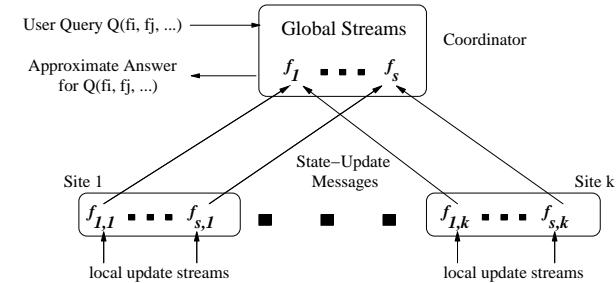
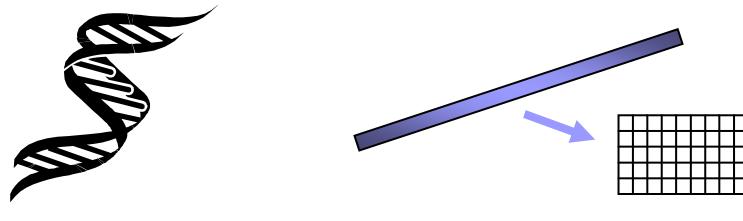


Processing Massive Data Streams



Minos Garofalakis

Yahoo! Research & UC Berkeley

minos@acm.org

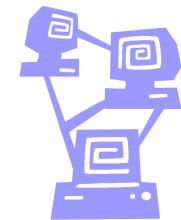
(Thanks to: Graham Cormode, Johannes Gehrke, Rajeev Rastogi)

Streams – A Brave New World

- Traditional DBMS: data stored in *finite, persistent data sets*
- Data Streams: distributed, continuous, unbounded, rapid, time varying, noisy, . . .
- Data-Stream Management: variety of modern applications
 - Network monitoring and traffic engineering
 - Sensor networks
 - Telecom call-detail records
 - Network security
 - Financial applications
 - Manufacturing processes
 - Web logs and clickstreams
 - Other massive data sets...

Massive Data Streams

- Data is *continuously growing* faster than our ability to store or index it
- There are 3 Billion **Telephone Calls** in US each day, 30 Billion emails daily, 1 Billion SMS, IMs
- **Scientific data:** NASA's observation satellites generate billions of readings each per day
- **IP Network Traffic:** up to 1 Billion packets per hour per router. Each ISP has many (hundreds) routers!
- Whole **genome sequences** for many species now available: each megabytes to gigabytes in size



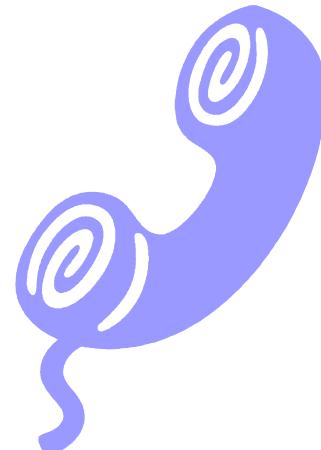
YAHOO!
RESEARCH

Massive Data Stream Analysis

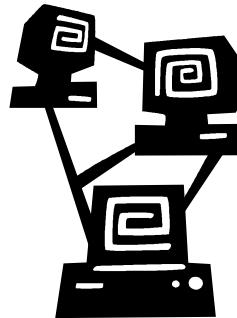
Must analyze this massive data:

- Scientific research (monitor environment, species)
- System management (spot faults, drops, failures)
- Business intelligence (marketing rules, new offers)
- For revenue protection (phone fraud, service abuse)

Else, why even measure this data?

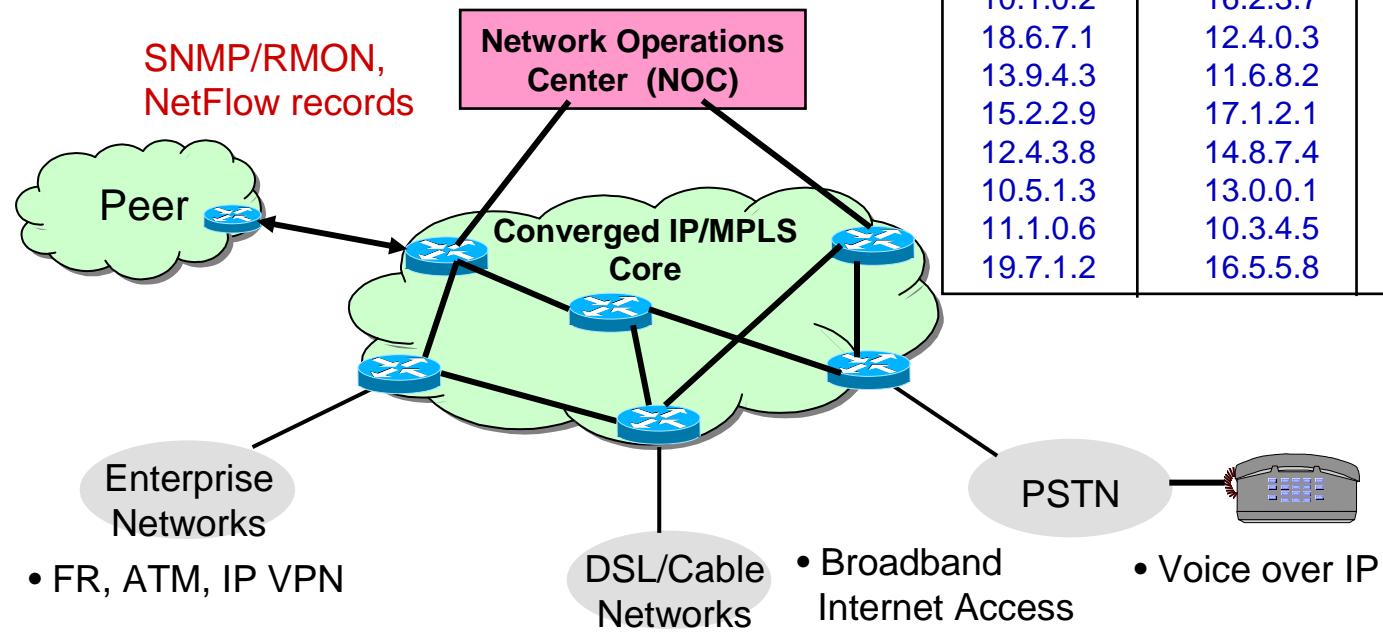


Example: IP Network Data



- Networks are sources of massive data: the **metadata** per hour per IP router is gigabytes
- Fundamental problem of data stream analysis:
*Too much information to **store** or transmit*
- So process data as it arrives – *One pass, small space:*
*the **data stream** approach*
- *Approximate answers* to many questions are OK, if there are guarantees of result quality

IP Network Monitoring Application



Source	Destination	Duration	Bytes	Protocol
10.1.0.2	16.2.3.7	12	20K	http
18.6.7.1	12.4.0.3	16	24K	http
13.9.4.3	11.6.8.2	15	20K	http
15.2.2.9	17.1.2.1	19	40K	http
12.4.3.8	14.8.7.4	26	58K	http
10.5.1.3	13.0.0.1	27	100K	ftp
11.1.0.6	10.3.4.5	32	300K	ftp
19.7.1.2	16.5.5.8	18	80K	ftp

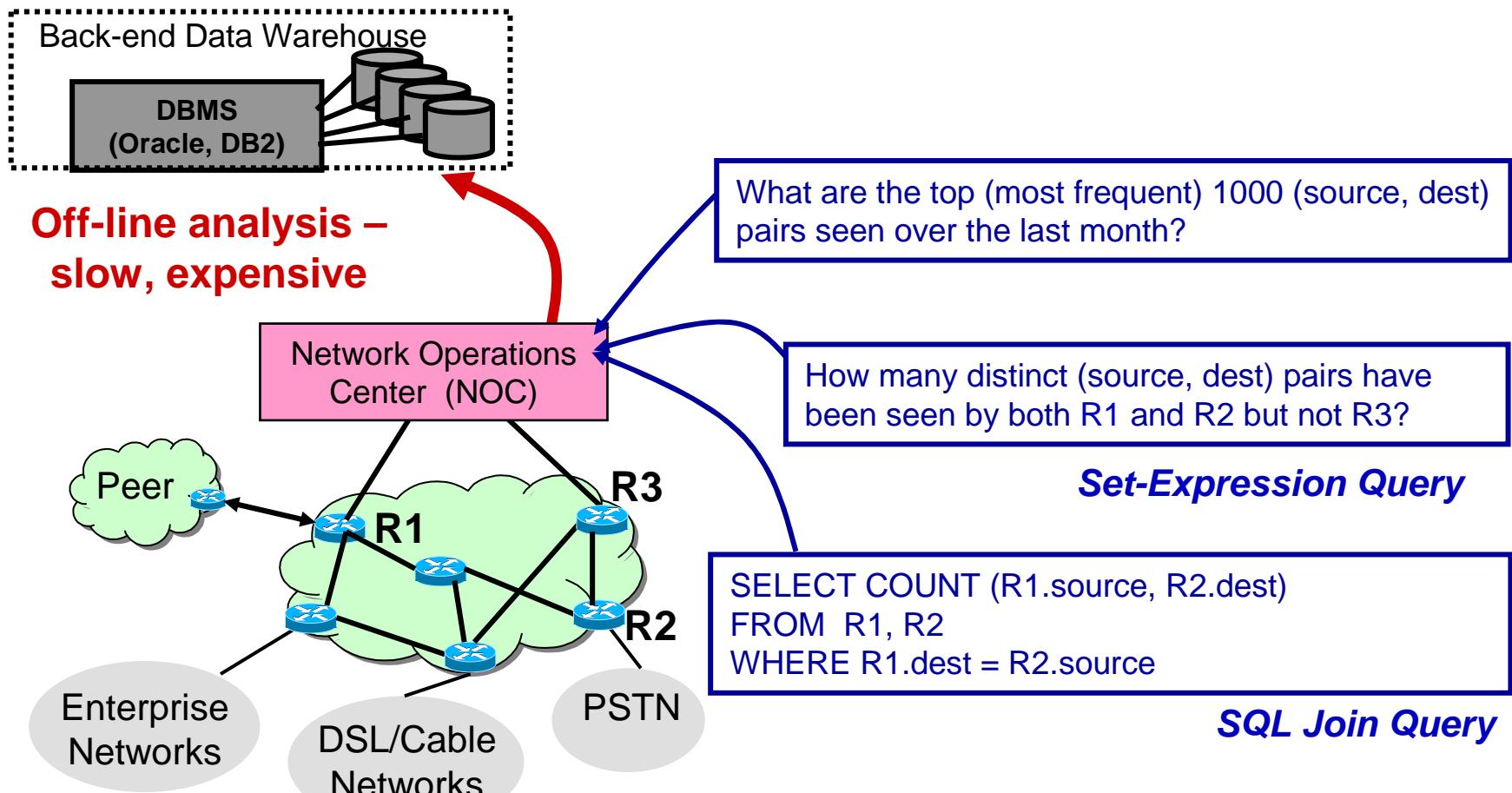
Example NetFlow
IP Session Data

- 24x7 IP packet/flow data-streams at network elements
- Truly massive streams arriving at rapid rates
 - AT&T/Sprint collect ~1 Terabyte of NetFlow data each day
- Often shipped off-site to data warehouse for off-line analysis

Packet-Level Data Streams

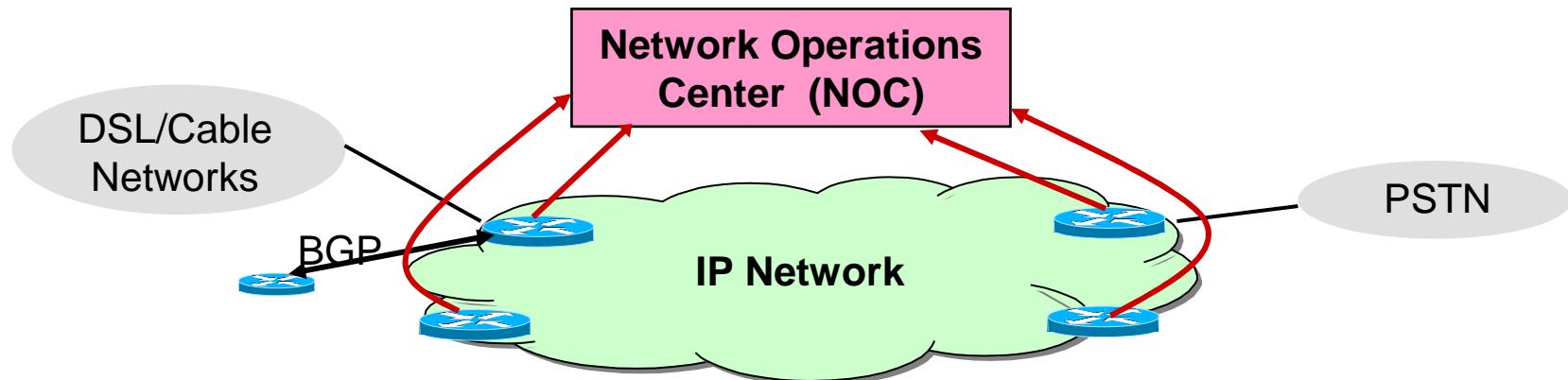
- Single 2Gb/sec link; say avg packet size is 50bytes
- Number of packets/sec = 5 million
- Time per packet = 0.2 microsec
- If we only capture **header information** per packet: src/dest IP, time, no. of bytes, etc. – at least 10bytes.
 - Space per second is 50Mb
 - Space per day is 4.5Tb per link
 - ISPs typically have hundreds of links!
- Analyzing **packet content streams** – whole different ballgame!!

Network Monitoring Queries



- Extra complexity comes from *limited space and time*
- Will introduce solutions for these and other problems

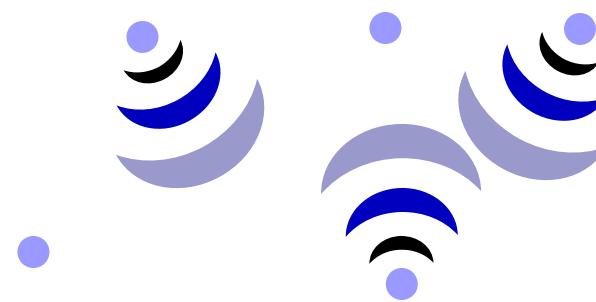
Real-Time Data-Stream Analysis



- Must process network streams in *real-time* and *one pass*
- Critical NM tasks: fraud, DoS attacks, SLA violations
 - Real-time traffic engineering to improve utilization
- *Tradeoff result accuracy vs. space/time/communication*
 - Fast responses, small space/time
 - Minimize use of communication resources

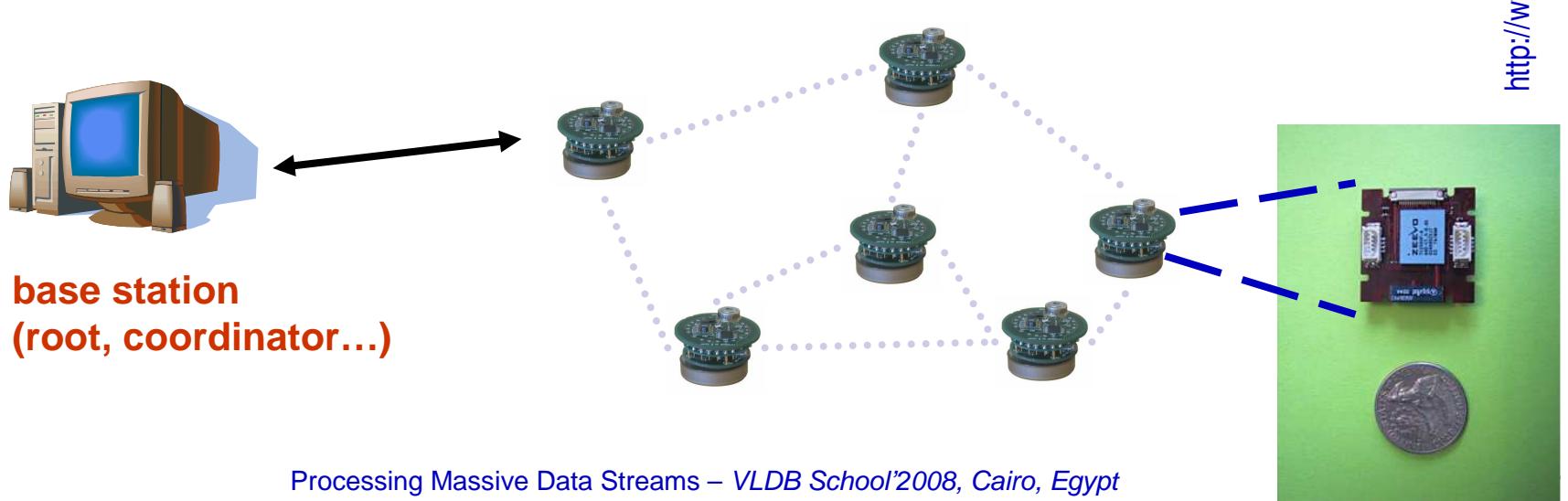
Sensor Networks

- Wireless sensor networks becoming ubiquitous in environmental monitoring, military applications, ...
- Many (100s, 10^3 , 10^6 ?) sensors scattered over terrain
- Sensors observe and process a local stream of readings:
 - Measure light, temperature, pressure...
 - Detect signals, movement, radiation...
 - Record audio, images, motion...



Sensornet Querying Application

- Query sensornet through a (remote) *base station*
- Sensor nodes have **severe resource constraints**
 - Limited battery power, memory, processor, radio range...
 - *Communication* is the major source of battery drain
 - “transmitting a single bit of data is equivalent to 800 instructions” [Madden et al.’02]



<http://www.intel.com/research/exploratory/motes.htm>

Tutorial Outline

- Motivation & Streaming Applications
- Centralized Stream Processing
 - Basic streaming models and tools
 - Stream synopses and applications
 - Sampling, sketches
 - The Sliding Window model
- Distributed Stream Processing
- Open Problems & Future Directions
- Conclusions

Some Disclaimers...

- Fairly broad coverage, but still biased view of data-streaming world
 - Revolve around personal biases (line of work and interests)
 - Main focus on key algorithmic concepts, tools, and results – for both the *centralized and distributed settings*
 - Only minimal discussion of systems/prototypes
 - A lot more information out there
 - Sensornets [Madden'06]
 - Systems issues [Koudas,Srivastava'03], [Babcock et al.'02]
 - Theory/algorithms [Muthukrishnan'03]

Data Streaming Model

- Underlying signal: One-dimensional array $A[1\dots N]$ with values $A[i]$ all initially zero
 - Multi-dimensional arrays as well (e.g., row-major)
- Signal is implicitly represented via a *stream of update tuples*
 - j -th update is $\langle x, c[j] \rangle$ implying
 - $A[x] := A[x] + c[j]$ ($c[j]$ can be >0 , <0)
- Goal: Compute functions on $A[]$ subject to
 - Small space
 - Fast processing of updates
 - Fast function computation
 - ...
- Complexity arises from massive length and domain size (N) of streams

Example IP Network Signals

- Number of bytes (packets) sent by a source IP address during the day
 - 2^{32} sized one-d array; increment only
- Number of flows between a source-IP, destination-IP address pair during the day
 - 2^{64} sized two-d array; increment only, aggregate packets into flows
- Number of **active** flows per source-IP address
 - 2^{32} sized one-d array; increment and decrement

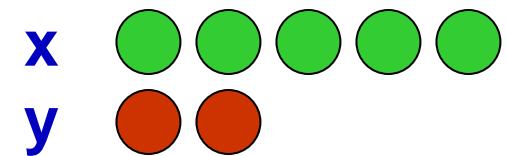
Streaming Model: Special Cases

■ Time-Series Model

- Only x -th update updates $A[x]$ (i.e., $A[x] := c[x]$)

■ Cash-Register Model: Arrivals-Only Streams

- $c[x]$ is always > 0
- Typically, $c[x]=1$, so we see a multi-set of items in one pass
- Example: $\langle x, 3 \rangle, \langle y, 2 \rangle, \langle x, 2 \rangle$ encodes the arrival of 3 copies of item x , 2 copies of y , then 2 copies of x .
- Could represent, e.g., packets on a network; power usage



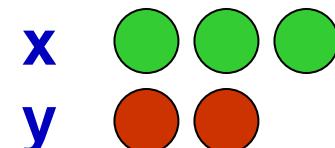
Streaming Model: Special Cases

■ Turnstile Model: Arrivals and Departures

- Most general streaming model
- $c[x]$ can be >0 or <0

■ Arrivals and departures:

- Example: $\langle x, 3 \rangle, \langle y, 2 \rangle, \langle x, -2 \rangle$ encodes final state of $\langle x, 1 \rangle, \langle y, 2 \rangle$.
- Can represent fluctuating quantities, or measure differences between two distributions



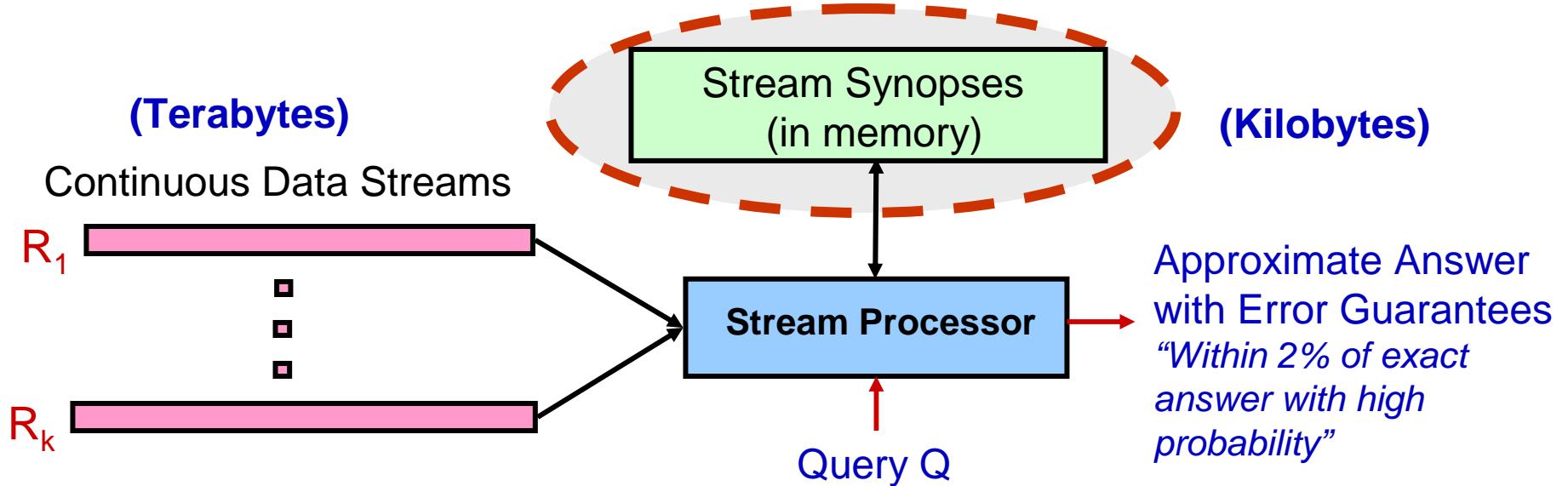
■ *Problem difficulty varies depending on the model*

- E.g., MIN/MAX in Time-Series vs. Turnstile!

Approximation and Randomization

- Many things are hard to compute exactly over a stream
 - Is the count of all items the same in two different streams?
 - Requires linear space to compute exactly
- Approximation: find an answer correct within some factor
 - Find an answer that is within 10% of correct result
 - More generally, a $(1 \pm \epsilon)$ factor approximation
- Randomization: allow a small probability of failure
 - Answer is correct, except with probability 1 in 10,000
 - More generally, success probability $(1 - \delta)$
- **Approximation and Randomization:** (ϵ, δ) -approximations

Data-Stream Algorithmics Model



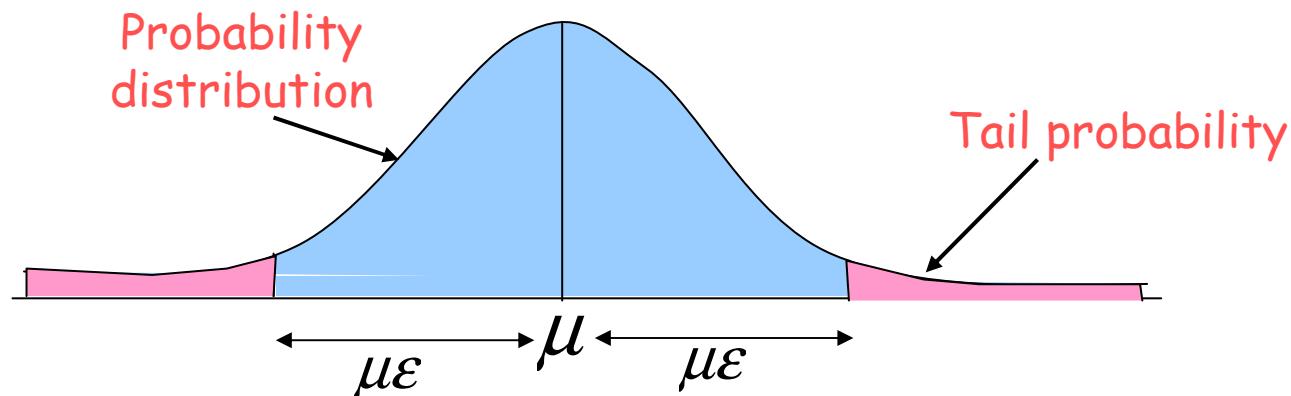
- *Approximate answers*— e.g. trend analysis, anomaly detection
- Requirements for stream synopses
 - *Single Pass*: Each record is examined at most once
 - *Small Space*: Log or polylog in data stream size
 - *Small-time*: Low per-record processing time (maintain synopses)
 - Also: *delete-proof, composable, ...*

Probabilistic Guarantees

- User-tunable (ε, δ) -approximations
 - Example: Actual answer is within 5 ± 1 with prob ≥ 0.9
- Randomized algorithms: Answer returned is a specially-built *random variable*
 - *Unbiased* (correct on expectation)
 - Combine several *Independent Identically Distributed (iid)* instantiations (average/median)
- Use *Tail Inequalities* to give probabilistic bounds on returned answer
 - *Markov Inequality*
 - *Chebyshev Inequality*
 - *Chernoff Bound*
 - *Hoeffding Bound*

Basic Tools: Tail Inequalities

- General bounds on *tail probability* of a random variable (that is, probability that a random variable deviates far from its expectation)



- Basic Inequalities: Let X be a random variable with expectation μ and variance $\text{Var}[X]$. Then, for any $\varepsilon > 0$

Markov:

$$\Pr(X \geq (1+\varepsilon)\mu) \leq \frac{1}{1+\varepsilon}$$

Chebyshev:

$$\Pr(|X - \mu| \geq \mu\varepsilon) \leq \frac{\text{Var}[X]}{\mu^2\varepsilon^2}$$

Tail Inequalities for Sums

- Possible to derive stronger bounds on tail probabilities for the sum of independent random variables
- Hoeffding Bound: Let X_1, \dots, X_m be independent random variables with $0 \leq X_i \leq r$. Let $\bar{X} = \frac{1}{m} \sum_i X_i$ and μ be the expectation of \bar{X} . Then, for any $\varepsilon > 0$,

$$\Pr(|\bar{X} - \mu| \geq \varepsilon) \leq 2 \exp \frac{-2m\varepsilon^2}{r^2}$$

- *Application*: Sample average \approx population average
 - See below...

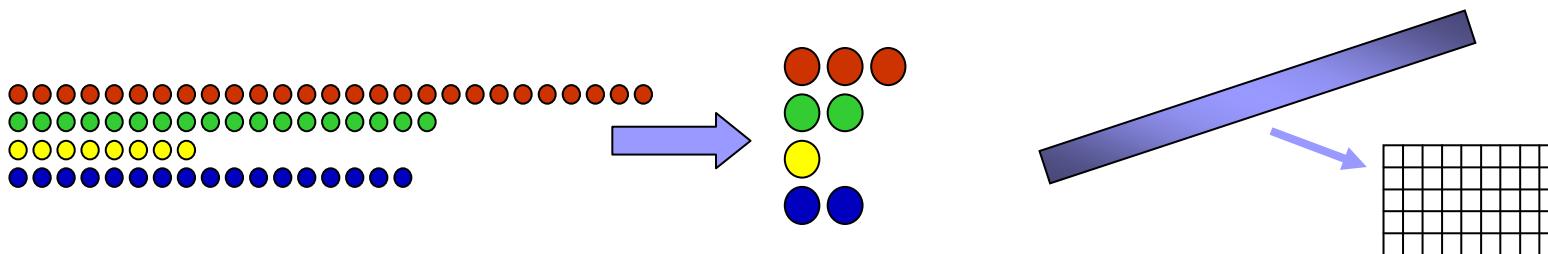
Tail Inequalities for Sums

- Possible to derive even stronger bounds on tail probabilities for the sum of independent *Bernoulli trials*
- *Chernoff Bound:* Let X_1, \dots, X_m be independent Bernoulli trials such that $\Pr[X_i=1] = p$ ($\Pr[X_i=0] = 1-p$). Let $X = \sum_i X_i$ and $\mu = mp$ be the expectation of X . Then, for any $\varepsilon > 0$,

$$\Pr(|X - \mu| \geq \mu\varepsilon) \leq 2\exp^{\frac{-\mu\varepsilon^2}{2}}$$

- *Application:* Sample selectivity \approx population selectivity
 - See below...
- *Remark:* Chernoff bound results in tighter bounds for *count queries* compared to Hoeffding bound

Sampling, Sketches and Applications



Sampling: Basics

- Idea: A small random sample S of the data often well-represents all the data
 - For a fast approx answer, apply “modified” query to S
 - Example: select agg from R where $R.e$ is odd

(n=12) Data stream:

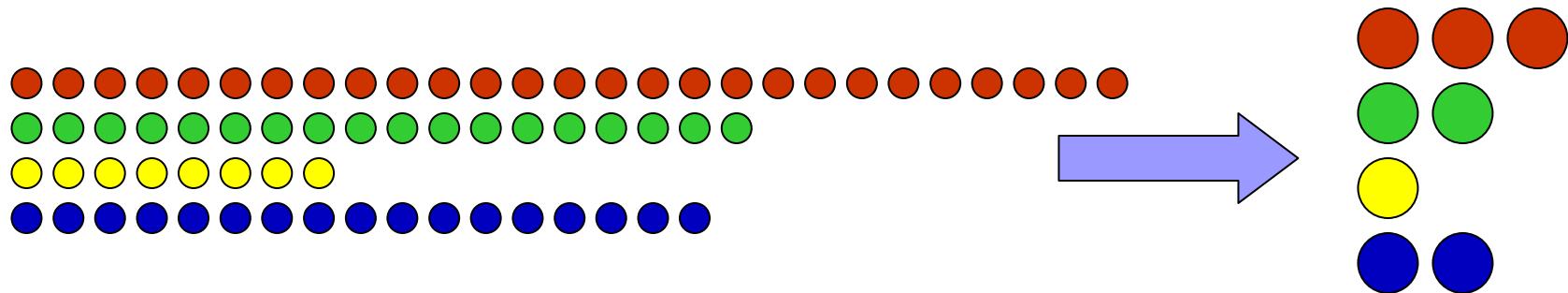
9	3	5	2	7	1	6	5	8	4	9	1
---	---	---	---	---	---	---	---	---	---	---	---

Sample S :

9	5	1	8
---	---	---	---

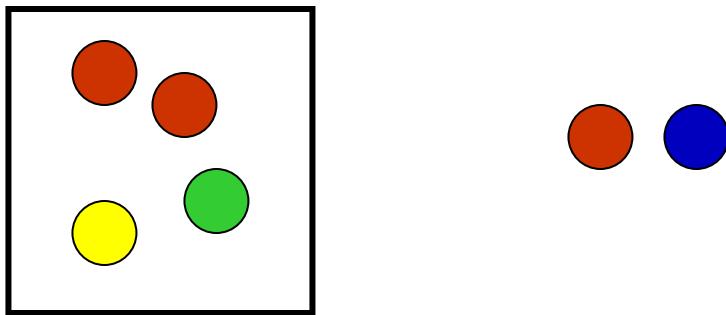
- If agg is avg, return average of odd elements in S **answer: 5**
 - If agg is count, return average over all elements e in S of
 - n if e is odd
 - 0 if e is even**answer: $12*3/4 = 9$**
- Unbiased Estimator (for count, avg, sum, etc.)
 - Bound error using *Hoeffding* (sum, avg) or *Chernoff* (count)

Sampling from a Data Stream



- Fundamental problem: sample m items uniformly from stream
 - Useful: approximate costly computation on small sample
- Challenge: don't know how long stream is
 - So when/how often to sample?
- Two solutions, apply to different situations:
 - Reservoir sampling (dates from 1980s?)
 - Min-wise sampling (dates from 1990s?)

