BU CS320 Assignment 6: Context Free Grammars

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1. Given the following grammar where $\langle expr \rangle$ is the starting symbol:

Demonstrate the grammar above is ambiguous.

Suppose we want to derive the statement let z = 3 in z; c

Left-associative:

Leit-associative.

let z = 3 in z; c

<expr>

<expr> ; <expr> let <id> = <expr> in <expr> ; <expr> let z = <expr> in <expr> ; <expr> let z = <dig> in <expr> ; <expr> let z = 3 in <expr> ; <expr> let z = 3 in <id> ; <expr> let z = 3 in z ; <expr>

Right-associative:

```
<expr>
let <id> = <expr> in <expr>
let <id> = <expr> in <expr>; <expr>
let <id> = <expr> in <expr>; <id> let <id> = <expr> in <expr>; <id> let <id> = <expr> in <expr>; c
    let <id> = <expr> in <id>; c
    let <id> = <expr> in z; c
    let <id = <dig in z; c
    let <id = 3 in z; c
    let z = 3 in z; c</pre>
```

The grammar above generates at least 2 distinct parse trees for the sentenial form "let z = 3 in z; c". This can be seen in the left-associative and right-associative derivations, which shows that the sentence can be derived from two different definitions of <expr> - <expr> ; <expr> and let <math><id> = <expr> in <expr>. Therefore, the grammar is ambiguous.

2. Modify the grammar (reproduced below) to be unambiguous. Hint: There is not just one way.

```
\begin{array}{ll} \langle id \rangle & ::= \ \mathbf{a} \ | \ \mathbf{b} \ | \ \mathbf{c} \ | \ ... \ | \ \mathbf{z} \\ \\ \langle dig \rangle & ::= \ \mathbf{0} \ | \ \mathbf{1} \ | \ \mathbf{2} \ | \ ... \ | \ \mathbf{9} \\ \\ \langle expr \rangle & ::= \ () \ | \ \langle dig \rangle \ | \ \langle id \rangle \\ \\ & | \ \ \mathrm{let} \ \langle id \rangle = \langle expr \rangle \ \mathrm{in} \ \langle expr \rangle \\ \\ & | \ \ \langle expr \rangle \ ; \ \langle expr \rangle \\ \\ & | \ \ \mathrm{begin} \ \langle expr \rangle \ \mathrm{end} \end{array}
```

3. Demonstrate your modified grammar fixes the previously shown ambiguity.

Suppose we want to derive the statement let z = 3 in z; c

Attempt 1:

<expr>
let <id> = <expr> in <term>
let z = <expr> in <term>
let z = <term> in <term>
let z = <term> in <term>
let z = <val> in <term>
let z = <dig> in <term>
let z = 3 in <term>

Not able to derive the sentence let z = 3 in z; c

Attempt 2:

<expr>
<expr>; <term>
let <id> = <expr> in <term>; <term>
let z = <expr> in <term>; <term>
let z = <term> in <term>; <term>
let z = <term> in <term>; <term>
let z = <val> in <term>; <term>
let z = <dig> in <term>; <term>
let z = 3 in <term>; <term>
let z = 3 in <<term>
let z = 3 in <<val>; <term>
let z = 3 in z; <t

Only way to derive the sentence "let z = 3 in z; c". Therefore, grammar is no longer ambiguous.