Exam 1:

Due Date: Sunday, October 11, at 11:59pm.

This exam contains <u>three problems</u> asking multiple questions. Please answer each question in detail with clear explanation. :)

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Problem 1.

A. What is the growth of the below functions? Explain in detail and show ALL the work.

```
Test1(a)
  n = a.length;
  key = bad_fun(n<sup>4</sup>); // time complexity of bad_fun(k) is O(k!)
  print(key);
  binary_search(a,key);
end
```

```
Test2(n) for i = 1:n if(i<n/10) binary_search(a, key); //a.length = n^3, key does not exist in a else linear_search(a, a[1]); //a.length = n^3, key == a[1] end end
```

- **B.** Compare the growth of $T_{Test1}(n)$ and $T_{Test2}(n)$. Show all the work.
- C. Let's say you can finish running $T_{Test2}(10^6)$ in 1 sec. Could you estimate when you finish running $T_{Test1}(100)$?

end

<u>Problem 2.</u> A sorted array and a random number are given to you. Develop an algorithm to find the total number of the repetitions of the given number.

- A. How would you find the total number of repetitions for the given number? (Note: If you have multiple answers in mind, break them apart and explain each one separately.) Explain each solution/algorithm in a few lines.
- **B.** Write the pseudocode for the best algorithm you came up with.
- **C.** Implement your answer using any programming language you want to.
- **D.** What is the time complexity of your answer? **Explain in detail and show all the work**. (**Note**: If possible, break your code/pseudocode to different parts, calculate the runtime for each step and then try to calculate the total running time based on that.)

<u>Problem 3.</u> A random array of size n is given to you. You know that the elements in the array are nonnegative integers less than n. Develop an algorithm to <u>find the mode</u> (the value that appears most) <u>and the numbers repeated more than once.</u>

```
Example 1: Input: a = [6, 0, 1, 5, 1, 1, 4, 5], → Output1: "1 is the mode."
Output2: "5 was repeated 2 times,
1 was repeated 3 times."
Example 2: Input: a = [0, 2, 4, 2, 2, 0, 0, 5, 4], → Output1: "0 and 2 are the mode."
Output2: "0 was repeated 3 times,
2 was repeated 3 times,
4 was repeated 2 times.""
```

(Hint: Remember the algorithms we learned in the class (searchings and sortings). Could you pick a good one and use parts of it to solve this question?)

- A. How would you find the mode and the numbers occurring more than once? (Note: If you have multiple answers in mind, break them apart and explain each one separately.) Explain each solution/algorithm in a few lines.
- **B.** Write the pseudocode for the best algorithm you came up with.
- **C.** Implement your answer using any programming language you want to.
- **D.** What is the time complexity of your answer? **Explain in detail and show all the work**. (**Note**: If possible, break your code/pseudocode to different parts, calculate the runtime for each step and then try to calculate the total running time based on that.)