Reservoir Sampling



- Sample first m items
- Choose to sample the i 'th item ($i > m$) with probability m/i
- If sampled, randomly replace a previously sampled item

- Optimization: when i gets large, compute which item will be sampled next, skip over intervening items [Vitter'85]

Reservoir Sampling - Analysis

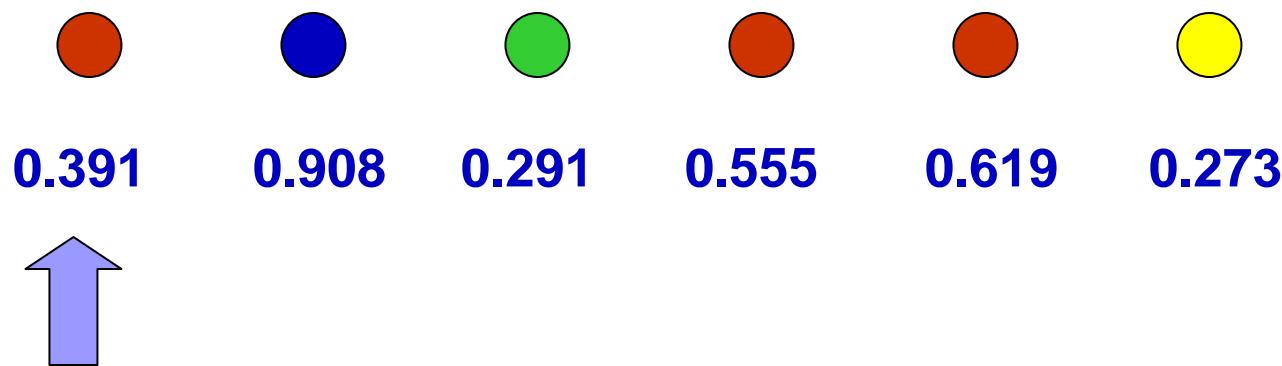
- Analyze simple case: sample size $m = 1$
- Probability i 'th item is the sample from stream length n :
 - Prob. i is sampled on arrival \times prob. i survives to end

$$\frac{1}{i} \times \frac{i}{i+1} \times \frac{i+1}{i+2} \dots \frac{n-2}{n-1} \times \frac{n-1}{n}$$
$$= 1/n$$

- Case for $m > 1$ is similar, easy to show uniform probability
- Drawbacks of reservoir sampling: hard to parallelize

Min-wise Sampling

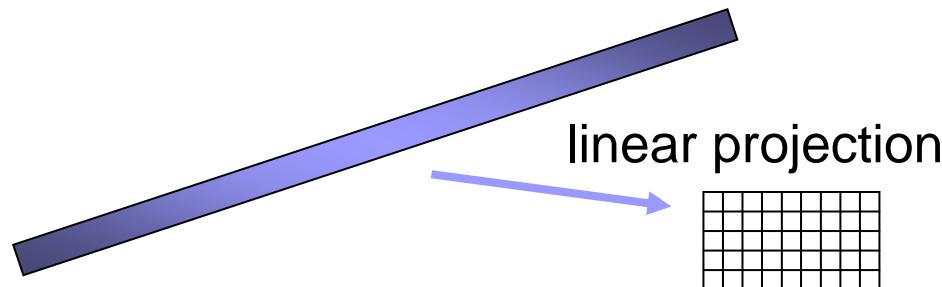
- For each item, pick a random fraction between 0 and 1
- Store item(s) with the smallest random tag [Nath et al.'04]



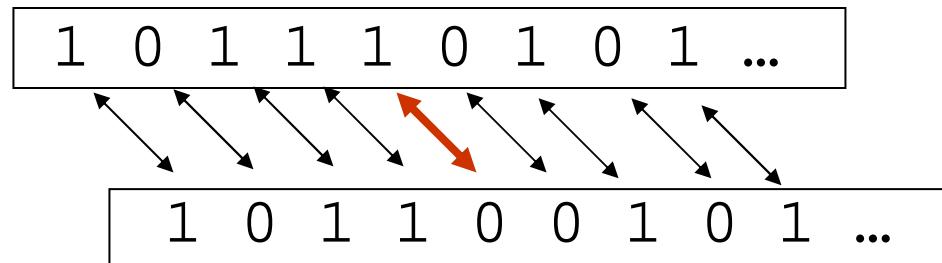
- Each item has same chance of least tag, so uniform
- Can run on multiple streams separately, then merge

Sketches

- Not every problem can be solved with sampling
 - Example: counting how many distinct items in the stream
 - If a large fraction of items aren't sampled, don't know if they are all same or all different
- Other techniques take advantage that the algorithm can “see” all the data even if it can't “remember” it all
- “*Sketch*”: essentially, a linear transform of the input
 - Model stream as defining a vector, sketch is result of multiplying stream vector by an (implicit) matrix



Trivial Example of a Sketch

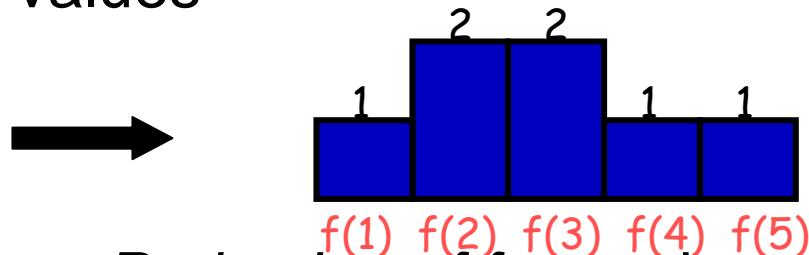


- Test if two (asynchronous) binary streams are equal
 $d_=(x,y) = 0$ iff $x=y$, 1 otherwise
- To test in small space: pick a random hash function h
- Test $h(x)=h(y)$: small chance of false positive, no chance of false negative.
- Compute $h(x)$, $h(y)$ incrementally as new bits arrive
(Karp-Rabin: $h(x) = x_i 2^i \bmod p$)
 - Exercise: extend to real valued vectors in update model

AMS Sketching

- **Goal:** Build small-space summary for distribution vector $f[v]$ ($v=1, \dots, N$) seen as a stream of v -values

Data stream: $[3, 1, 2, 4, 2, 3, 5, \dots]$



- **Basic Construct:** Randomized Linear Projection of f = project onto dot product of f -vector

$$X = \sum_v f[v] \xi_v$$

where ξ = vector of random values from an appropriate distribution

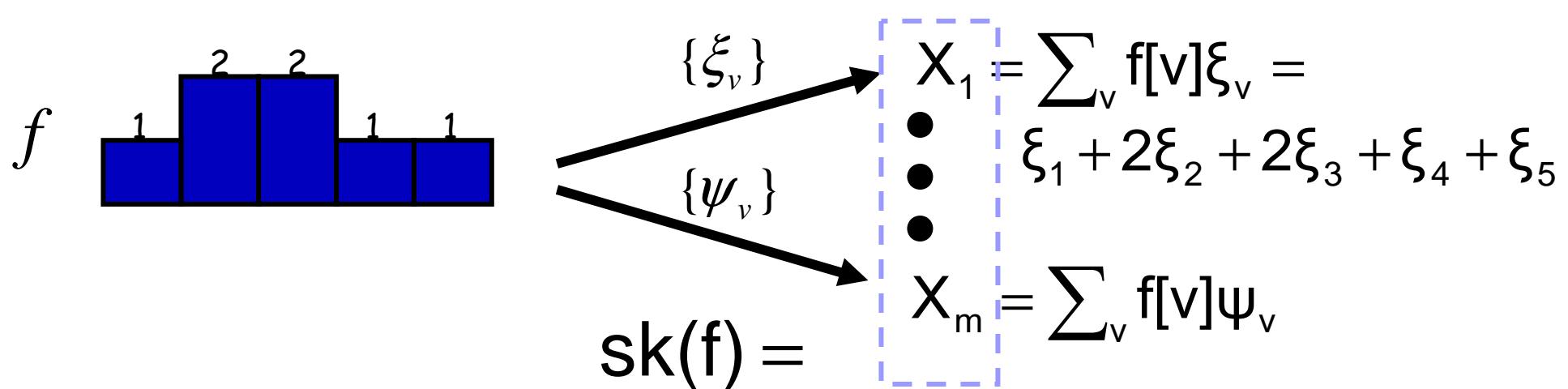
- Simple to compute: Add ξ_v whenever the value v is seen

Data stream: $[3, 1, 2, 4, 2, 3, 5, \dots]$

$$\xi_1 + 2\xi_2 + 2\xi_3 + \xi_4 + \xi_5$$

- Generate ξ_v 's in small ($\log N$) space using pseudo-random generators

AMS Sketching (contd.)

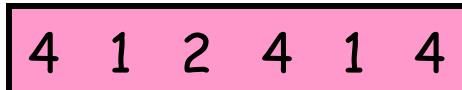


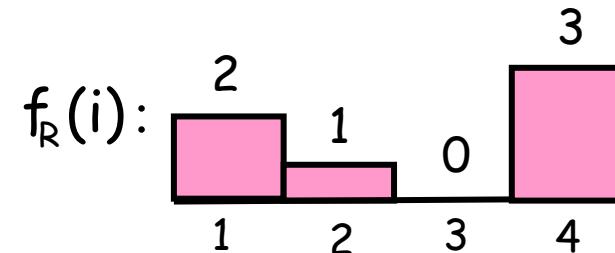
- Simple randomized linear projections of data distribution
 - Easily computed over stream using logarithmic space
 - *Linear*: Compose through simple addition
- *Theorem[AGMS]*: Given sketches of size $O\left(\frac{\log(1/\delta)}{\epsilon^2}\right)$

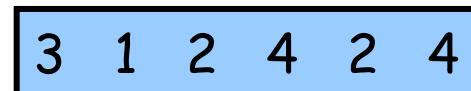
$$\text{sk}(f_i) \cdot \text{sk}(f_j) \in f_i \cdot f_j \pm \epsilon \|f_i\|_2 \|f_j\|_2$$

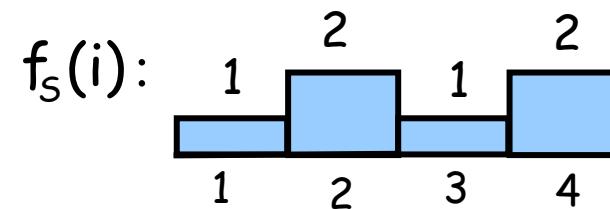
Application: Binary-Join COUNT Query

- Problem: Compute answer for the query $\text{COUNT}(R \bowtie_A S)$
- Example:

Data stream R.A: 



Data stream S.A: 



$$\begin{aligned}\text{COUNT}(R \bowtie_A S) &= \sum_i f_R(i) \cdot f_S(i) \\ &= 10 \quad (2 + 2 + 0 + 6)\end{aligned}$$

Inner Product

- Exact solution: too expensive, requires $O(N)$ space!
 - $N = \text{sizeof}(\text{domain}(A))$

Basic AMS Sketching Technique

- Key Intuition: Use randomized linear projections of $f[]$ to define random variable X such that

- X is easily computed over the stream (in small space)
- $E[X] = \text{COUNT}(R \bowtie_A S)$
- $\text{Var}[X]$ is small



Probabilistic error guarantees
(e.g., actual answer is 10 ± 1 with probability 0.9)

- Basic Idea:

- Define a family of **4-wise independent** $\{-1, +1\}$ random variables

$$\{\xi_i : i=1, \dots, N\}$$

- $\Pr[\xi_i = +1] = \Pr[\xi_i = -1] = 1/2$
 - Expected value of each ξ_i , $E[\xi_i] = 0$
- Variables ξ_i are **4-wise independent**
 - Expected value of product of 4 distinct $\xi_i = 0$
- Variables ξ_i can be generated using pseudo-random generator using only $O(\log N)$ space (for seeding)!

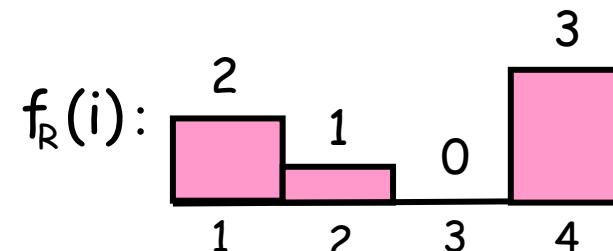
AMS Sketch Construction

- Compute random variables: $X_R = \sum_i f_R(i) \xi_i$ and $X_S = \sum_i f_S(i) \xi_i$
 - Simply add ξ_i to $X_R(X_S)$ whenever the i-th value is observed in the R.A (S.A) stream
- Define $X = X_R X_S$ to be estimate of COUNT query

■ Example:

Data stream R.A: 

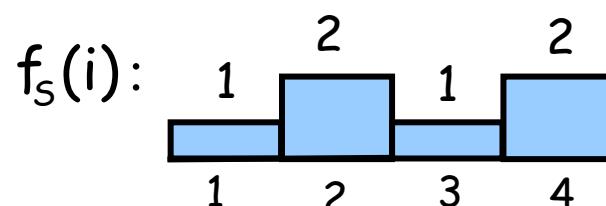
$$X_R = X_R + \xi_4$$



$$X_R = 2\xi_1 + \xi_2 + 3\xi_4$$

Data stream S.A: 

$$X_S = X_S + \xi_1$$



$$X_S = \xi_1 + 2\xi_2 + \xi_3 + 2\xi_4$$

Binary-Join AMS Sketching Analysis

- Expected value of $X = \text{COUNT}(R \bowtie_A S)$

$$\begin{aligned} E[X] &= E[X_R \cdot X_S] \\ &= E\left[\sum_i f_R(i) \xi_i \cdot \sum_i f_S(i) \xi_i\right] \\ &= E\left[\sum_i f_R(i) \cdot f_S(i) \xi_i^2\right] + E\left[\sum_{i \neq i'} f_R(i) \cdot f_S(i') \xi_i \xi_{i'}\right] \\ &= \sum_i f_R(i) \cdot f_S(i) \end{aligned}$$

1 0

- Using 4-wise independence, can show that

$$\text{Var}[X] \leq 2 \cdot \|f_R\|_2^2 \|f_S\|_2^2$$

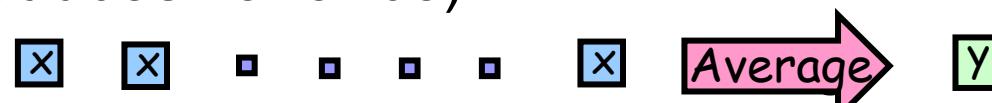
- $\|f_R\|_2^2 = \sum_i f_R(i)^2$ is self-join size of R (second/L2 moment)

Boosting Accuracy

- Chebyshev Inequality:

$$\Pr(|X - E[X]| \geq \varepsilon E[X]) \leq \frac{\text{Var}[X]}{\varepsilon^2 E[X]^2}$$

- Boost accuracy to ε by averaging over several iid copies of X (reduces variance)


$$s = \frac{8 \cdot (2 \cdot \|f_R\|_2^2 \cdot \|f_S\|_2^2)}{\varepsilon^2 \text{COUNT}^2}$$

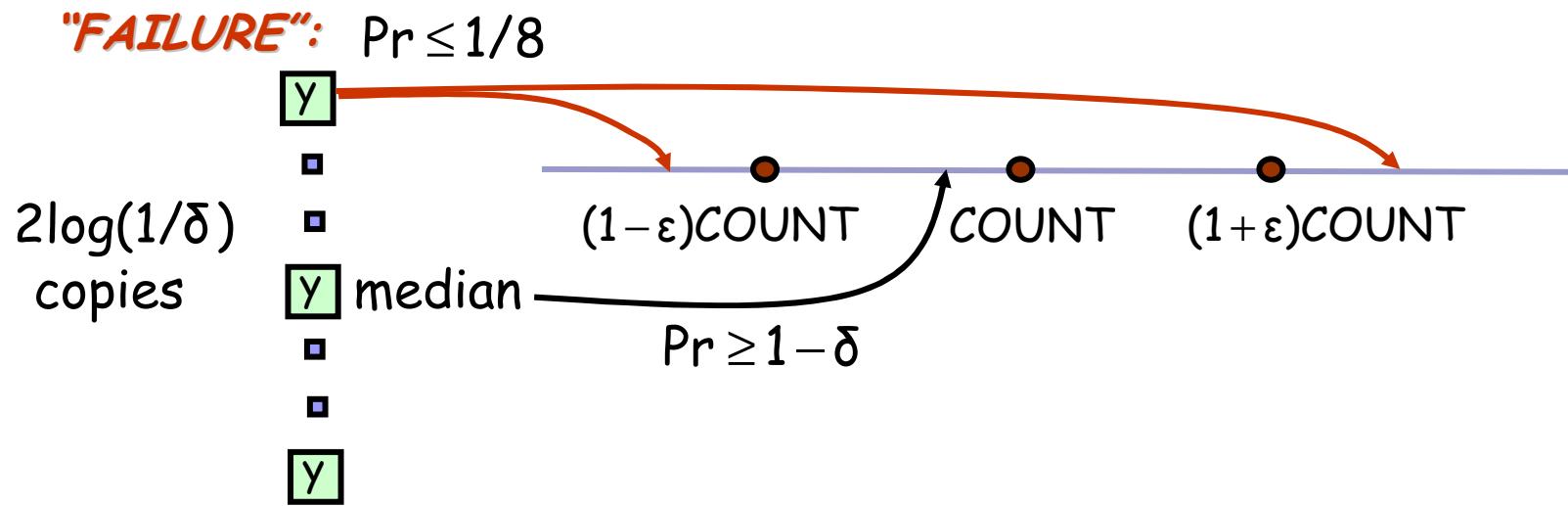
copies $E[Y] = E[X] = \text{COUNT}(R \bowtie S)$

$$\text{Var}[Y] = \frac{\text{Var}[X]}{s} \leq \frac{\varepsilon^2 \text{COUNT}^2}{8}$$

- By Chebyshev: $\Pr(|Y - \text{COUNT}| \geq \varepsilon \cdot \text{COUNT}) \leq \frac{\text{Var}[Y]}{\varepsilon^2 \text{COUNT}^2} \leq \frac{1}{8}$

Boosting Confidence

- Boost confidence to $1 - \delta$ by taking median of $2\log(1/\delta)$ independent copies of Y
- Each $Y = \text{Bernoulli Trial}$

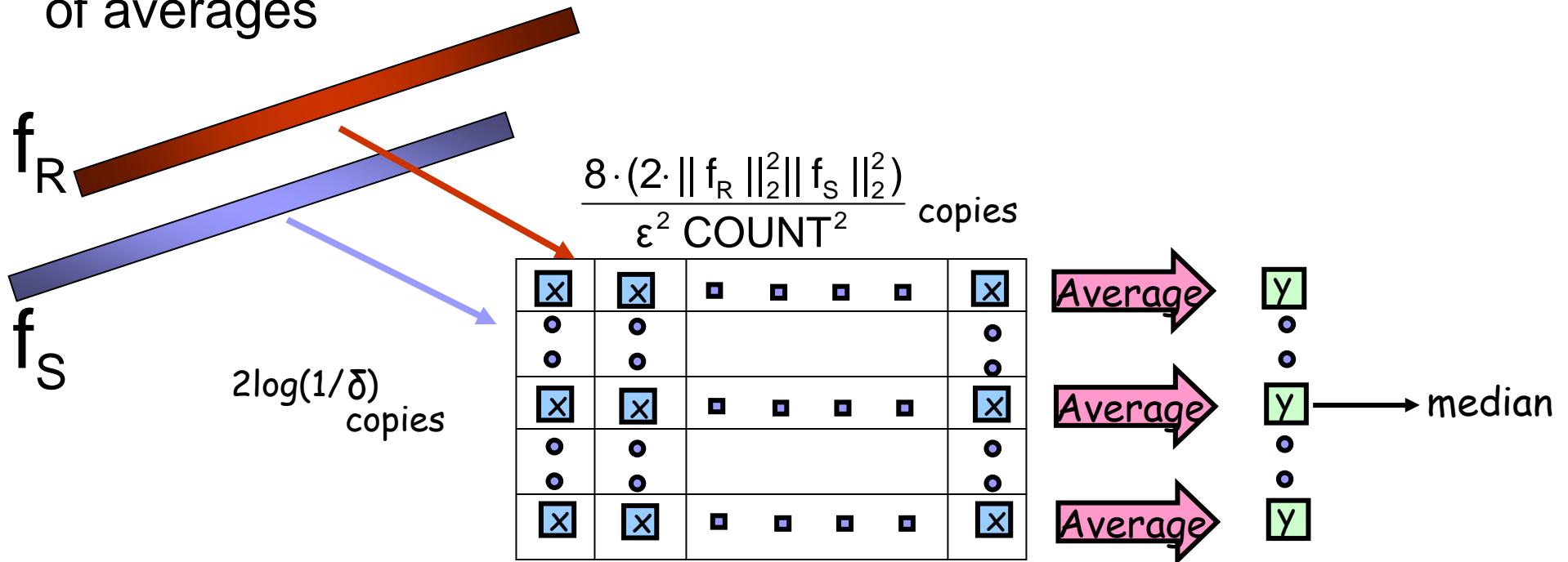


$$\Pr[|\text{median}(Y) - \text{COUNT}| \geq \varepsilon \cdot \text{COUNT}]$$

$$= \Pr[\# \text{ failures in } 2\log(1/\delta) \text{ trials} \geq \log(1/\delta)] \leq \delta \quad (\text{by Chernoff Bound})$$

Summary of Binary-Join AMS Sketching

- Step 1: Compute random variables: $X_R = \sum_i f_R(i) \xi_i$ and $X_S = \sum_i f_S(i) \xi_i$
- Step 2: Define $X = X_R X_S$
- Steps 3 & 4: Average independent copies of X ; Return median of averages



Summary of Binary-Join AMS Sketching

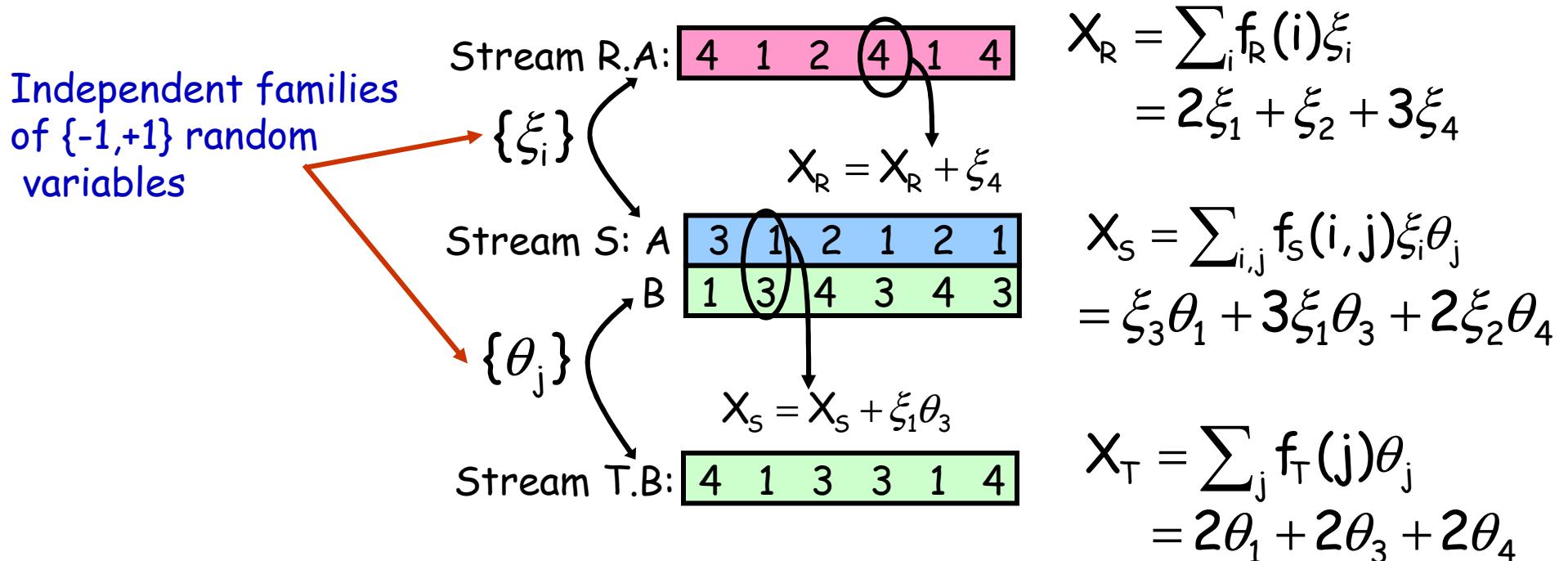
- Main Theorem [AGMS99]: Sketching approximates COUNT to within a *relative error of ϵ* with probability $\geq 1-\delta$ using space

$$O\left(\frac{\|f_R\|_2^2 \|f_S\|_2^2 \cdot \log(1/\delta) \log N}{\epsilon^2 \text{COUNT}^2}\right)$$

- Remember: $O(\log N)$ space for “seeding” the construction of each X
- Special Case – Self-join size: $\text{COUNT}(R \bowtie_A R) = \|f_R\|_2^2$
 - Gini index of heterogeneity, measure of skew in the data
 - (ϵ, δ) -estimate using space only $O\left(\frac{\log(1/\delta) \log N}{\epsilon^2}\right)$
 - *Best-case for AMS streaming join-size estimation...*
 - *Q: What's the worst case??*

AMS Sketching for Multi-Joins [Dobra et al.02]

- Problem: Estimate $\text{COUNT}(R \bowtie_A S \bowtie_B T) = \sum_{i,j} f_R(i)f_S(i,j)f_T(j)$
- Sketch-based solution
 - Compute random variables X_R , X_S and X_T



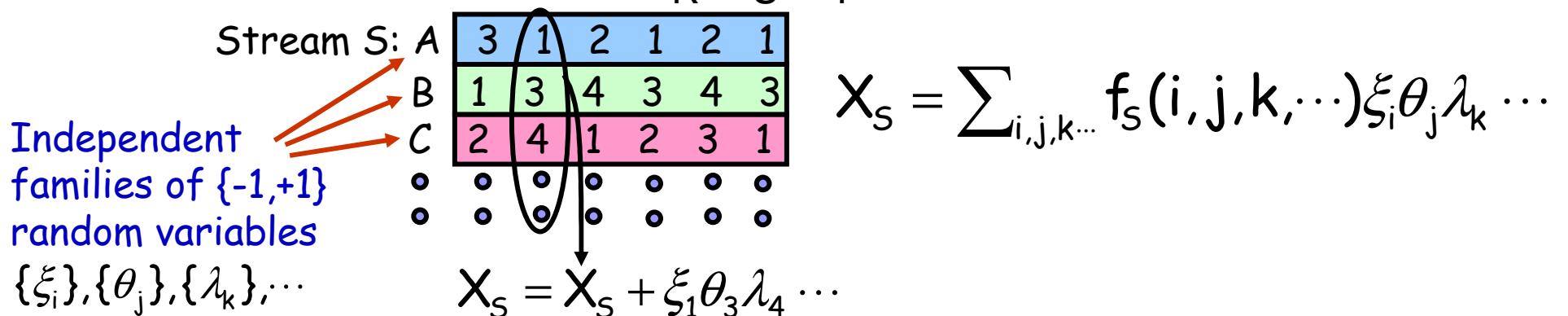
– Return $X = X_R X_S X_T$

$$(\mathbb{E}[X] = \text{COUNT}(R \bowtie_A S \bowtie_B T))$$

$$\mathbb{E}[f_R(i) \cdot f_S(i', j) \cdot f_T(j') \xi_i \xi_{i'} \theta_j \theta_{j'}] = 0 \text{ if } i \neq i' \text{ or } j \neq j'$$

AMS Sketching for Multi-Joins [Dobra et al.02]

- Sketches for general *multi-join COUNT queries* (over streams R, S, T, \dots)
 - For each pair of attributes in equality join constraint, use independent family of $\{-1, +1\}$ random variables
 - Compute random variables X_R, X_S, X_T, \dots



– Return $X = X_R X_S X_T \dots$ ($E[X] = \text{COUNT}(R \bowtie S \bowtie T \bowtie \dots)$)

$$\text{Var}[X] \leq 2^{2m} \cdot \|f_R\|_2^2 \|f_S\|_2^2 \|f_T\|_2^2 \dots$$

– *Explosive increase with the number of joins!*

Boosting Accuracy by Sketch Partitioning

- For ϵ error, need $\text{Var}[Y] \leq \frac{\epsilon^2 \text{COUNT}^2}{8}$

The diagram illustrates a process of averaging. On the left, there is a sequence of data points represented by small squares. Some squares contain an 'X' and others contain a small square. A pink arrow labeled 'Average' points from this sequence to a single green square on the right, which contains a 'Y'. Below the sequence, the formula for calculating the number of copies (s) is given:

$$s = \frac{8 \cdot (2^{2m} \|f_R\|_2^2 \|f_S\|_2^2 \dots)}{\epsilon^2 \text{COUNT}^2}$$

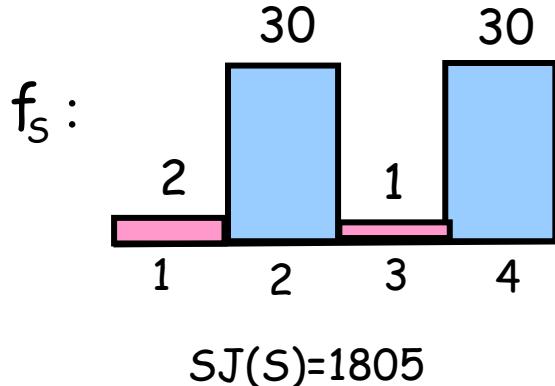
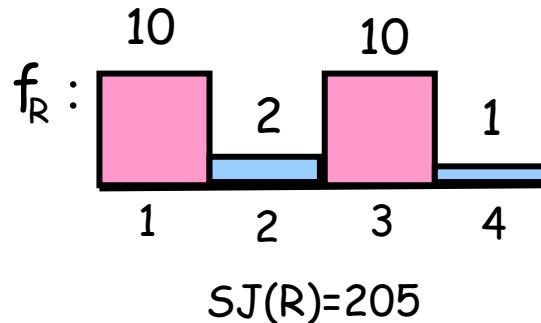
copies

$$\text{Var}[Y] = \frac{\text{Var}[X]}{s} \leq \frac{\epsilon^2 \text{COUNT}^2}{8}$$

- Key Observation: Product of self-join sizes for *partitions of streams* can be *much smaller* than product of self-join sizes
 - Reduce space requirements by partitioning join attribute domains
 - Overall join size = sum of join size estimates for partitions
 - Exploit coarse statistics (e.g., histograms) based on historical data or collected in an initial pass, to compute the *best partitioning*

Sketch Partitioning Example: Binary Join

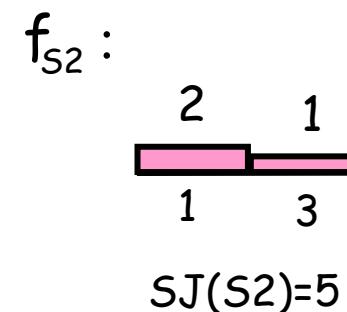
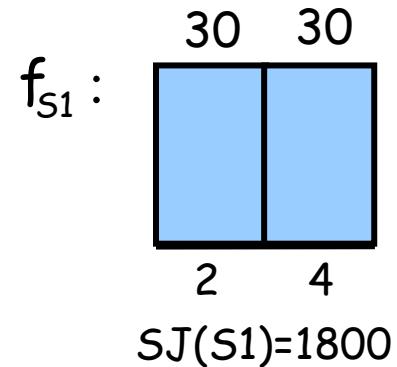
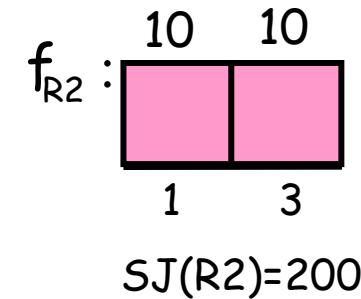
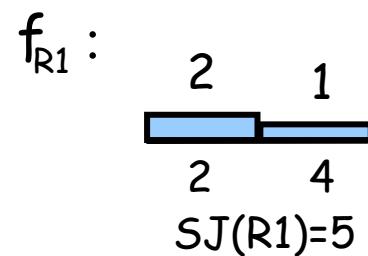
Without Partitioning



$$VAR[X] \approx 2 \cdot SJ(R) \cdot SJ(S)$$

$\approx 720K$

With Partitioning ($P1=\{2,4\}$, $P2=\{1,3\}$)



$$VAR[X1] \approx 2 \cdot SJ(R1) \cdot SJ(S1) \quad VAR[X2] \approx 2 \cdot SJ(R2) \cdot SJ(S2)$$

$\approx 18K$ $\approx 2K$

$$X = X1 + X2, \quad E[X] = COUNT(R \bowtie S)$$

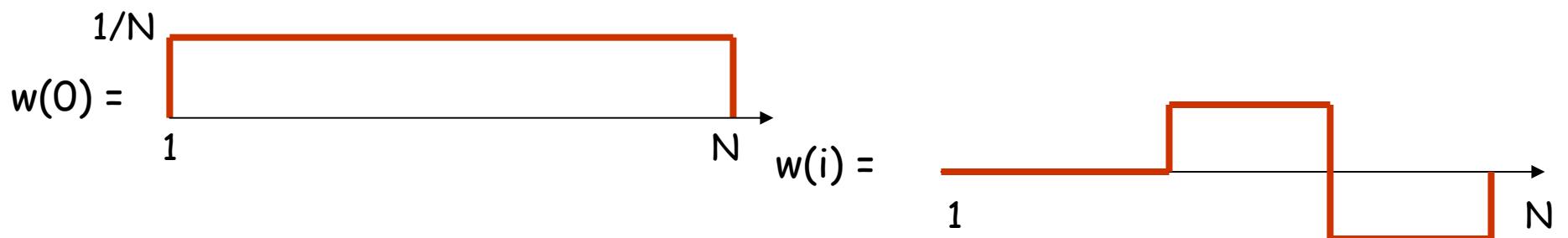
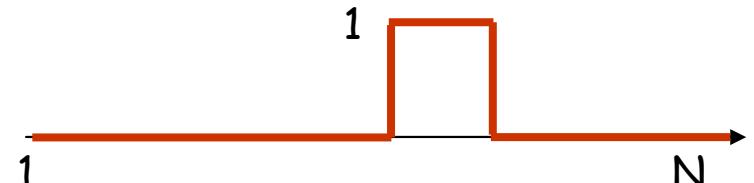
$$VAR[X] = VAR[X1] + VAR[X2] \approx 20K$$

Overview of Sketch Partitioning

- Maintain independent sketches for partitions of join-attribute space
- Improved error guarantees
 - $\text{Var}[X] = \sum \text{Var}[X_i]$ is smaller (by *intelligent domain partitioning*)
 - “*Variance-aware*” boosting: More space to higher-variance partitions
- Challenging optimization problems!
- Significant accuracy benefits for small number (2-4) of partitions

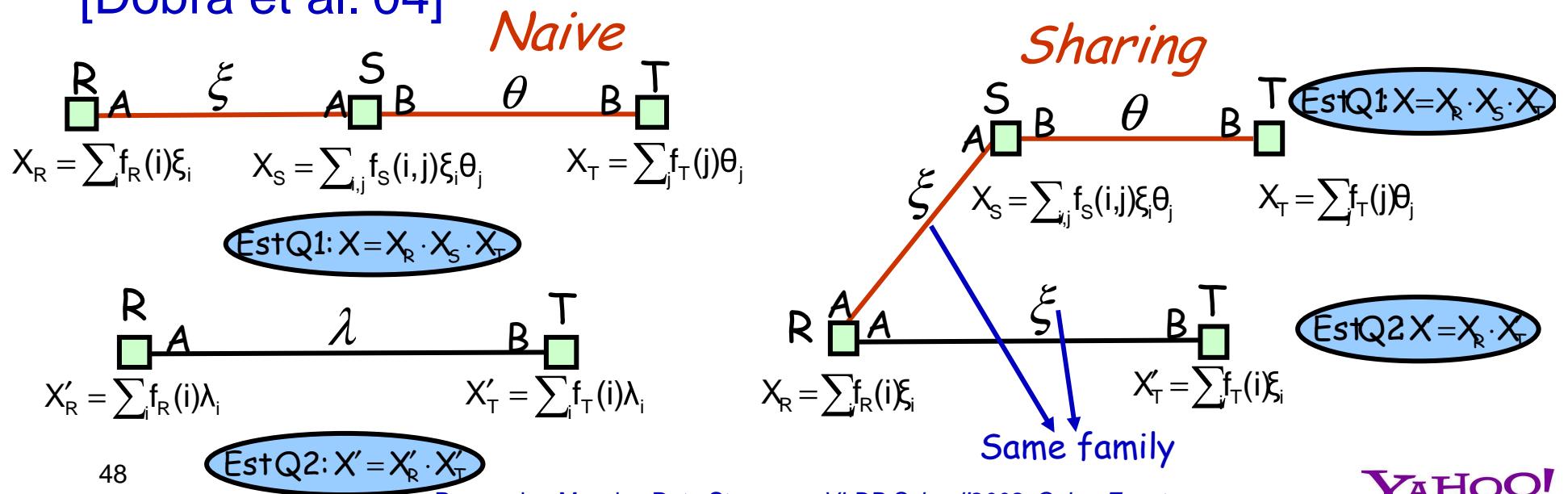
Other Applications of AMS Sketching

- *General result:* Streaming (ε, δ) estimation of “*large inner products*” using AMS sketches
- Other streaming inner products of interest
 - Top- k frequencies [Charikar et al.’02]
 - Item frequency = $\langle f, \text{“unit_pulse”} \rangle$
 - Large *wavelet coefficients* [Gilbert et al.’01], [Cormode et al.’06]
 - $\text{Coeff}(i) = \langle f, w(i) \rangle$, where $w(i) = i\text{-th wavelet basis vector}$



