Sovereign Risk and Intangible Investment*

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Abstract

This paper measures the output and TFP costs of sovereign risk by focusing on firm-level investment. Combining Italian aggregate and firm-level data, we show that firms reduced their investment and reallocated resources away from intangible assets and towards tangible assets during the recent sovereign debt crisis. This asset reallocation is more pronounced among small and high-leverage firms, indicating the role of financial constraints. In our model, sovereign risk deteriorates bank balance sheets, disrupting banks' ability to finance firms. Firms with greater external financing needs are more exposed to sovereign risk. Facing tightening financial constraints, firms internalize that tangible assets can be used as collateral while intangibles cannot, thus reallocating resources towards tangible investment to offset tightening financial conditions. In a counterfactual analysis, we find that elevated sovereign risk explains 86% of the output losses and 72% of TFP losses during the 2011-2013 Italian sovereign debt crisis.

Keywords: Sovereign debt crisis, intangible asset, output loss, TFP loss

JEL classification: F34, E22, E44, G12, G15

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1 Introduction

The recent European sovereign debt crisis was associated with substantial declines in both private sector lending and real economic activity. Recent literature emphasizes the pass-through of sovereign risk to the private sector through the banking sector (Gennaioli et al. (2014), Perez et al. (2015), Bocola (2016), Arellano et al. (2019), Bottero et al. (2020)). Because banks are often the main creditors of governments, sovereign risk deteriorates bank balance sheets and disrupts private lending to firms. A key open question is to quantify the real economic impacts of sovereign risk on the private sector, such as investment, output, and future growth.

We use Italian firm-level data to quantify the impact of sovereign risk on firm investment. Importantly, beyond tangible investment, we focus on investment in intangible assets, which has often been ignored in previous sovereign default literature. Investment in intangible assets accounts for an increasing proportion of total investment (EU KLEMS database). Furthermore, the positive effects of intangible assets on firm productivity and performance are well-established in the literature (Griliches (1958), Griliches (1979), Geroski (1989), Hall et al. (2010)). Declines in investment in intangible assets (hereafter, intangible investment) during the sovereign debt crisis should therefore be expected to affect firm productivity and output. Our key contribution is to estimate the impact of sovereign risk on firm intangible investment and introduce intangible investment into a sovereign default model.

We start by empirically documenting the impact of sovereign risk on firms' intangible and tangible investment. First, during the Italian sovereign debt crisis, firms reduced their investment in both intangible assets and tangible assets. Second, intangible investment fell more than tangible investment as firms reallocated assets towards tangible investments. We call this behavior as asset reallocation. Third, the asset reallocation pattern is more pronounced within small and high-leverage firms. Our results are robust to alternative measures for investment, sovereign risk, and firm-level variables, and are also robust to different empirical specifications.

To explain the investment decline, asset reallocation and measure the aggregate costs of sovereign risk, we build a sovereign default model incorporating firm investment in both tangible and intangible assets. In our framework, an increase in government default risk results in deteriorating bank balance sheets, which leads to a

higher loan interest rate for firms. The firm-specific loan interest rate also depends on each firm's collateral. Banks accept tangible assets, but not intangible assets, as collateral. As a result, firms reduce intangible investment much more than tangible investment to offset the tightening borrowing constraint. The declines in intangible investment hurt future productivity and output. Firms are not equally affected by the elevated sovereign risk and higher loan interest rate: firms heavily relying on external borrowing from banks are more exposed to sovereign risk.

Our framework incorporates heterogeneous firms with both intangible and tangible investment into an otherwise canonical general equilibrium model of sovereign debt and default. The economy is composed of final goods firms, heterogeneous intermediate goods firms, financial intermediaries, households, and a central government. The government collects tax revenues from the final goods firms and borrows from the financial intermediaries to finance lump-sum transfers to the households and service the outstanding government debt. The government may default on its bonds, following an exogenous process. The final goods firms are competitive and they convert intermediate goods to final goods. The intermediate goods firms need to borrow from the financial intermediaries to finance a fraction of their investment and they differ in their productivity and external financing needs.

The financial intermediaries play a key role in transmitting sovereign risk to the firms: they use their net worth to purchase long-term government bonds and provide loans to firms. An elevated sovereign default risk deteriorates the financial position of intermediaries and hence their private lending to the firms. Tightening financing conditions for the firms depress their investment. Since intangible assets can not be used as collateral, firms reduce their intangible investment. Lower intangible investment hurts firms' future productivity and output.

We parametrize the model using Italian data to assess the output and productivity losses due to sovereign risk. We target sample moments that pertain to the behavior of firms, banks, and government from 2006 to 2015. Using the estimated model, we show that firms decrease their future intangible and tangible assets following an increase in the sovereign spread, and the ratio of tangible assets to intangible assets goes up. With fewer capital inputs, firm output declines. The decline in intangible investment further decreases future firm TFP. The model endogenously generates the output decline and the TFP decline when the sovereign spread increases, as opposed

to a large previous literature that assumes exogenous declines in endowments, output, or TFP when the government defaults.

We then feed the model a series of exogenous shocks to replicate the observed path of Italian sovereign risk and real GDP from 2006-2016. Using the 2006-2016 model-simulated sample, we run the same regression as in the empirical part. We show that the model can replicate the empirical findings: firms increase their tangibles-to-intangibles ratio during a sovereign debt crisis. Moreover, small and high-leverage firms reallocate their assets more aggressively compared to other firms.

We also construct two reference models to highlight the role of intangible assets. In the first reference model, we eliminate intangible assets and denote this the *no-intangible-asset* model. In the second reference model, we fix intangible assets at the median level of the invariant distribution from the benchmark model and call this the *fixed-intangible-asset* model. The comparison between the benchmark model and the reference models isolates the impact of endogenous intangible investment. When firms can choose intangible investment, they have higher leverage and lower tangible asset volatility. Amid a sovereign debt crisis, firms reduce their intangible investment, thus reducing measured TFP, further reducing output. The reference models are silent on the TFP decline and generate less decline in output during a sovereign debt crisis.

To measure the output and TFP costs due to sovereign risk, we specifically focus on the debt crisis period and construct a counterfactual scenario in which the Italian economy does not experience a debt crisis. We then compare the results of our benchmark model and the counterfactual model with no debt crisis. The differences between the economies of the benchmark model and the no debt crisis counterfactual model isolate the impact of the sovereign crisis on the Italian economy. We find that the losses associated with sovereign default risk are sizable. During 2011-2013, output would have declined only 0.6% without the sovereign debt crisis, instead of 4.3% in the benchmark model. TFP would have declined only 0.7% without the sovereign debt crisis, instead of 2.5% in the benchmark model. Our quantitative results suggest that elevated sovereign risk was responsible for 86% of the observed output losses and 72% of the TFP losses during the Italian debt crisis.

Related literature. Our paper measures the output and TFP costs of sovereign risk by focusing on firm-level responses, thus combining elements of the sovereign default

literature with those of the literature on the impact of firm financial frictions. We also contribute to the growing literature on intangible assets and financial frictions.

The model builds on the sovereign default models pioneered by Eaton and Gersovitz (1981), Aguiar and Gopinath (2006), and Arellano (2008). Most sovereign default literature assumes exogenous endowment or output declines when a sovereign defaults (e.g., Arellano (2008), Chatterjee and Eyigungor (2012), Mendoza and Yue (2012)), while most of the rest features a production economy and assumes an exogenous TFP decline when a sovereign defaults (e.g., Arellano et al. (2018), Alessandria et al. (2020), Deng (2019)). Unlike these approaches, the model in this paper adopts a reduced-form exogenous shock that determines the government default probability, which is similar to Bocola (2016). Our model endogenously generates the output decline and TFP decline when the sovereign spread increases. The TFP decline through the intangible investment channel is novel in the sovereign default literature.

Recent papers in the sovereign debt and default literature also study the links between sovereign default risk and the private sector through financial intermediation. During a sovereign debt crisis, firms lose access to external financing and cut their production, leading to reduced output (Mendoza and Yue (2012)). The link between sovereign default and the private sector through banking and finance is also analyzed in Perez et al. (2015), Sosa-Padilla (2018), Arellano et al. (2019), and D'Erasmo et al. (2020). Our paper shares the focus of studying the transmission of sovereign risk to the firms through the financial intermediation. An increase in the probability of future default can affect the private sector through financial intermediation, even when the government keeps repaying the debt. Our contribution is to estimate the real economic impacts of sovereign risk on firm intangible and tangible investment, productivity and output.

Our empirical findings also relate to literature that uses micro data to test the impacts of bank balance sheet on firm credit (Bofondi et al. (2018), Acharya et al. (2018), Bottero et al. (2020)), sales (Arellano et al. (2019)), and investment (Kalemli-Özcan et al. (2018)). We use a similar approach but focus on firm-level investment, especially intangible investment.

¹As mentioned in Bocola (2016), this shock captures empirical evidence that movements in Italian sovereign spreads during the European debt crisis were driven by factors orthogonal to domestic fundamentals.

This paper also connects to the literature that studies the relationship between credit constraints and intangible investment over the business cycle. Lopez and Olivella (2018) finds that intangible capital, which cannot be used by financially constrained firms as collateral, is key to generating labor market volatility in response to financial shocks. Several studies also find declines in intangible investment due to financial frictions during recessions or even periods of normal growth (Garcia-Macia (2017), Demmou et al. (2020)). Similar to these papers, the key to our mechanism is the firm-level collateral constraint and asset tangibility. We contribute by quantifying the impact of sovereign risk on firm intangible investment and the role of financial frictions. We also quantify the aggregate costs of a sovereign debt crisis through our theoretical model.

Our model implications for the TFP costs of sovereign debt crises relates to an extensive literature that studies the financial frictions and R&D investment. The positive effects of intangible assets on firm productivity and economic performance are well established in the literature.² Although traditional literature shows that R&D investment is countercyclical due to the lower opportunity cost of long-term innovative investments in recessions than in booms (Bean (1990), Aghion and Saint-Paul (1998)), more recent literature, such as Aghion et al. (2012), show that this traditional view is only true for firms that are not constrained financially. Several contributions also highlight the key role of credit constraints in R&D investment more generally (Brown et al. (2012), Hall et al. (2016), Peia and Romelli (2020), Xue et al. (2021)).

Road map. This paper proceeds as follows. Section 2 shows the data and key empirical findings. Section 3 presents our model with sovereign default risk, financial intermediaries, and firm investment in both tangible and intangible assets. Section 4 calibrates the model and uses the model to measure the output and TFP costs of sovereign risk. Section 5 concludes.

²This branch of literature traces back to Griliches (1958); research on R&D investment and firm productivity has bloomed ever since (Griliches (1979); Geroski (1989); Hall et al. (2010)). Several recent studies show that low firm-level incentives to invest in intangibles would result in TFP and output losses. The lack of incentive can be caused by either distortions (Ranasinghe (2014)), monetary policy (Moran and Queralto (2018)), equity financing shocks (Bianchi et al. (2019)), or financial crises (Queralto (2020)).

2 Empirical facts

This section documents the empirical results about the impact of sovereign risk on firm tangible and intangible investment. Section 2.1 describes the construction of the variables of interest and provides summary statistics. Section 2.2 shows the firm-level responses in terms of both tangible and intangible investment during sovereign debt crises. Section 2.3 provides additional empirical evidence for robustness.

2.1 Data description

Firm-level variables. Our main sample uses annual firm-level data from the Orbis dataset, covering the period 2006-2016. The dataset covers a large majority of Italian firms including both private and public firms, and includes rich balance-sheet information.³ The core variables in our analysis are firm investment (investment in intangible fixed assets and tangible fixed assets), key balance sheet indicators (total assets, short-term debt, and long-term debt), and additional firm-level variables.

We first perform standard steps to check and ensure the quality of the data. For nominal variables, we scale them by the producer price index. For intangible and tangible assets, the prices of intangibles and tangibles are calculated according to price information in the EU KLEMS database. We further restrict the sample to firms that already exist in 2006 and exclude firms that are not in the manufacturing sector. In Appendix A, we provide extensive detail on variables and sample selection.

Intangible fixed assets in the Orbis dataset are defined as all balance sheet intangible assets such as formation expenses, research expenses, goodwill, development expenses, and all other expenses with a long-term effect. To measure investment in intangible assets, we take the log difference of intangible fixed assets. We use this log-difference specification because investment is highly skewed, suggesting a log-linear rather than a simple linear regression specification. One possible concern about this log-difference measure of intangible investment stems from the discontinuity of intangible fixed assets. Using the log-difference measure of intangible investment results in the loss of some observations if firms have zero intangible fixed assets in

³Appendix A.3 shows the aggregate distribution of wage bills and employment by firm size to illustrate the representativeness of our sample.

some certain years, which may bias our baseline estimation. To ensure that this loss of data is not influencing our results, we also consider the extensive margin of intangible investment and use alternative measures for investment as robustness checks.

In our baseline regression, leverage is defined as the ratio of total debt over total assets, where total debt is the sum of short-term debt and long-term debt. We label leverage calculated according to this method as "total leverage". We also use short-term leverage (short-term debt over total assets) and net leverage (the ratio of net debt to total assets, where net debt is the sum of short-term loans and long-term debt net of net current assets) as robustness checks. As standard in literature, we define size, liquidity, sales growth, and the net current asset ratio. Table 1 reports a set of summary statistics for the main variables.

Table 1: Summary statistics

	Obs.	Mean	St.Dev.	Min.	Max.	P25	Median	P75
Net leverage	389560	0.053	0.37	-0.937	3.963	-0.205	0.054	0.309
Short-term leverage	389560	0.131	0.148	0	0.796	0	0.078	0.229
Total leverage	389560	0.202	0.195	0	0.983	0	0.165	0.349
Size	389560	10.123	1.203	4.565	13.323	9.283	10.145	11.011
Liquidity	389560	0.075	0.111	0	0.848	0.004	0.025	0.1
Investment in tangibles (log-diff)	389560	-0.124	0.746	-2.769	3.623	-0.462	-0.197	0.046
Investment in intangibles (log-diff)	389560	-0.04	0.397	-1.877	2.484	-0.204	-0.086	0.041

Notes: Statistics are calculated using the manufacturing firm-level data from the Orbis dataset, covering the period 2006-2016. The detailed sample selection can be found in Appendix A.

Sovereign debt crisis. The Italian economy was hit by the global financial crisis in 2008-2009 and recovered slightly in 2010. Then the economy experienced a second deep recession featuring a sovereign debt crisis in 2011-2013, when real GDP further declined by a further 4.4%. Figure 1 plots monthly sovereign spreads for Italy. The sovereign spread is defined as the gap between Italian and German 30-year government bond yields.⁵ During 2011-2013, the spread spiked to about 4.5%. Sovereign debt credit ratings can also indicate the severity of a sovereign debt crisis. In 2011, the Standard & Poor's (S&P) revised their credit rating for Italian bonds from A+ to A, and further downgraded the rating to BBB+ in 2012, BBB in 2013, and BBB- in 2014.

