
## X6
##
                                                                            Х4
                                                                                                                      Х5
## (Intercept) -8.656346e-06 4.328173e-06 -8.656346e-06
                                            -5.193808e-05 -3.524369e-05 -1.298452e-05
## X1
## X2
                                            -3.029721e-05 -4.328173e-06 8.656346e-06
## X3
                                            -3.029721e-05 -4.328173e-06 8.656346e-06
## X4
                                               1.644706e-04 -4.328173e-06 8.656346e-06
## X5
                                            -4.328173e-06 1.051128e-04 -4.328173e-05
                                              8.656346e-06 -4.328173e-05 8.656346e-05
## X6
Construct: L = \tau_1 - \tau_3 = 2 * \tau_1 + \tau_2
\hat{L} = 2 * \hat{\tau_1} + \hat{\tau_2} = 2 * 0.2508 + 0.1626 = 0.6642
According to the covariance matrix of model coefficients, s^2\{\hat{\tau}_1\} = 1.051128e - 04, s^2\{\hat{\tau}_2\} = 8.656346e - 05,
s\{\hat{\tau}_1, \hat{\tau}_2\} = -4.328173e - 05. Therefore:
s\{\hat{L}\} = sqrt(4*1.051128e - 04 + 8.656346e - 05 + 4*(-4.328173e - 05)) = 0.0182726
t(0.99, 6) = 3.142668
\hat{L} + t(0.99, 6) * s\{\hat{L}\} = 0.6642 + 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 3.142668 * 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 0.0182726 = 0.7216247 \; \hat{L} - t(0.99, 6) * s\{\hat{L}\} = 0.6642 - 0.0182726 = 0.0182726 = 0.0182726 = 0.0182726 = 0.0182726 = 0.0182726 = 0.0182726 = 0.018272
0.0182726 = 0.6067753
```

Therefore, the 98% confidence interval for diffrence in diet1 and diet3 is [0.6068, 0.7216]. We can find that the CI does not include zero, indicating that mean reduction in lipid for diet 1 is significantly larger than the reduction for diet3.

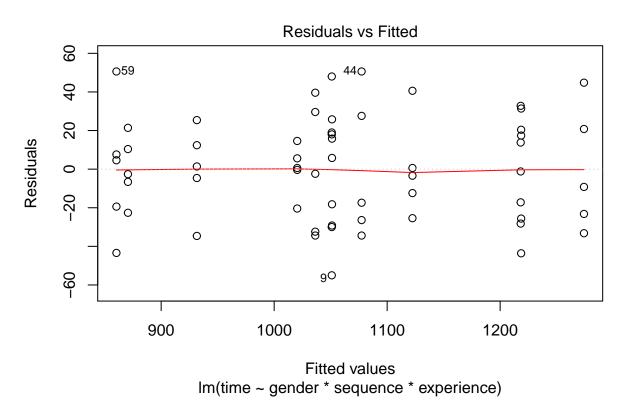
24.12

(d)

```
assembly <- read.table("CH24PR12.txt")
colnames(assembly) <- c("time", "gender", "sequence", "experience", "replication")
assembly <- assembly[,-5]
assembly$gender <- as.factor(assembly$gender)
assembly$sequence <- as.factor(assembly$sequence)
assembly$experience <- as.factor(assembly$experience)
aov_out <- lm(time ~ gender*sequence*experience, data = assembly)
residuals(aov_out)</pre>
```

```
2
                                   5
                                                                                  12
##
        1
                      3
                            4
                                          6
                                                 7
                                                        8
                                                               9
                                                                    10
                                                                           11
    31.4 -43.6
                         20.4 -25.6 -30.0
                                             48.0
                                                                         44.8
                                                                               -23.2
##
                  17.4
                                                    18.0 -55.0
                                                                  19.0
                                                              21
                                                                    22
                                                                           23
                                                                                  24
##
       13
             14
                    15
                           16
                                  17
                                         18
                                                19
                                                       20
   -33.2
           20.8
                  -9.2
                         -3.4 -12.4
                                        0.6
                                            -25.4
                                                    40.6
                                                           -1.2
                                                                 -28.2 -17.2
                                                                                13.8
##
                                         30
                                                31
                                                              33
                                                                    34
##
       25
             26
                    27
                           28
                                  29
                                                       32
                                                                           35
                                                                                  36
##
    32.8
          -18.2
                  15.8
                          5.8
                                25.8 -29.2
                                              29.6
                                                    39.6
                                                          -32.4
                                                                 -34.4
                                                                         -2.4
                                                                                -6.6
##
       37
             38
                    39
                           40
                                  41
                                         42
                                                43
                                                       44
                                                              45
                                                                     46
                                                                           47
                                                                                  48
                                                                         12.4
   -22.6
           10.4
                  21.4
                         -2.6
                                27.6 -34.4 -26.4
                                                    50.6 -17.4
                                                                  -4.6
                                                                                25.4
##
##
       49
             50
                    51
                           52
                                  53
                                         54
                                                55
                                                       56
                                                             57
                                                                    58
                                                                           59
                                                                                  60
                                               5.6 -19.4
                                                             4.6 -43.4
## -34.6
            1.4
                   0.6
                         -0.4
                                14.6 -20.4
                                                                         50.6
                                                                                 7.6
```

plot(aov_out, which = 1)

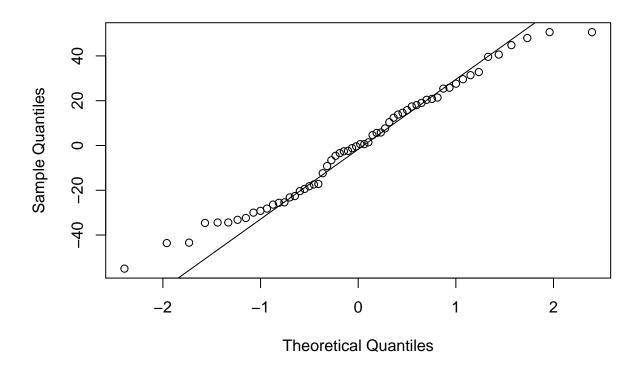


From the plot, we can conclude that this anova model is appropriate.

(e)