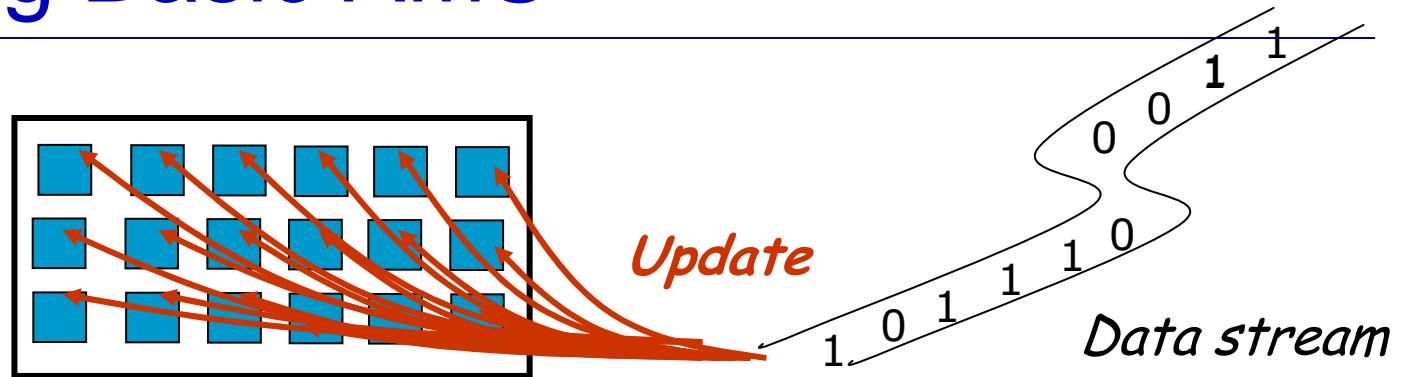
Recent Results on Stream Joins

- Better accuracy using “*skimmed sketches*” [Ganguly et al.’04]
 - “Skim” dense items (i.e., large freqs) from the AMS sketches
 - Use the “skimmed” sketch only for sparse elements
 - Stronger worst-case guarantees, and much better in practice
 - Same effect as sketch partitioning with *no apriori knowledge!*
- Sharing sketch space/computation among *multiple queries* [Dobra et al.’04]



Improving Basic AMS

*Local stream
AMS sketch*

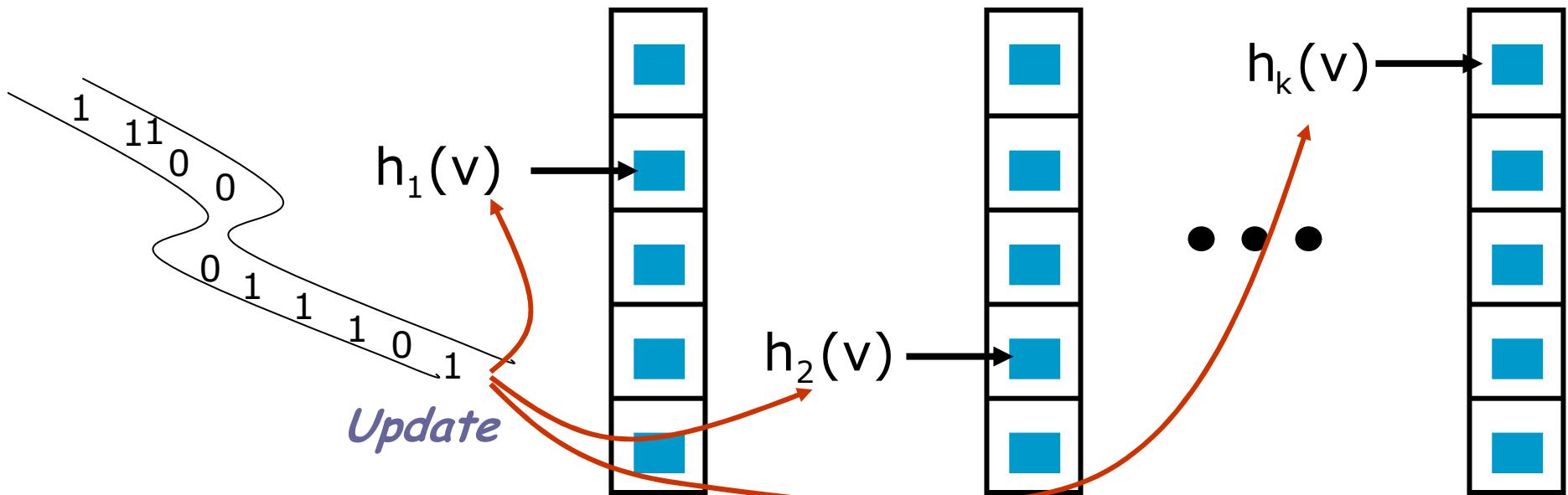


- Update time for basic AGMS sketch is $\Omega(|\text{sketch}|)$

■ *BUT...*

- Sketches can get large – cannot afford to touch every counter for rapid-rate streams!
 - Complex queries, stringent error guarantees, ...
- Sketch size may not be the limiting factor (PCs with GBs of RAM)

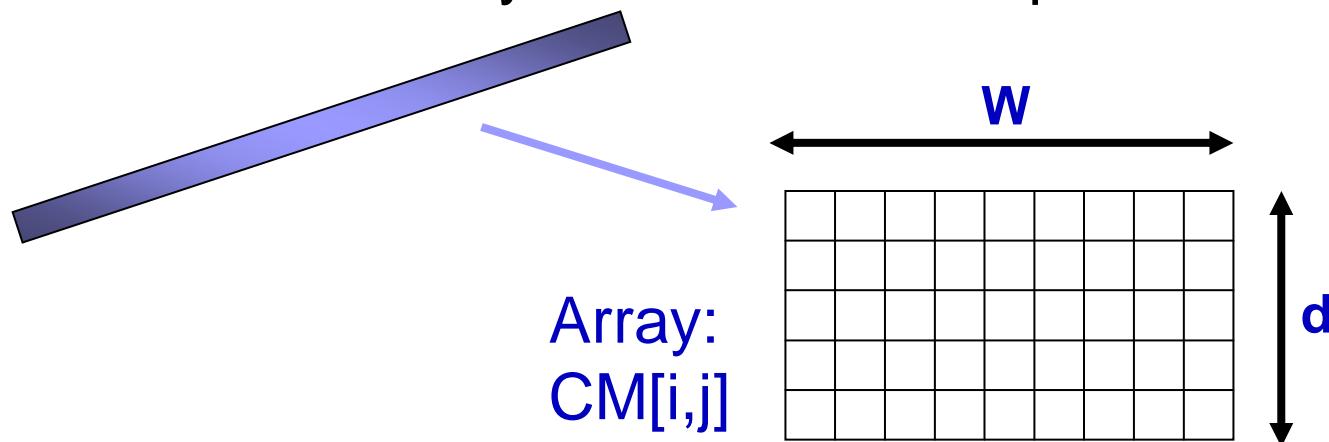
The Fast AMS Sketch [Cormode, Garofalakis'05]



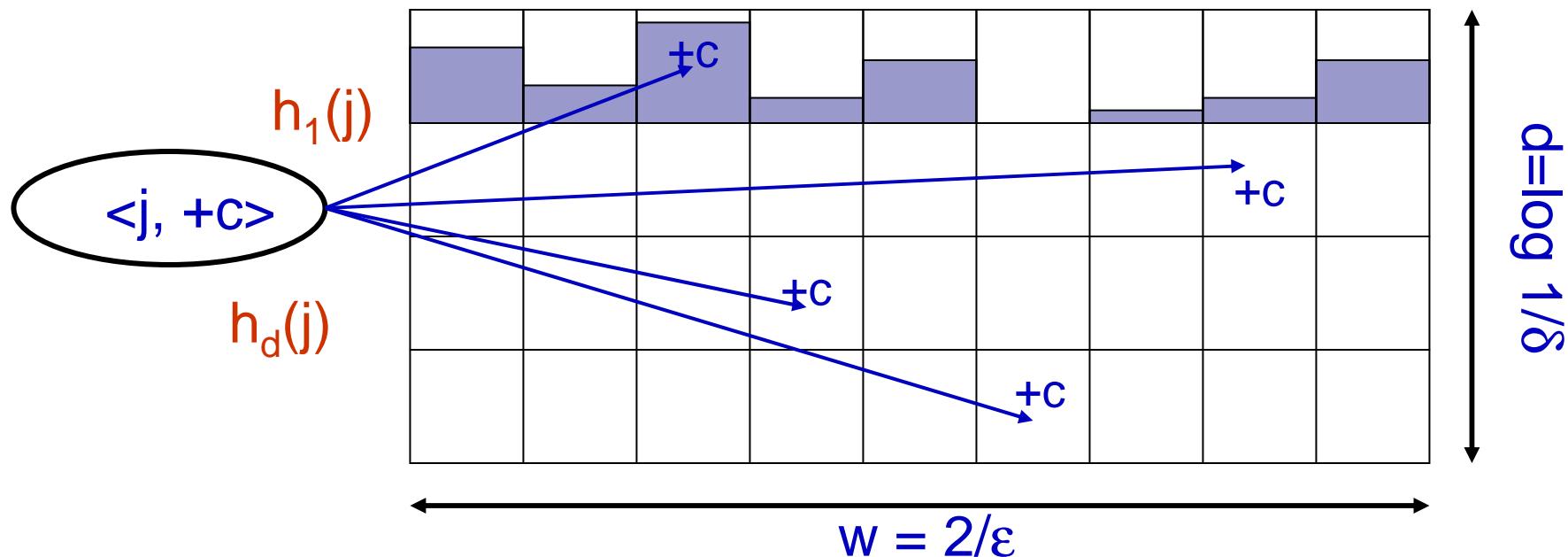
- **Fast AMS Sketch:** Organize the atomic AMS counters into hash-table buckets
 - Each update touches only a few counters (one per table)
 - Same space/accuracy tradeoff as basic AMS (in fact, better ☺)
 - *BUT, guaranteed logarithmic update times (regardless of sketch size)!!*

Count-Min Sketch [Cormode, Muthukrishnan'04]

- Simple sketch idea, can be used for as the basis of many different stream mining tasks
 - Join aggregates, range queries, moments, ...
- Model input stream as a vector A of dimension N
- Creates a small summary as an array of $w \times d$ in size
- Use d hash functions to map vector entries to $[1..w]$
- Works on arrivals only and arrivals & departures streams



CM Sketch Structure



- Each entry in input vector $A[]$ is mapped to one bucket per row
 - $h()$'s are *pairwise independent*
- Merge two sketches by entry-wise summation
- Estimate $A[j]$ by taking $\min_k \{ CM[k, h_k(j)] \}$

CM Sketch Guarantees

- [Cormode, Muthukrishnan'04] CM sketch guarantees approximation error on point queries less than $\epsilon \|\mathbf{A}\|_1$ in space $O(1/\epsilon \log 1/\delta)$
 - Probability of more error is less than $1-\delta$
 - Similar guarantees for range queries, quantiles, join size,...
- Hints
 - Counts are *biased* (*overestimates*) due to collisions
 - Limit the expected amount of extra “mass” at each bucket? *(Use Markov)*
 - *Use Chernoff-like argument* to boost the confidence for the $\min\{\}$ estimate
 - Based on independence of row hashes

CM Sketch Analysis

Estimate $A'[j] = \min_k \{ CM[k, h_k(j)] \}$

- Analysis: In k 'th row, $CM[k, h_k(j)] = A[j] + X_{k,j}$
 - $X_{k,j} = \sum A[i] \mid h_k(i) = h_k(j)$
 - $E[X_{k,j}] = \sum A[i] * Pr[h_k(i)=h_k(j)] \leq (\varepsilon/2) * \sum A[i] = \varepsilon \|A\|_1 / 2$ (pairwise independence of h)
 - $Pr[X_{k,j} \geq \varepsilon \|A\|_1] = Pr[X_{k,j} \geq 2E[X_{k,j}]] \leq 1/2$ by Markov inequality
- So, $Pr[A'[j] \geq A[j] + \varepsilon \|A\|_1] = Pr[\forall k. X_{k,j} > \varepsilon \|A\|_1] \leq 1/2^{\log 1/\delta} = \delta$
- Final result: with certainty $A[j] \leq A'[j]$ and
with probability at least $1-\delta$, $A'[j] < A[j] + \varepsilon \|A\|_1$
- Q: *How do CM sketch guarantees compare to AMS??*

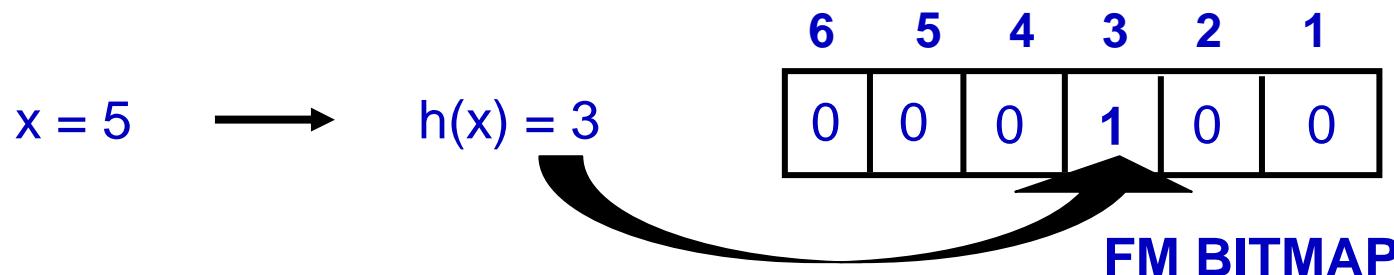
Distinct Value Estimation

- Problem: Find the *number of distinct values* in a stream of values with domain $[1, \dots, N]$
 - Zeroth frequency moment F_0 , L_0 (Hamming) stream norm
 - Statistics: number of *species* or *classes* in a population
 - Important for query optimizers
 - *Network monitoring*: distinct destination IP addresses, source/destination pairs, requested URLs, etc.
- Example ($N=64$) Data stream: 3 2 5 3 2 1 7 5 1 2 3 7

Number of distinct values: 5
- Hard problem for random sampling! [Charikar et al.'00]
 - Must sample almost the entire table to guarantee the estimate is within a factor of 10 with probability $> 1/2$, regardless of the estimator used!
- AMS and CM only good for *multiset semantics*

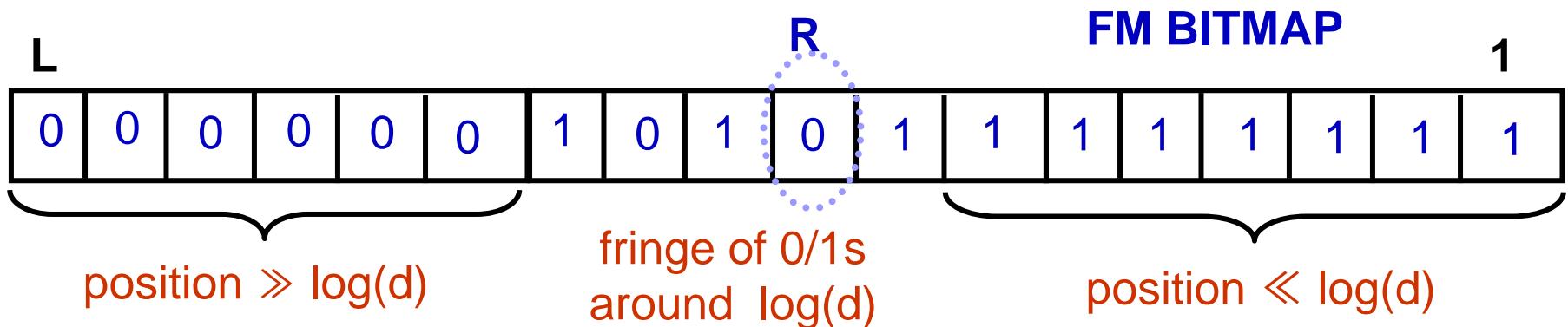
FM Sketch [Flajolet, Martin'85]

- Estimates number of distinct inputs (**count distinct**)
- Uses hash function mapping input items to i with prob 2^{-i}
 - i.e. $\Pr[h(x) = 1] = \frac{1}{2}$, $\Pr[h(x) = 2] = \frac{1}{4}$, $\Pr[h(x)=3] = 1/8 \dots$
 - Easy to construct $h()$ from a uniform hash function by counting trailing zeros
- Maintain FM Sketch = bitmap array of $L = \log N$ bits
 - Initialize bitmap to all 0s
 - For each incoming value x , set $FM[h(x)] = 1$



FM Sketch Analysis

- If d distinct values, expect $d/2$ map to FM[1], $d/4$ to FM[2]...



- Let R = position of rightmost zero in FM, indicator of $\log(d)$
- Basic estimate $d = c2^R$ for scaling constant $c \approx 1.3$
- Average many copies (different hash fns) improves accuracy

FM Sketch Properties

- With $O(1/\epsilon^2 \log 1/\delta)$ copies, get $(1 \pm \epsilon)$ accuracy with probability at least $1 - \delta$ [Bar-Yossef et al'02], [Ganguly et al.'04]
 - 10 copies gets $\approx 30\%$ error, 100 copies $< 10\%$ error
- *Delete-Proof*: Use counters instead of bits in sketch locations
 - +1 for inserts, -1 for deletes
- *Composable*: Component-wise OR/add distributed sketches together

$$\begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{0} & \boxed{1} & \boxed{1} \end{array} + \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{1} & \boxed{1} & \boxed{0} & \boxed{0} & \boxed{1} \end{array} = \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{1} & \boxed{1} & \boxed{0} & \boxed{1} & \boxed{1} \end{array}$$

- Estimate $|S_1 \cup \dots \cup S_k| = \text{set union cardinality}$

Generalization: Distinct Values Queries

```
SELECT COUNT( DISTINCT target-attr )
```

```
FROM relation
```

Template

```
WHERE predicate
```

```
SELECT COUNT( DISTINCT o_custkey )
```

```
FROM orders
```

TPC-H example

```
WHERE o_orderdate >= '2008-01-01'
```

- “How many distinct customers have placed orders this year?”
- Predicate not necessarily only on the DISTINCT target attribute
- *Approximate answers with error guarantees over a stream of tuples?*

Distinct Sampling [Gibbons'01]

Key Ideas

- Use FM-like technique to collect a specially-tailored sample over the *distinct values in the stream*
 - ***Use hash function to sample values from the data domain!!***
 - Uniform random sample of the distinct values
 - Very different from traditional random sample: each distinct value is chosen uniformly regardless of its frequency
 - DISTINCT query answers: simply scale up sample answer by sampling rate
- To handle additional predicates
 - *Reservoir sampling* of tuples for each distinct value in the sample
 - Use reservoir sample to evaluate predicates

Building a Distinct Sample [Gibbons'01]

- Use FM-like hash function $h()$ for each streaming value x
 - $\text{Prob}[h(x) = k] = 1/2^k$
- **Key Invariant:** “All values with $h(x) \geq \text{level}$ (and only these) are in the distinct sample”

```
DistinctSampling( B , r )
```

```
// B = space bound, r = tuple-reservoir size for each distinct value
```

```
level = 1; S =  $\emptyset$ 
```

```
for each new tuple t do
```

```
    let x = value of DISTINCT target attribute in t
```

```
    if  $h(x) \geq \text{level}$  then // x belongs in the distinct sample
```

```
        use t to update the reservoir sample of tuples for x
```

```
    if  $|S| \geq B$  then // out of space
```

```
        evict from S all tuples with  $h(\text{target-attribute-value}) = \text{level}$ 
```

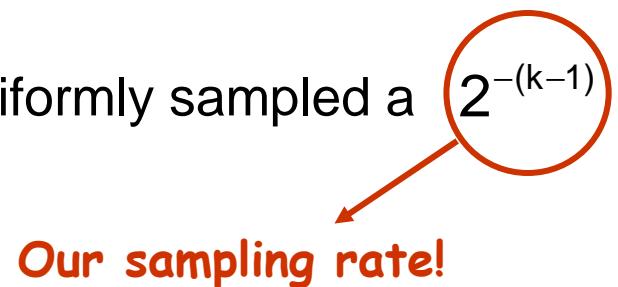
```
        set level = level + 1
```

Using the Distinct Sample

- If $\text{level} = k$ for our sample, then we have selected all distinct values x such that $h(x) \geq k$
 - $\text{Prob}[h(x) \geq k] = 1/2^{k-1}$
 - By $h()$'s randomizing properties, we have uniformly sampled a fraction of the distinct values in our stream
- *Query Answering:* Run distinct-values query on the distinct sample and scale the result up by 2^{k-1}
- *Distinct-value estimation:* Guarantee ϵ relative error with probability $\geq 1 - \delta$ using $O(\log(1/\delta)/\epsilon^2)$ space
 - For $q\%$ selectivity predicates the space goes up inversely with q
- *Experimental results:* 0-10% error vs. 50-250% error for previous best approaches, using 0.2% to 10% synopses

$2^{-(k-1)}$

Our sampling rate!



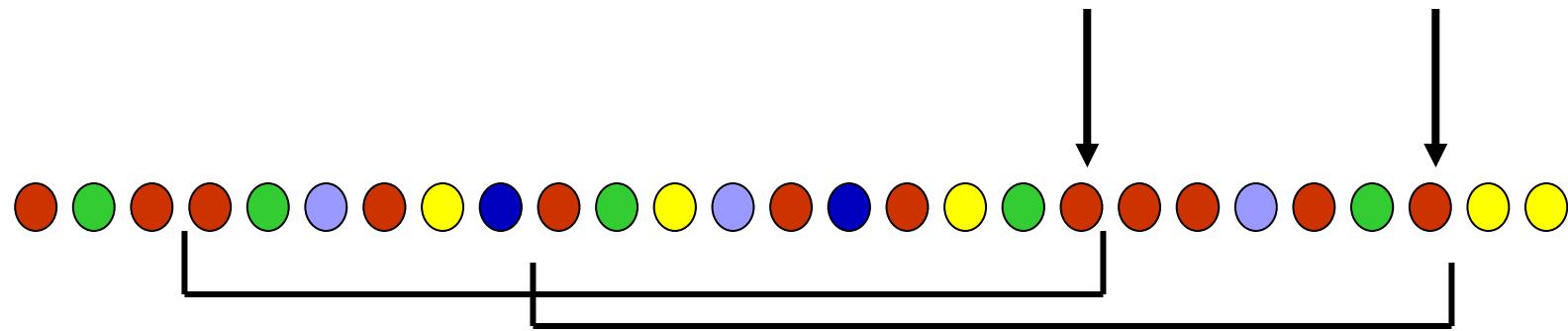
Sketching and Sampling Summary

- Sampling and sketching ideas are at the heart of many stream mining algorithms
 - Moments/join aggregates, histograms, wavelets, top-k, frequent items, other mining problems, ...
- A sample is a quite **general representative** of the data set; sketches tend to be ***specific to a particular purpose***
 - FM sketch for count distinct, AMS sketch for joins/ L_2 estimation, ...
- Traditional sampling does not work in the **turnstile (arrivals & departures) model**
 - BUT... see recent generalizations of distinct sampling [Ganguly et al.'04], [Cormode et al.'05]; as well as [Gemulla et al.'08]

Practicality

- Algorithms discussed here are quite simple and very fast
 - Sketches can easily process millions of updates per second on standard hardware
 - Limiting factor in practice is often I/O related
- Implemented in several practical systems:
 - AT&T's Gigascope system on live network streams
 - Sprint's CMON system on live streams
 - Google's log analysis
- Sample implementations available on the web
 - <http://www.cs.rutgers.edu/~muthu/massdal-code-index.html>
 - or web search for 'massdal'

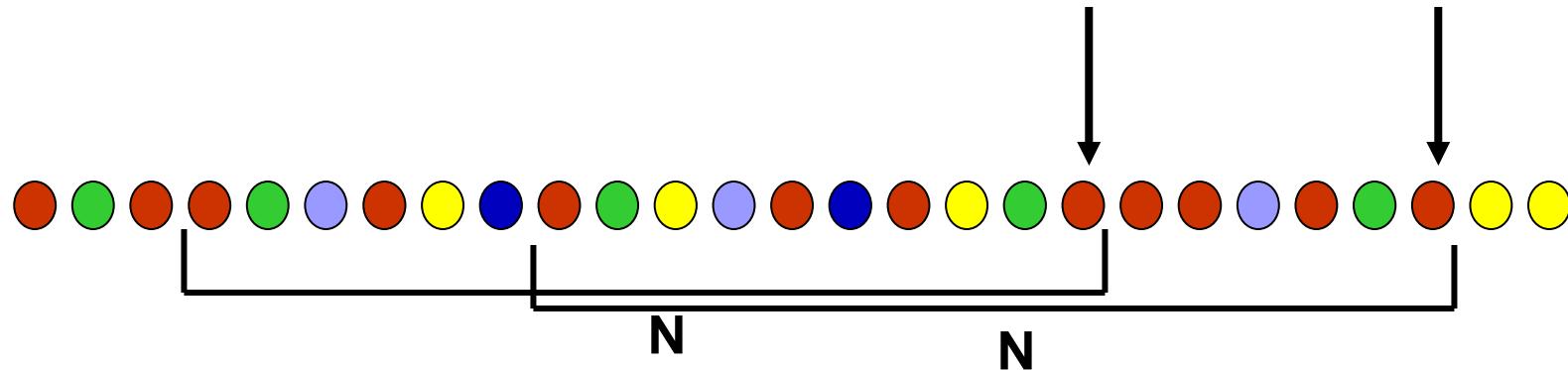
The Sliding Window Model



Sliding Window Streaming Model

■ Model

- At every time t , a data record arrives
- The record “expires” at time $t+N$ (N is the window length)



■ When is it useful?

- Make decisions based on “recently observed” data
- Stock data
- Sensor networks

Time in Data Stream Models

Tuples arrive $X_1, X_2, X_3, \dots, X_t, \dots$

- Function $f(X, t, \text{NOW})$
 - Input at time t : $f(X_1, 1, t), f(X_2, 2, t), f(X_3, 3, t), \dots, f(X_t, t, t)$
 - Input at time $t+1$: $f(X_1, 1, t+1), f(X_2, 2, t+1), f(X_3, 3, t+1), \dots, f(X_{t+1}, t+1, t+1)$
- Full history: $f == \text{identity}$
- Partial history: Decay
 - *Exponential decay*: $f(X, t, \text{NOW}) = 2^{-(\text{NOW}-t)} * X$
 - Input at time t : $2^{-(t-1)} * X_1, 2^{-(t-2)} * X_2, \dots, \frac{1}{2} * X_{t-1}, X_t$
 - Input at time $t+1$: $2^{-t} * X_1, 2^{-(t-1)} * X_2, \dots, \frac{1}{4} * X_{t-1}, \frac{1}{2} * X_t, X_{t+1}$
 - *Sliding window* (special type of decay):
 - $f(X, t, \text{NOW}) = X$ if $\text{NOW}-t < N$
 - $f(X, t, \text{NOW}) = 0$, otherwise
 - Input at time t : $X_1, X_2, X_3, \dots, X_t$
 - Input at time $t+1$: $X_2, X_3, \dots, X_t, X_{t+1}$

Simple Statistics over Sliding Windows

- Bitstream input – Count the number of ones [Datar et al.'02]
 - Exact solution: $\Theta(N)$ bits
 - Algorithm **BasicCounting**
 - $(1 \pm \epsilon)$ relative error approximation
 - Space: $O(1/\epsilon (\log^2 N))$ bits
 - Time: $O(\log N)$ worst case, $O(1)$ amortized per record
 - Lower Bound:
 - Space: $\Omega(1/\epsilon (\log^2 N))$ bits

Approach: Temporal Histograms

Example: ... 01101010011111110110 0101 ...

Equi-width histogram:

... 0110 1010 0111 1111 0110 0101 ...

■ Issues:

- Error is in the **last (leftmost) bucket**
- Bucket counts (left to right): $C_m, C_{m-1}, \dots, C_2, C_1$
- Absolute error $\leq C_m/2$
- Answer $\geq C_{m-1} + \dots + C_2 + C_1 + 1$.

- ## ■ Relative error $\leq C_m / (2(C_{m-1} + \dots + C_2 + C_1 + 1))$
- Maintain: $C_m / (2(C_{m-1} + \dots + C_2 + C_1 + 1)) \leq \varepsilon$ ($= 1/k$)

Naïve: Equi-Width Histograms

- Goal: Maintain $C_m/2 \leq \varepsilon (C_{m-1} + \dots + C_2 + C_1 + 1)$

Problem case:

... 0110 1010 0111 1111 0110 1111 0000 0000 0000 0000 ...

- Note:
 - *Every bucket will be the last bucket sometime!*
 - New records may be all zeros →
 - For **every** bucket i , require $C_i/2 \leq \varepsilon (C_{i-1} + \dots + C_2 + C_1 + 1)$

Exponential Histograms (EHs)

- Data structure invariant:
 - Bucket sizes are non-decreasing powers of 2
 - For every bucket size other than that of the last bucket, there are at least $k/2$ and at most $k/2+1$ buckets of that size
 - Example: $k=4$: $(8, 4, 4, 4, 2, 2, 2, 1, 1\dots)$
- Invariant implies:
 - Assume $C_i = 2^j$, then
$$C_{i-1} + \dots + C_2 + C_1 + 1 \geq k/2 * (\sum(1+2+4+\dots+2^{j-1})) \geq k * 2^j / 2 \geq k/2 * C_i$$
 - Setting $k = 1/\epsilon$ implies the required error guarantee!