⁴The detailed definitions can be found in Appendix A.1.

⁵Similar patterns hold for sovereign spreads data with different maturities.

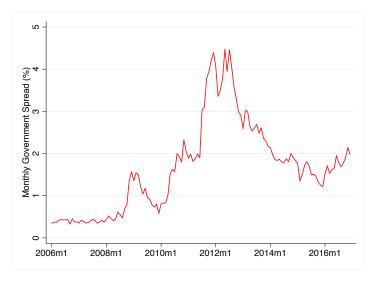


Figure 1: Sovereign spreads

Notes: Italian sovereign spread (monthly data). The spread is defined as the gap between 30-year Italian and German sovereign yields. Data is obtained from GFDFinaeon.

2.2 Firm-level responses during a sovereign debt crisis

We focus on how firm investments react differently during a sovereign debt crisis. We first examine and estimate how the heterogeneous effects of sovereign risk on investment (including intangible and tangible investment) depend on firm characteristics, controlling for sector-year fixed effects. To obtain the average effect of sovereign risk, we relax the sector-year fixed effects and include more aggregate controls in a second estimation. This specification allows us to include government spreads in the regression. After examining the responses of intangible investment and tangible investment, we test for asset reallocation from intangible assets to tangible assets during the sovereign debt crisis.

2.2.1 Heterogeneous effects

To estimate the responses of firm-level investment to sovereign risk and how the responses depend on firm-level characteristics, we estimate variants of our baseline empirical specification:

$$\Delta \log(assets_{i,t+1}) = \beta(x_i \times sp_t) + Controls + \delta_i + \eta_{st} + \epsilon_{it}, \tag{1}$$

where assets represent two types of assets: intangible assets and tangible assets. $\Delta \log(assets_{i,t+1}) \in \{\Delta \log(intangibles_{i,t+1}), \Delta \log(tangibles_{i,t+1})\}$ denotes intangible investment or tangible investment of firm i at time t, which are defined as the log-difference of intangible assets $[\log(intangibles_{i,t+1}) - \log(intangibles_{it})]$ or the log-difference of tangible assets $[\log(tangibles_{i,t+1}) - \log(tangibles_{it})]$. sp_t is the sovereign spread at time t. x_i represents firm-level characteristics and we focus on two key characteristics: size and leverage. Thus, $x_i \in \{size_{i,2006}, totallev_{i,2006}\}$ is a firm's size or total leverage in 2006. 6 Controls contains the interaction term of x_i and GDP growth (Δ GDP $_t$) and a vector of firm-level variables at time t-1, which includes size, total leverage, liquidity, sales growth, the ratio of liabilities to total assets, and the ratio of net current assets to total assets. δ_i controls for a firm fixed effects, which captures permanent differences in investment behavior across firms. η_{st} is a sector-year fixed effects, which captures differences in sectoral exposure to aggregate shocks. ϵ_{it} is a residual. Our main coefficient of interest is β , which depicts how firms invest in response to the sovereign spread, conditional on firm characteristics.

Panel (a) of Table 2 reports the results from estimating this baseline specification (1) for intangible investment. We have standardized size and total leverage over the entire sample relative to the year 2006, so their units are in standard deviations relative to the mean. We cluster the standard errors at the firm level. Column (1) in Table 2 Panel (a) shows the result when only focusing on firm heterogeneity in size. Column (2) reports the results when focusing on firm heterogeneity in total leverage. Column (3) adds both interactions. The results show that a firm of one standard deviation larger size than average has approximately a 2.0 *higher* semi-elasticity of intangible investment when the spread increases, and a firm of one standard deviation higher leverage than average has approximately a 0.652 *lower* semi-elasticity.

Panel (b) of Table 2 reports the results of estimating Eq. (1) for tangible investment. Column (3) of Panel (b) shows that a firm of one standard deviation larger size than average has approximately a 0.652 *higher* semi-elasticity of tangible investment when the spread increases, and a firm of one standard deviation higher leverage than average has approximately a 0.13 *higher* semi-elasticity. Comparing Panel (a) and (b),

⁶We use firm characteristics in the first year of the sample to guarantee the variables are predetermined. We also use other measures of leverage including net leverage and short leverage for robustness checks.

 $^{^{7}}$ standardized size_{i,2006} = $\frac{size_{i,2006} - \frac{1}{N_{2006}} \sum_{i} size_{i,2006}}{std(size_{i,2006})}$. Same standardization applies for leverage.

we find that firms at each leverage level have opposite responses in terms of intangible and tangible investment: a high leverage firm would invest less in intangible assets but invest more in tangible assets, compared to other firms, during a sovereign debt crisis.

As the sector-year fixed effects absorbs the average effect of sovereign risk, we can only estimate the heterogeneity stemming from the spread by estimating Eq. (1). We now relax the sector-year fixed effects and instead include aggregate controls, which allows us to compare the heterogeneous responses to the average effects.

Table 2: Heterogeneous responses of firm investment

(a) Intangible investment

(b) Tangible investment

	$\Delta \log(intangibles_{i,t+1})$					
	(1)	(2)	(3)			
$size_{i,2006} \times sp_t$	1.905***		1.998***			
	(0.189)		(0.191)			
$totallev_{i,2006} \times sp_t$		-0.426***	-0.652***			
,		(0.165)	(0.166)			
Firm controls	Yes	Yes	Yes			
Firm FE	Yes	Yes	Yes			
Sector-year FE	Yes	Yes	Yes			
Observations	303,935	303,935	303,935			
R-squared	0.026	0.025	0.026			
Number of id	59,706	59,706	59,706			

Notes: Results from estimating Eq. (1) for intangible investment. We have normalized $x_i \in \{size_{i,2006}, totallev_{i,2006}\}$ to standardized size and leverage, so their units are in standard deviation relative to he mean. Robust standard errors (in parentheses) are clustered by firms. *** p<0.01, ** p<0.05, * p<0.1.

	$\Delta \log(tangibles_{i,t+1})$					
	(1)	(2)	(3)			
$size_{i,2006} \times sp_t$	0.671***		0.652***			
	(0.091)		(0.092)			
$totallev_{i,2006} \times sp_t$		0.202***	0.129*			
,		(0.074)	(0.074)			
Firm controls	Yes	Yes	Yes			
Firm FE	Yes	Yes	Yes			
Sector-year FE	Yes	Yes	Yes			
Observations	303,935	303,935	303,935			
R-squared	0.068	0.068	0.068			
Number of id	59,706	59,706	59,706			

Notes: Results from estimating Eq. (1) for tangible investment. We have normalized $x_i \in \{size_{i,2006}, totallev_{i,2006}\}$ to standardized within-firm size and total leverage, so their units are in standard deviation relative to he mean. Robust standard errors (in parentheses) are clustered by firms. *** p<0.01, ** p<0.05, * p<0.1.

2.2.2 Average effects

To assess the economic significance of our estimated interaction coefficients β , we now relax the sector-year fixed effects to obtain the average effect of sovereign risk by estimating:

$$\Delta \log(assets_{i,t+1}) = \beta_0 sp_t + \beta_1(x_i \times sp_t) + Controls + AggControls + \delta_i + \epsilon_{it}, \quad (2)$$

where $\Delta \log(assets_{i,t+1}) \in \{\Delta \log(intangibles_{i,t+1}), \Delta \log(tangibles_{i,t+1})\}$ denotes intangible or tangible investment of firm i at time t, sp_t is the sovereign spread at time t, and $x_i \in \{size_{i,2006}, totallev_{i,2006}\}$ is firm's size or total leverage in the year 2006.

Controls is a vector of firm-level variables at time t-1 as defined in Eq. (1). We also include a vector of aggregate controls AggControls, which includes GDP growth (ΔGDP_t) and its interactions with firm characteristics $(x_i \times \Delta GDP_t)$.⁸ δ_i is a firm fixed effects. Our coefficients of interest are β_0 and β_1 . β_0 shows the average effect of the sovereign spread on firm investment, and β_1 measures how the semi-elasticity of investment with respect to the spread depends on firm size or total leverage.

Table 3 reports the results from estimating Eq. (2). The coefficient of sp_t for intangible (tangible) investment is around 0.1-0.3 (0.6-0.7) in absolute value. The interaction coefficients imply an economically meaningful degree of heterogeneity. The coefficients for the interaction terms are similar to the ones in Table 2. We make several observations. First, on average, firms invest less in both intangible assets and tangible assets. Second, firms are heterogeneous in their investment responses. Especially, compared with other firms, high-leverage firms invest more in tangible assets and less in intangible assets, indicating a higher degree of asset reallocation. In the next section, we use the tangibles-to-intangibles ratio as the dependent variable to examine the asset reallocation in depth.

Table 3: Average responses of firm investment

(a) Intangible investment

(b) Tangible investment

		$\Delta \log(i)$	ntangibles _{it}	+1)
	(1)	(2)	(3)	(4)
sp_t	-0.117	-0.376**	-0.109	-0.375**
	(0.163)	(0.164)	(0.163)	(0.164)
$size_{i,2006} \times sp_t$		1.984***		2.073***
,		(0.187)		(0.189)
$totallev_{i,2006} \times sp_t$			-0.376**	-0.617***
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,			(0.164)	(0.166)
Firm controls	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes
Observations	303,935	303,935	303,935	303,935
R-squared	0.012	0.013	0.012	0.013
Number of id	59,706	59,706	59,706	59,706

Notes: Results from estimating Eq. (2) for intangible investment. Robust standard errors are in parentheses. *** p < 0.01, ** p < 0.05, * p < 0.1.

		$\Delta \log(ta)$	$ingibles_{it+1}$	
	(1)	(2)	(3)	(4)
sp_t	-0.689***	-0.777***	-0.693***	-0.778***
	(0.074)	(0.078)	(0.074)	(0.078)
$size_{i,2006} \times sp_t$		0.683***		0.663***
,		(0.089)		(0.089)
$totallev_{i,2006} \times sp_t$			0.219***	0.142*
,			(0.073)	(0.074)
Firm controls	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes
Observations	303,935	303,935	303,935	303,935
R-squared	0.042	0.042	0.042	0.043
Number of id	59,706	59,706	59,706	59,706

Notes: Results from estimating Eq. (2) for tangible investment. Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

⁸Appendix B.3 provides results when we add more aggregate controls, such as world GDP growth, trade openness, etc, and the results remain robust.

2.2.3 Reallocation towards tangibles

When firms cut more intangible investment than tangible investment, their asset allocation changes. To better visualize the reallocation pattern indicated by the previous results, we replace the dependent variable in Eq. (1) and (2) with the ratio of tangible fixed assets to intangible fixed assets. The estimation results are shown in Table 4. The positive sign for sp_t shows that on average, firms increase their tangibles-to-intangibles ratios when the sovereign spread goes up. This asset reallocation depends on firm characteristics: the negative sign for the $size \times spread$ interaction term and the positive sign for the $leverage \times spread$ show that small firms and high-leverage firms reallocate more resources towards tangible assets. In Section 4.2, we compare these estimation results with those using model-simulated data.

Table 4: Responses of tangibles-to-intangibles ratio

	$\log(\text{tangibles}_{i,t+1}) / \log(\text{intangibles}_{i,t+1})$						
	(1)	(2)	(3)	(4)	(5)	(6)	
sp_t				1.686***	1.453***	1.678***	
				(0.150)	(0.140)	(0.151)	
$size_{i,2006} \times sp_t$	-1.009***		-1.064***	-0.986***		-1.042***	
,	(0.166)		(0.169)	(0.165)		(0.167)	
$totallev_{i,2006} \times sp_t$		0.195	0.323**		0.199	0.327**	
, ,		(0.143)	(0.145)		(0.143)	(0.145)	
Firm controls	Yes	Yes	Yes	Yes	Yes	Yes	
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	
Sector-year FE	Yes	Yes	Yes	No	No	No	
Observations	380,769	380,769	380,769	380,769	380,769	380,769	
R-squared	0.145	0.144	0.145	0.141	0.141	0.141	
Number of id	73,697	73,697	73,697	73,697	73,697	73,697	

Notes: Results from estimating Eq. (1) and (2) for tangibles-to-intangibles ratios. Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

2.3 Additional empirical results

This section presents several key robustness checks, including using alternative measures for investment, for sovereign risk, and for firm-level leverage. More robustness checks, including accounting for depreciation, adding region-year fixed effects, adding more aggregate controls, clustering at sector level, winsorizing the sample

with alternative criteria, deflating with alternative price indices, using alternative maturities for government spreads, etc, can be found in Appendix B. None of these checks materially changes our conclusions.

In the baseline regressions, we use the log-difference of assets to measure investment. The log-difference measure captures the relative change that is symmetric, additive, and normed. However, one potential concern is that the log-difference measure omits observations with zero assets by construction, which could be more pronounced for intangible assets. To deal with this concern, we further characterize the effects of sovereign risk on the extensive margin of intangible investment and also use an alternative measure for investment.

Extensive margin of intangible investment. Here we focus on the extensive margin of intangible assets⁹, i.e., whether to continue holding any intangible assets. Denote $\mathbb{I}(intangibles_{i,t+1})$ as an indicator that equals 1 if firm i continues to hold any intangible fixed assets in period t+1, and equals 0 if firm i stops having any intangible fixed assets. Table 5 reports the results when we substitute the dependent variables with $\mathbb{I}(intangibles_{i,t+1})$ in Eq. (1) and (2). Table 5 shows that large firms and low-leverage firms are more likely to continue to hold intangible assets, consistent with the intensive margin results of adjusting intangible assets shown in Section 2.2.1 and 2.2.2.

Alternative measure for investment. To account for asset changes at both the intensive and extensive margin, we borrow a growth measure from the job creation literature (Davis and Haltiwanger (1992), Davis, Haltiwanger, and Schuh (1998), Huber, Oberhofer, and Pfaffermayr (2013), among others) that accounts for both the intensive and extensive margin. We analogously define a measure of firm investment that distinguishes between these two behaviors.

⁹For tangible assets, using the log-difference to measure investment is less of a concern (if any), because we exclude firms with negative or zero total assets, and the remaining firms have at least positive tangible assets.