```
qqnorm_assembly <- qqnorm(aov_out$residuals)
qqline(aov_out$residuals)</pre>
```

Normal Q-Q Plot



```
cor(qqnorm_assembly$x, qqnorm_assembly$y)
```

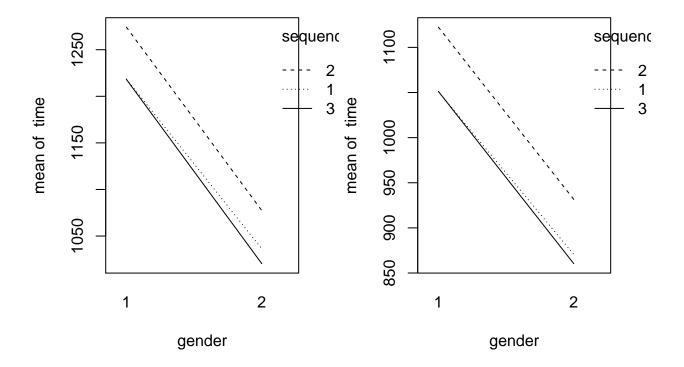
[1] 0.9906479

The correlation indicates the normality assumption is reasonable here.

24.13

(a)

```
assembly_experience_split <- split(assembly[, -4], assembly$experience)
par(mfrow = c(1, 2))
with(assembly_experience_split[[1]], interaction.plot(gender, sequence, time))
with(assembly_experience_split[[2]], interaction.plot(gender, sequence, time))</pre>
```



Almost no interaction is seen in this plot for the three factors.

(b)

```
(anova_out <- anova(aov_out))</pre>
## Analysis of Variance Table
##
## Response: time
                               Df Sum Sq Mean Sq F value
                                                              Pr(>F)
                                          540361 629.7603 < 2.2e-16 ***
## gender
                                1 540361
## sequence
                                   49320
                                            24660
                                                   28.7396
                                                            6.22e-09 ***
                                          382402 445.6679 < 2.2e-16 ***
## experience
                                1
                                  382402
## gender:sequence
                                     543
                                              271
                                                    0.3161
                                                              0.7305
                                                    0.1064
                                                              0.7457
## gender:experience
                                1
                                      91
                                               91
## sequence:experience
                                2
                                     911
                                              456
                                                    0.5310
                                                              0.5914
                                                    0.0111
## gender:sequence:experience
                                2
                                      19
                                               10
                                                              0.9890
## Residuals
                               48
                                   41186
                                              858
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(c)
```

Null hypothesis: the coefficient of three-factor interactions ==0

Alternative hypothesis: the coefficient of three-factor interactions != 0

Test statistics: $F^* = 10/858 = 0.01165501$

Decision rule: F(0.95; 2, 48) = qf(0.95, 2, 48) = 3.190727, then reject H_0 is $F^* > F(0.95; 2, 48)$

Conclusion: since $F^* < F(0.95; 2, 48)$, then we cannot reject H_0 .

p-value: 0.9890

(d)

AB-interaction:

Null hypothesis: the coefficient of AB-interactions == 0

Alternative hypothesis: the coefficient of AB-interactions !=0

Test statistics: $F^* = 271/858 = 0.3158508$

Decision rule: F(0.95; 2, 48) = qf(0.95, 2, 48) = 3.190727, then reject H_0 is $F^* > F(0.95; 2, 48)$

Conclusion: since $F^* < F(0.95; 2, 48)$, then we cannot reject H_0 .

p-value: 0.7305AC-interaction:

Null hypothesis: the coefficient of AC-interactions == 0

Alternative hypothesis: the coefficient of AC-interactions !=0

Test statistics: $F^* = 91/858 = 0.1060606$

Decision rule: F(0.95; 1, 48) = qf(0.95, 1, 48) = 4.042652, then reject H_0 is $F^* > F(0.95; 1, 48)$

Conclusion: since $F^* < F(0.95; 1, 48)$, then we cannot reject H_0 .

p-value: 0.7457

BC-interaction:

Null hypothesis: the coefficient of BC-interactions == 0

Alternative hypothesis: the coefficient of BC-interactions !=0

Test statistics: $F^* = 456/858 = 0.5314685$

Decision rule: F(0.95; 2, 48) = qf(0.95, 2, 48) = 3.190727, then reject H_0 is $F^* > F(0.95; 2, 48)$

Conclusion: since $F^* < F(0.95; 2, 48)$, then we cannot reject H_0 .

p-value: 0.5914

(e)

A

Null hypothesis: the coefficient of A == 0

Alternative hypothesis: the coefficient of A != 0

Test statistics: $F^* = 540361/858 = 629.7914$

Decision rule: F(0.95; 2, 48) = qf(0.95, 1, 48) = 4.042652, then reject H_0 is $F^* > F(0.95; 1, 48)$

Conclusion: since $F^* > F(0.95; 1, 48)$, then we reject H_0 .