Space Complexity

- Number of buckets m :
 - $m \leq [\# \text{ of buckets of size } j]^* [\# \text{ of different bucket sizes}]$
 $\leq (k/2 + 1) * ((\log(2N/k)+1) = O(k * \log(N))$
- Each bucket requires $O(\log N)$ bits
- Total memory:
 $O(k \log^2 N) = O(1/\varepsilon * \log^2 N)$ bits
- Invariant (with $k = 1/\varepsilon$) maintains error guarantee!
- *Completely deterministic!*

EH Maintenance Algorithm

Data structures:

- *For each bucket:* timestamp of most recent 1, size = #1's in bucket
- **LAST** = size of the last bucket
- **TOTAL** = Total size of the buckets

New element arrives at time t

- If last bucket expired, update **LAST** and **TOTAL**
- If (element == 1)
 - Create new bucket with size 1; update **TOTAL**
- Merge buckets if there are more than **k/2+2** buckets of the same size
- Update **LAST** if changed

Anytime estimate: **TOTAL – (LAST/2)**

Example Run

- If last bucket expired, update **LAST** and **TOTAL**
- If (element == 1)
 - Create new bucket with size 1; update **TOTAL**
- Merge two oldest buckets if there are more than $k/2+2$ buckets of the same size
- Update **LAST** if changed

Example (k=2):

32,16,8,8,4,4,2,1,1

32,16,8,8,4,4,2,2,1

32,16,8,8,4,4,2,2,1,1

32,16,16,8,4,2,1

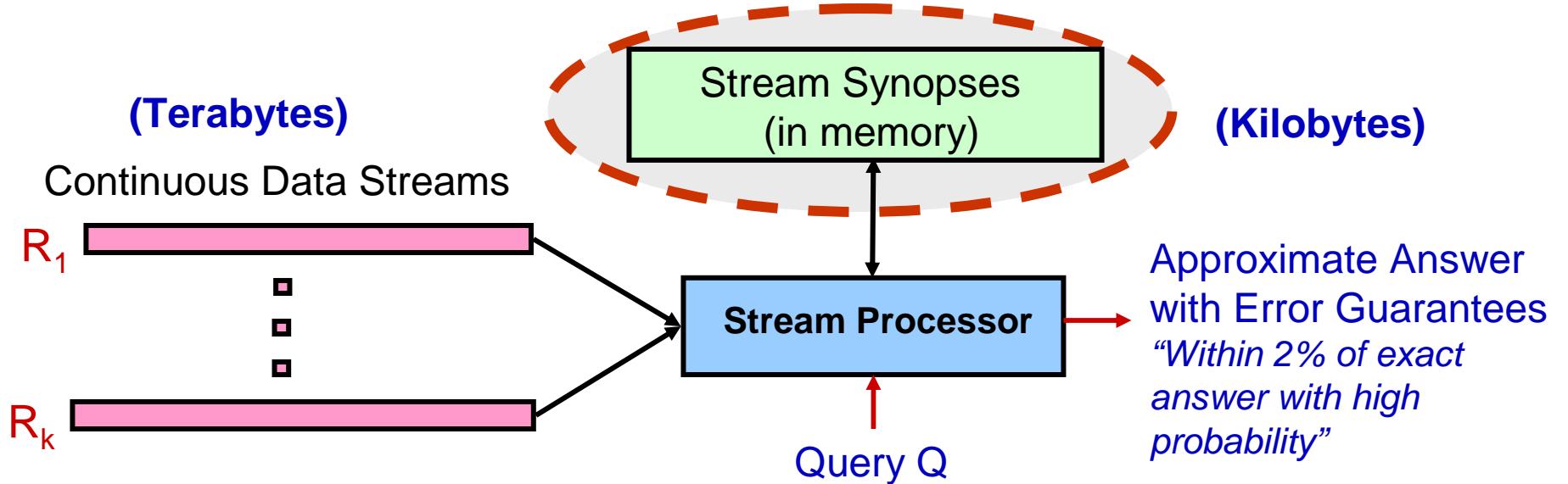
The Power of EHs

- Counter for N items = $O(\log N)$ space
- EH = ϵ -approximate counter over *sliding window* of N items that requires $O(1/\epsilon * \log^2 N)$ space
 - $O(1/\epsilon \log N)$ penalty for (approximate) sliding-window counting
 - *Deterministic error guarantee!*
- Can plug-in EH-counters to counter-based streaming methods → *work in sliding-window model!!*
 - Examples: histograms, CM-sketches, ...
- *Complication:* counting is now ϵ -approximate
 - Account for that in analysis

Tutorial Outline

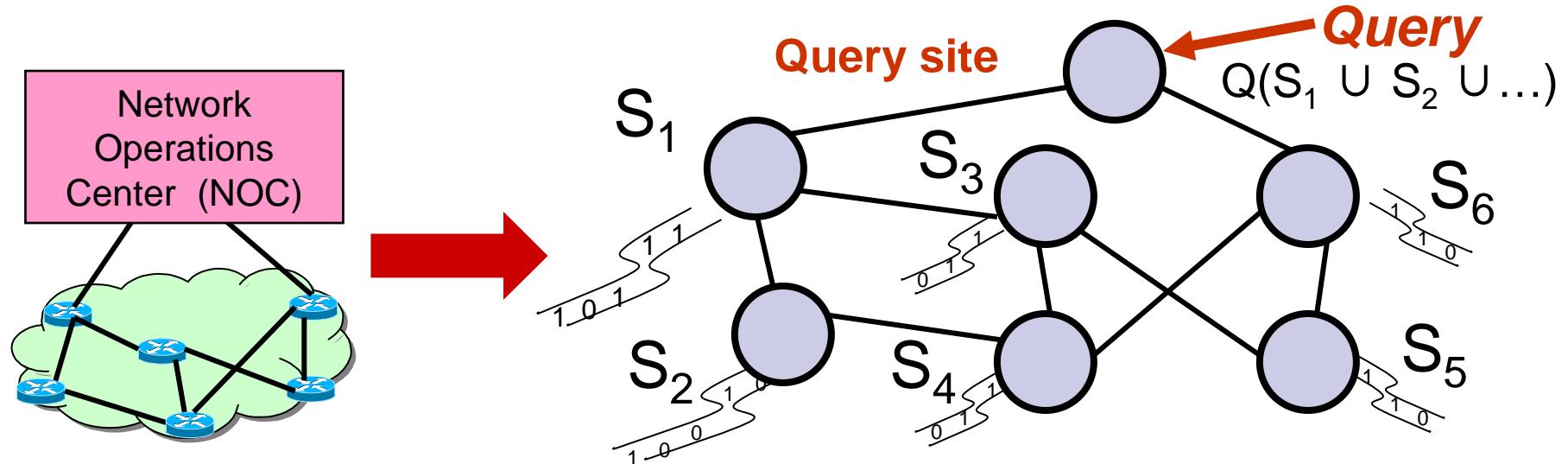
- Motivation & Streaming Applications
- Centralized Stream Processing
- Distributed Stream Processing
 - Basic model and problem setup
 - One-shot distributed-stream querying
 - Continuous distributed-stream tracking
 - Probabilistic distributed data acquisition
- Open Problems & Future Directions
- Conclusions

Data-Stream Algorithmics Model



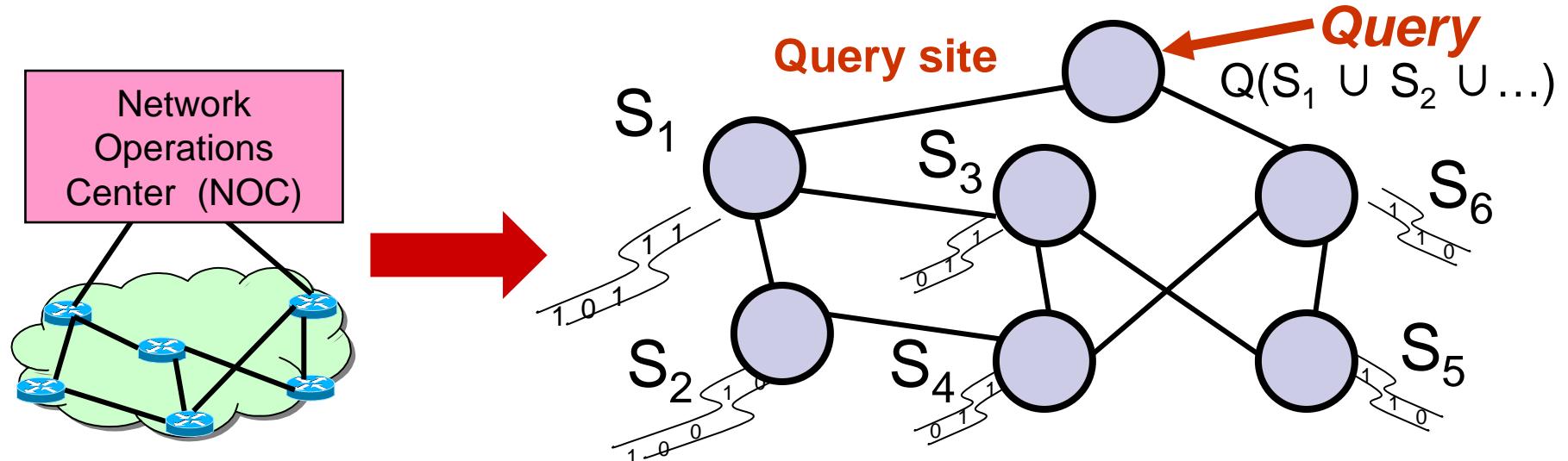
- *Approximate answers*— e.g. trend analysis, anomaly detection
- Requirements for stream synopses
 - *Single Pass*: Each record is examined at most once
 - *Small Space*: Log or polylog in data stream size
 - *Small-time*: Low per-record processing time (maintain synopses)
 - Also: *delete-proof, composable, ...*

Distributed Streams Model



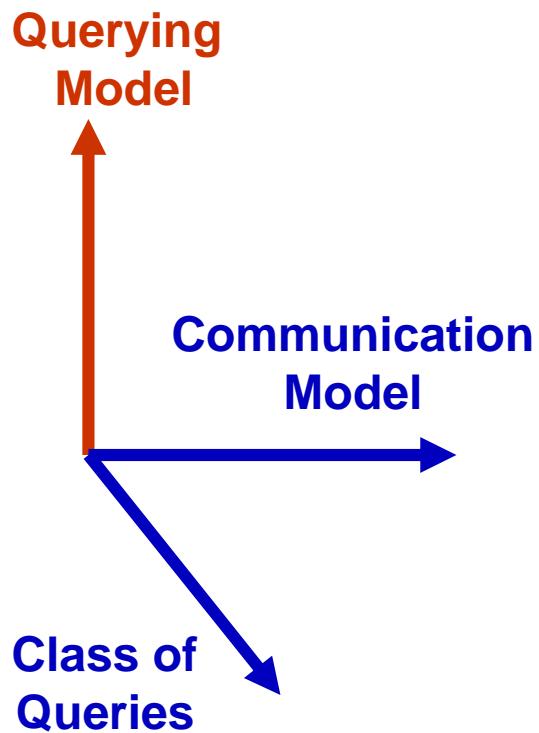
- Large-scale querying/monitoring: *Inherently distributed!*
 - Streams physically distributed across remote sites
E.g., stream of UDP packets through subset of edge routers
- *Challenge is “holistic” querying/monitoring*
 - Queries over the *union of distributed streams* $Q(S_1 \cup S_2 \cup \dots)$
 - Streaming data is spread throughout the network

Distributed Streams Model



- Need timely, accurate, and efficient query answers
- Additional complexity over centralized data streaming!
- Need space/time- *and communication-efficient* solutions
 - Minimize network overhead
 - Maximize network lifetime (e.g., sensor battery life)
 - Cannot afford to “centralize” all streaming data

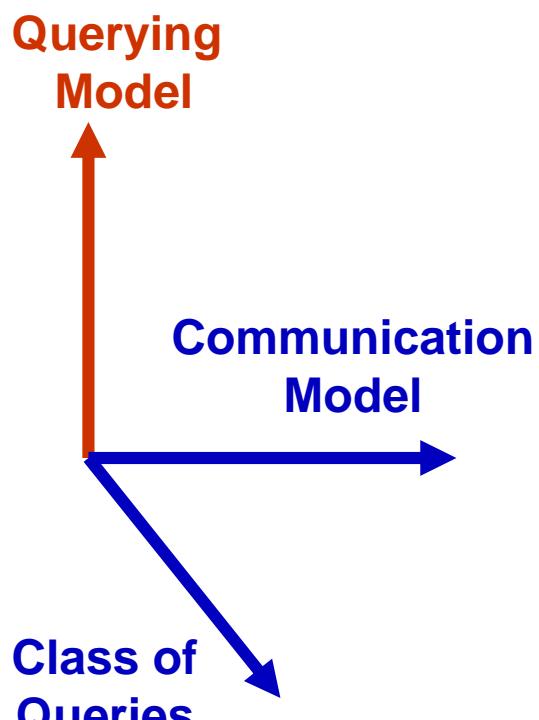
Distributed Stream Querying Space



“One-shot” vs. *Continuous Querying*

- **One-shot queries:** On-demand “pull” query answer from network
 - One or few rounds of communication
 - Nodes may prepare for a class of queries
- **Continuous queries:** Track/monitor answer at query site *at all times*
 - Detect anomalous/outlier behavior *in (near) real-time*, i.e., “Distributed triggers”
 - Challenge is to minimize communication
 - Use “push-based” techniques
 - May use one-shot algs as subroutines

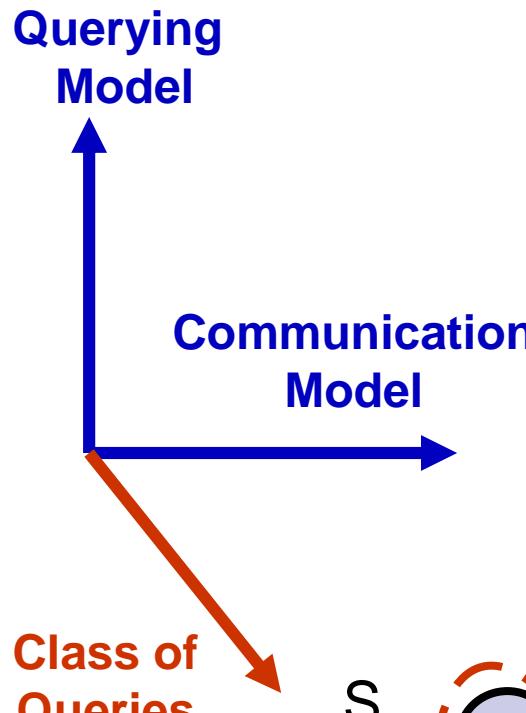
Distributed Stream Querying Space



Minimizing communication often needs approximation and randomization

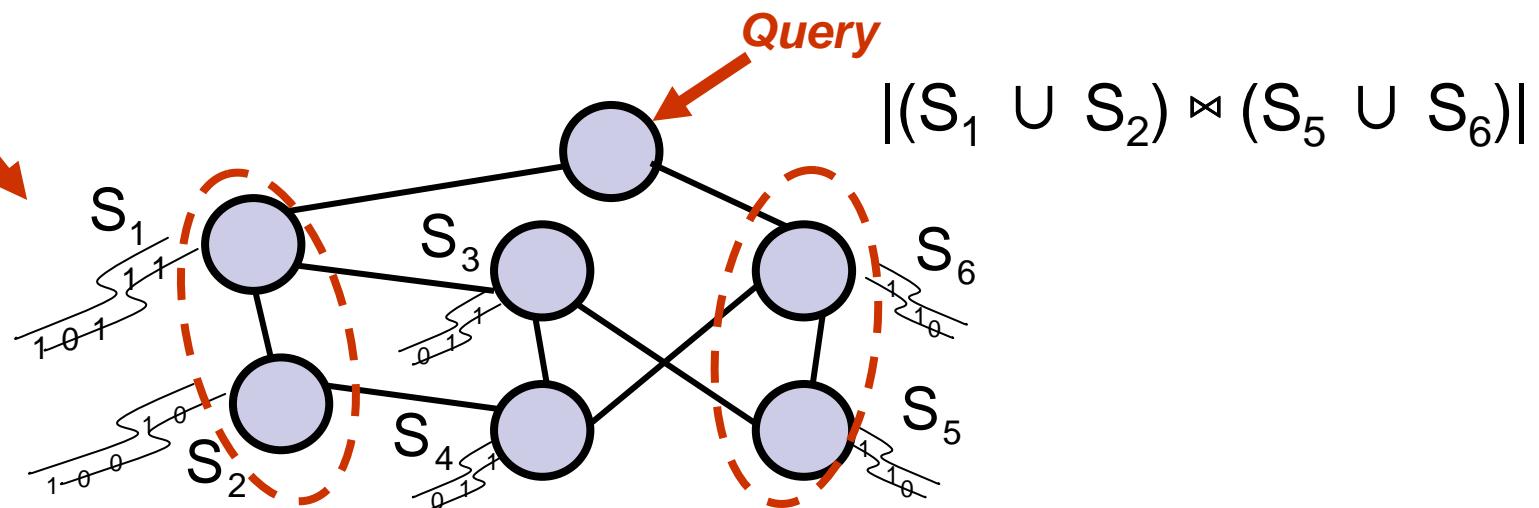
- E.g., Continuously monitor average value
 - Must send every change for exact answer
 - Only need ‘significant’ changes for approx (def. of “significant” specifies an algorithm)
- Probability sometimes vital to reduce communication
 - **count distinct** in one shot model needs randomness
 - Else **must** send complete data

Distributed Stream Querying Space

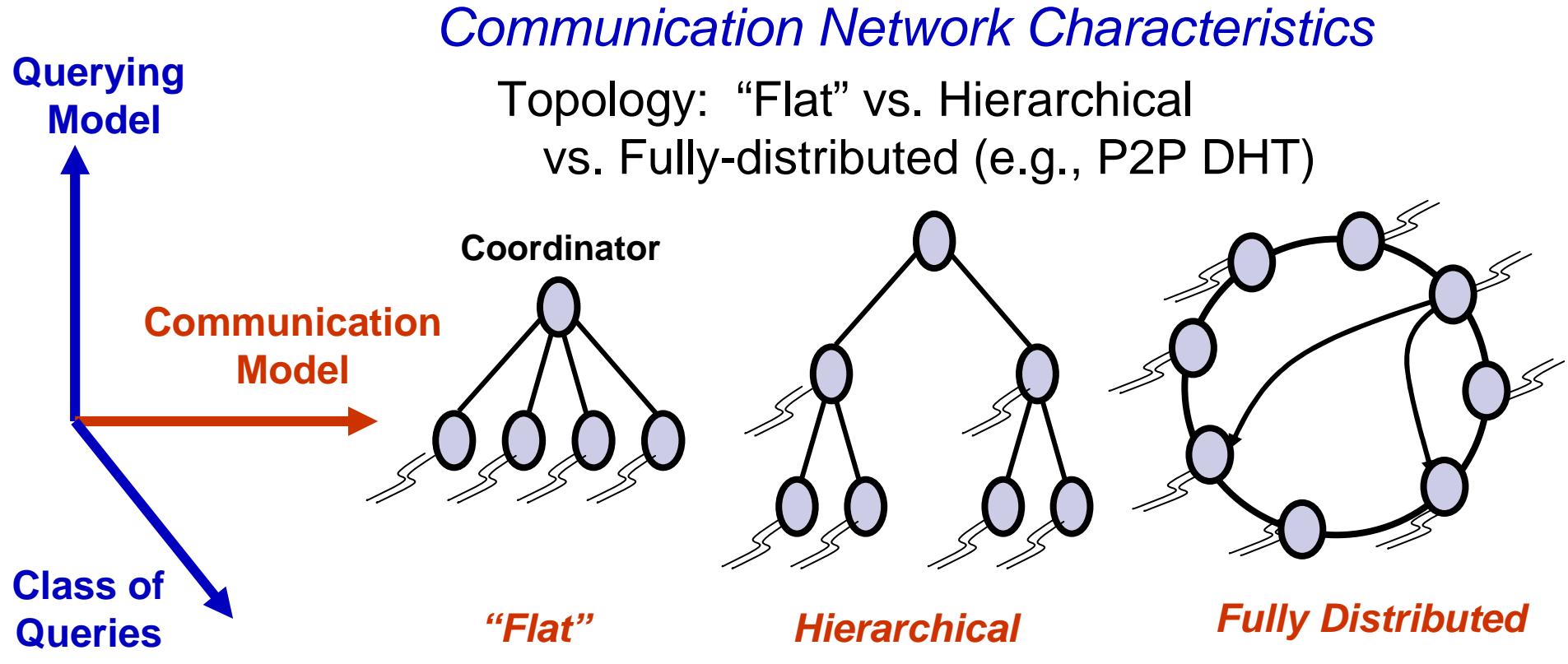


Class of Queries of Interest

- Simple algebraic vs. holistic aggregates
 - E.g., **count / max** vs. quantiles/top-k
- Duplicate-sensitive vs. duplicate-insensitive
 - “Bag” vs. “set” semantics
- Complex correlation queries
 - E.g., distributed joins, set expressions, ...



Distributed Stream Querying Space



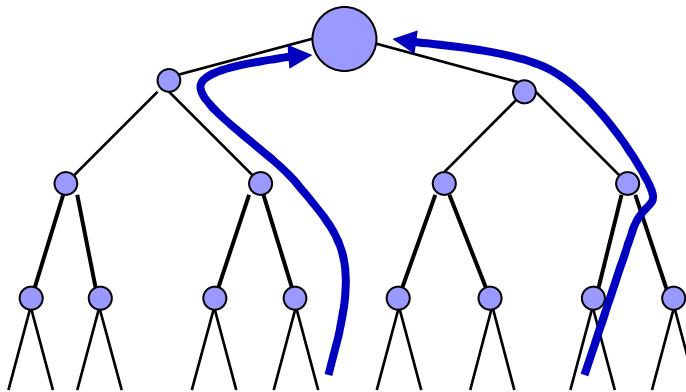
Other network characteristics:

- Unicast (traditional wired), multicast, broadcast (radio nets)
- Node failures, loss, intermittent connectivity, ...

Tutorial Outline

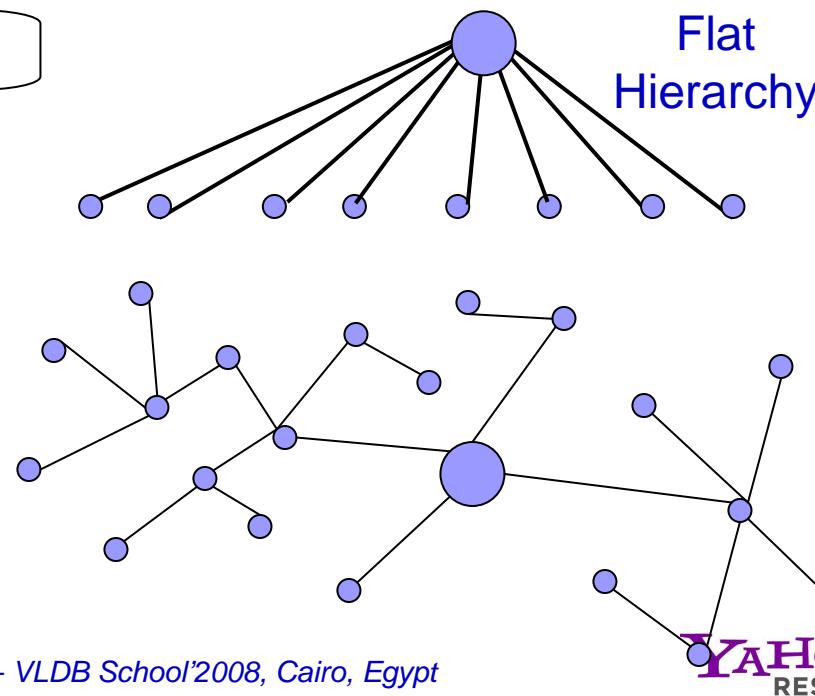
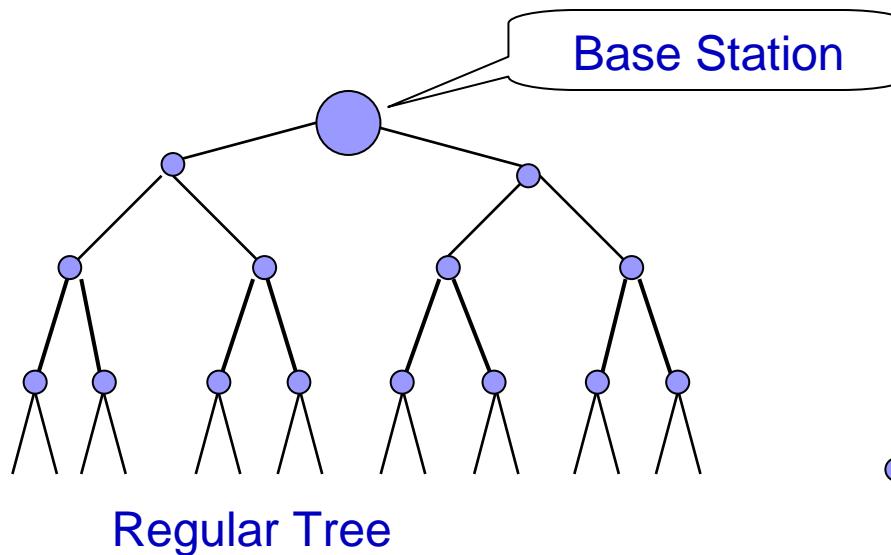
- Motivation & Streaming Applications
- Centralized Stream Processing
- Distributed Stream Processing
 - One-shot distributed-stream querying
 - Tree-based aggregation
 - Robustness and loss
 - Decentralized computation and gossiping
- Open Problems & Future Directions
- Conclusions

Tree Based Aggregation



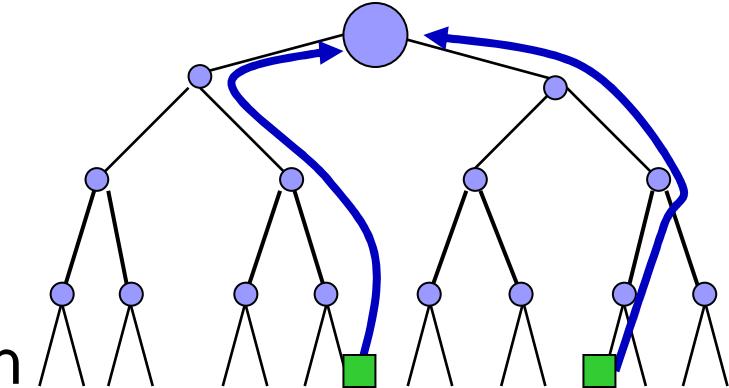
Network Trees

- Tree structured networks are a basic primitive
 - Much work in, e.g., sensor nets on building communication trees
 - We assume that tree has been built, focus on issues with a fixed tree



Computation in Trees

- Goal is for root to compute a function of data at leaves
- Trivial solution: push all data up tree and compute at base station
 - Strains nodes near root: batteries drain, disconnecting network
 - Very wasteful: no attempt at saving communication
- Can do much better by “**In-network**” query processing
 - Simple example: computing **max**
 - Each node hears from all children, computes max and sends to parent (each node sends only one item)



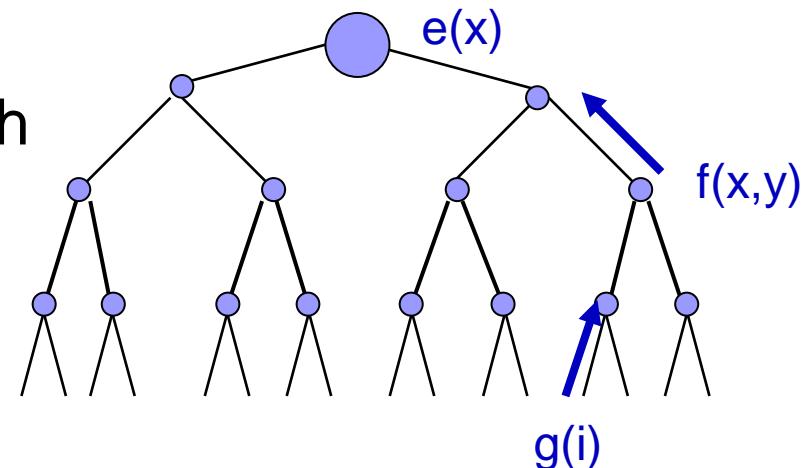
Efficient In-network Computation

- What are aggregates of interest?
 - SQL Primitives: `min`, `max`, `sum`, `count`, `avg`
 - More complex: `count distinct`, point & range queries, quantiles, wavelets, histograms, sample
 - Data mining: association rules, clusterings etc.
- Some aggregates are easy – e.g., SQL primitives
- Can set up a formal framework for in-network aggregation

Generate, Fuse, Evaluate Framework

- Abstract in-network aggregation. Define functions:
 - **Generate**, $g(i)$: take input, produce summary (at leaves)
 - **Fusion**, $f(x,y)$: merge two summaries (at internal nodes)
 - **Evaluate**, $e(x)$: output result (at root)
- E.g. **max**: $g(i) = i$ $f(x,y) = \max(x,y)$ $e(x) = x$
- E.g. **avg**: $g(i) = (i,1)$ $f((i,j),(k,l)) = (i+k,j+l)$ $e(i,j) = i/j$

- Can specify any function with
 $g(i) = \{i\}$, $f(x,y) = x \cup y$
Want to bound $|f(x,y)|$



Classification of Aggregates

- Different properties of aggregates
(from TAG paper [Madden et al '02])
 - Duplicate sensitive – is answer same if multiple identical values are reported?
 - Example or summary – is result some value from input (**max**) or a small summary over the input (**sum**)
 - Monotonicity – is $F(X \cup Y)$ monotonic compared to $F(X)$ and $F(Y)$ (affects push down of selections)
 - Partial state – are $|g(x)|$, $|f(x,y)|$ constant size, or growing?
Is the aggregate *algebraic*, or *holistic*?

Classification of some aggregates

	Duplicate Sensitive	Example or summary	Monotonic	Partial State
min, max	No	Example	Yes	algebraic
sum, count	Yes	Summary	Yes	algebraic
average	Yes	Summary	No	algebraic
median, quantiles	Yes	Example	No	holistic
count distinct	No	Summary	Yes	holistic
sample	Yes	Example(s)	No	algebraic?
histogram	Yes	Summary	No	holistic

adapted from [Madden et al.'02]

Cost of Different Aggregates

Slide adapted from <http://db.lcs.mit.edu/madden/html/jobtalk3.ppt>

Simulation Results

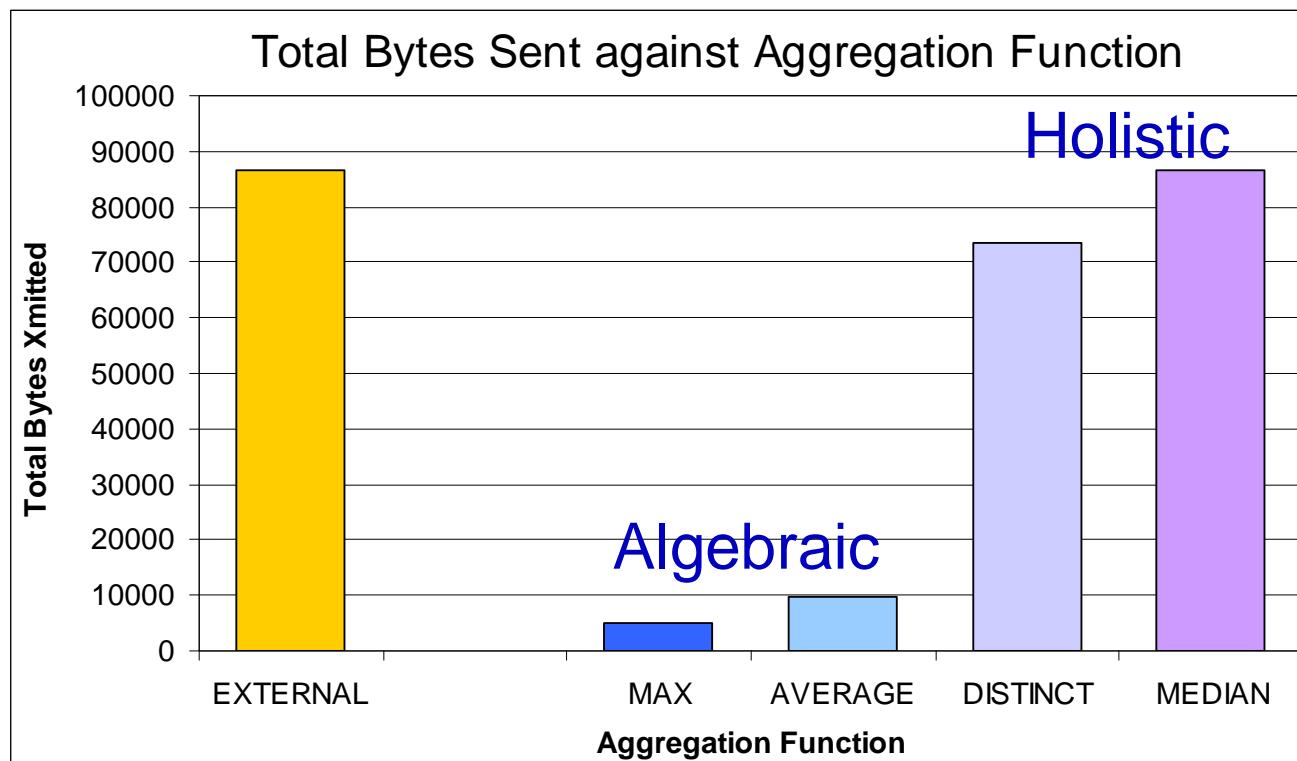
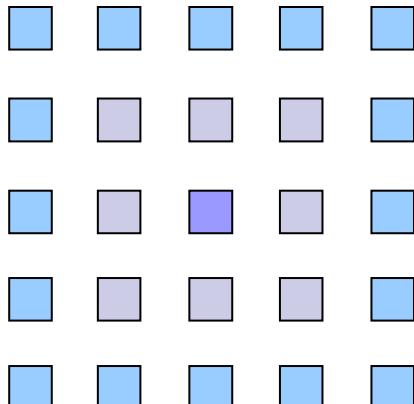
2500 Nodes

50x50 Grid

Depth = ~10

Neighbors = ~20

Uniform Dist.

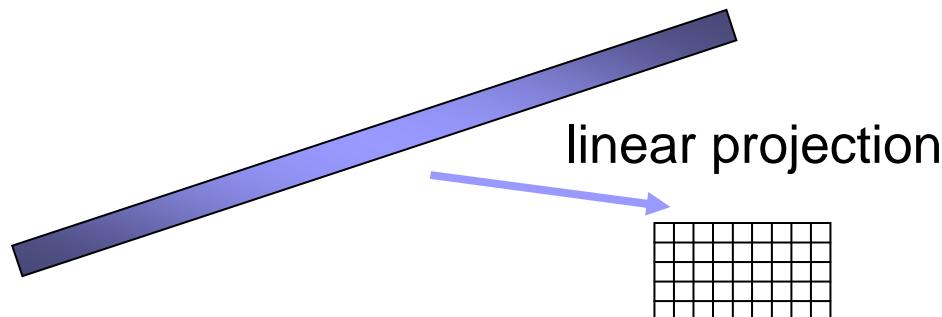


Holistic Aggregates

- Holistic aggregates need the whole input to compute (no summary suffices)
 - E.g., **count distinct**, need to remember all distinct items to tell if new item is distinct or not
- So, focus on **approximating** aggregates to limit data sent
 - Adopt ideas from sampling, data reduction, streams, etc.
- Many techniques for in-network aggregate approximation:
 - Sketch summaries
 - Other mergeable summaries
 - Building uniform samples, etc...

Sketch Summaries

- Sketch summaries are typically pseudo-random linear projections of data. Fits generate/fuse/evaluate model:
 - Suppose input is vectors x_i and aggregate is $F(\sum_i x_i)$
 - Sketch of x_i , $g(x_i)$, is a matrix product Mx_i
 - Combination of two sketches is their summation:
 $f(g(x_i), g(x_j)) = M(x_i + x_j) = Mx_i + Mx_j = g(x_i) + g(x_j)$
 - Extraction function $e()$ depends on sketch, different sketches allow approximation of different aggregates



Sketch Summary

- CM sketch guarantees approximation error on point queries less than $\epsilon \|\mathbf{x}\|_1$ in size $O(1/\epsilon \log 1/\delta)$
 - Probability of more error is less than $1-\delta$
 - Similar guarantees for range queries, quantiles, join size
- AMS sketches approximate self-join and join size with error less than $\epsilon \|\mathbf{x}\|_2 \|\mathbf{y}\|_2$ in size $O(1/\epsilon^2 \log 1/\delta)$
 - [Alon, Matias, Szegedy '96, Alon, Gibbons, Matias, Szegedy '99]
- FM sketches approximate number of distinct items ($\|\mathbf{x}\|_0$) with error less than $\epsilon \|\mathbf{x}\|_0$ in size $O(1/\epsilon^2 \log 1/\delta)$
- Bloom filters: compactly encode sets in sketch like fashion

Other approaches: Careful Merging

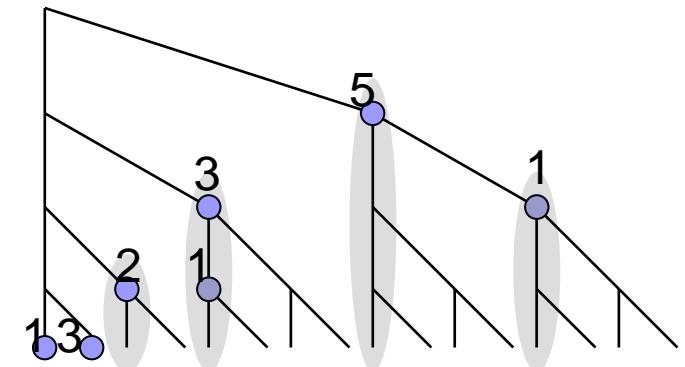
■ Approach 1. Careful merging of summaries

- Small summaries of a large amount of data at each site
- E.g., Greenwald-Khanna algorithm (**GK**) keeps a small data structure to allow quantile queries to be answered
- Can sometimes carefully merge summaries up the tree
Problem: if not done properly, the merged summaries can grow very large as they approach root
- Balance final quality of answer against number of merges by decreasing approximation quality (*precision gradient*)
- See [Greenwald, Khanna '04; Manjhi et al.'05; Manjhi, Nath, Gibbons '05]

Other approaches: Domain Aware

■ Approach 2. Domain-aware Summaries

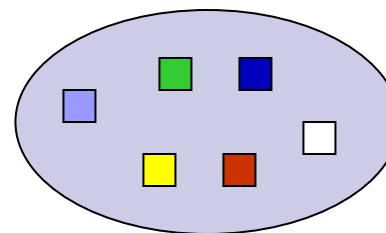
- Each site sees information drawn from discrete domain $[1 \dots N]$ – e.g., for IP addresses, $N = 2^{32}$
- Build summaries by imposing tree-structure on domain and keeping counts of nodes representing subtrees
- [Agrawal et al '04] show $O(1/\epsilon \log N)$ size summary for quantiles and range & point queries
- Can merge repeatedly without increasing error or summary size



Other approaches: Random Samples

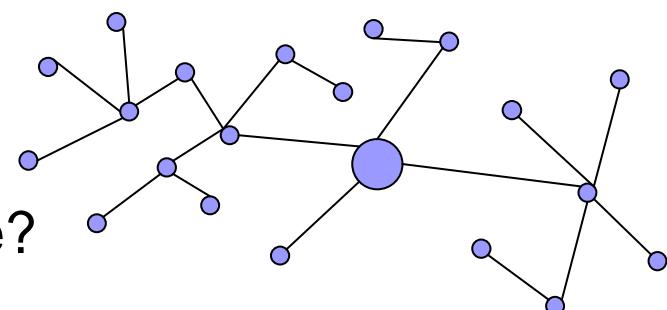
■ Approach 3. Uniform random samples

- As in centralized databases, a uniform random sample of size $O(1/\varepsilon^2 \log 1/\delta)$ answers many queries
- Can collect a random sample of data from each node, and merge up the tree (will show algorithms later)
- Works for frequent items, quantile queries, histograms
- No good for count distinct, min, max, wavelets...