Table 5: Extensive margin of intangibles

	$\mathbb{1}(intangibles_{i,t+1})$						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
sp_t				-1.789***	-1.866***	-1.788***	-1.866***
				(0.041)	(0.043)	(0.041)	(0.043)
$size_{i,2006} \times sp_t$	0.607***		0.621***		0.630***		0.643***
	(0.050)		(0.050)		(0.050)		(0.050)
$totallev_{i,2006} \times sp_t$		-0.017	-0.093**			-0.002	-0.083*
,		(0.043)	(0.043)			(0.043)	(0.043)
Firm controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Sector-year FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Observations	383,121	383,121	383,121	383,121	383,121	383,121	383,121
R-squared	0.029	0.028	0.029	0.017	0.018	0.017	0.018
Number of id	71,339	71,339	71,339	71,339	71,339	71,339	71,339

Notes: Results from estimating Eq. (1) and (2) with the dependent variable as an indicator that equals 1 if continuing to hold any intangible assets and equals 0 if ceasing to hold any intangible assets. Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

For intangible assets, firms in each year can be classified into three groups:

$$\begin{cases} \text{exiting firms} & G_x = \{i | k_{it} \neq 0, k_{i,t+1} = 0\} \\ \text{continuing firms} & G_c = \{i | k_{it} \neq 0, k_{i,t+1} \neq 0\} \\ \text{entering firms} & G_n = \{i | k_{it} = 0, k_{i,t+1} \neq 0\} \end{cases}$$

where k_{it} denotes intangible fixed assets of firm i at period t. Here "exiting" and "entering" only indicate whether firm i continues to hold intangible fixed assets. Then, investment in intangible assets (which is also the growth rate between two averages) can be defined as:

$$g(intangibles_{i,t+1}) = \frac{k_{i,t+1} - k_{it}}{0.5(k_{i,t+1} + k_{it})} = \begin{cases} -2 & i \in G_x \\ \frac{k_{i,t+1}/k_{it} - 1}{0.5(k_{i,t+1}/k_{it} + 1)} & i \in G_c \\ 2 & i \in G_n \end{cases}$$
(3)

We refer to this measure of investment as DHS (abbreviation for Davis, Haltiwanger, and Schuh (1998)) investment. The main advantage of DHS investment is that it can accommodate both entry (into the asset market, i.e., beginning to hold assets) and exit (from the asset market, i.e., no longer holding assets). It is a second-order

approximation of the log-difference growth rate around 0 and it is bounded in the range [–2,2]. We estimate both empirical specifications, Eq. (1) and (2), using DHS investment as the dependent variable.

Table 6 shows that, consistent with our baseline regression results, small firms and high-leverage firms decrease their intangible investment more than other firms during a sovereign debt crisis.

Table 6: Alternative measure for intangible investment: DHS investment

		$g(intangibles_{i,t+1})$						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	
sp _t				-2.672***	-2.964***	-2.671***	-2.975***	
				(0.150)	(0.152)	(0.150)	(0.152)	
$size_{i,2006} \times sp_t$	2.469***		2.589***		2.580***		2.697***	
	(0.174)		(0.175)		(0.171)		(0.173)	
$totallev_{i,2006} \times sp_t$		-0.465***	-0.786***			-0.415***	-0.758***	
		(0.154)	(0.155)			(0.154)	(0.155)	
Firm controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	
Sector-year FE	Yes	Yes	Yes	No	No	No	No	
Observations	392,201	392,201	392,201	392,201	392,201	392,201	392,201	
R-squared	0.032	0.031	0.032	0.013	0.014	0.013	0.015	
Number of id	71,523	71,523	71,523	71,523	71,523	71,523	71,523	

Alternative measure for sovereign risk. Another way to measure the severity of a sovereign debt crisis is to use credit ratings for sovereign bonds from a credit rating agency, such as Standard & Poor's (S&P). The credit rating from S&P ranges from AAA (prime grade) to D (default). For instance, A+ implies an upper medium grade and B+ suggests highly speculative. As shown in Table 7, the S&P credit rating for Italian sovereign bonds was downgraded from A+ to A in 2011, and further downgraded to BBB+ in 2012, BBB in 2013, and BBB- in 2014.

These letter credit ratings are converted to as discrete numerical scale between 100 (riskless) and 0 (likely to default) by Trading Economics.¹⁰ The values corresponding to Italian sovereign credit ratings from 2006 to 2016 are: A+ (80), A (75), BBB+ (65), BBB (60), BBB- (55).

¹⁰Refer to https://tradingeconomics.com/italy/rating for full correspondence table. It is easy to infer that AAA corresponds to 100, AA+ corresponds to 95, and each downgrade corresponds to a reduction by 5 in the score.

Table 7: Credit rating for Italy by S&P

Year (end of year)	S&P	Assigned number
2006	A+	80
2007	A+	80
2008	A+	80
2009	A+	80
2010	A+	80
2011	A	75
2012	BBB+	65
2013	BBB	60
2014	BBB-	55
2015	BBB-	55
2016	BBB-	55

We estimate the empirical specifications in the baseline regressions using the credit rating score rather than the debt spread. Table 8 shows the results. Column (1) shows the heterogeneous effect of credit rating on intangible investment by estimating Eq. (1). Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t+1, and 0 if firm i stops holding any intangible fixed assets. Column (4) and (5) are the results for tangible investment. In general, during the sovereign debt crisis (lower credit rating for sovereign debt), small and high-leverage firms decrease their intangible investment more than other firms, consistent with our baseline results.

Table 8: Alternative measure for sovereign risk using credit rating

Dependent variable	∆ log(intangil	$bles_{i,t+1})$	$\mathbb{1}(intangibles_{i,t+1})$	∆ log(tangib	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average	
rating _t		-0.031***	-0.010***		-0.013***	
		(0.001)	(0.000)		(0.000)	
$size_{i,2006} \times rating_t$	0.008***	0.007***	0.004***	0.001*	0.001	
	(0.001)	(0.001)	(0.000)	(0.001)	(0.000)	
$totallev_{i,2006} \times rating_t$	-0.003***	-0.003***	-0.000	-0.000	-0.000	
	(0.001)	(0.001)	(0.000)	(0.000)	(0.000)	
Firm controls	Yes	Yes	Yes	Yes	Yes	
Firm FE	Yes	Yes	Yes	Yes	Yes	
Observations	303,935	303,935	383,121	303,935	303,935	
R-squared	0.025	0.019	0.020	0.068	0.047	
Number of id	59,706	59,706	71,339	59,706	59,706	

Notes: Column (1) shows the heterogeneous effect of sovereign credit rating on intangible investment by estimating Eq. (1). Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, and 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

Alternative measure for leverage. In the baseline regressions, leverage is defined as the ratio of total debt to total assets (we refer to this ratio as "total leverage"), where total debt includes both short-term loans and long-term debt. Here we use net leverage and short leverage as alternative measures of leverage. Table 9 and Table 10 show that the baseline results are robust to these alternative definitions.

Table 9: Alternative measure for leverage: net leverage

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangib)$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average	
sp_t		-0.402**	-1.879***		-0.767***	
		(0.163)	(0.043)		(0.077)	
$size_{i,2006} \times sp_t$	1.886***	1.961***	0.628***	0.674***	0.682***	
,	(0.189)	(0.187)	(0.050)	(0.091)	(0.089)	
$netlev_{i,2006} \times sp_t$	-0.523***	-0.433**	-0.089*	0.150*	0.184**	
,	(0.179)	(0.177)	(0.048)	(0.081)	(0.079)	
Firm controls	Yes	Yes	Yes	Yes	Yes	
Firm FE	Yes	Yes	Yes	Yes	Yes	
Observations	303,715	303,715	382,908	303,715	303,715	
R-squared	0.026	0.013	0.019	0.068	0.042	
Number of id	59,583	59,583	71,209	59,583	59,583	

Notes: Estimation results here use net leverage instead of total leverage. Column (1) shows the heterogeneous effect of spreads on intangible investment by estimating Eq. (1). Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, and 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. **** p < 0.01, *** p < 0.05, * p < 0.1.

Table 10: Alternative measure for leverage: short-term leverage

Dependent variable	$\Delta \log(intangibles_{it})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tang)$	ihles:+)
Dependent variable	(1) heterogeneity	(2) average	$\frac{1}{(3) \text{ extensive}}$	(4) heterogeneity	(5) average
sp_t	(*)	-0.403**	-1.861***	_(")"""""""""""""""""""""""""""""""""""	-0.797***
,		(0.164)	(0.043)		(0.078)
$size_{i,2006} \times sp_t$	1.916***	1.991***	0.629***	0.644***	0.655***
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	(0.189)	(0.186)	(0.049)	(0.091)	(0.088)
$shortlev_{i,2006} \times sp_t$	-0.493***	-0.465***	-0.067	0.122	0.133*
,	(0.165)	(0.165)	(0.043)	(0.077)	(0.076)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	304,704	304,704	383,904	304,704	304,704
R-squared	0.025	0.013	0.018	0.068	0.042
Number of id	59,699	59,699	71,295	59,699	59,699

Notes: Estimation results here use short-term leverage instead of total leverage. Column (1) shows the heterogeneous effect of spreads on intangible investment by estimating Eq. (1). Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, and 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses.

*** p<0.01, ** p<0.05, * p<0.1.

Appendix B provides some further robustness checks, none of which materially change our conclusions. Appendix B.1 provides results when we allow for tangible and intangible assets to depreciate at different rates. Appendix B.2 additionally

controls for region-year fixed effects or province-year fixed effects, which capture possible geographical differences across sample firms. Appendix B.3 includes more aggregate controls in the empirical specifications. In the baseline regression, we use continuous standardized size and leverage in 2006 ¹¹ as our main measures for firm size and financial condition. Our results are also robust to the use of alternative group dummies (Appendix B.4 and B.5). For example, if we replace standardized size in 2006 with a dummy that equals 1 for firms larger than the median size and 0 otherwise, the baseline results are still robust. Appendix B.6 clusters the standard errors at the sector level. Appendix B.7 winsorizes the variables of interest at the top and bottom 0.5% (baseline uses 1%). In the baseline regression, the intangible and tangible fixed assets are deflated by the price of intangible and tangible assets, respectively. Appendix B.8 shows robustness to deflating intangible and tangible fixed assets by the Producer Price Index (PPI). We then replace the baseline sovereign spread with a variety of measures including an aggregate-level firm spread (Appendix B.9), sovereign spreads with different maturities (Appendix B.10), and changes in total loans to domestic non-financial corporations sector (Appendix B.11). Appendix B.12 further documents that the debt crisis depressed firm borrowings and small and high-leverage firms were more affected. Throughout all of these, our results remain robust.

2.4 Summary

Sovereign debt crises are transmitted through the financial sector to private firms, where they affect investment. In a novel contribution, we focus on firm investment in both intangible assets and tangible assets. During the recent sovereign debt crisis, firms reduced both intangible and tangible investment, but small and high-leverage firms reduced their investment in intangible assets by more than other firms. The heterogeneous responses and the reallocation pattern are robust to several alternative scenarios, such as alternative measures for investment, for sovereign risk, and for firm-level leverage, etc.

To rationalize heterogeneous firm investment behavior and quantify the aggregate impact of the sovereign debt crisis on investment, output, and productivity, we now

¹¹Please refer to Section 2.2.1 for the construction of continuous standardized size and leverage.

develop a sovereign default model with heterogeneous firms who accumulate both intangible and tangible assets.

3 Model

The economy is composed of a central government, heterogeneous firms, financial intermediaries, and households. The government issues long-term government bonds to the financial intermediaries. The probability of a government default evolves over time according to a reduced-form stochastic process. Government collects tax revenues from final goods firms and borrows from the financial intermediaries to finance the lump-sum transfers to the households and service the outstanding government debt. Government can default on its debt.

There are two types of firms: final goods firms and intermediate goods firms. Final goods firms are competitive, and they convert intermediate goods to final goods. Intermediate goods firms operate under monopolistic competition, and they use both tangible capital and intangible capital to produce differentiated goods. They borrow from the financial intermediaries to finance a fraction of all investment costs, and the borrowing interest rate is firm-specific depending on the firm's tangible collateral. The intermediate goods firms are exogenously heterogeneous in productivity and financing needs.

Households are composed of consumers and bankers, and they own the intermediate goods firms. Households decide on their consumption and how much to save with the financial intermediaries. The financial intermediaries are run by bankers who use repayments of prior loans and the savings of households to lend to the intermediate goods firms and the government.

The economy is perturbed by an aggregate shock which exogenously determines the process for government default risk. We start by describing the problems of each type of agent: the government, final goods firms, intermediate goods firms, consumers, and financial intermediaries. We then define the equilibrium for this economy.

3.1 The government

The government provides transfers to households. It finances the transfers T_t by issuing long-term bonds to the financial intermediaries and levying a tax rate τ on aggregate final goods Y_t . In every period, a fraction ϑ of debt matures and the remaining fraction remains outstanding. The government can default on its debt in every period by writing off a fraction $f \in [0,1]$ of its outstanding obligations.

Following Bocola (2016), we assume an exogenous process for government default risk. Assume that in every period the economy is hit by a shock ε_d that follows a standard logistic distribution. The default process follows:

$$d_{t+1} = \begin{cases} 1 & \text{if } \varepsilon_{d,t+1} < s_t \\ 0 & \text{otherwise,} \end{cases}$$
 (4)

where s is an AR(1) process:¹²

$$\log(s_t) = (1 - \rho_s)\log(s^*) + \rho_s\log(s_{t-1}) + \sigma_s\varepsilon_{st}, \quad \varepsilon_{st} \sim N(0, 1).$$
 (5)

The probability of default is then given by:

$$p_t^d \equiv \text{Prob}(d_{t+1} = 1|s_t) = \frac{\exp(s_t)}{1 + \exp(s_t)}.$$
 (6)

Every period, the government maximizes transfers T_t by choosing a new stock of bonds B_{t+1} , subject to its budget constraint:

$$q_t[B_{t+1} - (1-\vartheta)(1-d_t f)B_t] + \tau Y_t = \vartheta(1-d_t f)B_t + \frac{\phi_b}{2}[B_{t+1} - (1-\vartheta)(1-d_t f)B_t]^2 + T_t,$$
 (7)

where q_t is the government bond price and B_t is the stock of bonds at time t. When the government defaults, $d_t = 1$ and a fraction $f \in [0,1]$ of its outstanding obligations is written off. ϕ_b parametrizes the bond adjustment cost.¹³

¹²As explained in Bocola (2016), this default process is consistent with literature showing that self-fulfilling beliefs were key drivers of sovereign risk during the European debt crisis. It also allows us to isolate the economic mechanisms underlying the propagation of sovereign default risk.

¹³This is a parsimonious way to pin down government bonds. Alternatively, one could set a reduced-form fiscal rule, and then government bonds would balance the budget constraint as in Bocola (2016).

3.2 Final goods firms

The final good Y_t is produced from a fixed variety of intermediate goods $i \in [0, 1]$ using the technology:

$$Y_t \le \left[\int (y_{it})^{\eta} di \right]^{\frac{1}{\eta}},\tag{8}$$

where the elasticity of demand is $\frac{1}{1-\eta} > 1$. We normalize the price of final goods to one, so total taxes paid to the government is τY_t . The price of intermediate good i is p_{it} . The final goods producers choose quantities of intermediate goods $\{y_{it}\}$ to solve:

$$\max_{\{y_{it}\}} (1 - \tau) Y_t - \int p_{it} y_{it} di, \tag{9}$$

subject to (8). Thus, the demand function y_{it} for intermediate good i is solved as:

$$y_{it} = (\frac{1-\tau}{p_{it}})^{\frac{1}{1-\eta}} Y_t. \tag{10}$$

Demand function (10) shows that the demand for good i is negatively correlated with price p_{it} , and positively correlated with total output Y_t .