```
p-value: 0.0000
B
Null hypothesis: the coefficient of B == 0
Alternative hypothesis: the coefficient of B != 0
Test statistics: F^* = 24660/858 = 28.74126
Decision rule: F(0.95; 2, 48) = qf(0.95, 2, 48) = 3.190727, then reject H_0 is F^* > F(0.95; 2, 48)
Conclusion: since F^* > F(0.95; 2, 48), then we reject H_0.
p-value: 0.0000
C
Null hypothesis: the coefficient of C == 0
Alternative hypothesis: the coefficient of C = 0
Test statistics: F^* = 382402/858 = 445.69
Decision rule: F(0.95; 1, 48) = qf(0.95, 1, 48) = 4.042652, then reject H_0 is F^* > F(0.95; 1, 48)
Conclusion: since F^* > F(0.95; 1, 48), then we reject H_0.
p-value: 0.0000
(f)
```

Only the single effect of A, B and C are significant.

The Kimball Inequality shows that the upper bound for the family level of significance for the set of tests is $1-0.95^7 = 0.3016627.$

(g)

Yes, because the upper bound for the family level of significance for the set of tests (0.3016627) is still small than the P-values of AB = 0.7305. We cannot reject H_0 of the coefficient of AB-interaction is 0.

24.14

(a)

```
assembly_mean <- with(assembly, tapply(time, list(gender = gender, sequence = sequence, experience = ex
(d1 <- apply(assembly_mean, 1, mean)[1] - apply(assembly_mean, 1, mean)[2])</pre>
##
       1
## 189.8
(d2 <- apply(assembly_mean, 2, mean)[1] - apply(assembly_mean, 2, mean)[2])</pre>
##
## -57.25
```

```
(d3 <- apply(assembly_mean, 2, mean)[1] - apply(assembly_mean, 2, mean)[3])</pre>
##
    1
## 6.6
(d4 <- apply(assembly_mean, 2, mean)[2] - apply(assembly_mean, 2, mean)[3])</pre>
##
        2
## 63.85
(d5 <- apply(assembly_mean, 3, mean)[1] - apply(assembly_mean, 3, mean)[2])</pre>
##
## 159.6667
(mse <- anova_out$`Mean Sq`[8])</pre>
## [1] 858.0417
(sd1 \leftarrow sqrt(2* mse / (5*2*3)))
## [1] 7.563252
(sd2 <- sqrt(2* mse / (5*2*2)))
## [1] 9.263054
(sd3 \leftarrow sd2)
## [1] 9.263054
(sd4 \leftarrow sd2)
## [1] 9.263054
(sd5 \leftarrow sqrt(2* mse / (5*2*3)))
## [1] 7.563252
Bonferroni: B = t(1 - \frac{0.05}{5}, 48) = t(0.99, 48) = 2.306 = 2.406581
So the intervals:
D_1: 189.8 \pm 2.406581 * 7.563252 = (171.5984, 208.0016)
D_2: -57.25 \pm 2.406581 * 9.263054 = (-79.54229, -34.95771)
D_3: 6.6 \pm 2.406581 * 9.263054 = (-15.69229, 28.89229)
D_4: 63.85 \pm 2.406581 * 9.263054 = (41.55771, 86.14229)
D_5: 159.6667 \pm 2.406581 * 7.563252 = (141.4651, 177.8683)
```

(b)

```
(mu231 <- assembly_mean[2,3,1])

## [1] 1020.4

(sd231 <- (mse/5)^0.5)

## [1] 13.09994

qt(0.975, 48)

## [1] 2.010635

So the interval is 1020.4 ± 2.011 * 13.09994 = (994.056, 1046.744)</pre>
```