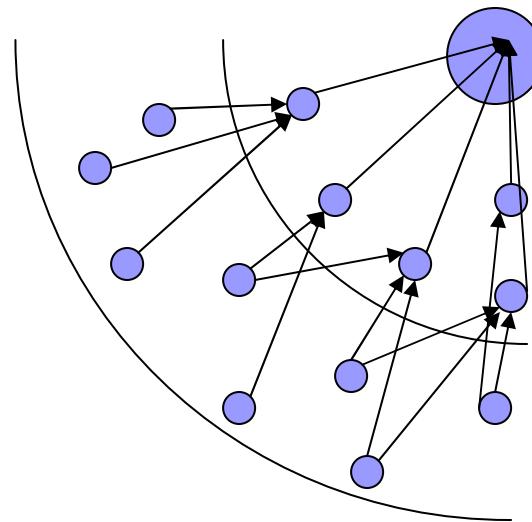


Thoughts on Tree Aggregation

- Some methods too heavyweight for today's sensor nets, but as technology improves may soon be appropriate
- Most are well suited for, e.g., [wired network monitoring](#)
 - Trees in wired networks often treated as flat, i.e. send directly to root without modification along the way
- Techniques are fairly well-developed owing to work on data reduction/summarization and streams
- Open problems and challenges:
 - Improve size of larger summaries
 - Avoid randomized methods?
Or use randomness to reduce size?

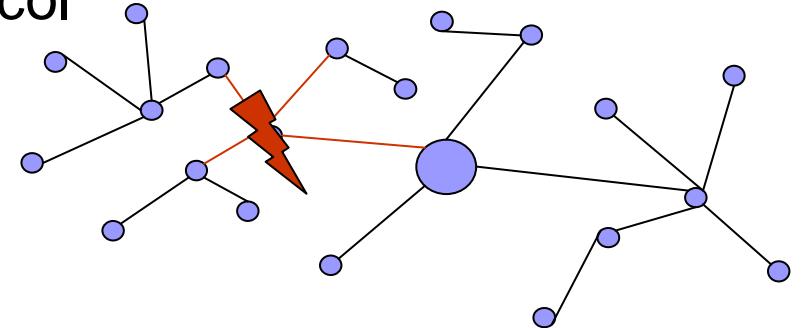


Robustness and Loss



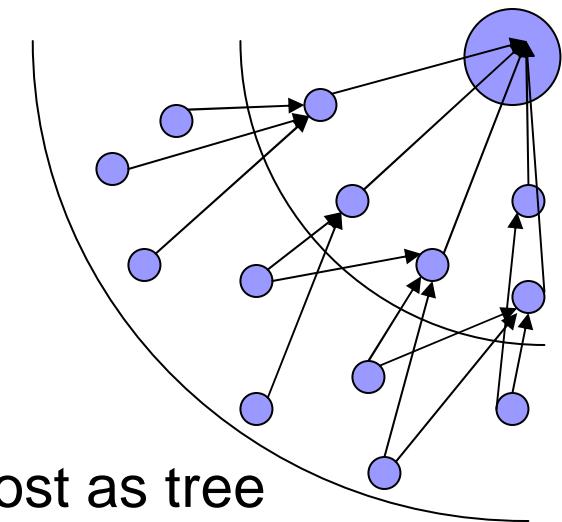
Unreliability

- Tree aggregation techniques assumed a reliable network
 - we assumed no node failure, nor loss of any message
- Failure can dramatically affect the computation
 - E.g., **sum** – if a node near the root fails, then a whole subtree may be lost
- Clearly a particular problem in sensor networks
 - If messages are lost, maybe can detect and resend
 - If a node fails, may need to rebuild the whole tree and re-run protocol
 - Need to detect the failure, could cause high uncertainty



Sensor Network Issues

- Sensor nets typically based on radio communication
 - So broadcast (within range) cost the same as unicast
 - Use multi-path routing: improved reliability, reduced impact of failures, less need to repeat messages
- E.g., computation of **max**
 - structure network into rings of nodes in equal hop count from root
 - listen to all messages from ring below, then send max of all values heard
 - converges quickly, high path diversity
 - each node sends only once, so same cost as tree

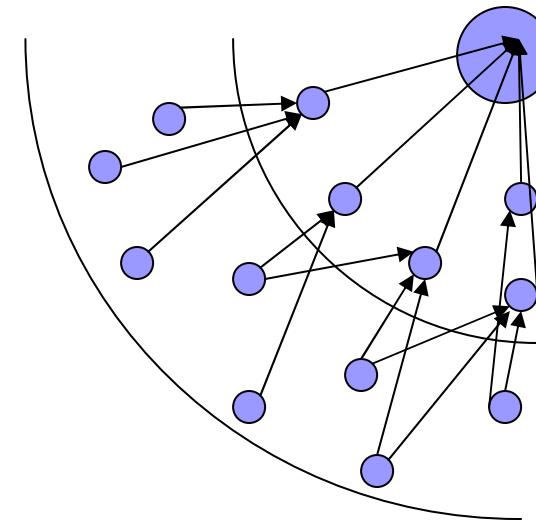


Order and Duplicate Insensitivity

- It works because **max** is *Order and Duplicate Insensitive (ODI)* [Nath et al.'04]
- Make use of the same $e()$, $f()$, $g()$ framework as before
- Can prove correct if $e()$, $f()$, $g()$ satisfy properties:
 - g gives same output for duplicates: $i=j \Rightarrow g(i) = g(j)$
 - f is associative and commutative:
$$f(x,y) = f(y,x); f(x,f(y,z)) = f(f(x,y),z)$$
 - f is same-synopsis idempotent: $f(x,x) = x$
- Easy to check **min**, **max** satisfy these requirements, **sum** does not

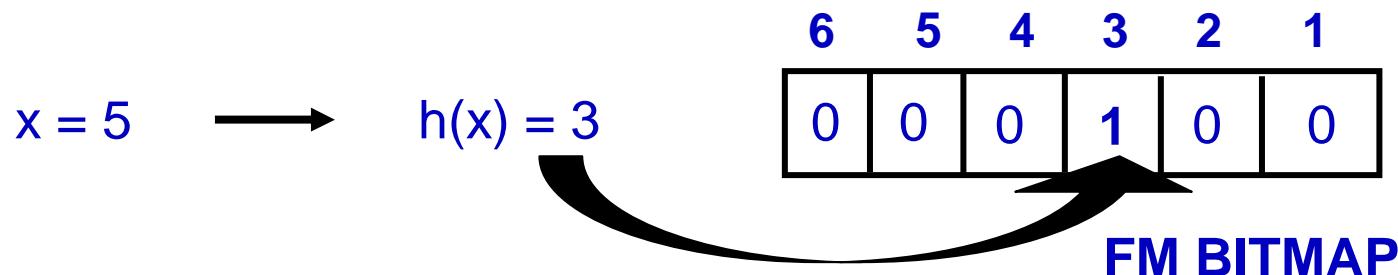
Applying ODI idea

- Only **max** and **min** seem to be “naturally” ODI
- How to make ODI summaries for other aggregates?
- Will make use of duplicate insensitive primitives:
 - Flajolet-Martin Sketch (FM)
 - Min-wise hashing
 - Random labeling
 - Bloom Filter



FM Sketch [Flajolet, Martin'85]

- Estimates number of distinct inputs (**count distinct**)
- Uses hash function mapping input items to i with prob 2^{-i}
 - i.e. $\Pr[h(x) = 1] = \frac{1}{2}$, $\Pr[h(x) = 2] = \frac{1}{4}$, $\Pr[h(x)=3] = 1/8 \dots$
 - Easy to construct $h()$ from a uniform hash function by counting trailing zeros
- Maintain FM Sketch = bitmap array of $L = \log N$ bits
 - Initialize bitmap to all 0s
 - For each incoming value x , set $FM[h(x)] = 1$



FM Sketch – ODI Properties

$$\begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{0} & \boxed{1} & \boxed{1} \end{array} + \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{1} & \boxed{1} & \boxed{0} & \boxed{0} & \boxed{1} \end{array} = \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \boxed{0} & \boxed{1} & \boxed{1} & \boxed{0} & \boxed{1} & \boxed{1} \end{array}$$

- Fits into the Generate, Fuse, Evaluate framework.
 - Can fuse multiple FM summaries (with same hash $h()$): take bitwise-OR of the summaries
- With $O(1/\epsilon^2 \log 1/\delta)$ copies, get $(1 \pm \epsilon)$ accuracy with probability at least $1 - \delta$
 - 10 copies gets $\approx 30\%$ error, 100 copies $< 10\%$ error
 - Can pack FM into e.g., 32 bits. Assume $h()$ is known to all.
- Similar ideas used in [Gibbons, Tirthapura '01]
 - improves time cost to create summary, simplifies analysis

FM within ODI

- What if we want to count, not count distinct?
 - E.g., each site i has a count c_i , we want $\sum_i c_i$
 - Tag each item with site ID, write in unary: $(i,1), (i,2) \dots (i,c_i)$
 - Run FM on the modified input, and run ODI protocol
- What if counts are large?
 - Writing in unary might be too slow, need to make efficient
 - [Considine et al.'05]: simulate a random variable that tells which entries in sketch are set
 - [Aduri, Tirthapura '05]: allow range updates, treat (i, c_i) as range.

Other applications of FM in ODI

- Can take sketches and other summaries and make them ODI by replacing counters with FM sketches
 - CM sketch + FM sketch = CMFM, ODI point queries etc.
[Cormode, Muthukrishnan '05]
 - Q-digest + FM sketch = ODI quantiles
[Hadjieleftheriou, Byers, Kolios '05]
 - Counts and sums
[Nath et al.'04, Considine et al.'05]

6	5	4	3	2	1
0	1	1	0	1	1

Combining ODI and Tree

- *Tributaries and Deltas* idea
[Manjhi, Nath, Gibbons '05]
- Combine small synopsis of tree-based aggregation with reliability of ODI
 - Run tree synopsis at edge of network, where connectivity is limited (tributary)
 - Convert to ODI summary in dense core of network (delta)
 - Adjust crossover point adaptively

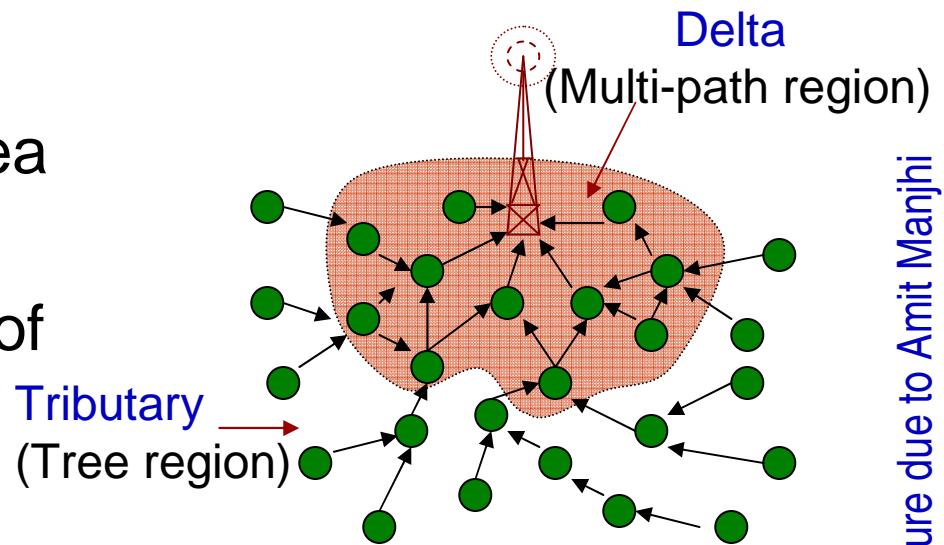
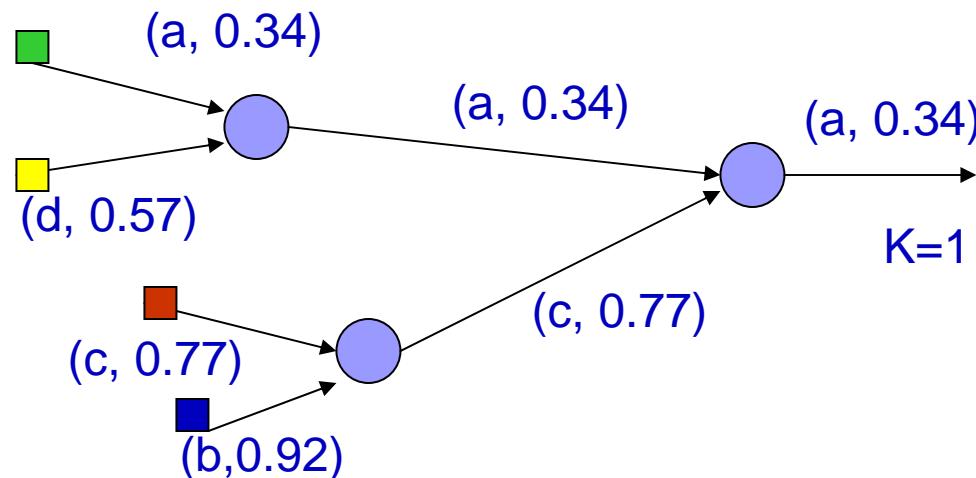


Figure due to Amit Manjhi

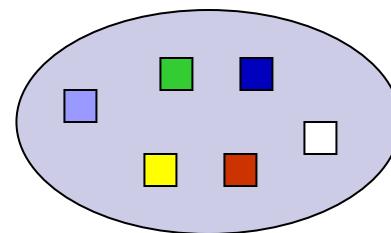
Random Samples

- Suppose each node has a (multi)set of items.
- How to find a random sample of the union of all sets?
- Use a “random tagging” trick [Nath et al.’05]:
 - For each item, attach a random label in range $[0\dots 1]$
 - Pick the items with the K smallest labels to send
 - Merge all received items, and pick K smallest labels



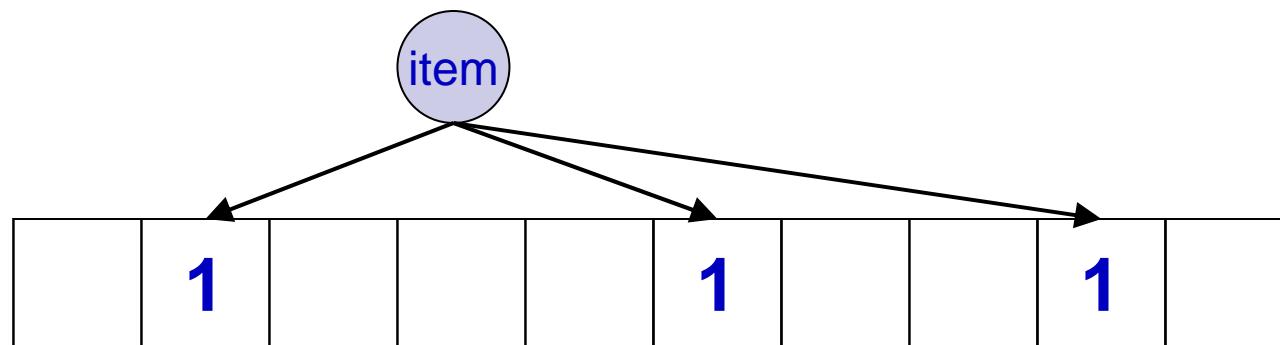
Uniform Random Samples

- Result at the coordinator:
 - A sample of size K items from the input
 - Can show that the sample is chosen uniformly at random without replacement (could make “with replacement”)
- Related to **min-wise hashing**
 - Suppose we want to sample from distinct items
 - Then replace random tag with hash value on item name
 - Result: uniform sample from **set** of present items
- Sample can be used for quantiles, frequent items, etc.



Bloom Filters

- Bloom filters compactly encode set membership
 - k hash functions map items to bit vector k times
 - Set all k entries to **1** to indicate item is present
 - Can lookup items, store set of size n in $\sim 2n$ bits



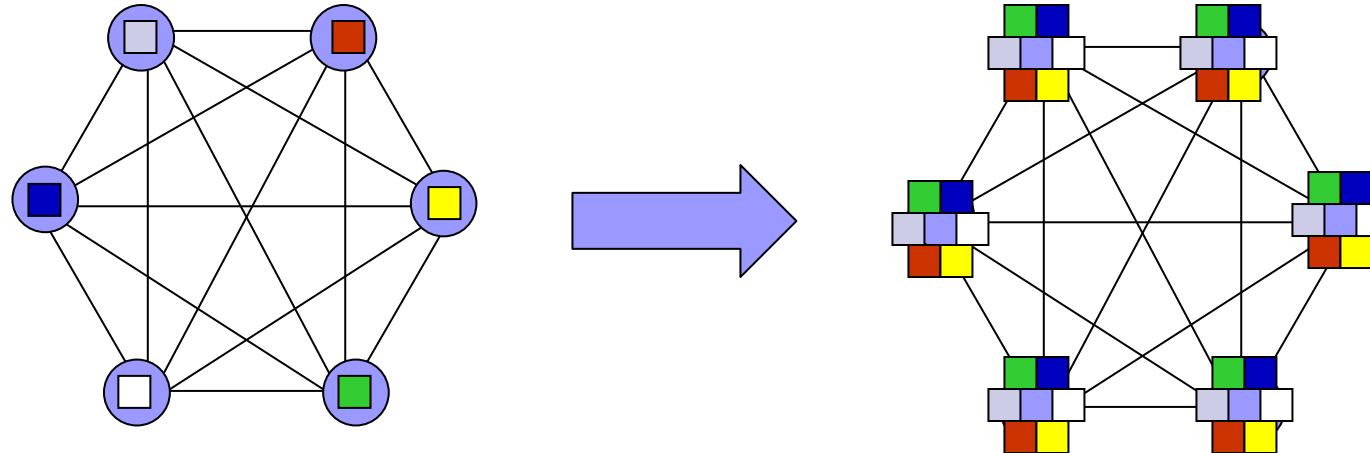
- Bloom filters are ODI, and merge like FM sketches

Open Questions and Extensions

- Characterize all queries – can everything be made ODI with small summaries?
- How practical for different sensor systems?
 - Few FM sketches are very small (10s of bytes)
 - Sketch with FMs for counters grow large (100s of KBs)
 - What about the computational cost for sensors?
- Amount of randomness required, and implicit coordination needed to agree hash functions, etc.?
- Other implicit requirements: unique sensor IDs?

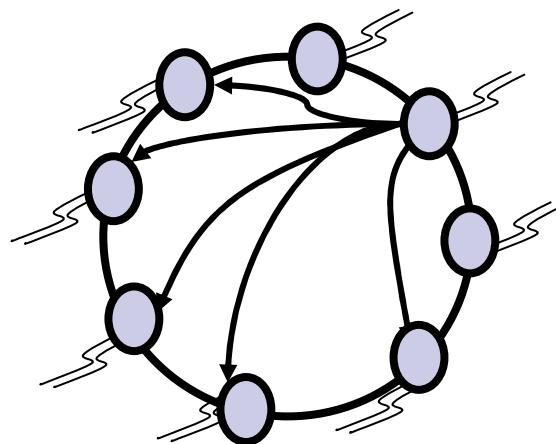
6	5	4	3	2	1
0	1	1	0	1	1

Decentralized Computation and Gossiping



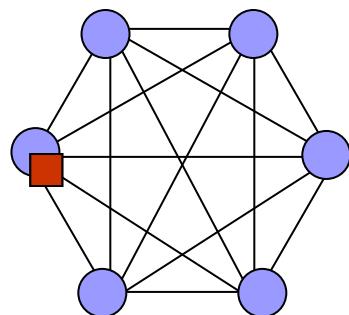
Decentralized Computations

- All methods so far have a single point of failure: if the base station (root) dies, everything collapses
- An alternative is **Decentralized Computation**
 - Everyone participates in computation, all get the result
 - Somewhat resilient to failures / departures
- Initially, assume anyone can talk to anyone else directly



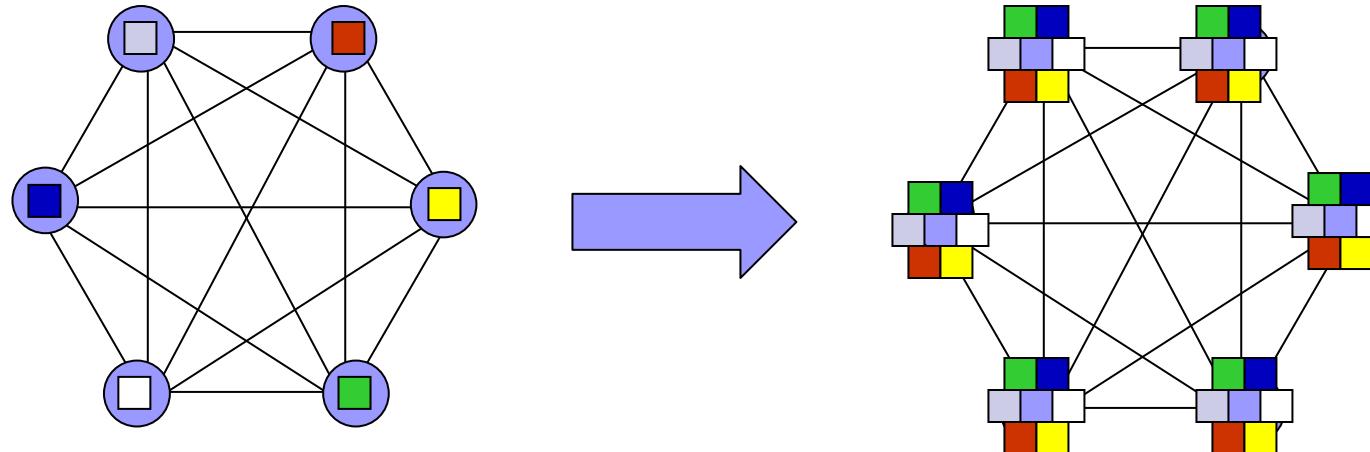
Gossiping

- “Uniform Gossiping” is a well-studied protocol for spreading information
 - I know a secret, I tell two friends, who tell two friends ...
 - Formally, each round, everyone who knows the data sends it to one of the n participants chosen at random
 - After $O(\log n)$ rounds, all n participants know the information (with high probability) [Pittel 1987]



Aggregate Computation via Gossip

- Naïve approach: use uniform gossip to share all the data, then everyone can compute the result.
 - Slightly different situation: gossiping to exchange n secrets
 - Need to store all results so far to avoid double counting
 - Messages grow large: end up sending whole input around

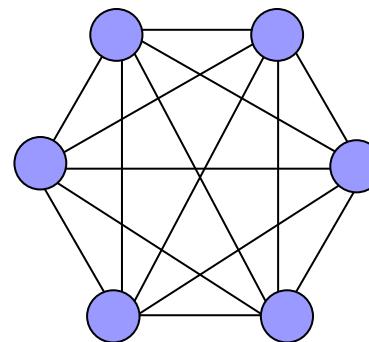


ODI Gossiping

- If we have an ODI summary, we can gossip with this
 - When new summary received, merge with current summary
 - ODI properties ensure repeated merging stays accurate
- Number of messages required is same as uniform gossip
 - After $O(\log n)$ rounds everyone knows the merged summary
 - Message size and storage space is a single summary
 - $O(n \log n)$ messages in total
 - So, this works for FM, FM-based sketches, samples, etc.

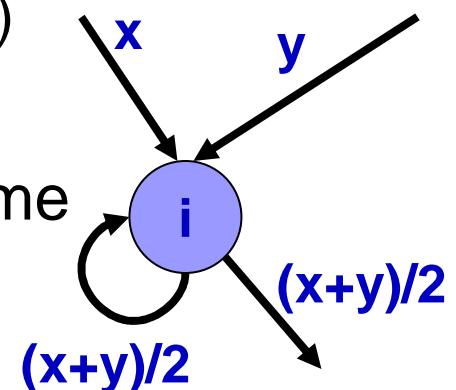
Aggregate Gossiping

- ODI gossiping doesn't always work
 - May be too heavyweight for really restricted devices
 - Summaries may be too large in some cases
- An alternate approach due to [Kempe et al. '03]
 - A novel way to avoid double counting: split up the counts and use “**conservation of mass**”

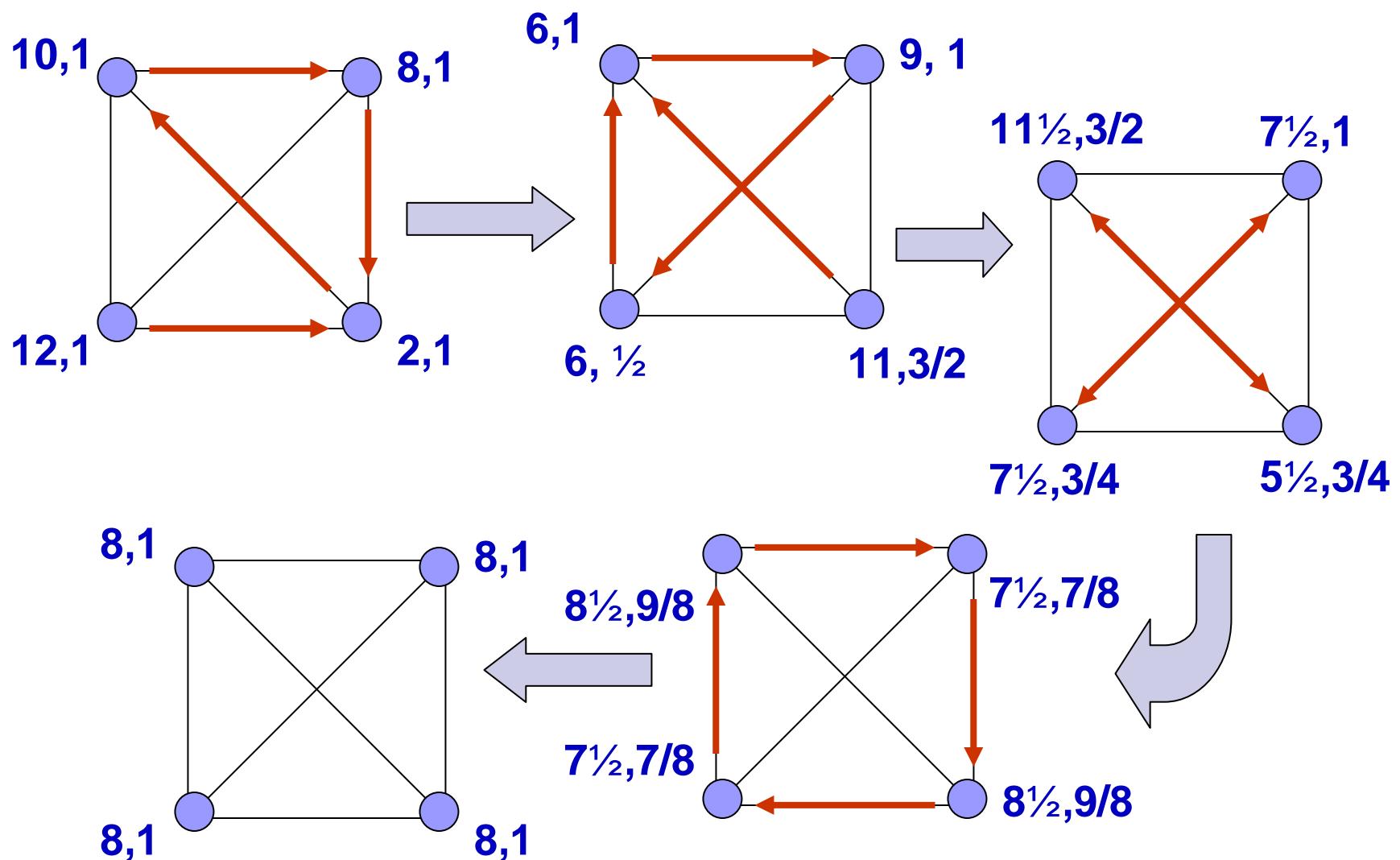


Push-Sum

- Setting: all n participants have a value, want to compute average
- Define “**Push-Sum**” protocol
 - In round t , node i receives set of $(\text{sum}_j^{t-1}, \text{count}_j^{t-1})$ pairs
 - Compute $\text{sum}_i^t = \sum_j \text{sum}_j^{t-1}$, $\text{count}_i^t = \sum_j \text{count}_j^{t-1}$
 - Pick k uniformly from other nodes
 - Send $(\frac{1}{2} \text{sum}_i^t, \frac{1}{2}\text{count}_i^t)$ to k and to i (self)
- Round zero: send $(\text{value}, 1)$ to self
- Conservation of counts: $\sum_i \text{sum}_i^t$ stays same
- Estimate $\text{avg} = \text{sum}_i^t / \text{count}_i^t$



Push-Sum Convergence

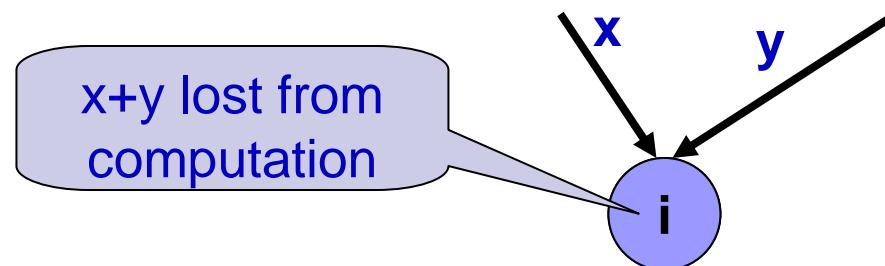


Convergence Speed

- Can show that after $O(\log n + \log 1/\varepsilon + \log 1/\delta)$ rounds, the protocol converges within ε
 - n = number of nodes
 - ε = (relative) error
 - δ = failure probability
- Correctness due in large part to conservation of counts
 - Sum of values remains constant throughout
 - (Assuming no loss or failure)

Resilience to Loss and Failures

- Some resilience comes for “free”
 - If node detects message was not delivered, delay 1 round then choose a different target
 - Can show that this only increases number of rounds by a small constant factor, even with many losses
 - Deals with message loss, and “dead” nodes without error
- If a node fails during the protocol, some “mass” is lost, and count conservation does not hold
 - If the mass lost is not too large, error is bounded...



Gossip on Vectors

- Can run **Push-Sum** independently on each entry of vector
- More strongly, generalize to **Push-Vector**:
 - Sum incoming vectors
 - Split sum: half for self, half for randomly chosen target
 - Can prove same conservation and convergence properties
- Generalize to sketches: a sketch is just a vector
 - But ϵ error on a sketch may have different impact on result
 - Require $O(\log n + \log 1/\epsilon + \log 1/\delta)$ rounds as before
 - Only store $O(1)$ sketches per site, send 1 per round

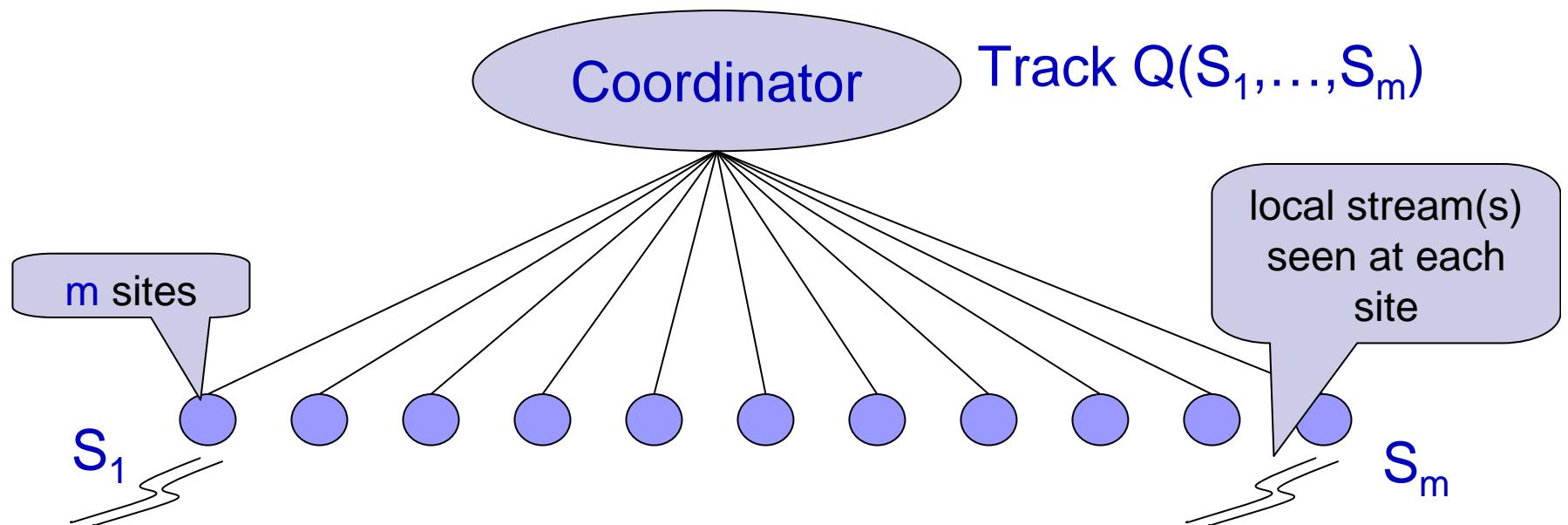
Thoughts and Extensions

- How realistic is complete connectivity assumption?
 - In sensor nets, nodes only see a local subset
 - Variations: spatial gossip ensures nodes hear about local events with high probability [Kempe, Kleinberg, Demers '01]
- Can do better with more structured gossip, but impact of failure is higher [Kashyap et al.'06]
- Is it possible to do better when only a subset of nodes have relevant data and want to know the answer?