3.3 Intermediate goods firms

There is a unit measure of intermediate goods firms producing differentiated goods.¹⁴ Each firm i produces output y_{it} with tangible capital $k_{T,it}$ and intangible capital $k_{L,it}$:

$$y_{it} = z_{it} k_{T,it}^{\alpha_T} k_{I,it}^{\alpha_I} \tag{11}$$

where z_{it} is the idiosyncratic productivity shock, which evolves following $\log(z_{it}) = \rho_z \log(z_{it-1}) + \sigma_z \varepsilon_{it}$, where ε_{it} follows a standard normal random process. $k_{T,it}$ is the stock of tangible capital, and $k_{I,it}$ is the stock of intangible capital. α_T and α_I are the income shares of tangible capital and intangible capital, respectively. $\alpha_T + \alpha_I \leq 1$ so the production function is non-increasing returns to scale technology. $z_{it}k_{I,it}^{\alpha_I}$ determines the marginal return of tangible capital, which we refer to as TFP in the model. Tangible capital depreciates every period at the rate δ_T , and there is an

¹⁴We abstract from firm entry and exit for simplicity.

adjustment cost for changing the capital stock. Thus, the investment in tangible capital at period t is given by:

$$i_{T,it} = k_{T,it+1} - (1 - \delta_T)k_{T,it} + \Theta(k_{T,it+1}, k_{T,it}), \tag{12}$$

where $\Theta(k_{T,it+1},k_{T,it}) = \frac{\theta_T}{2}(\frac{k_{T,it+1}}{k_{T,it}} - 1 + \delta_T)^2 k_{T,it}$ is the convex adjustment cost for tangible capital. Similarly, the investment in intangible capital at period t is given by:

$$i_{I,it} = k_{I,it+1} - (1 - \delta_I)k_{I,it} + \Theta(k_{I,it+1}, k_{I,it}), \tag{13}$$

where δ_I is the depreciation rate for intangible capital, and $\Theta(k_{I,t+1},k_{I,t}) = \frac{\theta_I}{2}(\frac{k_{I,t+1}}{k_{I,t}} - 1 + \delta_I)^2 k_{I,t}$ is the adjustment cost for investing in intangible capital.

At the beginning of the period, firm i's idiosyncratic productivity z_{it} is realized. Then firm i makes choices for next period tangible capital $k_{T,it+1}$ and intangible capital $k_{T,it+1}$. We assume that firms need to borrow a fraction of their investment before production, and the financing needs λ_i are firm-specific and time-invariant. Heterogeneity in λ_i captures the heterogeneous borrowing requirement. The financial intermediaries provide loans b_{it} to firm i at a firm-specific interest rate R_{it} , and the financing requirement for firm i is:

$$b_{it} = \lambda_i (i_{T,it} + i_{I,it}), \tag{14}$$

where $i_{T,it}$ is the investment in tangible capital and $i_{I,it}$ is the investment in intangible capital. We assume the distribution of λ_i is time-invariant, and denote it by Λ . The firm-specific interest rate R_{it} depends on the tangible capital of firm i. The financial intermediaries' problem in Section 3.4 will introduce the functional form of the firm-specific interest rate.

At the end of the period, production takes place. Firm i decides on the price p_{it} for its production y_{it} , taking the demand function (10) as given, and repays its debt $R_{it}b_{it}$. The dividend of firm i at period t is:

$$D_{it} = p_{it} z_{it} k_{T,it}^{\alpha_T} k_{I,it}^{\alpha_I} - [k_{T,it+1} - (1 - \delta_T) k_{T,it} + \Theta(k_{T,it+1}, k_{T,it})] - [k_{I,it+1} - (1 - \delta_I) k_{I,it} + \Theta(k_{I,it+1}, k_{I,it})] + b_{it} - R_{it} b_{it}.$$
(15)

Taking aggregate demand Y_t and the interest rate R_{it} as given, the intermediate goods firm i chooses intangible and tangible investment to maximize the present value of the dividends $\sum_{t=0}^{\infty} \beta^t D_{it}$, subject to the demand function (10) and the working capital constraint (14). Appendix C.1 provides the analytical optimality conditions for a simplified case with no capital adjustment costs.

3.4 Households

The representative household is composed of consumers and bankers. The household's preferences over consumption C_t are given by:

$$U = \mathbb{E}_0\left[\sum_{t=0}^{\infty} \beta^t C_t\right],\tag{16}$$

where $\beta \in (0,1)$ is the discount factor and C_t is consumption in period t. The assumption of the linearity of preferences over consumption simplifies the problem. Each period, the household sends bankers to operate the financial intermediaries, and provides them with net worth N_t . At the end of the period, the bankers bring back their returns from operations F_t to the household. Alternatively, the household can save using one-period deposits M_t with the financial intermediary at the price q_t^m .

Every period, the household also receives dividends D_t from the intermediate goods firms and a lump-sum transfer T_t from the government. The budget constraint of the household is:

$$C_t + q_t^m M_t + N_t = M_{t-1} + D_t + F_t + T_t. (17)$$

The household maximizes (16) subject to (17). The optimality conditions indicate that the price of deposits is given by $q_t^m = \beta$, which is constant over time.

Financial intermediaries. The bankers run the financial intermediaries. The financial intermediaries use their net worth N_t and the deposits of the household M_t to purchase government bonds and issue loans to firms. The financial intermediaries are competitive.

The net worth N_t the household provides to the bankers consists of a constant transfer \bar{n} and the value of government bonds that did not mature:

$$N_t = \bar{n} + (1 - d_t f)(1 - \vartheta)q_t B_t.$$
 (18)

The evolution of government default risk drives the dynamics of the government bond price q_t , as well as actual default behavior d_t , which changes the value of the net worth for the financial intermediaries.

The *budget constraint* of the financial intermediaries at the beginning of the period is:

$$q_t B_{t+1} + \int b_{it} di \leq \underbrace{\bar{n} + (1 - d_t f)(1 - \vartheta)q_t B_t}_{N_t} + q_t^m M_t. \tag{19}$$

Aside from the budget constraint, the financial intermediaries are also subject to a *deposit constraint* that limits the amount of deposits the financial intermediaries can get from households:

$$q_t^m M_t \le q_t B_{t+1} + \int \theta_{it} b_{it} di. \tag{20}$$

Here we assume that government bonds can be fully pledged, while loans to firms can only be partially pledged. θ_{it} denotes the fraction of firm i's debt can be pledged. This fraction θ_{it} depends on firm i's tangible capital share, as intangible capital typically cannot be used as collateral. We assume the firm-specific fraction θ_{it} that can be pledged is given by:

$$\theta_{it} = \frac{k_{T,it}}{\bar{k}} < 1, \tag{21}$$

where \bar{k} is constant ¹⁵ and $k_{T,it}$ is the stock of tangible capital of firm i at time t. $\theta_{it} < 1$ reflects that firms' loans can't be fully pledged.

Combining the budget constraint (19) and the deposit constraint (20) gives the amount of debt that can be lent to firms (adjusted by θ_{it}) as a function of financial intermediaries' net worth, and we label this the *leverage constraint*:

$$\int (1 - \theta_{it}) b_{it} di \le N_t. \tag{22}$$

¹⁵In the quantitative part, we set \bar{k} to the maximum capital level that firms can choose in order to guarantee $\theta_{it} < 1$.

At the end of the period, the financial intermediaries receive payments from firms and the government, and repay household deposits. The return for the financial intermediaries equals:

$$F_{t+1} = (1 - d_{t+1}f)[\vartheta B_{t+1} + q_{t+1}(1 - \vartheta)B_{t+1}] + \int R_{it}b_{it}di - M_t.$$
 (23)

The financial intermediary chooses $\{M_t, B_{t+1}, b_{it}\}$ to maximize the expected return $\mathbb{E}_t[\beta F_{t+1}]$ subject to (19) and (22). The optimality conditions give the following pricing conditions for government bonds and firm loans:

$$q_t = \mathbb{E}_t \beta[(1 - d_{t+1}f)(\vartheta + q_{t+1}(1 - \vartheta))], \tag{24}$$

$$R_{it} = \frac{1 + (1 - \theta_{it})\zeta_t}{\beta},\tag{25}$$

where ζ_t is the Lagrange multiplier on the leverage constraint (22). The price for firm i's loans (25) implies that firm i will pay a premium $\frac{(1-\theta_{it})\zeta_t}{\beta}$ over the risk-free rate when the leverage constraint binds on the financial intermediaries. When firms determine their investment in tangible and intangible capital, they are aware of how their capital decisions affect their financing costs.

3.5 Equilibrium

We now define the equilibrium for this economy. Define $S = [s, B, d, \Lambda]$ as the state variables, where s is the government default risk process, B denotes the initial level of government debt, d(s) is the default event determined by the exogenous default risk process, and $\Lambda(z, \lambda, k_T, k_I)$ is the distribution of the intermediate firms. We omit the time subscript t and use x' to denote a variable x in the next period.

Given an aggregate state S, the equilibrium consists of: (i) intermediate goods firms' policies for tangible capital $k'_T(z, \lambda, k_T, k_I; S)$, intangible capital $k'_I(z, \lambda, k_T, k_I; S)$ and borrowing $b(z, \lambda, k_T, k_I; S)$, and resulting final goods firms' output Y(S); (ii) policies for aggregate tangible capital $K_T(S)$, aggregate intangible capital $K_I(S)$, and consumption C(S); (iii) price functions for firm borrowing rates $R(k_T, S)$, a government bond price function q(S), and a constant deposit price q^m ; and (iv) the distribution of

firms over idiosyncratic productivity and capitals $\Lambda(z, \lambda, k_T, k_I)$ such that: (a) policy functions of intermediate and final goods firms satisfy their optimization problem; (b) intermediate firms' borrowing rates satisfy (25) and the leverage constraint (22) holds; (c) the distribution of firms is consistent with the idiosyncratic shocks; (d) policies for households satisfy their optimal conditions; (e) next period government bonds satisfy the government budget constraint; (f) the government bond price satisfies (24); and (g) the markets for capital, goods, and bonds clear.

Next, we analyze key conditions that explain how an increase in sovereign risk affects private loan interest rates and firm investment choices.

Recall that the financial intermediaries hold government bonds and face a leverage constraint which could be binding. When the sovereign spread increases, the value of the government bonds on the financial intermediaries' balance sheets falls, which leads to a lower net worth N_t .

Recall that the loan interest rate for firm *i* is given by

$$R_{it} = \frac{1 + (1 - \theta_{it})\zeta_t}{\beta}, \text{ where } \theta_{it} = \frac{k_{T,it}}{\bar{k}} < 1.$$
 (26)

The Lagrange multiplier $\zeta_t > 0$ when the leverage constraint (22) binds. A decline in financial intermediaries' net worth N_t reduces credit supply and further tighten the leverage constraint, leading to an increase in ζ_t and thus the loan interest rate R_{it} . The firm's interest rate R_{it} also depends on its tangible assets, which can be used as collateral, through θ_{it} . Thus, firms internalize the impact of tangible capital on interest rates when choosing tangible and intangible investment. Tangible investment helps offset tightening financial conditions by decreasing a firm's interest rate, while intangible investment does not $(\partial R_{it}/\partial k_{T,it} < 0$ and $\partial R_{it}/\partial k_{I,it} = 0$ when the leverage constraint binds).

Eq. (27) shows the first order condition for firm i's next period tangible capital $k_{T,it+1}$. The left-hand-side is the marginal cost of increasing tangible capital, and the right-hand-side is the marginal benefit of tangible capital. Unlike intangible capital, investing in tangible capital has an extra benefit of decreasing the firm's interest rate,

¹⁶To simplify notation, Eq. (27) is for the case when the adjustment costs equal zero. This simplification is only for analytical purposes. We solve for the general case quantitatively.

as shown in the bracket.

$$[1 + (R_{it} - 1)\lambda_{i}] = \beta [\eta(1 - \tau)Y_{t+1}^{1-\eta}y_{it+1}^{\eta-1}(\alpha_{T}z_{it+1}k_{T,it+1}^{\alpha_{T}-1}k_{I,it+1}^{\alpha_{I}}) + (1 - \delta_{T})[1 + (R_{it+1} - 1)\lambda_{i}]$$

$$- \left[k_{T,it+2} - (1 - \delta_{T})k_{T,it+1} + k_{I,it+2} - (1 - \delta_{I})k_{I,it+1}\right]\lambda_{i}\frac{\partial R_{it+1}}{\partial k_{T,it+1}}]$$
extra benefit of tangible capital investment (27)

During sovereign debt crises, the net worth of the financial intermediaries shrinks, thus tightening the leverage constraint. When ζ_t increases, the impact of tangible capital on private sector interest rates is larger, i.e., a higher absolute value of $\partial R_i/\partial k_{T,i}$. For firms who largely rely on external financing (high- λ firms), the marginal benefit of investing in tangibles is larger. This explains our empirical finding that high-leverage firms reallocate more resources from intangible capital to tangible capital during the Italian sovereign debt crisis. The movements in the loan interest rate affect firms' capital choices and production decisions, which then affect aggregate TFP and output.

4 Quantitative Analysis

We now fit the model to Italian data. This section proceeds in four steps. Section 4.1 describes our strategy to parametrize the model, reports the parameters of the model, and assesses the model fit. Section 4.2 studies the impulse responses of firm investment, output, and TFP to an increase in government default risk, as well as the heterogeneity of the responses across firms. Section 4.3 highlights the role of endogenous intangible investment by comparing our benchmark model to two reference models. Section 4.4 reports the results of our quantitative experiment, in which we use the model to measure the output and TFP losses during the Italian debt crisis.

4.1 Parameterization

The model is at an annual frequency. There are two groups of parameters. The parameters in the first group are fixed exogenouly and are taken directly from the literature or from our empirical exercise, and those in the second group are jointly chosen to match a set of moments relating to the Italian economy and its constituent firms. Table 11 lists all the parameter values.

Fixed parameters. The fixed parameters are $\{\alpha_T, \eta, \delta_T, \delta_I, \tau, \rho_z, \sigma_z, \beta, \vartheta, \rho_s, f\}$. The parameters $\{\alpha_T, \eta\}$ affect the shape of the production function of intermediate and final goods firms. We set α_T to 0.36 following Pérez-Orive (2016). η is set to be 0.75, which is the conventional value in the literature. The depreciation rate for intangible assets δ_I is 24.3% and the depreciation rate for tangible assets δ_T is 10.1%, according to our estimation for Italian depreciation rates in 2006 using the EU KLEMS database.¹⁷ The tax rate τ is 0.24, which is the corporate tax rate in Italy. The persistence and standard deviation of the firm productivity shock are set to be 0.9516 and 0.0033, following Lopez and Olivella (2018). The discount factor β is set to match an annual risk-free rate of 2%. The fraction of bonds maturing is set to be 0.05. The parameters governing the persistence of the sovereign risk process ρ_S are taken from Bocola (2016). The haircut fraction f is consistent with empirical evidence in Cruces and Trebesch (2013).

Fitted parameters. The remaining parameters in the model include parameters for the income share of intangible capital α_I , investment adjustment costs $\{\theta_T, \theta_I\}$, parameters for the working capital requirement $\{\lambda_I, \lambda_h\}$, a constant transfer to the financial intermediaries \bar{n} , a parameter ϕ_B measuring government bond adjustment cost, and parameters for the sovereign risk process $\{\sigma_s, s^*\}$.

To set these parameters, we target 9 sample moments that reflect the behavior of firms, banks, and government. Firm statistics include the volatility of tangible capital relative to the volatility of real sales, the counterpart statistic for intangible capital, the average leverage for firms within the low-leverage and high-leverage groups in 2006, and the average asset tangibility (ratio of tangible asset over total assets). The

¹⁷For more details on the estimation of depreciation rates, please refer to Appendix B.1.

bank statistics is the ratio of credit to non-financial corporations to government credit (=0.644), which is the average value from 2006 to 2015. The government statistics include the ratio of government bonds to tax revenues in 2006, and the average spread and the volatility of the spread from 2006 to 2015.¹⁸

We solve the model using global methods.¹⁹ Given the model policy functions, we perform simulations to obtain the model-implied counterparts of our targets. We jointly choose the fitted parameters to match these 9 sample moments by minimizing the sum of the distance between the moments in the model and their corresponding counterparts in the data.

Although we choose all parameters jointly to match the moments, we can provide a heuristic description of how the moments inform specific parameters. First, the income share of intangible capital and the capital adjustment costs mostly affect firm tangibility and capital volatility. Second, the leverage statistics mainly pin down the working capital parameters $\{\lambda_l, \lambda_h\}$. Third, there is a tight relationship between \bar{n} —how much lending financial intermediaries can at least do—and the ratio of credit to non-financial corporations to government credit. In the model, this ratio is given by $\int b_i di/B$. Fourth, the ratio of government bonds to tax revenue disciplines the government adjustment cost parameter ϕ_B . Finally, the mean and volatility of the spread primarily inform the sovereign risk process parameters $\{\sigma_s, s^*\}$. Table 12 reports the moments in the data and in the model. The model generates similar statistics to the ones in the data.

4.2 Effects of elevated sovereign risk

During sovereign debt crises, firms reduce their investment in part because of higher borrowing costs. To offset tightening financial conditions, firms also reallocate their investment from intangible capital to tangible capital. That is to say, although they reduce both their tangible and intangible investment, they cut their intangible investment more.

To see this in the model, we plot the firms' impulse response functions (IRFs) to a

¹⁸Here we use 30-year government bond spreads data. Using the spread data with alternative maturities does not affect the main results.

¹⁹See Appendix D for the computational algorithm.

Table 11: Parameters

Parameter	Description	Value	Target/Source		
Fixed parameters					
α_T	Income share of tangible capital	0.36	Pérez-Orive (2016)		
η	Markup parameter	0.75	Conventional value		
δ_T	Depreciation of tangible capital	0.101	Our estimation		
δ_I	Depreciation of intangible capital	0.243	Our estimation		
au	Tax rate	0.24	Corporate tax rate		
$ ho_z$	Persistence of firm productivity shock	0.9516	Lopez and Olivella (2018)		
σ_z	Volatility of firm productivity shock	0.0033	Lopez and Olivella (2018)		
β	Discount factor	0.98	Annual risk-free rate of 2%		
v	Fraction of bonds maturing	0.05	Conventional value		
$ ho_s$	Sovereign risk process	0.95	Bocola (2016)		
f	Haircut fraction	0.37	Cruces and Trebesch (2013)		
Fitted paran	ieters				
α_I	Income share of intangible capital	0.11	Firm tangibility		
$ heta_T$	Adjustment cost of tangible investment	3.82	Vol(tangible capital)/Vol(sales)		
$ heta_I$	Adjustment cost of intangible investment	0.003	Vol(intangible capital)/Vol(sales)		
$[\lambda_l, \lambda_h]$	Working capital requirements	[0.11, 1.95]	Average leverage of firms		
\bar{n}	Constant transfer	0.03	credit to firms/credit to government		
ϕ_B	Bond adjustment cost	49.6	Average government bonds/tax revenue		
σ_{s}	Sovereign risk process	0.255	Volatility of spread		
s^*	Sovereign risk process	-3.35	Average spread		

Table 12: Moments in the data and model

	Data	Model
std(tangible capital)/std(sales)	1.606	1.592
std(intangible capital)/std(sales)	3.026	2.825
mean(leverage) for low-leverage firms	0.020	0.021
mean(leverage) for high-leverage firms	0.338	0.338
government bonds/tax revenue	2.595	2.550
credit to firms/credit to government	0.644	0.656
mean(firm tangibility)	0.865	0.850
mean(spread)	0.017	0.017
std(spread)	0.011	0.011

Notes: See Appendix A.4 for the construction of moments in the data.

positive spread shock, s, so that the government spread increases by one standard deviation. We simulate 40,000 paths for the model for 200 periods. From periods 1 to 100, the aggregate s shock follows its underlying Markov chain. In period 101, there is a positive shock to s so that the government spread increases by one standard deviation. From period 101 on, the s shocks follow the conditional Markov process. The impulse responses plot the average, across the 40,000 paths, of the variables for the last 100 periods.

Figure 2 shows these impulse responses for the firms when there is a one standard deviation increase in sovereign spreads (Panel (a)). When sovereign spreads increase, the balance sheets of the financial intermediaries deteriorate. With lower net worth, the financial intermediaries' leverage constraint binds, increasing the interest rates offered to firms, who respond by lowering their investment. Face a higher borrowing cost, the firms lower their investment. Thus both tangible assets (Panel (b)) and intangible assets (Panel (c)) decrease. However, firms reduce their intangible investment by more because intangible assets can't be used as collateral. Tangible assets, as collateral, can help lower their loan interest rate. Panel (d) shows this asset reallocation pattern where the ratio of tangible assets to intangible assets increases following the shock. Since capital decreases, firms' output decreases in response (Panel (e)). Because firms decrease their intangible investment, their TFP also decreases (Panel (f)). Note that the only shock here is the *s* shock. Thus, the model *endogenously* generates the output decline and TFP decline when the sovereign spread increases.

The model can also generate the observed heterogeneous asset reallocation for firms based on their size and leverage as in the empirical section. We use the calibrated model to mimic the Italian economy and generate model-simulated data. Consistent with the sample length in our empirical section, we focus on the Italian economy from 2006 to 2016. We feed the model a sequence of s_t shocks and z_t shocks²⁰ such that the model replicates the observed path of Italian sovereign risk and real GDP. Then we simulate the model to generate a panel sample of heterogeneous firms. Using the model-simulated sample, we run the same regressions as those in Table 4, where the dependent variable is the ratio of tangible assets to intangible assets in the next period. We investigate how the sovereign debt crisis affects this ratio and how firm characteristics (size and leverage) affect the magnitude of the reallocation.

²⁰This exogenous productivity shock summarizes the shocks that are not directly induced by the sovereign debt crisis, e.g., aggregate demand declining due to the global recession.

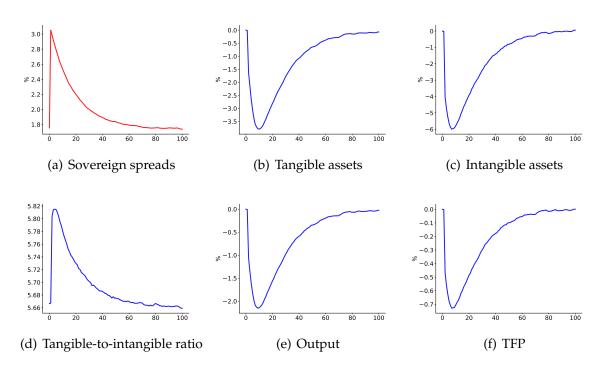


Figure 2: IRFs to a one standard deviation increase in sovereign spreads Notes: Impulse response functions to a positive s shock (so that the sovereign spread increases by one standard deviation). Before the shock, the aggregate s follows its underlying Markov chain. In period 1 in the figure, there is a positive shock to s so that the government spread increases by 1 standard deviation. From period 1 on, the s shocks follow the conditional Markov process. The impulse responses plot the average across the simulations.

Table 13 compares the estimated coefficients using the Italian data and using the model-simulated data. The coefficients from the real data are the taken from column (6) in Table 4. The model generates a similar asset reallocation pattern as in the data: firms increase their tangibles-to-intangibles ratio during the sovereign debt crisis. Moreover, small and high-leverage firms reallocate more investment compared with other firms.

Table 13: Regression results: data and model

	Data	Model
sp_t	1.678	0.536
$size_{i,2006} \times sp_t$	-1.042	-0.317
$totallev_{i,2006} \times sp_t$	0.327	0.611

Notes: Regression coefficients for the data and the model. The coefficients from the data are taken from column (6) in Table 4. The model regression specification mimics the data regression as much as possible. For example, the model regression has firm controls, firm fixed effects, and time fixed effects as in the data regression. The sample time length is consistent with data regression.

4.3 Role of intangible assets

To highlight the role of intangible assets, we compare the benchmark model to two reference models. In the first reference model, we eliminate intangible assets completely. We refer to this model as the *no-intangible-asset* model. In the second reference model, we fix intangible assets for each firm to the median level of the invariant distribution from the benchmark model and call this the *fixed-intangible-asset* model. Then we compare the benchmark model to these reference models.

We first show the results of the reference models using the same set of parameters as in the benchmark model, then we recalibrate the reference models so that they also match the data moments. Fixing the parameters across different models provides us a direct comparison of the model-generated moments under the same parameters, while recalibrating the parameters in different models allows us to compare the model implications conditional on matching target data moments.

4.3.1 Comparison under benchmark parameters

Table 14 reports the moments in different models under the benchmark parameters. In the no-intangible-asset model and the fixed-intangible-asset model, the volatility of tangible capital is around 50% higher than in the benchmark model. The average leverage for low-leverage firms is 1.5% in the reference models, lower than that in the benchmark model (2.1%). The average leverage for high-leverage firms is around 26%, also lower than in the benchmark model (34%). These differences in leverage highlight the role of intangible assets. Without endogenous intangible assets, firms only borrow for tangible investment, reducing average leverage. Also, when firms can only choose one type of investment, asset volatility is higher.

Table 14: Moments in different models (under benchmark parameters)

	benchmark	no-intangible-asset	fixed-intangible-asset
std(tangible capital)/std(sales)	1.592	2.412	2.297
std(intangible capital)/std(sales)	2.825	-	0
mean(leverage) for low-leverage firms	0.021	0.015	0.015
mean(leverage) for high-leverage firms	0.338	0.253	0.268
government bonds/tax revenue	2.550	1.784	2.356
credit to firms/credit to government	0.656	0.698	0.580
mean(firm tangibility)	0.850	1	0.854
mean(spread)	0.017	0.017	0.017
std(spread)	0.011	0.011	0.011

Notes: Moments in the benchmark, no-intangible-asset model, and fixed-intangible-asset model under the benchmark parameters.

To compare the IRFs in different models, Figure 3 plots the IRFs following the same positive *s* shock so that the sovereign spread increases by one standard deviation (Panel (a)). The red solid lines show the responses for our benchmark model, the blue dotted lines are for the no-intangible-asset model, and the black dashed lines are for the fixed-intangible-asset model.

Panel (b) of Figure 3 plots the responses of tangible assets. The benchmark model (red solid line) generates a larger decline than the fixed-intangible-asset model (black dashed line). This is because the decline in intangible assets (as shown in Panel (c)) reduces measured TFP, thus lowering the marginal product of tangible assets in the benchmark model. In contrast, intangible assets are fixed as a constant in the fixed-intangible-asset model. The benchmark model generates a slightly smaller decline in tangible assets than the no-intangible-asset model (blue dotted line). This is

because the asset reallocation channel in the benchmark model encourages increasing tangible assets, which offsets part of the decline in tangible assets from the debt crisis.

Panel (d) plots the tangible-to-intangible ratio. In our benchmark model, firms that face tightening financing conditions reallocate assets toward tangible assets, thus increasing the tangible-to-intangible ratio. However, in the fixed-intangible-asset model, the decline in tangible assets directly leads to a decline in the tangible-to-intangible ratio.

Panel (e) plots the IRFs of output. The benchmark model shows the largest decline. The reduction in intangible assets lowers measured TFP (as shown in Panel (f)) and thus leads to a larger decline in output. In contrast, the responses of TFP in the reference models are muted.

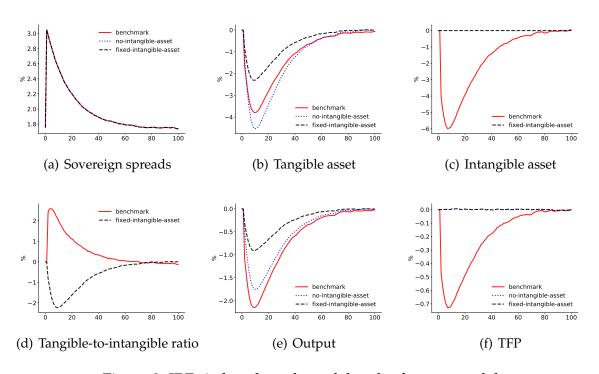


Figure 3: IRFs in benchmark model and reference models

Notes: Impulse response functions to a positive *s* shock (the sovereign spread increases by one standard deviation) in the benchmark model (red solid lines), no-intangible-asset model (blue dotted lines), and fixed-intangible-asset model (black dashed lines). The models share the same set of parameters. Before the shock, *s* follows its underlying Markov chain. In period 1, there is a positive shock to *s* so that the government spread increases by 1 standard deviation. From period 1 on, the *s* shocks follow the conditional Markov process. The impulse responses plot the average responses across the simulations.

4.3.2 Comparison under recalibration

We now recalibrate both the no-intangible-asset model and fixed-intangible-asset model so the parameters again match the key data moments. Table 15 reports the parameters in each after recalibration. The bottom panel shows that now the benchmark model and the reference models generate similar moments as in the data. The middle panel lists the parameters that are different from the benchmark.

For the no-intangible-asset model, we discard intangible assets and keep the implied labor share constant, thus the income share of tangible capital α_T is now the sum of the original shares of tangible and intangible capital (α_T =0.47). We then choose $\{\theta_T, \lambda_l, \lambda_h, \bar{n}, \phi_B\}$ to match the relative volatility of tangible capital, the average leverage for firms within the low-leverage and high-leverage groups, the ratio of government bonds to tax revenues, and the ratio of credit to non-financial corporations to government credit. For the fixed-intangible-asset model, we fix each firm's intangible assets to the median level of the invariant distribution from the benchmark model and assume no depreciation of intangible assets. The capital shares are the same as in the benchmark model (α_T =0.36, α_I =0.11). We then choose $\{\theta_T, \lambda_l, \lambda_h, \bar{n}, \phi_B\}$ to match the same set of moments as in the no-intangible-asset model.