Tutorial Outline

- Motivation & Streaming Applications
- Centralized Stream Processing
- Distributed Stream Processing
 - One-shot distributed-stream querying
 - Continuous distributed-stream tracking
 - Adaptive slack allocation
 - Predictive local-stream models
 - Distributed triggers
- Open Problems & Future Directions
- Conclusions

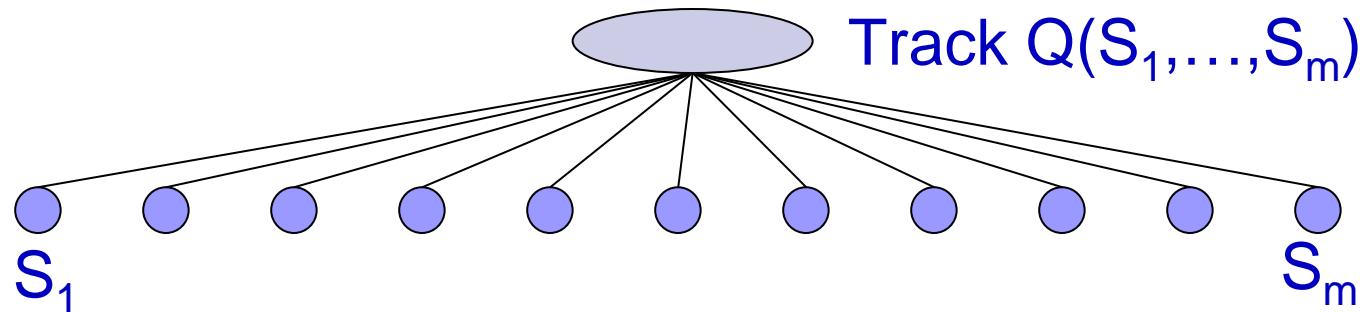
Continuous Distributed Model



- Other structures possible (e.g., hierarchical)
 - Could allow site-site communication, but mostly unneeded
- Goal:** Continuously track (global) query over streams at the coordinator
- Large-scale network-event monitoring, real-time anomaly/DDoS attack detection, power grid monitoring, ...

Continuous Distributed Streams

- But... local site streams continuously change!
 - E.g., new readings are made, new data arrives
 - *Assumption:* Changes are somewhat smooth and gradual
- Need to guarantee an answer at the coordinator that is always correct, within some guaranteed accuracy bound
- Naïve solutions must *continuously* centralize all data
 - Enormous communication overhead!

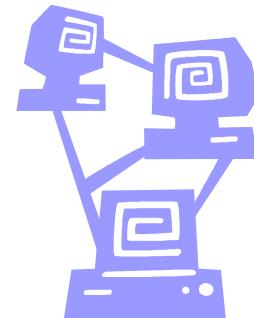


Challenges

- Monitoring is **Continuous...**
 - Real-time tracking, rather than one-shot query/response
- ...**Distributed...**
 - Each remote site only observes part of the global stream(s)
 - *Communication constraints*: must minimize monitoring burden
- ...**Streaming...**
 - Each site sees a high-speed local data stream and can be resource (CPU/memory) constrained
- ...**Holistic...**
 - Challenge is to monitor the *complete global data distribution*
 - Simple aggregates (e.g., aggregate traffic) are easier

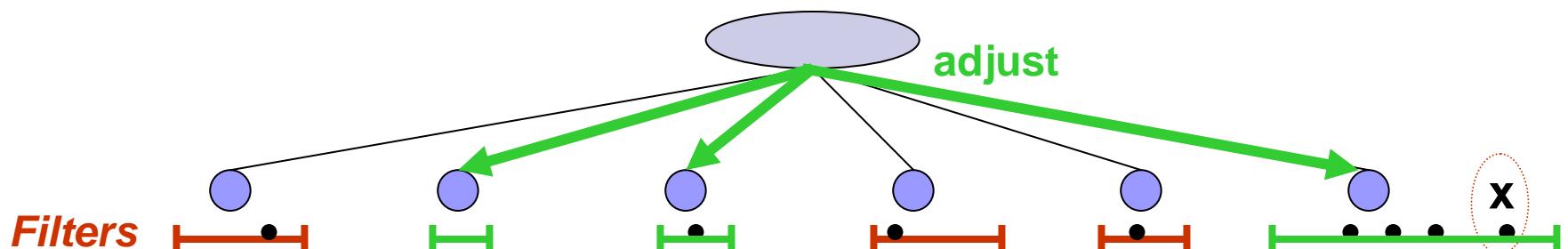
How about Periodic Polling?

- Sometimes **periodic polling** suffices for simple tasks
 - E.g., SNMP polls total traffic at coarse granularity
- Still need to deal with holistic nature of aggregates
- Must balance polling frequency against communication
 - Very frequent polling causes high communication, excess battery use in sensor networks
 - Infrequent polling means delays in observing events
- Need techniques to reduce communication while guaranteeing rapid response to events

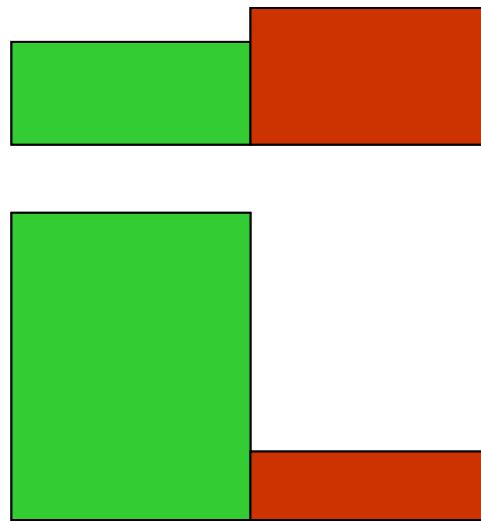


Communication-Efficient Monitoring

- Exact answers are not needed
 - Approximations with accuracy guarantees suffice
 - Tradeoff accuracy and *communication/ processing cost*
- Key Insight: “*Push-based*” *in-network processing*
 - Local filters installed at sites process local streaming updates
 - Offer bounds on local-stream behavior (at coordinator)
 - “Push” information to coordinator only when filter is violated
 - Coordinator sets/adjusts local filters to guarantee accuracy



Adaptive Slack Allocation



Slack Allocation

- A key idea is Slack Allocation
- Because we allow approximation, there is slack: the tolerance for error between computed answer and truth
 - May be absolute: $|Y - \hat{Y}| \leq \varepsilon$: slack is ε
 - Or relative: $\hat{Y} / Y \leq (1 \pm \varepsilon)$: slack is εY
- For a given aggregate, show that the slack can be divided between sites
- Will see different slack division heuristics

Top-k Monitoring

- Influential work on monitoring [Babcock, Olston'03]
 - Introduces some basic heuristics for dividing slack
 - Use local offset parameters so that all local distributions look like the global distribution
 - Attempt to fix local slack violations by negotiation with coordinator before a global readjustment
 - Showed that message delay does not affect correctness

Billboard
Top 100

1	1	Nelly Furtado Featuring Timbaland Promiscuous	Mosley 006818* Geffen				Peak 1	Wks On 11
2	2	Gnarls Barkley Crazy	Downton 70002* Lava				Peak 2	Wks On 11
3	3	Cassie Me & U	Next Selection/Bad Boy 94976 Atlantic				Peak 3	Wks On 14
4	4	Shakira Featuring Wyclef Jean Hips Don't Lie	Epic 84467*				Peak 1	Wks On 18
5	5	Yung Joc It's Goin' Down	Block/Bad Boy South 94249* Atlantic				Peak 3	Wks On 16
6	6	Rihanna Unfaithful	SRR/Def Jam DIGITAL IDJMG				Peak 9	Wks On 12
7	12	The Pussycat Dolls Featuring Snoop Dogg Doll Domination	The Pussycat Dolls 006818* Geffen				Peak 12	Wks On 11

Images from <http://www.billboard.com>

Top-k Scenario

- Each site monitors n objects with local counts $V_{i,j}$
 - item $i \in [n]$
 - site $j \in [m]$
- Values change over time with updates seen at site j
- Global count $V_i = \sum_j V_{i,j}$
- Want to find topk , an ϵ -approximation to true top-k set:
 - OK provided $i \in \text{topk}$, $I \notin \text{topk}$, $V_i + \epsilon \geq V_I$

gives a little
“wiggle room”

Adjustment Factors

- Define a set of 'adjustment factors', $\delta_{i,j}$
 - Make top-k of $V_{i,j} + \delta_{i,j}$ same as top-k of V_i

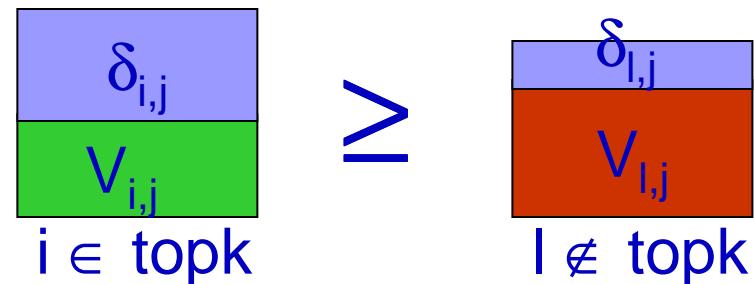


- Maintain invariants:
 1. For item i , adjustment factors sum to zero
 2. $\delta_{l,0}$ of non-topk item $l \leq \delta_{i,0} + \varepsilon$ of topk item i
 - Invariants and local conditions used to prove correctness

Local Conditions and Resolution

Local Conditions:

At each site j check adjusted topk counts dominate non-topk

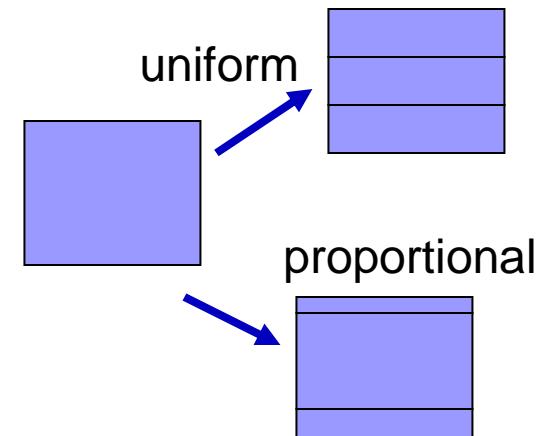


If any local condition violated at site j , resolution is triggered

- Local resolution: site j and coordinator only try to fix
 - Try to “borrow” from $\delta_{i,0}$ and $\delta_{l,0}$ to restore condition
- Global resolution: if local resolution fails, contact all sites
 - Collect all affected $V_{i,j}$ s – i.e., topk plus violated counts
 - Compute slacks for each count, and reallocate (next)
 - Send new adjustment factors $\delta'_{i,j}$, continue

Slack Division Strategies

- Define “slack” based on current counts and adjustments
- What fraction of slack to keep back for coordinator?
 - $\delta_{i,0} = 0$: No slack left to fix local violations
 - $\delta_{i,0} = 100\% \text{ of slack}$: Next violation will be soon
 - Empirical setting: $\delta_{i,0} = 50\% \text{ of slack}$ when ε very small
 $\delta_{i,0} = 0$ when ε is large ($\varepsilon > V_i/1000$)
- How to divide remainder of slack?
 - Uniform: $1/m$ fraction to each site
 - Proportional: $V_{i,j}/V_i$ fraction to site j for i



Pros and Cons

- Result has many advantages:
 - Guaranteed correctness within approximation bounds
 - Can show convergence to correct results even with delays
 - Communication reduced by 1 order magnitude
(compared to sending $V_{i,j}$ whenever it changes by ϵ/m)
- Disadvantages:
 - Reallocation gets complex: must check $O(km)$ conditions
 - Need $O(n)$ space at each site, $O(mn)$ at coordinator
 - Large ($\approx O(k)$) messages
 - Global resyncs are expensive: m messages to k sites

Other Problems: Aggregate Values

■ Problem 1: Single value tracking

Each site has one value v_i , want to compute $f(v)$, e.g., **sum**

■ Allow small bound of uncertainty in answer

- Divide uncertainty (slack) between sites
- If new value is outside bounds, re-center on new value

■ Naïve solution: allocate equal bounds to all sites

- Values change at different rates; queries may overlap

■ Adaptive filters approach [Olston, Jiang, Widom '03]

- Shrink all bounds and selectively grow others:
moves slack from stable values to unstable ones
- Base growth on frequency of bounds violation, optimize

Other Problems: Set Expressions

■ Problem 2: Set Expression Tracking

$A \cup (B \cap C)$ where A, B, C defined by distributed streams

■ Key ideas [Das et al.'04]:

- Use semantics of set expression: if b arrives in set B , but b already in set A , no need to send
- Use cardinalities: if many copies of b seen already, no need to send if new copy of b arrives or a copy is deleted
- Combine these to create a *charging scheme* for each update: if sum of charges is small, no need to send.
- Optimizing charging is NP-hard, heuristics work well.

Other Problems: ODI Aggregates

- **Problem 3: ODI aggregates**

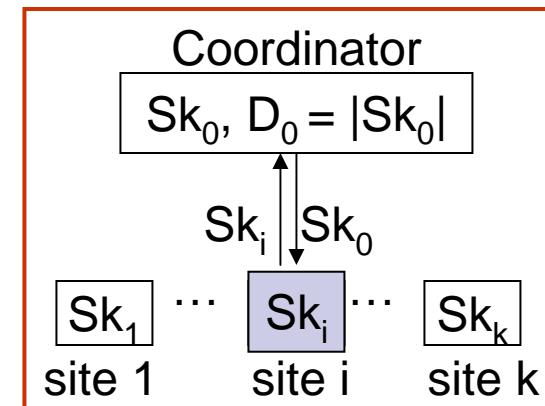
e.g., `count distinct` in continuous distributed model

- Two important parameters emerge:

- How to divide the slack
 - What the site sends to coordinator

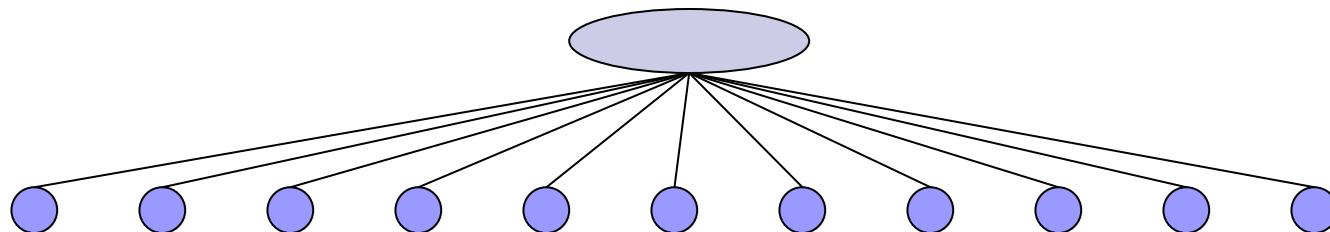
- In [Cormode et al.'06]:

- Share slack evenly: hard to do otherwise for this aggregate
 - Sharing sketch of global distribution saves communication
 - Better to be lazy: send sketch in reply, don't broadcast

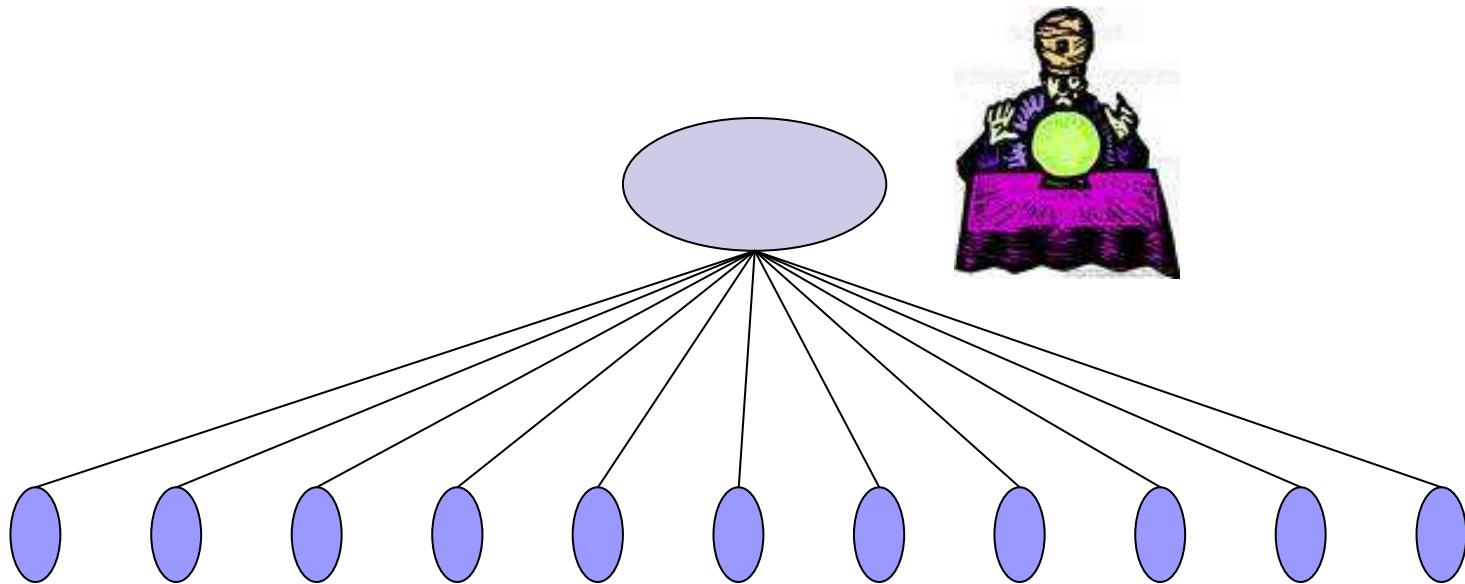


General Lessons

- Break a global (holistic) aggregate into “safe” local conditions, so local conditions \Rightarrow global correctness
- Set local parameters to help the tracking
- Use the approximation to define slack, divide slack between sites (and the coordinator)
- Avoid global reconciliation as much as possible, try to patch things up locally

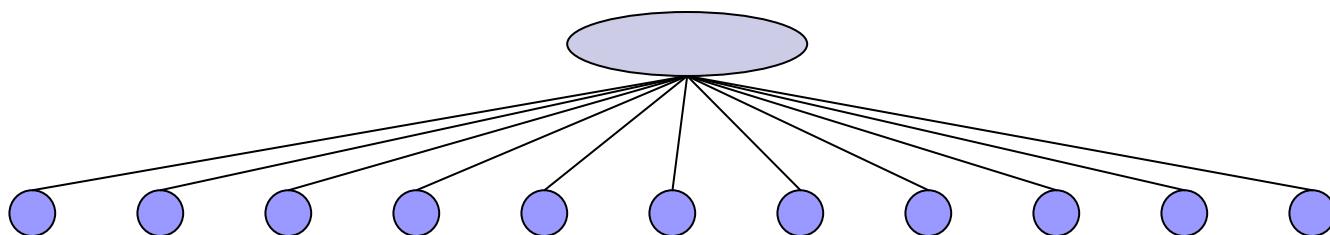


Predictive Local-Stream Models

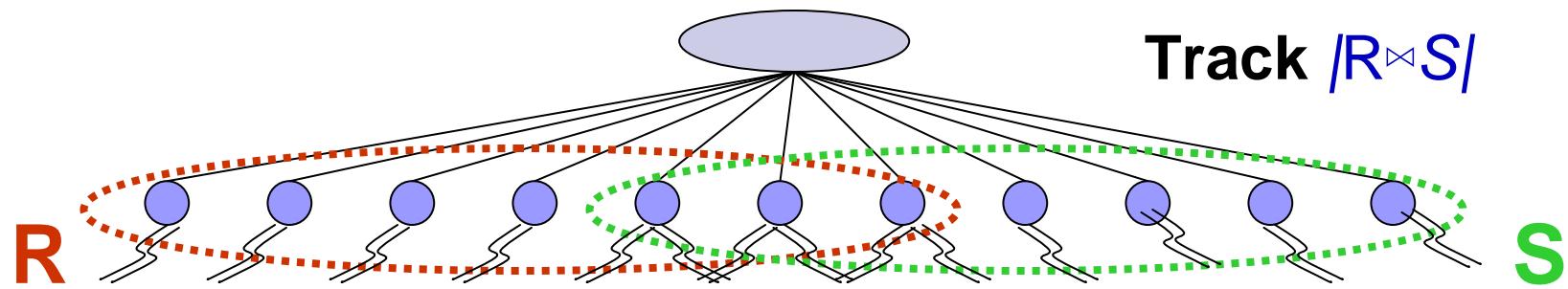


More Sophisticated Local Predictors

- Slack allocation methods use simple “*static*” prediction
 - Site value implicitly assumed constant since last update
 - No update from site \Rightarrow last update (“predicted” value) is within required slack bounds \Rightarrow global error bound
- *Dynamic, more sophisticated prediction models* for local site behavior?
 - Model complex stream patterns, reduce number of updates to coordinator
 - **But...** more complex to maintain and communicate (to coordinator)



Tracking Complex Aggregate Queries



- Continuous distributed tracking of complex aggregate queries using AMS sketches and local prediction models [Cormode, Garofalakis'05]
- *Class of queries:* Generalized inner products of streams

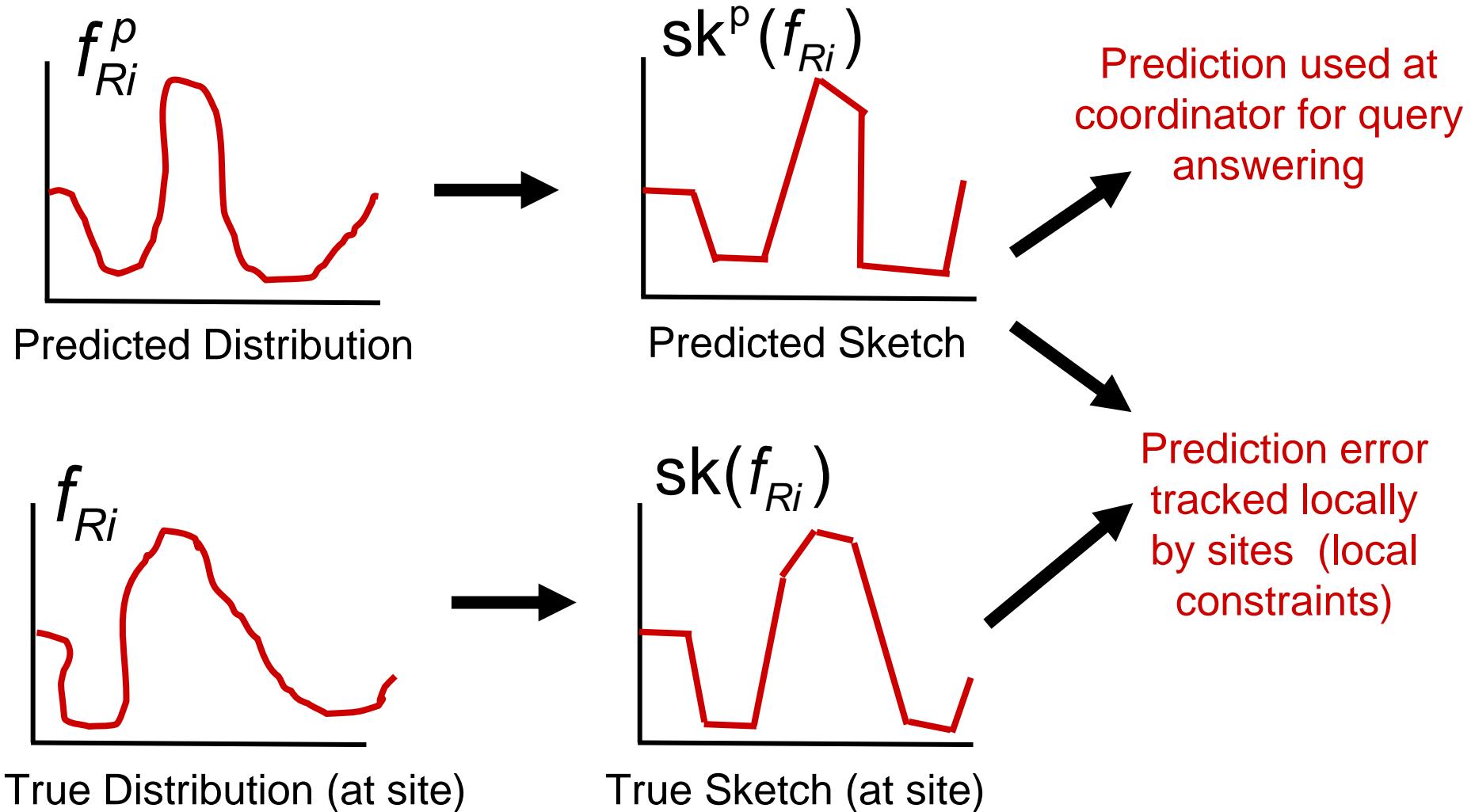
$$|R \bowtie S| = f_R \cdot f_S = \sum_v f_R[v] f_S[v] \quad (\pm \epsilon \|f_R\|_2 \|f_S\|_2)$$

- Join/multi-join aggregates, range queries, heavy hitters, histograms, wavelets, ...

Local Sketches and Sketch Prediction

- Use (AMS) sketches to summarize local site distributions
 - Synopsis=small collection of random linear projections $\text{sk}(f_{R,i})$
 - *Linear transform:* Simply add to get global stream sketch
- Minimize updates to coordinator through *Sketch Prediction*
 - Try to predict how local-stream distributions (and their sketches) will evolve over time
 - Concise *sketch-prediction models*, built locally at remote sites and communicated to coordinator
 - *Shared knowledge* on expected stream behavior over time:
Achieve “stability”

Sketch Prediction



Query Tracking Scheme

Tracking. At site j keep sketch of stream so far, $\text{sk}(f_{R,i})$

- Track local deviation between stream and prediction:

$$\|\text{sk}(f_{R,i}) - \text{sk}^p(f_{R,i})\|_2 \leq \theta/\sqrt{k_i} \|\text{sk}(f_{R,i})\|_2$$

- Send current sketch (and other info) if violated

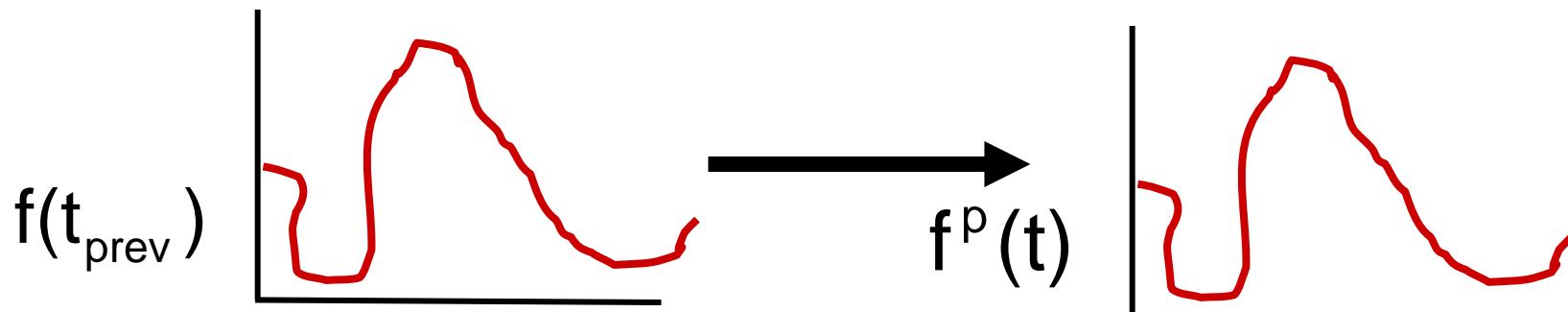
Querying. At coordinator, query error $\leq (\varepsilon + 2\theta)\|f_R\|_2 \|f_S\|_2$

- ε = local-sketch summarization error (at remote sites)
- θ = upper bound on local-stream deviation from prediction (“Lag” between remote-site and coordinator view)

- **Key Insight:** *With local deviations bounded, the predicted sketches at coordinator are guaranteed accurate*

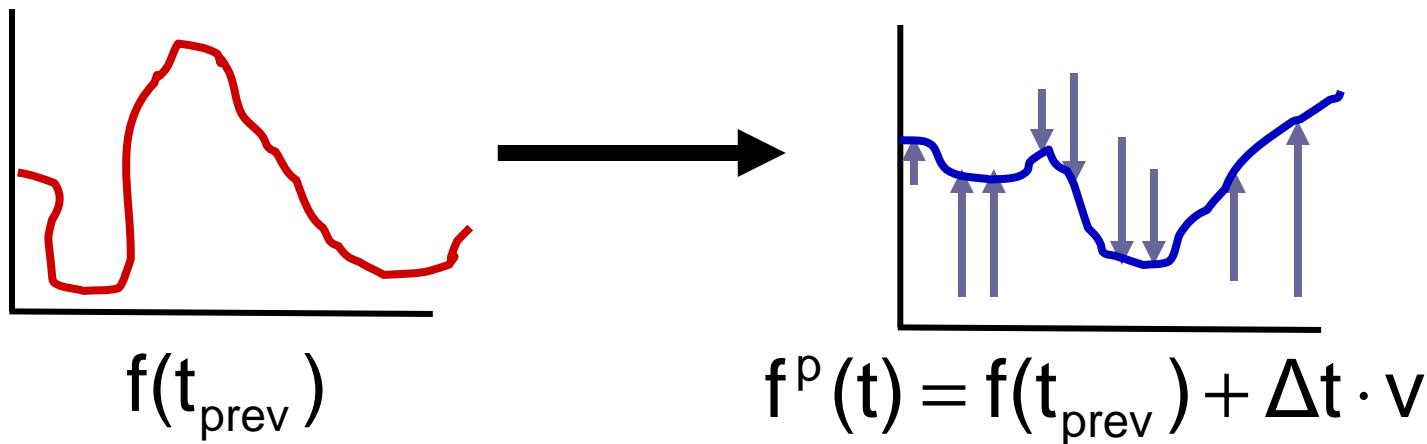
Sketch-Prediction Models

- Simple, concise models of local-stream behavior
 - Sent to coordinator to keep site/coordinator “in-sync”
 - Many possible alternatives
- Static model: No change in distribution since last update
 - Naïve, “no change” assumption:
 - No model info sent to coordinator, $\text{sk}^p(f(t)) = \text{sk}(f(t_{\text{prev}}))$



Sketch-Prediction Models

- **Velocity model:** Predict change through “velocity” vectors from recent local history (simple linear model)
 - Velocity model: $f^p(t) = f(t_{\text{prev}}) + \Delta t \cdot v$
 - By sketch linearity, $\text{sk}^p(f(t)) = \text{sk}(f(t_{\text{prev}})) + \Delta t \cdot \text{sk}(v)$
 - Just need to communicate one extra sketch
 - Can extend with acceleration component



Sketch-Prediction Models

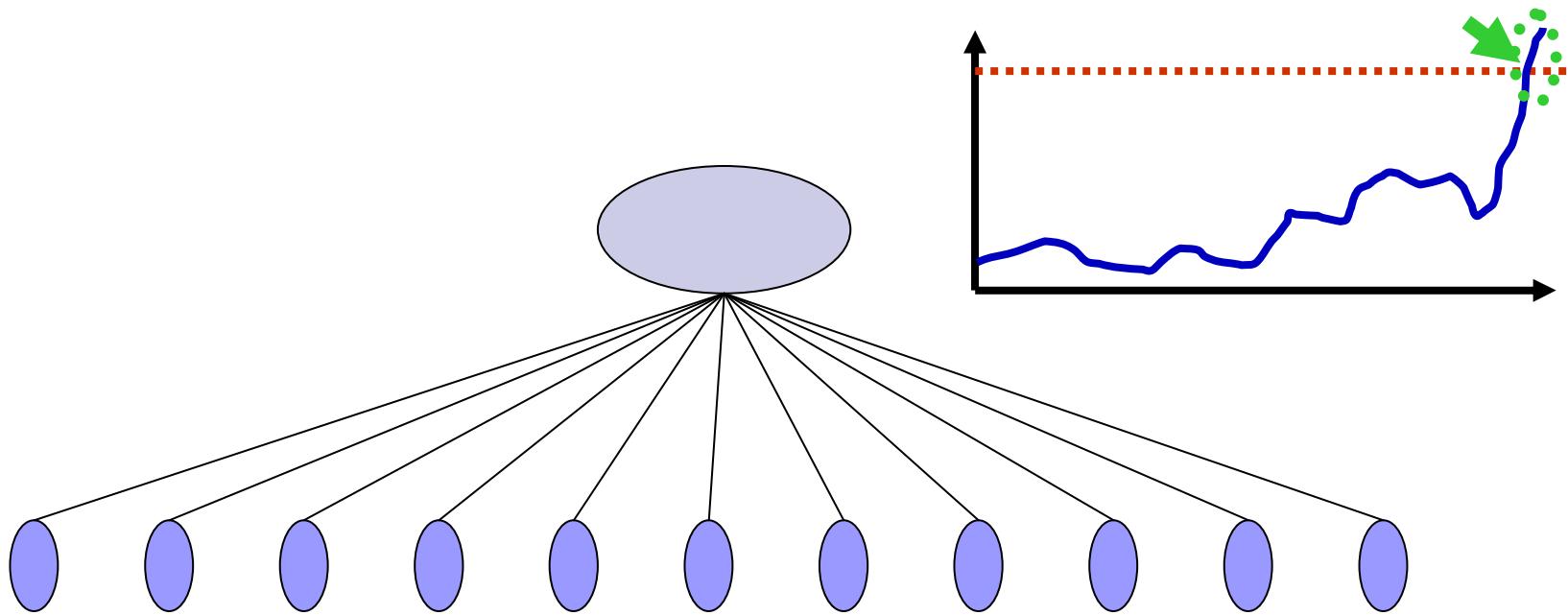
Model	Info	Predicted Sketch
Static	\emptyset	$\text{sk}^p(f(t)) = \text{sk}(f(t_{\text{prev}}))$
Velocity	$\text{sk}(v)$	$\text{sk}^p(f(t)) = \text{sk}(f(t_{\text{prev}})) + \Delta t \cdot \text{sk}(v)$

- 1 – 2 orders of magnitude savings over sending all data

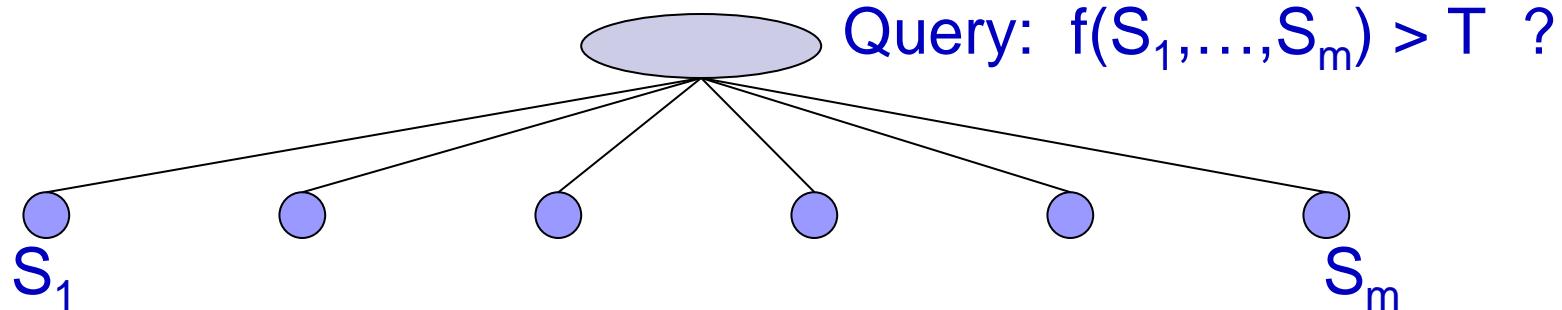
Lessons, Thoughts, and Extensions

- Dynamic prediction models are a natural choice for continuous in-network processing
 - Can capture complex temporal (and spatial) patterns to reduce communication
- Many model choices possible
 - Need to carefully balance power & conciseness
 - Principled way for model selection?
- General-purpose solution (generality of AMS sketch)
 - Better solutions for special queries
E.g., continuous quantiles [Cormode et al.'05]