With the recalibrated reference models, we compare the IRFs in Figure 4. The IRFs plot the responses following the same positive *s* shock so that the sovereign spread increases by one standard deviation (Panel (a)). Again, the red solid lines are the responses for our benchmark model, the blue dotted lines are for the no-intangible-asset model, and the black dashed lines are for the fixed-intangible-asset model.

Figure 4 shows several takeaways. First of all, our benchmark model generates the key empirical implications for intangible assets, asset reallocation, and measured TFP as in the data. Second, the benchmark model generates a larger decline in tangible assets. The response in the no-intangible-asset model is more persistent, as we use a higher capital share (0.47, instead of 0.36) in this reference model. Third, the benchmark model generates a larger decline in output compared with both reference models. This is due to a larger decline in tangible assets as well as a significant drop in measured TFP.

Table 15: Parameters and moments in different models (following recalibration)

	benchmark	no-intangible-asset	fixed-intangible-asset
Parameters same with benchmark			
Markup parameter η	0.75	0.75	0.75
Depreciation of tangible capital δ_T	0.101	0.101	0.101
Tax rate τ	0.24	0.24	0.24
Persistence of firm productivity shock ρ_z	0.9516	0.9516	0.9516
Volatility of firm productivity shock σ_z	0.0033	0.0033	0.0033
Discount factor β	0.98	0.98	0.98
Fraction of bonds maturing <i>ϑ</i>	0.05	0.05	0.05
Sovereign risk process ρ_s	0.95	0.95	0.95
Haircut fraction <i>f</i>	0.37	0.37	0.37
Sovereign risk process σ_s	0.255	0.255	0.255
Sovereign risk process s^*	-3.35	-3.35	-3.35
Parameters changed from benchmark			
Income share of tangible capital α_T	0.36	0.47	0.36
Income share of intangible capital α_I	0.11	-	0.11
Depreciation of intangible capital δ_I	0.243	-	0
Adjustment cost of tangible investment θ_T	3.82	5	7.3
Adjustment cost of intangible investment θ_I	0.003	-	-
Working capital requirements $[\lambda_l, \lambda_h]$	[0.11, 1.95]	[0.116,2.08]	[0.147,2.56]
Constant transfer \bar{n}	0.03	0.02	0.066
Bond adjustment cost ϕ_B	49.6	36	48
Model moments			
std(tangible capital)/std(sales)	1.592	1.597	1.603
std(intangible capital)/std(sales)	2.825	-	0
mean(leverage) for low-leverage firms	0.021	0.020	0.021
mean(leverage) for high-leverage firms	0.338	0.332	0.338
government bonds/tax revenue	2.550	2.597	2.594
credit to firms/credit to government	0.656	0.641	0.663
mean(firm tangibility)	0.850	-	0.823
mean(spread)	0.017	0.017	0.017
std(spread)	0.011	0.011	0.011

Notes: Parameters in the benchmark, no-intangible-asset model, and fixed-intangible-asset model. In both alternative models, we recalibrate so that the model moments are approximately identical to those generated by the benchmark model.

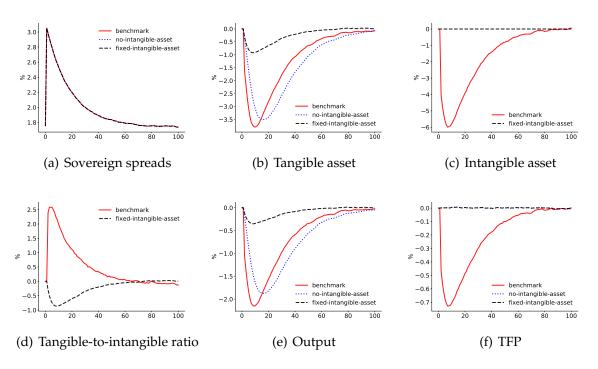


Figure 4: IRFs in benchmark model and reference models following recalibration

Notes: Impulse response functions to a positive s shock (so that the sovereign spread increases by one standard deviation) in the benchmark model (red solid lines), no-intangible-asset model (blue dotted lines), and fixed-intangible-asset model (black dashed lines). The parameters for the reference models are recalibrated so that the reference models also match the data moments. Before the shock, s follows its underlying Markov chain. In period 1, there is a positive shock to s so that the government spread increases by 1 standard deviation. From period 1 on, the s shocks follow the conditional Markov process. The impulse responses plot the average across the simulations.

4.4 Output and TFP losses from the Italian debt crisis

In this section, we quantify the output and TFP losses from the debt crisis during 2011-2013. First, as in the previous section, we feed the model a sequence of s_t shocks and z_t shocks such that the model replicates the observed path of Italian sovereign risk and real GDP. Then we construct a counterfactual scenario in which the Italian economy does not experience a sovereign debt crisis. We then compare the result of our benchmark model and that of the counterfactual model with no debt crisis. The differences between the paths of key variables in the benchmark model and those in the no debt crisis counterfactual model isolate the impact of the sovereign crisis on the Italian economy.

Figure 5 reports the time paths for sovereign spreads, GDP, and TFP during 2006-2016. The black dotted lines plot the paths in the data, the red solid lines plot the result of the benchmark model, and the blue dashed lines plot the result of the counterfactual scenario where there was no debt crisis. The unit of sovereign spreads in Panel (a) is percentage points. Panel (b) and Panel (c) plot the percentage changes of GDP and TFP from the 2006 level.

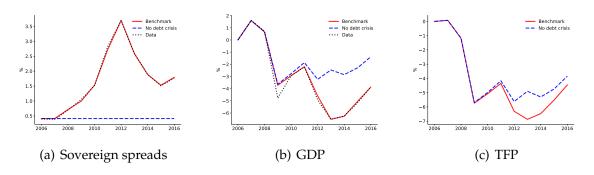


Figure 5: Measuring the costs of sovereign default risk *Notes*: Paths for Italian sovereign spreads, GDP and TFP during 2006-2016. The black dotted lines plot for the data, the red solid lines plot for the benchmark model result, and the blue dashed lines plot the results from the counterfactual scenario where there was no debt crisis.

By construction, the benchmark model (red solid lines) matches the sovereign spread and GDP in the data (black dotted lines). In general, the model needs a negative z shock and a positive s shock to reproduce the dynamics of sovereign spreads and GDP observed in the data. The sovereign spread increases from 0.4% in 2006 to 3.7% in 2012. Real GDP decreases by 4.7% from 2006 to 2009, recovers slightly

in 2010, and then decreases another 4.3% during 2011-2013.

The blue dashed lines show the corresponding result in the counterfactual no debt crisis case, where we adjust the series of s_t shocks to fix the sovereign spread at their 2006 average throughout the simulation. Thus, the sovereign spread is constant in this counterfactual case. In this scenario, there is no increase in sovereign default risk and there is no transmission of sovereign risk to the financial intermediaries or the firms.

Comparing the red solid lines and blue dashed lines, we can isolate the output losses and TFP losses directly due to the 2011-2013 Italian sovereign debt crisis. The losses associated with sovereign default risk are sizable. During 2011-2013, output would have declined by only 0.6% without the sovereign debt crisis, instead of 4.3% in the benchmark model. TFP would have declined by only 0.7% without the sovereign debt crisis, instead of 2.5% in the benchmark model. Our model indicates that sovereign default risk explains 86% of output losses and 72% of TFP losses during the 2011-2013 Italian debt crisis.

5 Conclusion

Sovereign debt crises have adverse effects on firm investment. Empirical evidence shows that firms reduce investment in both intangible assets and tangible assets during a crisis. Furthermore, although firms reduce tangible investment, they reallocate their investment away from intangible assets and towards tangible assets. This asset reallocation pattern is more pronounced in small and high-leverage firms.

We build a sovereign default model incorporating firm investment in both tangible and intangible assets to explain these empirical findings and measure the aggregate output and TFP costs of sovereign risk. Firms internalize that tangibles can be used as collateral and thus can help offset tightening financial constraints. When sovereign risk is transmitted to firms through the financial intermediaries, firms lower their investment, especially investment in intangible assets. Quantitatively, sovereign risk explains a large fraction of the output and TFP losses during the 2011-2013 Italian debt crisis.

We focus on firm investment and our approach could be generalized along other dimensions. Sovereign risk could impact firms though different channels. For example, sovereign debt crises may affect the entry and exit decisions of firms, or their import and export decisions. We believe using firm-level data to estimate the impact of sovereign risk and explore other potential mechanisms is a compelling future research opportunity.

Due to data limitations, we do not observe substantial detail on the nature of firms' intangible asset holdings. It would also be interesting to decompose intangible assets and explore if different types of intangible assets play different roles in explaining firm choices and outcomes. Understanding the heterogeneous investment behaviors of firms during crises, especially in terms of investment—which has beneficial long-run effects—provides key information for policy makers. We leave these applications to future research.

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Online Appendix to "Intangible Investment during Sovereign Debt Crisis: Firm-level Evidence"

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A Data

This section provides additional details related to Section 2.1, including the definition of the variables, sample selection procedures, and sample distributions.

A.1 Variables

1. Investment

Our baseline measure of investment in period t is defined as the log difference of intangible fixed assets between period t + 1 and period t. That is, investment in Eq. (1) denotes the investment in intangibles of firm i at the end of period t. Similarly, tangible investment is defined as the log-difference of tangible fixed assets.

Intangible and tangible fixed assets are scaled by the price of intangibles and tangibles every year. We use the EU KLEMS database²¹ to construct the price indices for intangibles/tangibles. Figure A.1 shows the asset components for intangibles/tangibles. This database reports the price for each asset type. We construct the aggregate price for intangibles as the weighted average price of each component in the right square, weighted by the share of each asset.²² An identical construction is carried out for the price of tangibles.

2. Net leverage

Net leverage is measured as the ratio of firm *i*'s net debt to total assets, where net debt is the sum of short-term loans and long term debt net of net current assets.

²¹Documentation for the EU KLEMS database, 2019 release.

²²For example, Software and Database consists of 15% of intangible assets; R&D consists of 40%; Design consists of 20%, while AdvMRes constitutes 16%.

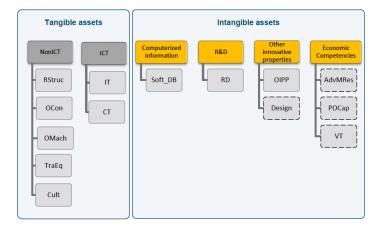


Figure A.1: Aggregates of capital services

Notes: Dashed lines indicate asset types outside the boundaries of National Accounts. Source: Report on methodologies and data construction for the EU KLEMS Release 2019 (Stehrer et al. (2019)).

3. Short leverage

Short leverage is defined as the ratio of firm i's short-term loans to total assets.

4. Total leverage

Total leverage is defined as the ratio of firm *i*'s total debt to total assets, where total debt is the sum of short-term loans and long-term debt.

5. Size

Size is measured as the log of total assets.

6. Liquidity

Liquidity is measured as the ratio of cash and cash equivalents to total assets.

7. Sales growth

Sales growth is defined as the log difference of sales, i.e. sales growth_{it} = $log(sales_{it}) - log(sales_{it-1})$.

8. Liability ratio

The liability ratio is defined as the ratio of total liabilities to total assets, where total

liabilities is the difference between total assets and shareholders funds.

9. Net current assets ratio

Net current assets ratio is measured as the ratio of net current assets to total assets.

A.2 Sample selection

Our main sample excludes (in order of operation):

- 1. Firms not in the manufacturing sector.
- 2. Firms with negative or zero total assets.
- 3. Firms with negative intangible fixed assets or tangible fixed assets.
- 4. Firms which have missing values for total assets, intangible fixed assets, or tangible fixed assets over the sample period.
- 5. Firms that were not observed in 2006.

After applying the sample selection operations, we winsorize the variables mentioned above at the top and bottom 1% of the distribution.

A.3 Aggregate distribution by size

Table A.1: Distribution of wage bills and employment by size

Wage Bill						
	Main Sample	Gopinath et al. (2017)				
1-19 employees	0.16	0.11				
20-249 employees	0.62	0.53				
250+ employees	0.23	0.36				
	Employmen	t				
	Main Sample	Gopinath et al. (2017)				
1-19 employees	0.20	0.13				
20-249 employees	0.73	0.55				
250+ employees	0.07	0.32				

A.4 Data moments

Standard deviation ratio For tangible/intangible investment $i_{T,it}$ and $i_{I,it}$, we construct the data counterparts as:

$$\begin{split} i_{T,it}^d &= k_{T,it+1}^d - (1 - \delta_T) k_{T,it}^d, \\ i_{I,it}^d &= k_{I,it+1}^d - (1 - \delta_I) k_{I,it}^d, \end{split}$$

where $k_{T,it}^d$ is real tangible fixed assets and $k_{I,it}^d$ denotes real intangible fixed assets in the data. We use the Hodrick–Prescott filter to derive the cyclical components of tangible/intangible investment along with real sales. The standard deviation of tangible investment is calculated as the average standard deviation of the cyclical component across firms. A similar calculation yields the standard deviation of intangible investment and real sales. The ratio of the standard deviation of tangible investment to that of real sales is 0.231, while the counterpart for intangible investment is 0.030.

Leverage Firms in our sample are divided into high-/low-leverage groups by each firm's total leverage in the base year of 2006. The mean leverage of the high-leverage group is 0.338, while that of the low-leverage group is 0.020.

Government bonds/tax revenue The ratio of government bonds to tax revenue is calculated by the ratio of general government debt to general government revenue, which is 2.595. Data is from the OECD.Stat database.

Firm tangibility We construct the tangibility measure for firm *i* at period t as:

$$tangibility_{it} = \frac{k_{T,it}^d}{k_{T,it}^d + k_{I,it}^d}.$$

Since our Italian data features an unbalanced sample, we first take the average tangibility across sample periods to derive the average tangibility of firm *i*. Aggregate tangibility is then defined as the mean of tangibility measures across firms.

B Robustness

This section shows some robustness checks of our main empirical findings in Section 2.

B.1 Depreciation

One difference between intangible assets and tangible assets is that they depreciate at different speeds. Relatively little is known about depreciation rates for intangibles. Corrado et al. (2009) estimates the depreciation rate of R&D capital in the U.S. to be 20%. The U.S. Bureau of Economic Analysis (BEA) places its central estimate of the depreciation rate for R&D at 15%. Pakes et al. (1978) get an average depreciation rate of 25%, using data for several European countries.

Fortunately, the EU KLEMS database provides depreciation rates for each asset type, which allows us to construct depreciation rates for intangible and tangible assets in Italy - at the aggregate level. The depreciation rate for intangible assets is the weighted average of the depreciation rates of: computer software and databases, research and development, and other intellectual property patent (IPP) assets, with the weight being the asset share. For tangible assets, the depreciation rate is the weighted average of the depreciation rates of: computing equipment, communications equipment, transport equipment, other machinery and equipment, total non-residential investment, residential structures and cultivated assets, with the weight being the asset share. The calculated depreciation rate for intangible assets is 24.3% and the depreciation rate for tangible assets is 10.1% in 2006. Our estimates are in line with the rates reported in the existing literature.

Alternatively, we can construct intangible investment as ²³:

$$\Delta \log(intangibles_{dep,it}) = [\log(y_{i,t+1}) - \log((1 - dep_{intangible}) * y_{it}] * (1 - dep_{intangible})$$

where y_{it} denotes the intangible fixed assets of firm i at period t. $dep_{intangible} = 0.243$ is the weighted average depreciation rate for intangible investment. Corresponding

²³intangible investment_{it}/ $y_{it} = [y_{i,t+1} - (1 - dep_{intangible}) * y_{it}]/y_{it} \approx [\log(y_{i,t+1}) - \log((1 - dep_{intangible}) * y_{it}] * (1 - dep_{intangible})$

tangible investment can be constructed similarly, with a depreciation rate of 0.101. Table B.2 presents the estimation results for investment with depreciation.

Table B.2: Results for investment with depreciation

Dependent variable	$\Delta \log(intangibles_{dep,it+1})$		$\mathbb{1}(intangibles_{dep,it+1})$	$\Delta \log(tangibles_{dep,it+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
$\overline{sp_t}$		-0.284**	-1.866***		-0.699***
		(0.124)	(0.043)		(0.070)
$size_{i,2006} \times sp_t$	1.513***	1.569***	0.643***	0.586***	0.596***
,	(0.145)	(0.143)	(0.050)	(0.082)	(0.080)
$totallev_{i,2006} \times sp_t$	-0.494***	-0.467***	-0.083*	0.116*	0.128*
,	(0.126)	(0.126)	(0.043)	(0.067)	(0.066)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.026	0.013	0.018	0.068	0.043
Number of id	59,706	59,706	71,339	59,706	59,706

Notes: Column (1) shows the heterogeneous effect of spreads on intangible investment by estimating Eq. (1) using $\Delta \log(intangibles_{dep,it})$ as the dependent variable. Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

Table B.3: Intangible investment with alternative depreciation rate

Dependent variable	$\Delta \log(intangibles_{CHS2009_dep,it+1})$		$\Delta \log(intangibles_E)$	$\Delta \log(intangibles_{BM2006_dep,it+1})$		$\Delta \log(intangibles_{PS1978_dep,it+1})$	
	(1) heterogeneity	(2) average	(3) heterogeneity	(4) average	(5) heterogeneity	(6) average	
sp_t		-0.300**		-0.307**		-0.281**	
		(0.131)		(0.135)		(0.123)	
$size_{i,2006} \times sp_t$	1.599***	1.658***	1.639***	1.700***	1.499***	1.555***	
	(0.153)	(0.151)	(0.157)	(0.155)	(0.143)	(0.142)	
$totallev_{i,2006} \times sp_t$	-0.522***	-0.494***	-0.535***	-0.506***	-0.489***	-0.463***	
,	(0.133)	(0.133)	(0.136)	(0.136)	(0.125)	(0.124)	
Firm controls	Yes	Yes	Yes	Yes	Yes	Yes	
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	
Observations	303,935	303,935	303,935	303,935	303,935	303,935	
R-squared	0.026	0.013	0.026	0.013	0.026	0.013	
Number of id	59,706	59,706	59,706	59,706	59,706	59,706	

Notes: Column (1) and (2) are results using an intangible depreciation rate of 0.2 (Corrado et al. (2009)). Column (3) and (4) are results using an intangible depreciation rate of 0.18 (Bernstein and Mamuneas (2006)). Column (5) and (6) are results using an intangible depreciation rate of 0.25 (Pakes et al. (1978)). Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

Table B.3 displays the results using $\Delta \log(intangibles_{dep,it+1})$ with alternative depreciation rates as dependent variables. The baseline results are robust to all choices of depreciation rate.

B.2 Region-year fixed effects

We further add region-year fixed effects and province-year fixed effects into our baseline regressions, controlling for any geographical differences. For example, firms near the border may be highly exposed to foreign trade, which is possibly less affected by the Italian sovereign debt crisis. Table B.4 and Table B.5 show that our baseline results are robust to including region-year fixed effects or province-year fixed effects.

Table B.4: Region-year FE

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		7.988	3.050		-0.147
		(5.932)	(1.921)		(2.702)
$size_{i,2006} \times sp_t$	1.986***	2.058***	0.619***	0.646***	0.674***
,	(0.194)	(0.191)	(0.050)	(0.093)	(0.091)
$totallev_{i,2006} \times sp_t$	-0.659***	-0.649***	-0.116***	0.110	0.104
,	(0.169)	(0.168)	(0.043)	(0.075)	(0.075)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Region_year FE	Yes	Yes	Yes	Yes	Yes
Observations	299,742	299,742	377,900	299,742	299,742
R-squared	0.026	0.025	0.029	0.069	0.068
Number of id	58,918	58,918	70,408	58,918	58,918

Notes: Column (1) shows the heterogeneous effect of spreads on intangible investment by estimating Eq. (1) with additional region-year fixed effects. Column (2) is the corresponding estimation of Eq. (2) with region-year fixed effects. The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

Table B.5: Province-year FE

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
$\overline{sp_t}$		8.997	-3.493		-1.324
		(11.169)	(3.070)		(6.614)
$size_{i,2006} \times sp_t$	1.977***	2.046***	0.621***	0.653***	0.683***
,	(0.194)	(0.191)	(0.050)	(0.093)	(0.091)
$totallev_{i,2006} \times sp_t$	-0.655***	-0.647***	-0.110**	0.121	0.116
, ,	(0.169)	(0.169)	(0.044)	(0.075)	(0.075)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Province-year FE	Yes	Yes	Yes	Yes	Yes
Observations	299,742	299,742	377,900	299,742	299,742
R-squared	0.029	0.028	0.032	0.071	0.070
Number of id	58,918	58,918	70,408	58,918	58,918

B.3 More aggregate controls

The baseline results for intangible investment hold when we add more aggregate controls, including GDP, world GDP growth, and trade openness.

Table B.6: Adding more aggregate controls

Dependent variable	$\Delta \log(intangibles_{i,t+1})$	$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$
sp_t	4.101***	-1.160***	1.386***
	(0.241)	(0.062)	(0.114)
$size_{i,2006} \times sp_t$	2.054***	0.634***	0.652***
,	(0.189)	(0.049)	(0.090)
$totallev_{i,2006} \times sp_t$	-0.641***	-0.094**	0.129*
, ,	(0.166)	(0.043)	(0.074)
Firm controls	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes
Observations	303,935	383,121	303,935
R-squared	0.022	0.028	0.050
Number of id	59,706	71,339	59,706

Notes: Column (1) shows the estimation of Eq. (2) with additional aggregate controls. The dependent variable in Column (2) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, 0 if firm i ceases to hold intangible fixed assets. Column (3) is the tangible investment counterpart to Column (1). Robust standard errors are in parentheses. **** p<0.01, *** p<0.05, ** p<0.1.

B.4 Group dummies

Instead of using continuous standardized size and total leverage in 2006, we construct dummies for size and total leverage. Eq. (1) and (2) are modified as:

$$\Delta \log(assets_{i,t+1}) = \beta(dx_i \times sp_t) + Controls + \delta_i + \eta_{st} + \epsilon_{it},$$

$$\Delta \log(assets_{i,t+1}) = \beta_0 sp_t + \beta_1(dx_i \times sp_t) + Controls + AggControls + \delta_i + \epsilon_{it},$$
(B.1)
$$(B.2)$$

where $dx_i \in \{dsize_{i,2006}, dtotallev_{i,2006}\}$ are the dummies for firm size or total leverage in the year 2006. $dsize_{i,2006}$ is 1 if the size of firm i is larger than the median in 2006, 0 otherwise. $dtotallev_{i,2006}$ is 1 if the total leverage of firm i is higher than the median in 2006, 0 otherwise. The baseline results hold for these alternative indicators for firm size and total leverage.

Table B.7: Group dummies

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{it+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		-1.329***	-2.267***		-1.294***
		(0.291)	(0.082)		(0.149)
$dsize_{i,2006} \times sp_t$	2.697***	2.852***	0.873***	0.706***	0.744***
,	(0.332)	(0.329)	(0.086)	(0.157)	(0.154)
$dtotallev_{i,2006} \times sp_t$	-0.812**	-0.748**	-0.026	0.341**	0.365**
,	(0.330)	(0.329)	(0.082)	(0.149)	(0.148)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	305,109	305,109	384,564	305,109	305,109
R-squared	0.025	0.013	0.018	0.068	0.042
Number of id	60,048	60,048	71,745	60,048	60,048

B.5 Group dummies based on sector median

There are concerns for Appendix B.4 because firm distribution in size or total leverage may be highly skewed in some specific sectors. Therefore, we use sector median as the standard to construct dummy indicators for size and total leverage. For Eq. (B.1) and (B.2), $dsize_{i,2006}$ is 1 if the size of firm i is larger than the sector median in 2006, and 0 otherwise. $dtotallev_{i,2006}$ is 1 if the total leverage of firm i is higher than the sector median in 2006, and 0 otherwise. The baseline results are also robust to this redefinition of the group dummies.

Table B.8: Group dummies based on sector median

Dependent variable	∆ log(intangil	$\overline{bles_{i,t+1}}$	$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		-1.324***	-2.253***		-1.267***
		(0.289)	(0.082)		(0.147)
$dsize_{i,2006} \times sp_t$	2.832***	2.782***	0.846***	0.745***	0.724***
,,,	(0.330)	(0.329)	(0.086)	(0.154)	(0.154)
$dtotallev_{i,2006} \times sp_t$	-0.710**	-0.668**	-0.019	0.308**	0.332**
,,,	(0.329)	(0.329)	(0.083)	(0.149)	(0.148)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	304,954	304,954	384,402	304,954	304,954
R-squared	0.025	0.013	0.018	0.068	0.042
Number of id	60,022	60,022	71,720	60,022	60,022

B.6 Clustering at sector-level

The baseline results are robust to clustering the standard errors at sector level.

Table B.9: Clustering at sector-level

Dependent variable	∆ log(intangil	$bles_{i,t+1})$	$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		-0.375**	-1.866***		-0.778***
		(0.169)	(0.072)		(0.118)
$size_{i,2006} \times sp_t$	1.998***	2.073***	0.643***	0.652***	0.663***
,	(0.218)	(0.193)	(0.050)	(0.112)	(0.114)
$total_{i,2006} \times sp_t$	-0.652***	-0.617**	-0.083**	0.129*	0.142**
,	(0.232)	(0.236)	(0.036)	(0.069)	(0.069)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.026	0.013	0.018	0.068	0.043
Number of id	59,706	59,706	71,339	59,706	59,706

B.7 Winsorizing at 0.5%

The baseline sample winsorizes the variables of interest at the top and bottom 1%. This section shows the baseline estimation results are robust if we instead winsorize the variables of interest at the top and bottom 0.5%.

Table B.10: 0.5% winsorizing

Dependent variable	∆ log(intangil	$bles_{i,t+1})$	$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		-0.749***	-1.882***		-0.972***
		(0.172)	(0.042)		(0.082)
$size_{i,2006} \times sp_t$	1.983***	2.091***	0.607***	0.670***	0.681***
	(0.193)	(0.190)	(0.046)	(0.093)	(0.090)
$totallev_{i,2006} \times sp_t$	-0.625***	-0.589***	-0.109**	0.018	0.024
,	(0.176)	(0.175)	(0.043)	(0.079)	(0.078)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	341,283	341,283	406,802	341,283	341,283
R-squared	0.026	0.014	0.019	0.066	0.044
Number of id	63,631	63,631	73,770	63,631	63,631

B.8 Deflating intangible and tangible fixed assets with PPI

The baseline estimation deflates intangible (tangible) fixed assets by the price of intangible (tangible) assets. We replace the price of investment with the PPI and the results remain robust.

Table B.11: PPI deflation

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		-0.772***	-1.866***		-0.719***
		(0.164)	(0.043)		(0.078)
$size_{i,2006} \times sp_t$	1.981***	2.052***	0.643***	0.651***	0.660***
	(0.191)	(0.189)	(0.050)	(0.092)	(0.089)
$totallev_{i,2006} \times sp_t$	-0.640***	-0.603***	-0.083*	0.133*	0.142*
	(0.166)	(0.166)	(0.043)	(0.074)	(0.074)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,941	303,941	383,121	303,941	303,941
R-squared	0.025	0.012	0.018	0.065	0.042
Number of id	59,705	59,705	71,339	59,705	59,705

B.9 Alternative measure of debt crisis severity: firm spreads

Figure B.2 plots the Italian firm-level spread which is defined as the gap between the interest rate for loans (other than bank overdrafts) to non-financial corporations and the risk-free interest rate. The nominal risk-free rate is given by the Eurosystem main refinancing operations interest rate. Data was accessed via the Bank of Italy Statistical Database. During the Italian sovereign debt crisis, the interest rate spread for firms also increased. We replace the sovereign spread with the firm spread and the baseline results do not vary too much.

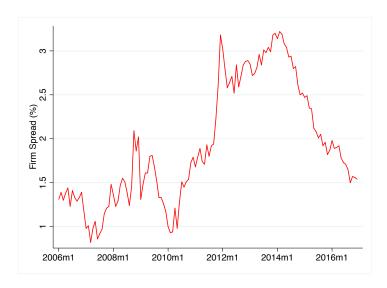


Figure B.2: Italy, firm spreads

Notes: A measure of average interest rate spreads for firms. The series is given by the spread over the risk-free rate of the interest rate for Italian non-financial corporations on non-overdraft loans (total maturity). The nominal risk-free rate is given by the Eurosystem main refinancing operations interest rate. Data source: Bank of Italy Statistical Database.

Table B.12: Alternative measure of debt crisis severity: firm spreads

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity (2) average		(3) extensive	(4) heterogeneity	(5) average
spt		-2.552***	-0.912***		-0.523***
		(0.159)	(0.041)		(0.079)
$size_{i,2006} \times sp_t$	0.950***	0.730***	0.102**	0.186**	0.016
	(0.186)	(0.181)	(0.046)	(0.092)	(0.090)
$totallev_{i,2006} \times sp_t$	-0.351**	-0.279*	-0.050	0.127*	0.143**
	(0.160)	(0.158)	(0.040)	(0.073)	(0.073)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.025	0.014	0.013	0.068	0.042
Number of id	59,706	59,706	71,339	59,706	59,706

B.10 Alternative measure of debt crisis severity: spreads using yields of government bonds with different maturities

We replace the baseline 30-year government bond spread with 1-year/5-year/10-year government bond spreads, and our baseline results are robust to alternative spreads.