Distributed Triggers

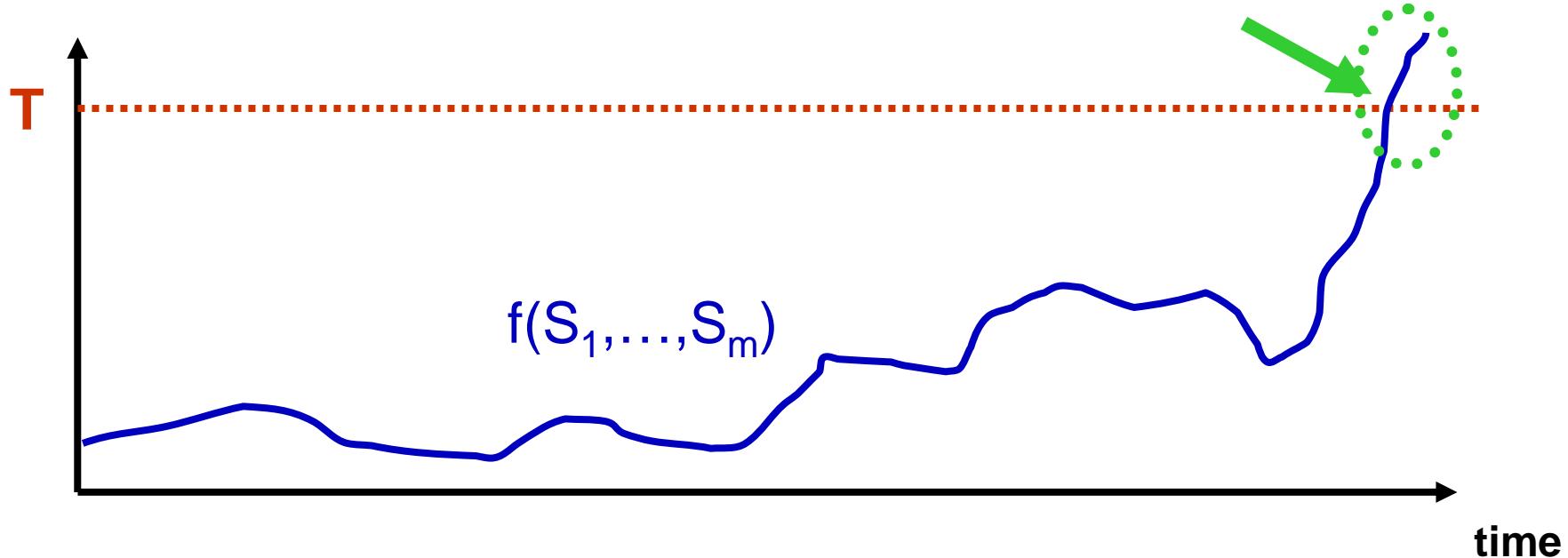


Tracking Distributed Triggers



- Only interested in values of the “global query” above a certain threshold T
 - Network anomaly detection (e.g., DDoS attacks)
 - Total number of connections to a destination, “fire” when it exceeds a threshold
 - Air / water quality monitoring, total number of cars on highway
 - Fire when count/average exceeds a certain amount
- Introduced in HotNets paper [Jain, Hellerstein et al.'04]

Tracking Distributed Triggers



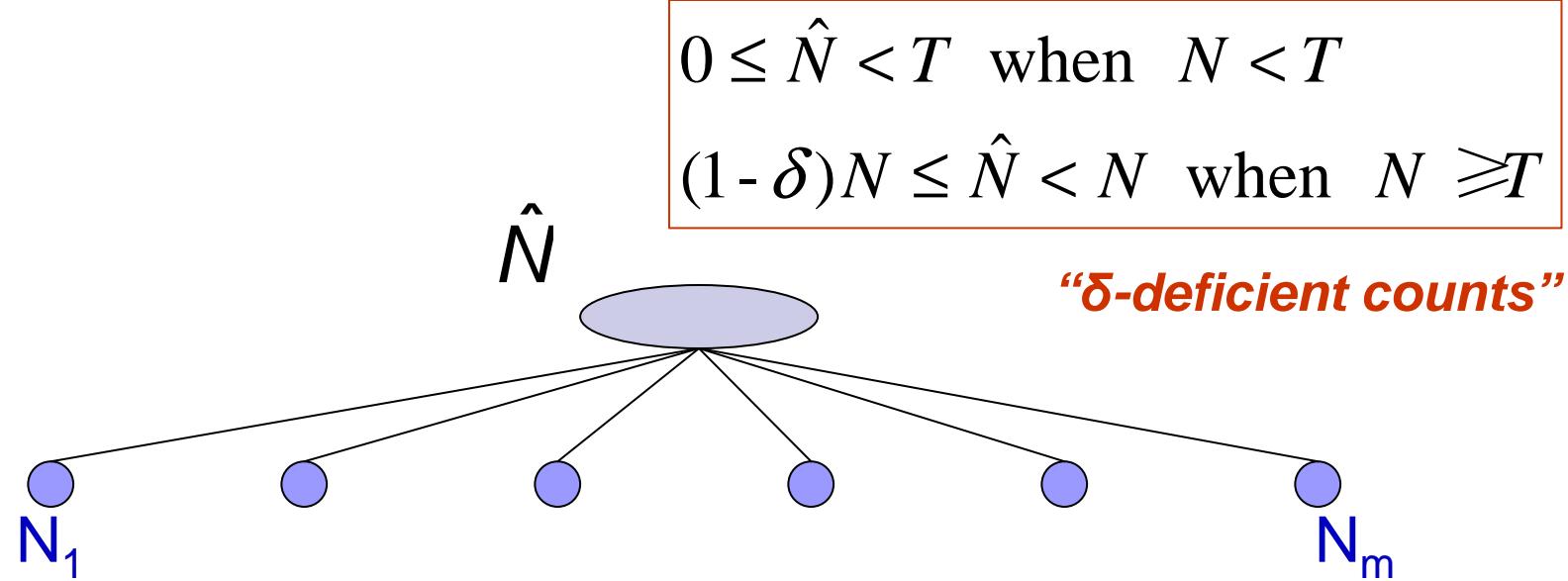
- Problem “easier” than approximate query tracking
 - Only want accurate $f()$ values when they’re close to threshold
 - *Exploit threshold for intelligent slack allocation to sites*
- Push-based in-network operation even more relevant
 - Optimize operation for “common case”

Tracking Thresholded Counts

- Monitor a distributed aggregate count
- Guarantee a user-specified accuracy δ only if the count exceeds a pre-specified threshold T [Kerlapura et al.'06]
 - E.g., N_i = number of observed connections to 128.105.7.31 and $N = \sum_i N_i$

$$0 \leq \hat{N} < T \text{ when } N < T$$

$$(1 - \delta)N \leq \hat{N} < N \text{ when } N \geq T$$



Thresholded Counts Approach

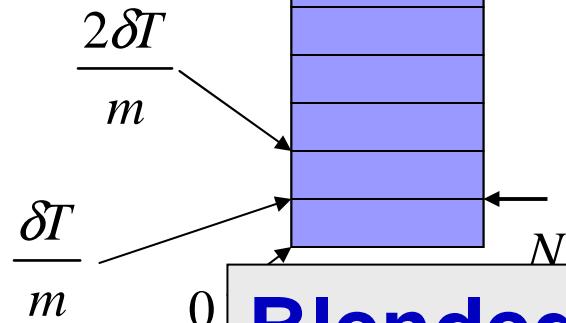
- Site i maintains a set of local thresholds $t_{i,j}$, $j = 0, 1, 2, \dots$
- Local filter at site i : $t_{i,f(i)} \leq N_i < t_{i,f(i)+1}$
 - Local count between adjacent thresholds
 - Contact coordinator with new “level” $f(i)$ when violated
- Global estimate at coordinator $\hat{N} = \sum_i t_{i,f(i)}$
- For δ -deficient estimate, choose local threshold sequences $t_{i,j}$ such that

$$\sum_i (t_{i,f(i)+1} - t_{i,f(i)}) < \delta \sum_i t_{i,f(i)} \quad \text{whenever} \quad \sum_i t_{i,f(i)+1} > T$$

*“large” to minimize communication!
“small” to ensure global error bound!*

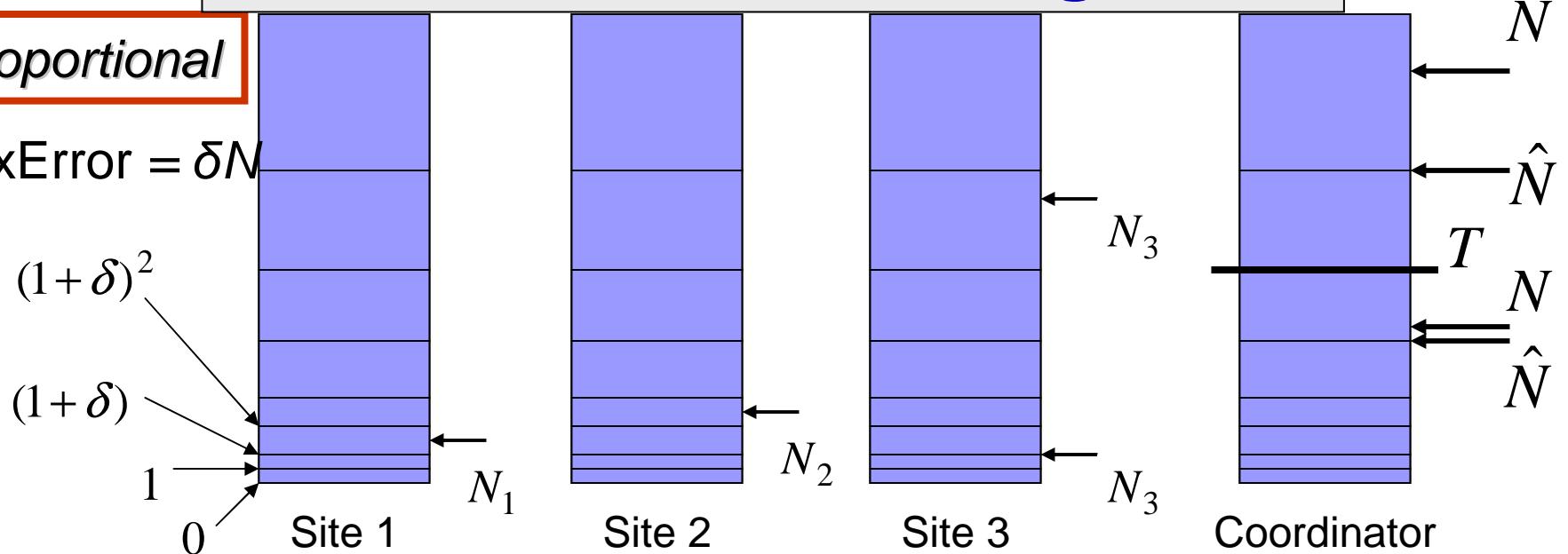
Uniform

MaxError = δT



Proportional

MaxError = δN



Blended threshold assignment

Blended Threshold Assignment

- Uniform: overly tight filters when $N > T$
- Proportional: overly tight filters when $N \ll T$
- **Blended Assignment:** combines best features of both:

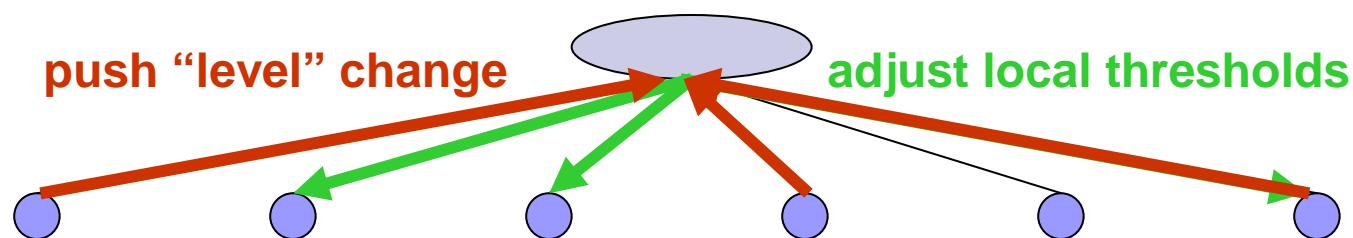
$$t_{i,j+1} = (1+\alpha\delta) \cdot t_{i,j} + (1-\alpha) \cdot \delta T/m \quad \text{where } \alpha \in [0,1]$$

- $\alpha = 0 \Rightarrow$ *Uniform assignment*
- $\alpha = 1 \Rightarrow$ *Proportional assignment*

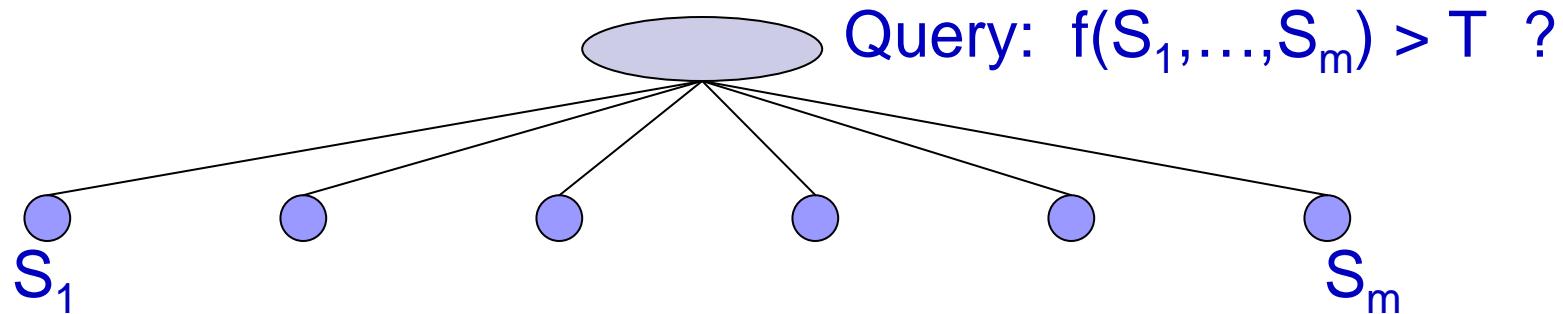
- Optimal value of α exists for given N (expected or distribution)
 - Determined through, e.g., gradient descent

Adaptive Thresholding

- So far, *static* threshold sequences
 - Every site only has “local” view and just pushes updates to coordinator
- Coordinator has global view of current count estimate
 - Can *adaptively* adjust the local site thresholds (based on estimate and T)
 - E.g., dynamically switch from *uniform* to *proportional* growth strategy as estimate approaches/exceeds T



What about Non-Linear Functions?



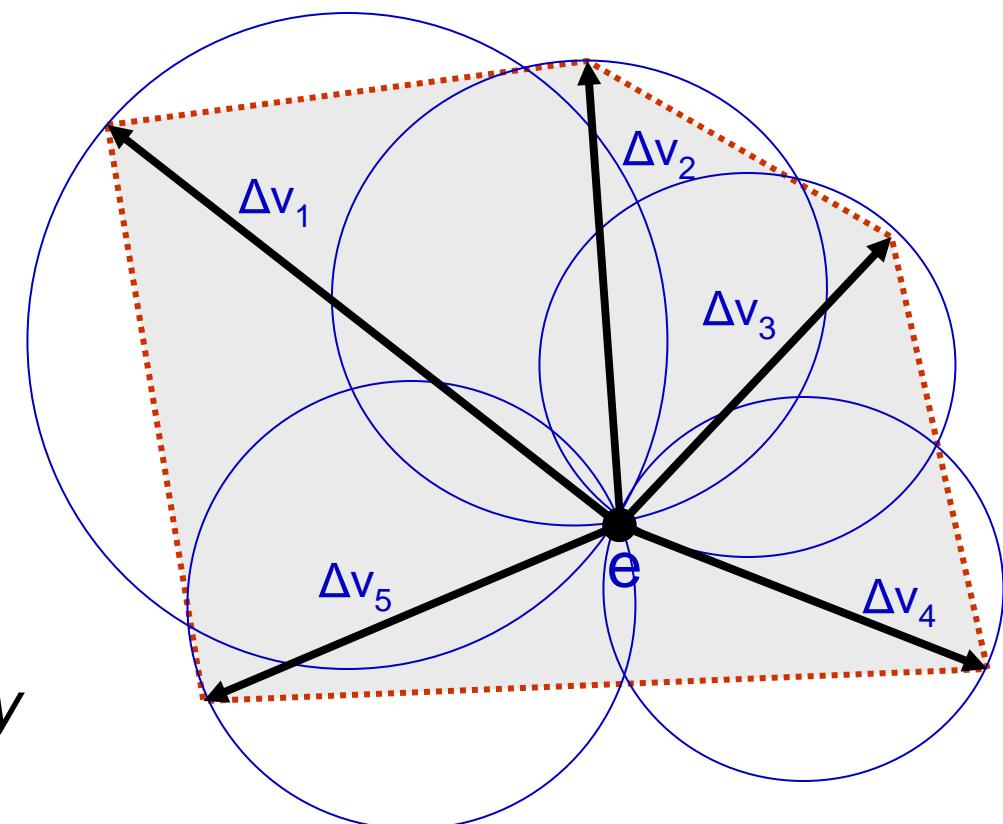
- For *general, non-linear* $f()$, the problem becomes a lot harder!
 - E.g., information gain or entropy over global data distribution
 - *Non-trivial* to decompose the global threshold into “safe” local site constraints
 - E.g., consider $N = (N_1 + N_2)/2$ and $f(N) = 6N - N^2 > 1$
Impossible to break into thresholds for $f(N_1)$ and $f(N_2)$

Monitoring General Threshold Functions

- Interesting *geometric* approach [Scharfman et al.'06]
- Each site tracks a *local statistics vector* v_i (e.g., data distribution)
- Global condition is $f(v) > T$, where $v = \sum_i \lambda_i v_i$ ($\sum_i \lambda_i = 1$)
 - v = convex combination of local statistics vectors
- All sites have an estimate $e = \sum_i \lambda_i v'_i$ of v based on latest update v'_i from site i
- Each site i continuously tracks its *drift* from its most recent update $\Delta v_i = v_i - v'_i$

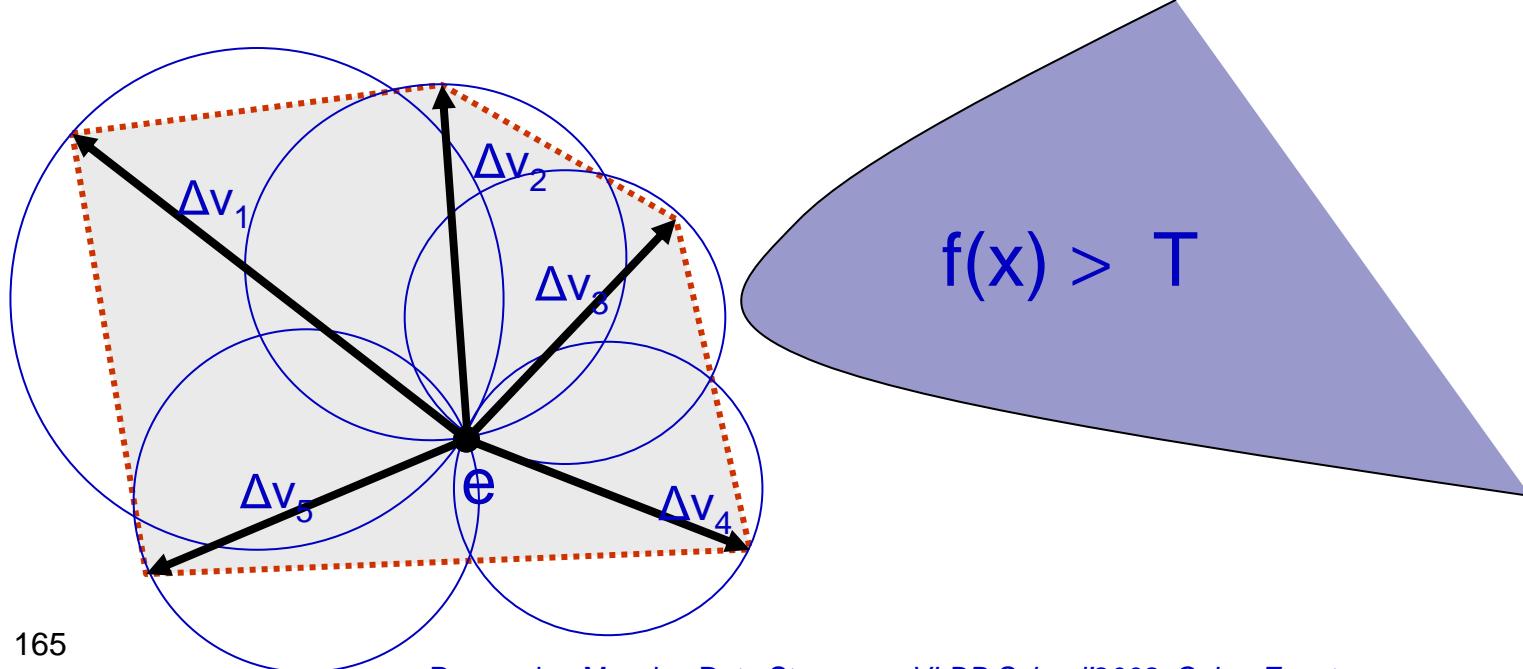
Monitoring General Threshold Functions

- Key observation: $v = \sum_i \lambda_i \cdot (e + \Delta v_i)$
(a *convex combination* of “translated” local drifts)
- v lies in the *convex hull* of the $(e + \Delta v_i)$ vectors
- Convex hull is completely covered by the *balls* with radii $\|\Delta v_i/2\|_2$ centered at $e + \Delta v_i/2$
- Each such ball can be constructed *independently*



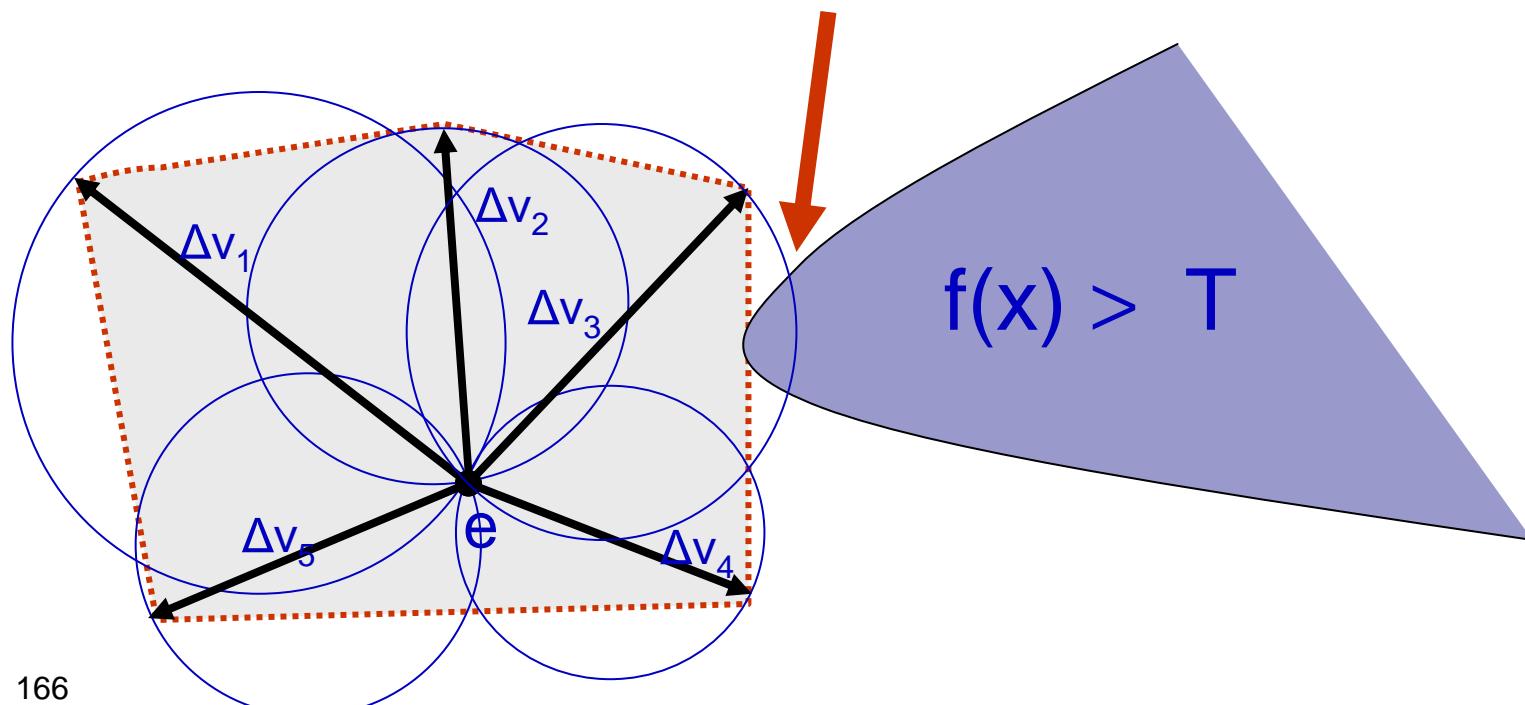
Monitoring General Threshold Functions

- *Monochromatic Region*: For all points x in the region $f(x)$ is on the same side of the threshold ($f(x) > T$ or $f(x) \leq T$)
- Each site independently checks its ball is monochromatic
 - Find **max** and **min** for $f()$ in local ball region (may be costly)
 - Broadcast updated value of v_i if not monochrome



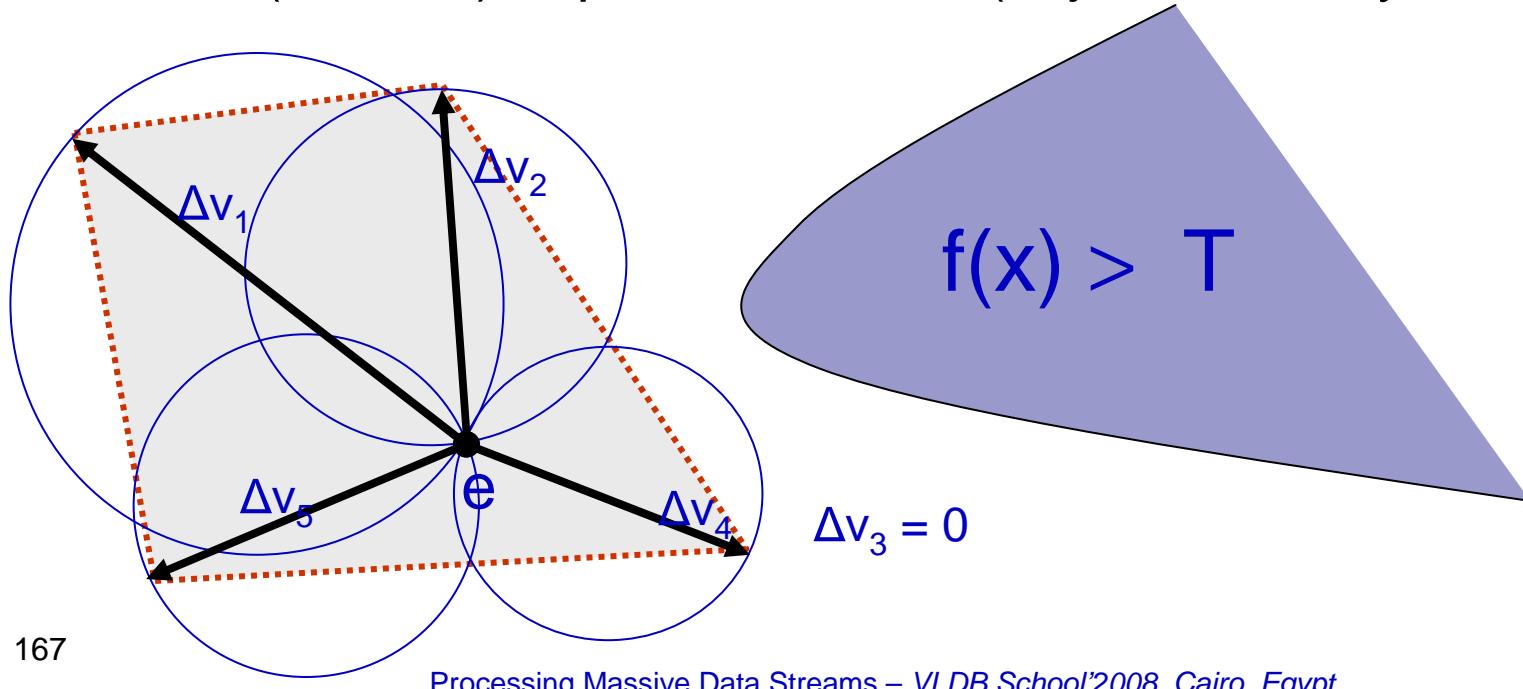
Monitoring General Threshold Functions

- After broadcast, $\|\Delta v_i\|_2 = 0 \Rightarrow$ Ball at i is monochromatic

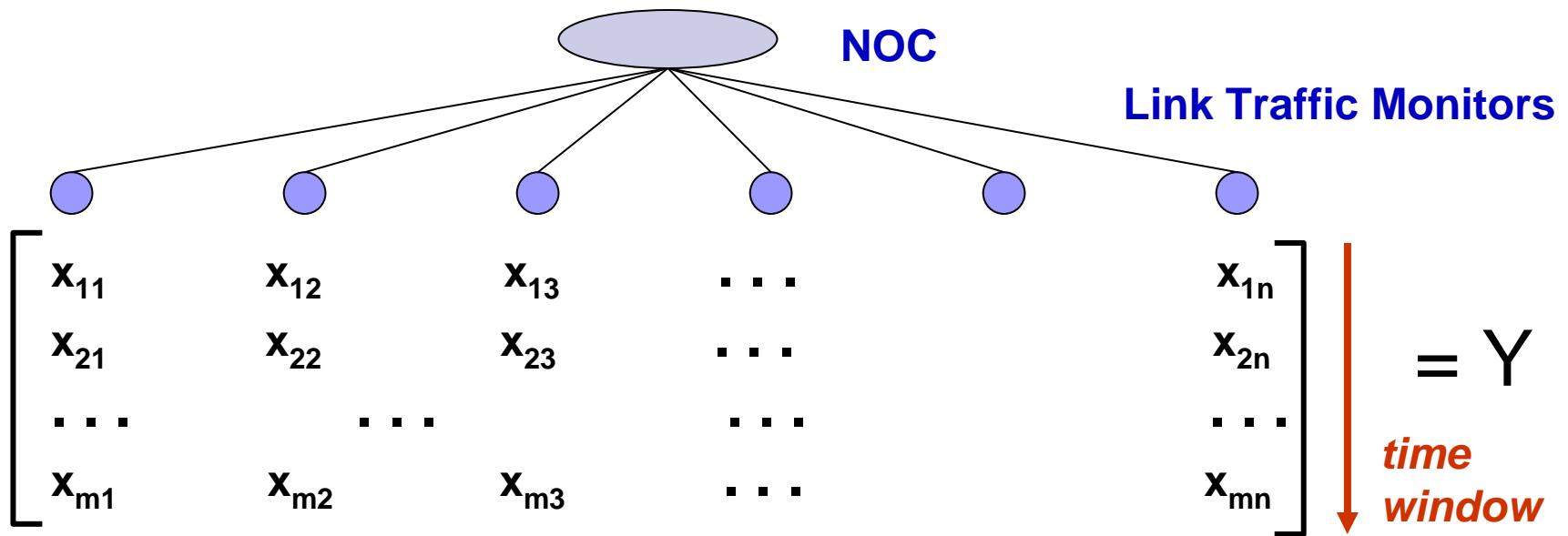


Monitoring General Threshold Functions

- After broadcast, $\|\Delta v_i\|_2 = 0 \Rightarrow$ Ball at i is monochromatic
 - Global estimate e is updated, which may cause more site update broadcasts
- *Coordinator case*: Can allocate local slack vectors to sites to enable “localized” resolutions
 - Drift (=radius) depends on slack (adjusted locally for subsets)



Extension: Filtering for PCA Tracking



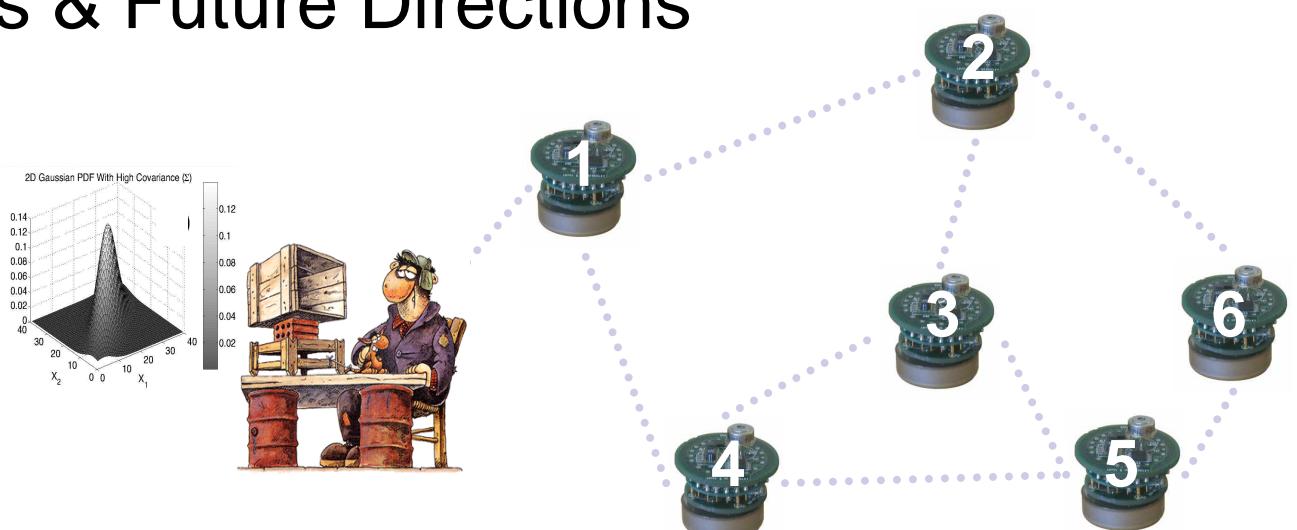
- Threshold total energy of the low PCA coefficients of Y = Robust indicator of network-wide anomalies [Lakhina et al.'04]
 - Non-linear matrix operator over combined time-series
- Can combine local filtering ideas with *stochastic matrix perturbation theory* [Huang et al.'06]

Lessons, Thoughts and Extensions

- Key idea in *trigger tracking*: The threshold is your friend!
 - Exploit for more intelligent (looser, yet “safe”) local filtering
- Also, optimize for the common case!
 - Threshold violations are typically “outside the norm”
 - “Push-based” model makes even more sense here
 - Local filters eliminate most/all of the “normal” traffic
- Use richer, dynamic prediction models for triggers?
 - Perhaps adapt depending on distance from threshold?
- More realistic network models?
- Geometric ideas for approximate query tracking?
 - Connections to approximate join-tracking scheme?