Table B.13: Results using 1-year government bond yield spreads

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangit)$	$\overline{oles_{i,t+1}}$
	(1) heterogeneity (2) average		(3) extensive	(4) heterogeneity	(5) average
sp_t		2.021***	-1.696***		0.220**
		(0.200)	(0.053)		(0.095)
$size_{i,2006} \times sp_t$	1.964***	2.189***	0.636***	0.758***	0.853***
	(0.230)	(0.229)	(0.061)	(0.112)	(0.110)
$totallev_{i,2006} \times sp_t$	-0.591***	-0.608***	-0.115**	0.140	0.140
	(0.201)	(0.202)	(0.053)	(0.091)	(0.090)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.025	0.014	0.015	0.068	0.042
Number of id	59,706	59,706	71,339	59,706	59,706

Notes: Column (1) shows the heterogeneous effect of spreads on intangible investment by estimating Eq. (1). Column (2) is the corresponding estimation of Eq. (2). The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. *** p<0.01, *** p<0.05, * p<0.1.

Table B.14: Results using 5-year government bond yield spreads

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp _t		0.684***	-1.178***		-0.240***
		(0.134)	(0.036)		(0.064)
$size_{i,2006} \times sp_t$	1.440***	1.544***	0.393***	0.523***	0.546***
,,,	(0.155)	(0.153)	(0.041)	(0.075)	(0.073)
$totallev_{i,2006} \times sp_t$	-0.419***	-0.418***	-0.084**	0.128**	0.139**
,	(0.135)	(0.135)	(0.035)	(0.060)	(0.060)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.026	0.013	0.015	0.068	0.042
Number of id	59,706	59,706	71,339	59,706	59,706

Table B.15: Results using 10-year government bond yield spreads

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
sp_t		0.228	-1.405***		-0.401***
		(0.146)	(0.039)		(0.070)
$size_{i,2006} \times sp_t$	1.644***	1.723***	0.451***	0.570***	0.574***
	(0.170)	(0.169)	(0.045)	(0.082)	(0.080)
$totallev_{i,2006} \times sp_t$	-0.497***	-0.484***	-0.088**	0.142**	0.155**
, ,	(0.148)	(0.148)	(0.039)	(0.066)	(0.065)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.026	0.013	0.016	0.068	0.042
Number of id	59,706	59,706	71,339	59,706	59,706

B.11 Alternative measure of debt crisis severity: total loans to domestic non-financial corporations sector, 12-month percentage changes

This section uses the changes in total loans to the domestic non-financial corporations sector as our measure of the severity of the debt crisis. As shown in Figure B.3, loans dropped significantly during 2011-2013 Italian sovereign debt crisis. Declining loans to non-financial corporations suggests tightening financial conditions for firms. Table B.16 reports the regression results when we replace the sovereign spread with the changes in total loans to domestic non-financial corporations. Consistent with the baseline results, small firms and high-leverage firms have lower intangible investment.

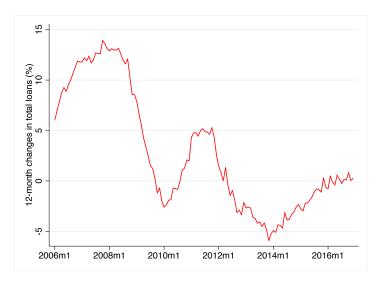


Figure B.3: Italy, total loans: 12-month percentage changes *Notes*: Total loans to domestic non-financial corporations sector: 12-month percentage changes (corrected for securitization). We use the observation in each December as the yearly observation. Data source: Bank of Italy Statistical Database.

Table B.16: Alternative measure for severity of debt crisis: total loans - 12-month % changes

Dependent variable	$\Delta \log(intangibles_{i,t+1})$		$\mathbb{1}(intangibles_{i,t+1})$	$\Delta \log(tangibles_{i,t+1})$	
	(1) heterogeneity	(2) average	(3) extensive	(4) heterogeneity	(5) average
Δloans		2.351***	0.981***		1.691***
		(0.064)	(0.017)		(0.033)
$size_{i,2006} \times \Delta loans$	-0.809***	-0.794***	-0.365***	-0.183***	-0.176***
	(0.074)	(0.073)	(0.020)	(0.038)	(0.037)
$totallev_{i,2006} \times \Delta loans$	0.291***	0.258***	0.005	-0.012	-0.013
,,	(0.065)	(0.064)	(0.017)	(0.030)	(0.030)
Firm controls	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes
Observations	303,935	303,935	383,121	303,935	303,935
R-squared	0.026	0.019	0.024	0.068	0.056
Number of id	59,706	59,706	71,339	59,706	59,706

Notes: Column (1) shows the heterogeneous effect of total loans changes on intangible investment. Column (2) reports the result when we relax the sector-year fixed effects and add the total loans changes as one independent variable. The dependent variable in Column (3) is a dummy variable which equals 1 if firm i continues to hold intangible fixed assets in period t, 0 if firm i ceases to hold intangible fixed assets. Column (4) and (5) are the tangible investment counterparts to Column (1) and (2). Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

B.12 Firm-level borrowing

In the main text, we focus on how firm investments are affected by the sovereign debt crisis. We emphasize the key role of firm debt and financial frictions in generating the (heterogeneous) investment responses across firms.

In this section, we show that firm borrowing is indeed affected by the debt crisis and the responses are heterogeneous. We use the log-difference of debt stock to measure firm borrowing, where the debt stock consists of both short-term debt and long-term debt. We replace the dependent variable in Eq. (1) and (2) with firm borrowing. Table B.17 reports the results. The negative sign for sp_t shows that firms borrow less during the sovereign debt crisis. The borrowing responses are heterogeneous. Firms that are less financially constrained, large firms and low-leverage firms, are less affected. In contrast, small firms and high-leverage firms are associated with major declines in borrowing.

Table B.17: Responses of firm borrowing

	$\Delta \log(debt_{i,t+1})$						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
sp _t				-2.060***	-2.193***	-1.932***	-2.064***
•				(0.164)	(0.182)	(0.200)	(0.213)
$size_{i,2006} \times sp_t$	0.616***		0.628***		0.486**		0.513**
,	(0.208)		(0.208)		(0.205)		(0.205)
$totallev_{i,2006} \times sp_t$		-0.207	-0.241			-0.413**	-0.442**
,		(0.189)	(0.189)			(0.189)	(0.190)
Firm controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Firm FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Sector-year FE	Yes	Yes	Yes	No	No	No	No
Observations	186,751	186,751	186,751	186,751	186,751	186,751	186,751
R-squared	0.174	0.174	0.174	0.155	0.156	0.156	0.156
Number of id	44,582	44,582	44,582	44,582	44,582	44,582	44,582

Notes: Results from estimating Eq. (1) and (2) using the log-difference of total debt as dependent variable, where total debt is the sum of short-term debt and long-term debt. Robust standard errors are in parentheses. *** p<0.01, ** p<0.05, * p<0.1.

C Proofs

C.1 Intermediate Goods Firms

Each intermediate goods firm i takes the aggregate demand Y_t and interest rate R_{it} as given, and maximizes the present value of dividends, which is subject to the demand function (10) and the working capital constraint (14).

$$\max \sum_{t=0}^{\infty} \beta^t D_{it},$$

where

$$D_{it} = p_{it}z_{it}k_{T,it}^{\alpha_T}k_{I,it}^{\alpha_I} - [k_{T,it+1} - (1 - \delta_T)k_{T,it} + \Theta(k_{T,it+1}, k_{T,it})] - [k_{I,it+1} - (1 - \delta_I)k_{I,it} + \Theta(k_{I,it+1}, k_{I,it})] + b_{it} - R_{it}b_{it},$$

subject to

$$y_{it} = (\frac{1-\tau}{p_{it}})^{\frac{1}{1-\eta}} Y_t,$$

 $b_{it} = \lambda_i (i_{T,it} + i_{I,it}).$

When there's no adjustment cost $(\theta_T = \theta_I = 0)^{24}$, the first order conditions (FOCs) are given by:

$$\begin{split} [k_{T,it+1}] \quad [1 + (R_{it} - 1)\lambda_i] = & \beta [\eta(1 - \tau)Y_{t+1}^{1 - \eta}y_{it+1}^{\eta - 1}(\alpha_T z_{it+1}k_{T,it+1}^{\alpha_T - 1}k_{I,it+1}^{\alpha_I}) \\ & \quad + (1 - \delta_T)[1 + (R_{it+1} - 1)\lambda_i] \\ & \quad - \left[k_{T,it+2} - (1 - \delta_T)k_{T,it+1} + k_{I,it+2} - (1 - \delta_I)k_{I,it+1}\right]\lambda_i \frac{\partial R_{it+1}}{\partial k_{T,it+1}} \end{split}$$

$$\begin{aligned} [k_{I,it+1}] \quad [1 + (R_{it} - 1)\lambda_i] = & \beta[\eta(1 - \tau)Y_{t+1}^{1-\eta}y_{it+1}^{\eta - 1}(\alpha_I z_{it+1}k_{T,it+1}^{\alpha_T}k_{I,it+1}^{\alpha_I - 1}) \\ & + (1 - \delta_I)[1 + (R_{it+1} - 1)\lambda_i]] \end{aligned}$$

²⁴This simplification is only for analytical purposes. We solved for the general case in the quantitative section.

Combining both FOCs, we get:

$$\eta(1-\tau)Y_{t+1}^{1-\eta}y_{it+1}^{\eta}(\frac{\alpha_T}{k_{T,it+1}} - \frac{\alpha_I}{k_{I,it+1}}) + (\delta_I - \delta_T)[1 + (R_{it+1} - 1)\lambda_i] = \lambda_i \frac{\partial R_{it+1}}{\partial k_{T,it+1}} \Big[k_{T,it+2} - (1 - \delta_T)k_{T,it+1} + k_{I,it+2} - (1 - \delta_I)k_{I,it+1} \Big]$$

C.2 Households

The problem of the households is to maximize their preferences (16), subject to the budget constraint (17). The FOCs are given as:

$$[C_t] \qquad \beta^t = \xi_t \tag{C.3}$$

$$[M_t] \qquad \xi_{t+1} = q_t^m \xi_t \tag{C.4}$$

where ξ_t is the Lagrange multiplier on the budget constraint (17). Then we obtain:

$$q_t^m = \beta \tag{C.5}$$

Notice the price of deposits is constant over time.

C.3 Financial intermediaries

The financial intermediary's problem is:

$$\max_{\{M_t, B_{t+1}, b_{it}\}} E_t[\beta F_{t+1}]$$
 (C.6)

where

$$F_{t+1} = (1 - d_{t+1}f)[\vartheta B_{t+1} + q_{t+1}(1 - \vartheta)B_{t+1}] + \int R_{it}b_{it}di - M_t.$$

subject to

$$(\mu_t) \qquad q_t B_{t+1} + \int b_{it} di \le N_t + q_t^m M_t, \tag{C.7}$$

$$(\zeta_t) \qquad \int (1 - \theta_{it}) b_{it} di \le N_t. \tag{C.8}$$

The FOCs are:

$$[b_{it}]$$
 $\beta R_{it} - \mu_t - (1 - \theta_{it})\zeta_t = 0$ (C.9)

$$[B_{t+1}] \qquad \beta \mathbb{E}_t[(1 - d_{t+1}f)(\vartheta + q_{t+1}(1 - \vartheta))] - \mu_t q_t = 0$$

$$[M_t] \qquad -\beta + \mu_t q_t^m = 0$$
(C.10)

$$[M_t] \qquad -\beta + \mu_t q_t^m = 0 \tag{C.11}$$

Using the FOC from the households' problem $q_t^m = \beta$, we can get the pricing conditions for government bonds (24) and firm loans (25).

D Numerical Solution

The aggregate state of the economy includes the aggregate shock to the government default risk process s and the initial level of government debt B. The government chooses borrowing B'(s, B, d) to maximize government expenditure, subject to the budget constraint and the bond price. The exogenous default risk process determines the default event d(s) and government bond price q(s).

The aggregate state variables and government sector outcome variables are relevant for the firms' choices for tangible capital and intangible capital only because they affect the firms' loan interest rate through the slackness of the leverage constraint ζ when the net worth of the financial intermediaries N changes. Thus, ζ and the idiosyncratic states $\{z,\lambda,k_T,k_I\}$ are sufficient to determine the firms' choices. For any state (s,B,d), net worth is given by $N(s,B,d)=\bar{n}+(1-df)(1-\vartheta)q(s)B$. Net worth affects the firm specific loan interest rate $R_{it}=\frac{1+(1-\theta_{it})\zeta_t}{\beta}$, where ζ_t is the Lagrange multiplier for the leverage constraint $\int (1-\theta_{it})b_{it}di \leq N_t$. When the leverage constraint does not bind, $\zeta_t=0$, otherwise, $\zeta_t>0$.

The government default risk transmits to the firms through the leverage constraint. When government defaults (d = 1) or the default risk increases so that the bond price q decreases, financial intermediaries' net worth N decreases. With lower net worth, the leverage constraint becomes binding, or binds more tightly. A tighter leverage constraint increases the shadow price of borrowing (Lagrange multiplier ζ), and thus increases the firm loan interest rate R.

We now describe the computational algorithm in detail.

- 1. Create grid points for the default risk process *s*, government bonds *B*, and an indicator *d* to denote whether the government is in default or not.
- 2. Create grid points for the productivity shock z, financing needs λ , tangible capital k_T , intangible capital k_I , and the Lagrange multiplier $\zeta \in [0, \zeta_{max}]$.
- 3. Guess the initial government bond price q(s).
- 4. Guess the initial value function of firm $V_0(z, \lambda, k_T, k_I, \zeta)$ and aggregate output $Y_0(\Lambda(z, \lambda, k_T, k_I), \zeta)$.

- 5. Update the bond price using Eq. (24).
- 6. Update the value function and policy functions $k'_T(z, \lambda, k_T, k_I, \zeta)$, $k'_I(z, \lambda, k_T, k_I, \zeta)$ and $b(z, \lambda, k_T, k_I, \zeta)$, and compute the stationary distribution.
- 7. Update aggregate output $Y_{upd}(\Lambda(z,\lambda,k_T,k_I),\zeta)$ and an aggregate term that summarizes firm loan demand b: $X(\Lambda(z,\lambda,k_T,k_I),\zeta) \equiv \int (1-\theta_{it})b_{it}di$.
- 8. Iterate until the firm value function, aggregate output, and the government bond price converge.
- 9. Given shocks and government policies $\{s, B, d\}$, compute net worth N(s, B, d).
- 10. Compute the equilibrium Lagrange multiplier $\zeta(s,B,d)$: if $X(\Lambda(z,\lambda,k_T,k_I),0) \le N(s,B,d)$, then $\zeta=0$, otherwise, ζ is chosen such that $X(\Lambda(z,\lambda,k_T,k_I),\zeta)=N(s,B,d)$.