Tutorial Outline

- Motivation & Streaming Applications
- Centralized Stream Processing
- Distributed Stream Processing
 - One-shot distributed-stream querying
 - Continuous distributed-stream tracking
 - Probabilistic distributed data acquisition
- Open Problems & Future Directions
- Conclusions



Model-Driven Data Acquisition

- *Not only aggregates* – Approximate, bounded-error acquisition of individual sensor values [Deshpande et al. '04]
 - (ε, δ) -approximate acquisition: $|Y - \hat{Y}| \leq \varepsilon$ with prob. $> 1 - \delta$
- Regular readings entails large amounts of data, noisy or incomplete data, inefficient, low battery life, ...
- *Intuition*: Sensors give (noisy, incomplete) samples of real-world processes
- Use *dynamic probabilistic model* of real-world process to
 - Robustly complement & interpret obtained readings
 - Drive efficient acquisitional query processing

Query Processing in TinyDB

Declarative Query

```
select nodeID, temp  
where nodeID in {1..6}
```

USER

Query Results

1, 22.73,
...
6, 22.1.

Query Processor

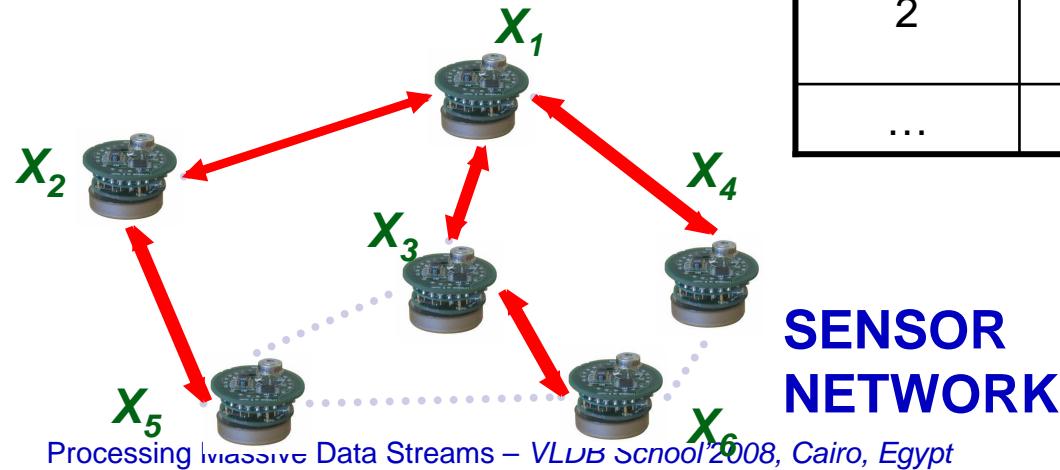
**Virtual Table seen
by the User**

Observation Plan

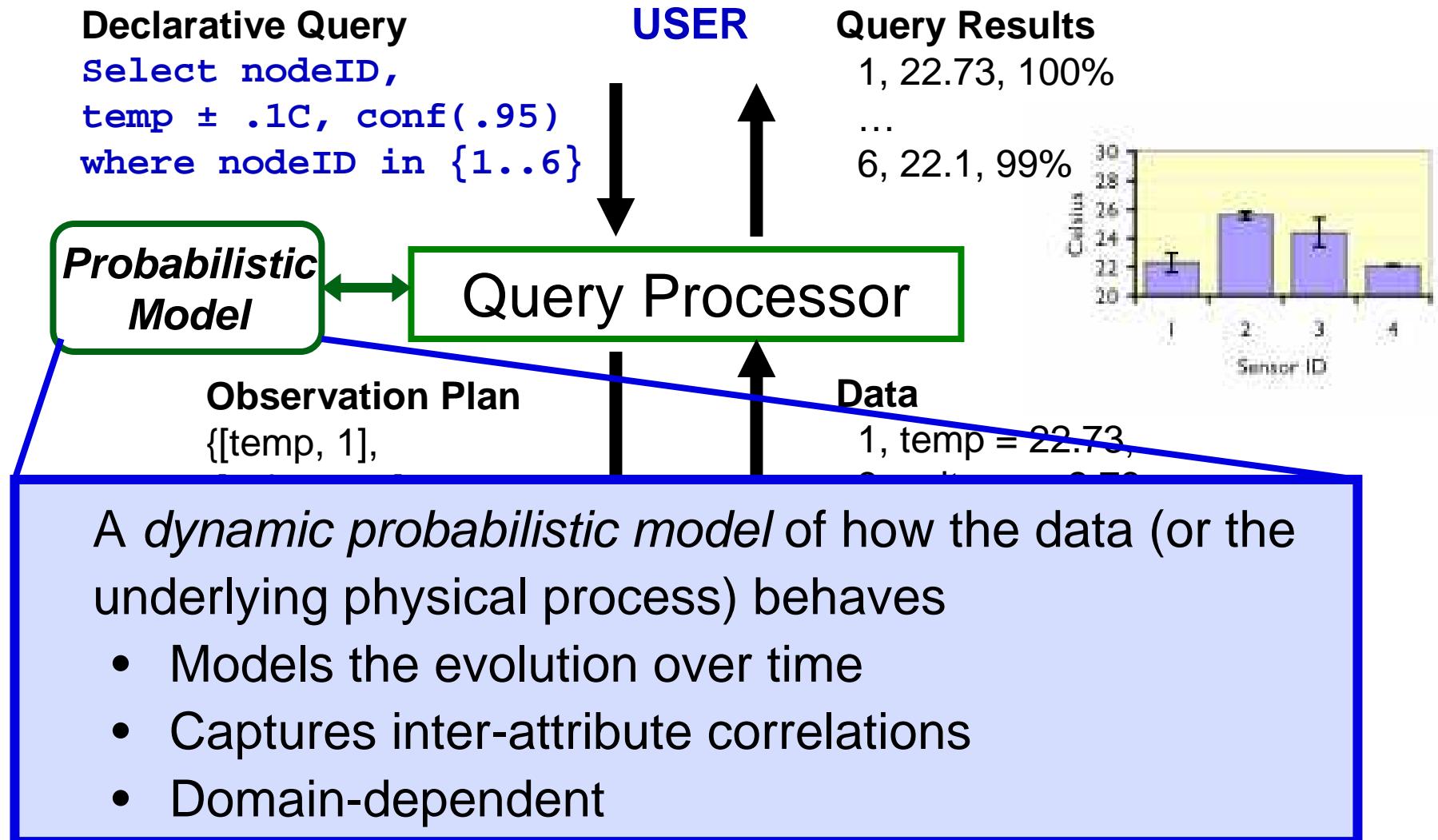
```
{[temp, 1], [temp, 2],  
..., [temp, 6]}
```

Data
1, ten
...
6, ten

nodeID	Time	temp
1	10am	21
2	10am	22
...



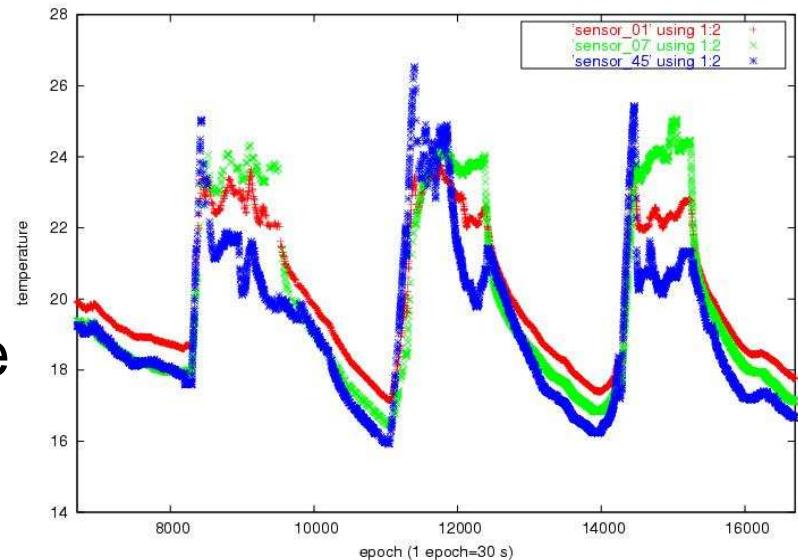
Model-Based Data Acquisition: BBQ



BBQ Details

Probabilistic model captures the joint pdf $p(X_1, \dots, X_n)$

- *Spatial/temporal correlations*
 - Sensor-to-sensor
 - Attribute-to-attribute
E.g., voltage & temperature
- *Dynamic*: pdf evolves over time
 - BBQ: Time-varying multivariate Gaussians
- Given user query Q and accuracy guarantees (ε, δ)
 - Try to answer Q directly from the current model
 - If not possible, use model to find efficient *observation plan*
 - Observations update the model & generate (ε, δ) answer



BBQ Probabilistic Queries

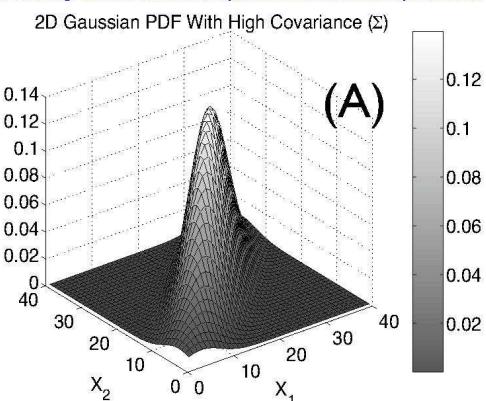
- Classes of probabilistic queries
 - *Range predicates*: Is $X_i \in [a_i, b_i]$ with prob. $> 1 - \delta$
 - *Value estimates*: Find X'_i such that $\Pr[|X_i - X'_i| < \varepsilon] > 1 - \delta$
 - *Aggregate estimates*: (ε, δ) -estimate $\text{avg/sum}(X_{i1}, X_{i2} \dots X_{ik})$
- Acquire readings if model cannot answer Q at δ conf. level
- Key model operations are
 - *Marginalization*: $p(X_i) = \int p(X_1, \dots, X_n) dx$
 - *Conditioning*: $p(X_1, \dots, X_n | \text{observations})$
 - *Integration*: $\int_a^b p(X_1, \dots, X_n) dx$, also expectation $X'_i = E[X_i]$

All significantly simplified for Gaussians!

BBQ Query Processing

Joint pdf at time=t

$$p(X_1^t, \dots, X_n^t)$$



Probabilistic query
Value of $X_2 \pm \epsilon$
with prob. $> 1 - \delta$

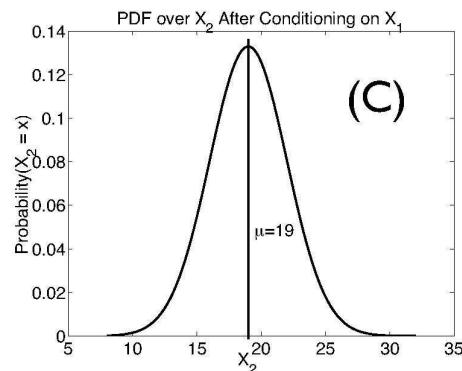
Is
 $P(X_2 \in [\mu_2 - \epsilon, \mu_2 + \epsilon]) = \int_{\mu_2 - \epsilon}^{\mu_2 + \epsilon} P(x_2) dx_2$

below $1 - \delta$?

Yes

Higher prob.,
can now
answer query

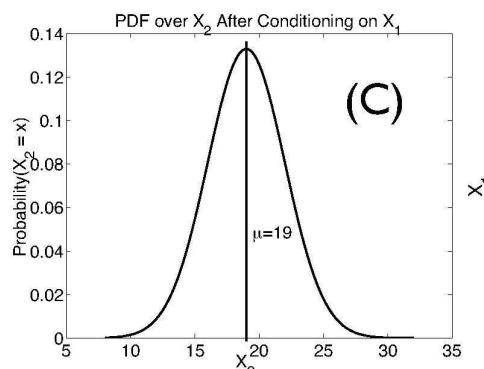
$$P(X_2 | X_1 = 18)$$



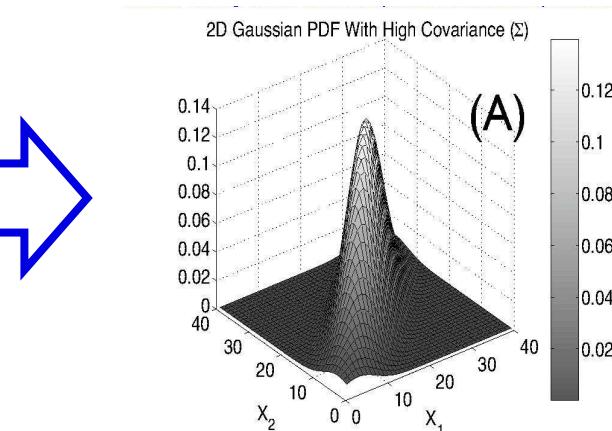
Must sense more data
Return μ_2
Example: Observe $X_1 = 18$
Incorporate into model

Evolving the Model over Time

Joint pdf at time=t
 $p(X_1^t, \dots, X_n^t | X_1^t = 18)$



Joint pdf at time=t+1
 $p(X_1^{t+1}, \dots, X_n^{t+1} | X_1^t = 18)$



Use a (Markov) Transition Model
 $P(\mathbf{X}^{t+1} | \mathbf{X}^t)$

- In general, a two-step process:

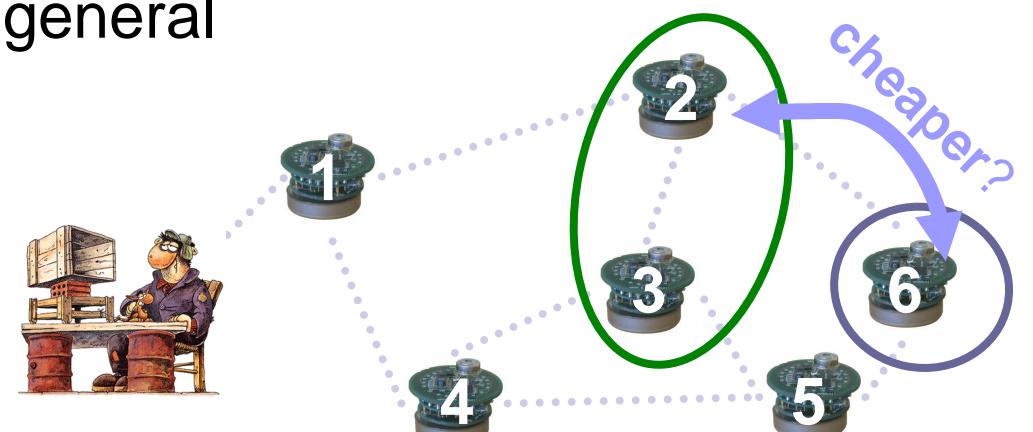
$$p(\mathbf{X}^t | \text{obs}^{1 \dots t}) \xrightarrow{\text{Trans. Model}} p(\mathbf{X}^{t+1} | \text{obs}^{1 \dots t}) \xrightarrow{\text{Condition}} p(\mathbf{X}^{t+1} | \text{obs}^{1 \dots t+1})$$

- *Bayesian filtering* (for Gaussians this yields *Kalman filters*)

Optimizing Data Acquisition

- Energy/communication-efficient observation plans
 - Non-uniform data acquisition costs and network communication costs
 - Exploit data correlations and knowledge of topology
- Minimize $\text{Cost}(obs)$ over all $obs \subseteq \{1, \dots, n\}$ so expected confidence in query answer given obs (from model) $> 1-\delta$
- **NP-hard** to optimize in general

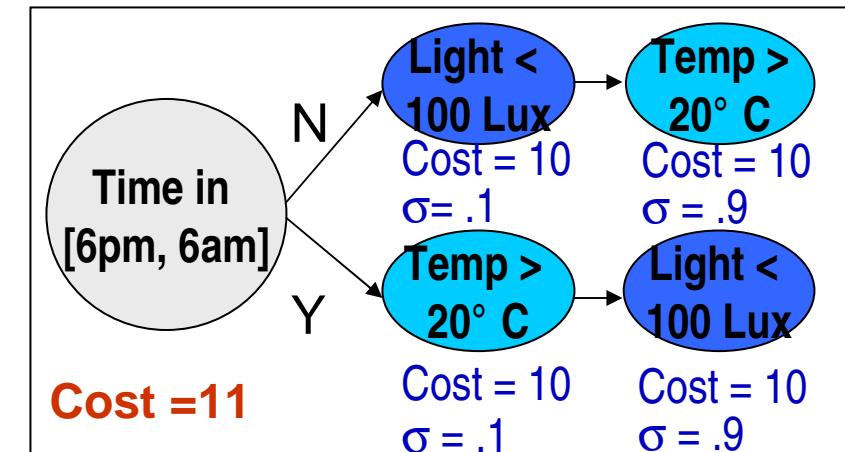
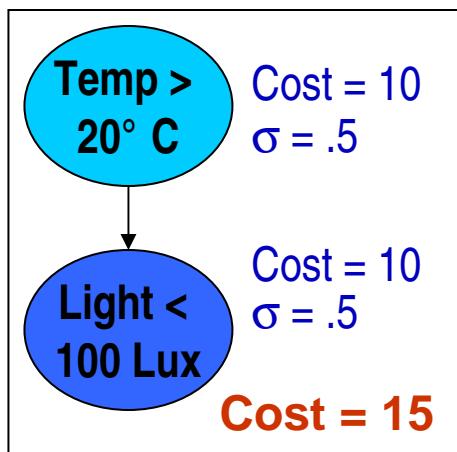
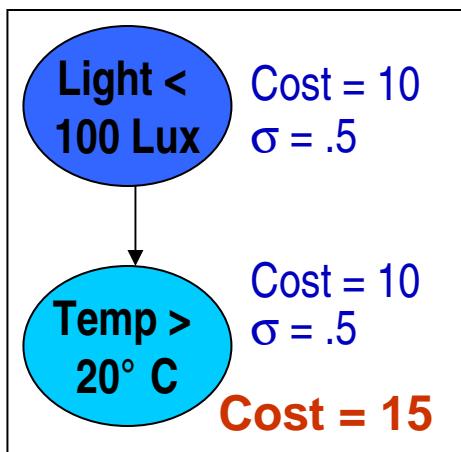
Sensor	Energy per sample (mJ)
Solar Radiation	.525
Barometric Pressure	0.003
Humidity and Temp.	0.5
Voltage	0.00009



Conditional Plans for Data Acquisition

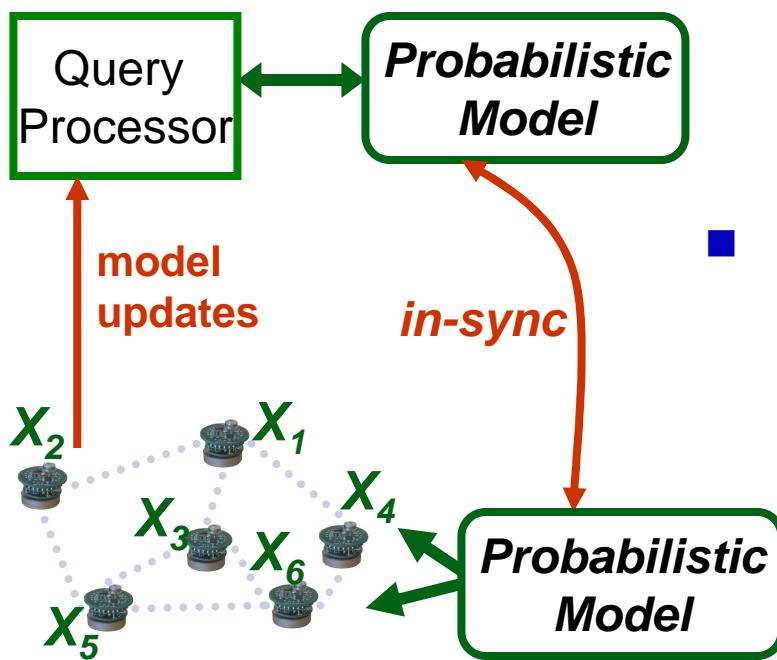
- Observation plans ignore the attribute values observed
 - Attribute subset chosen is observed in its entirety
 - The observed attribute values give a lot more information
- *Conditional* observation plans (outlined in [Deshpande et al.'05])
 - Change the plan depending on observed attribute values (not necessarily in the query)
 - Not yet explored for *probabilistic* query answers

```
SELECT * FROM sensors WHERE light<100Lux and temp>20°C
```



Continuous Model-Driven Acquisition

```
select nodeID,  
temp ± .1C, conf(.95)  
where nodeID in {1..6}  
epoch 2 min
```

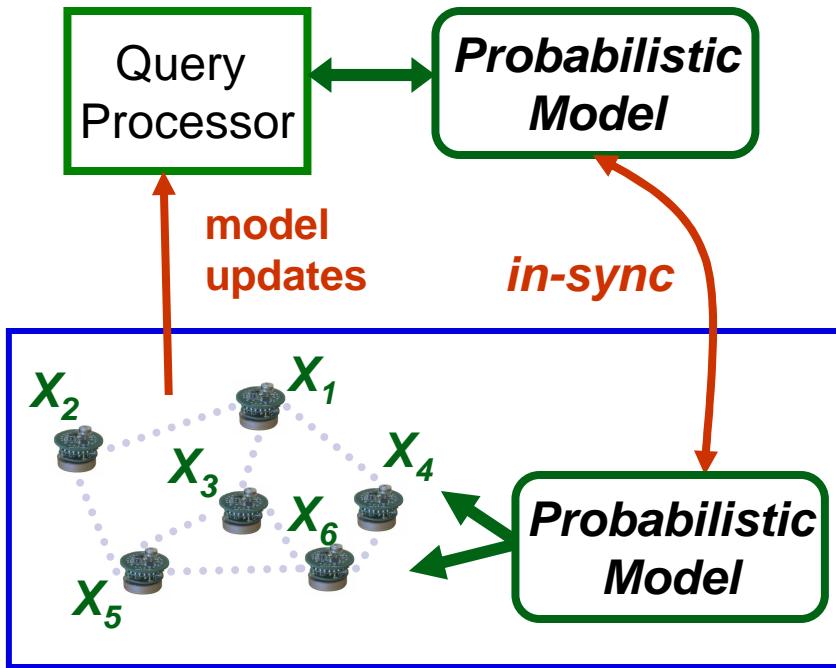


Dynamic Replicated Prob Models (Ken)

[Chu et al.'06]

- Model *shared and sync'd* across base-station and sensornet
- Nodes continuously check & maintain model accuracy based on ground truth
 - Push vs. Pull (BBQ)
- *Problem: In-network model maintenance*
 - Exploit spatial data correlations
 - Model updates decided in-network and sent to base-station
 - Always keep model (ε, δ) -approximate

In-Network Model Maintenance



- Mapping model maintenance onto network topology
 - At each step, nodes check (ϵ, δ) accuracy, send updates to base
- Choice of model drastically affects communication cost
 - Must centralize correlated data for model check/update
 - Can be expensive!

- Effect of *degree of spatial correlations*:

Single-node models $\prod p(X_i)$
No spatial correlations
Cheap – check is local!

Full-network model $p(X_1, \dots, X_n)$
Full spatial correlations
Expensive – centralize all data!

In-Network Model Maintenance

Single-node models $\prod p(X_i)$

No spatial correlations

Cheap – check is local!

Single-node Kalman filters

[Jain et al.'04]



Full-network model $p(X_1, \dots, X_n)$

Full spatial correlations

Expensive – centralize all data!

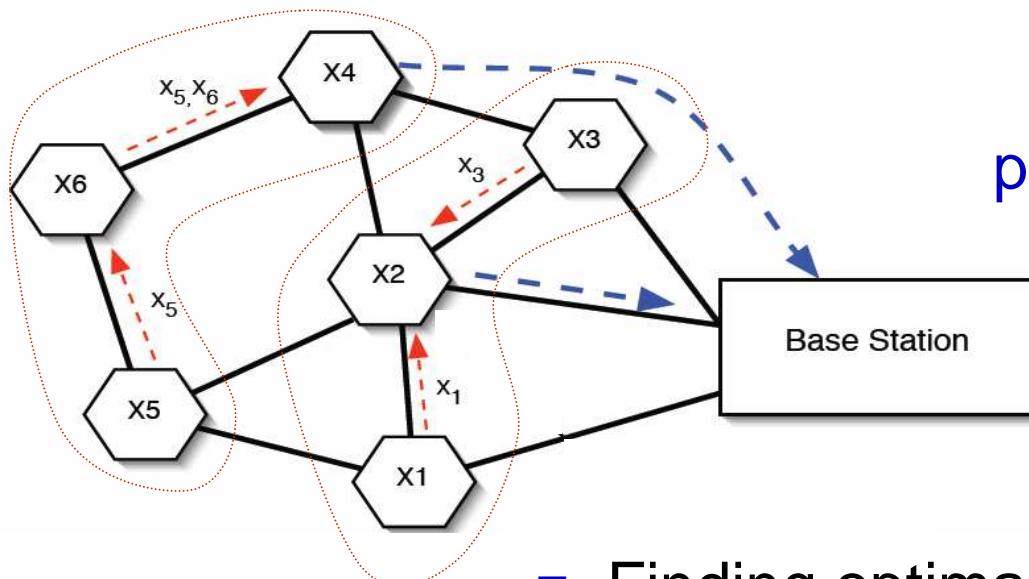
BBQ

[Deshpande et al. '04]

- **Problem:** Find dynamic probabilistic model and in-network maintenance schedule to minimize overall communication
 - Map maintenance/update operations to network topology
- Key idea for “practical” in-network models
 - Exploit *limited-radius* spatial correlations of measurements
 - Localize model checks/updates to small regions

Disjoint-Cliques Models

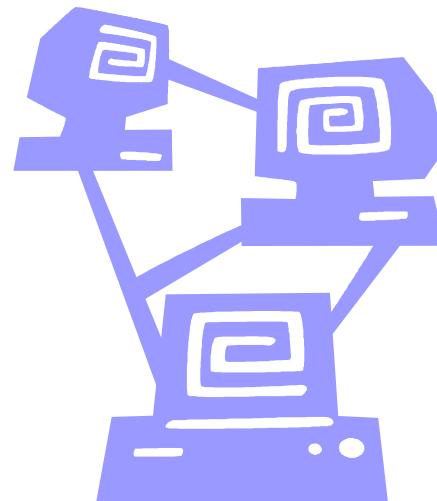
- *Idea:* Partition joint pdf into a set of small, localized “cliques” of random variables
 - Each clique maintained and updated *independently* at “clique root” nodes



$$\text{Model } p(X_1, \dots, X_6) = p(X_1, X_2, X_3) \cdot p(X_4, X_5, X_6)$$

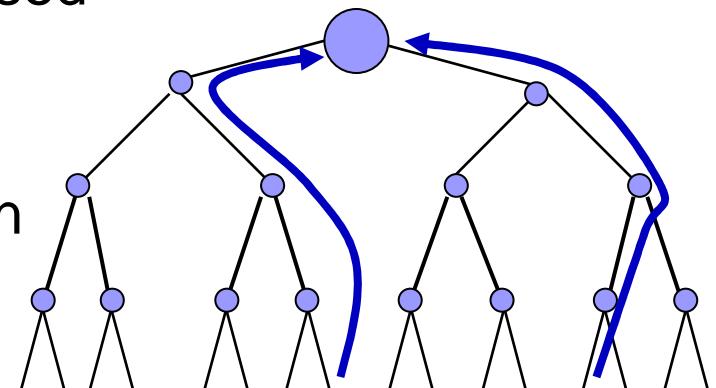
- Finding optimal DC model is NP-hard
 - Natural analogy to *Facility Location*

Distributed Data Stream Systems/Prototypes



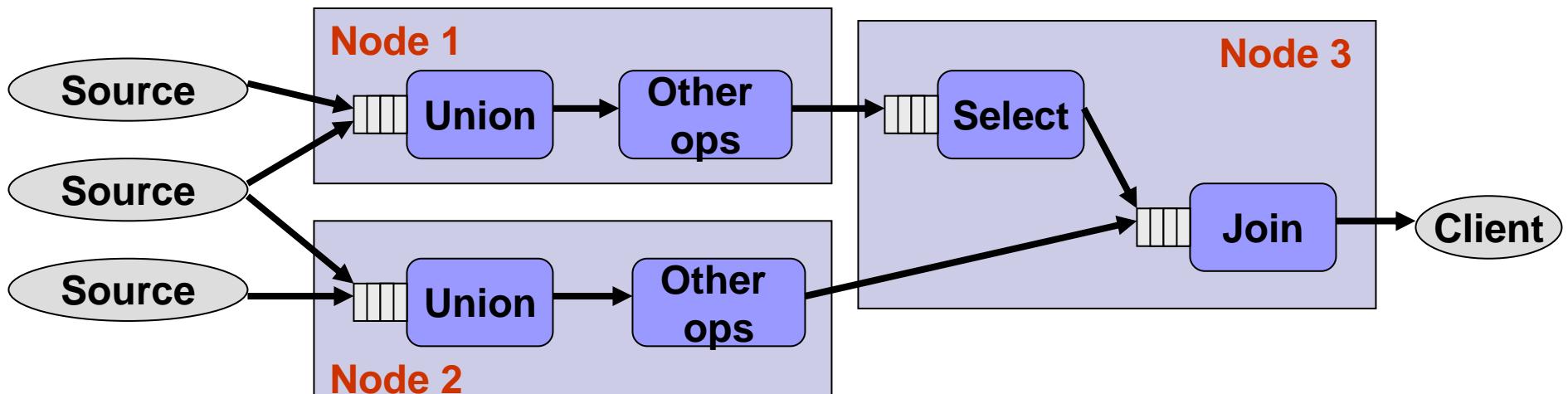
Current Systems/Prototypes

- Main algorithmic idea in the tutorial: Trade-off space/time *and communication* with approximation quality
- Unfortunately, approximate query processing tools are still not widely adopted in current Stream Processing engines
 - Despite obvious relevance, especially *for streaming data*
- In the sensornet context
 - Simple in-network aggregation techniques (e.g., for **average**, **count**, etc.) are widely used
E.g., TAG/TinyDB [Madden et al '02]
 - More complex tools for *approximate* in-network data processing/collection have yet to gain wider acceptance



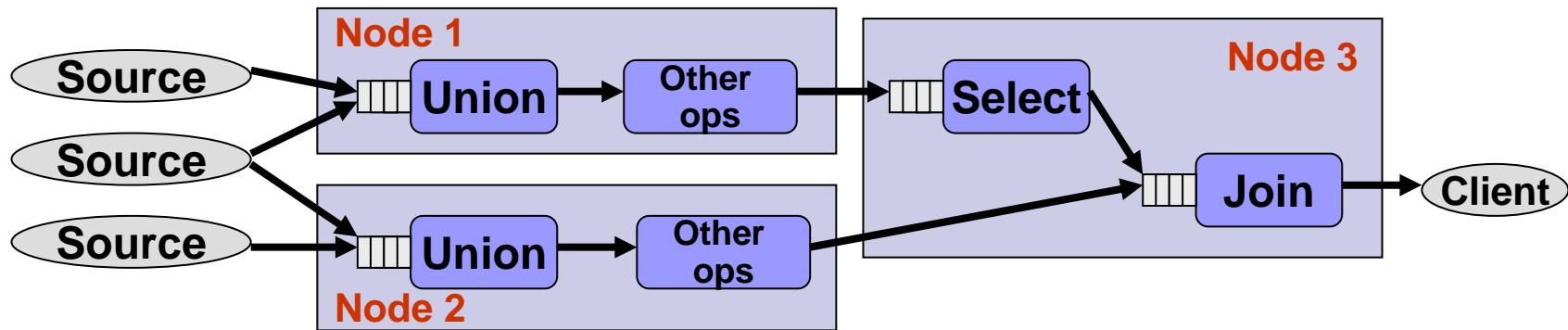
Distributed SP Engine Prototypes

- Telegraph/TelegraphCQ [Chandrasekaran et al.'03] ,
Borealis/Medusa [Balazinska et al.'05], P2 [Loo et al.'06]
- Query processing typically viewed as a *large dataflow*
 - Network of connected, pipelined query operators



- Schedule a large dataflow over a distributed system
 - Objectives: Load-balancing, availability, early results, ...

Distributed SP Engine Prototypes



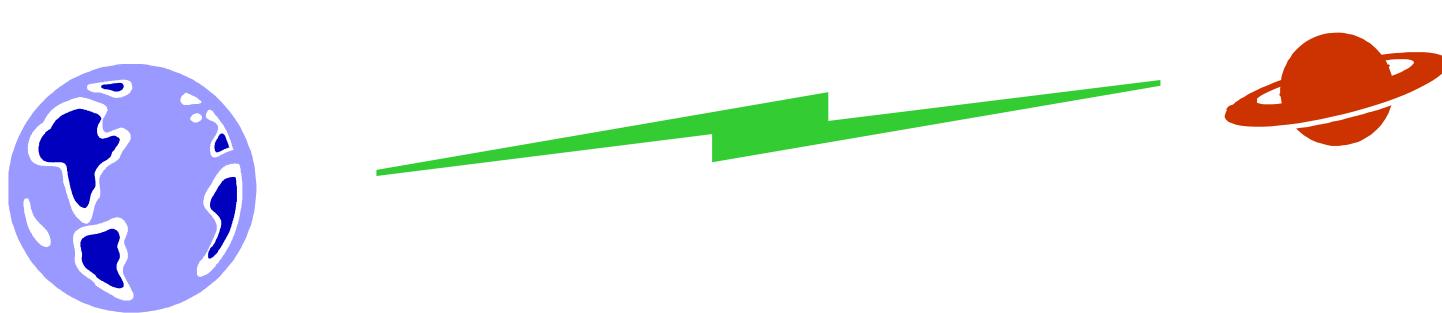
- Approximate answers and error guarantees not considered
 - General relational queries, push/pull-ing tuples through the query network
 - Load-shedding techniques to manage overload
 - No hard error guarantees
- Network costs (bandwidth/latency) considered in some recent work [Pietzuch et al.'06]

Other Systems & Prototypes

- **PIER** – Scaling to large, dynamic site populations using DHTs [Huebsch et al.'03]
 - See also the *Seaweed* paper [Narayanan et al.'06]
- **Gigascope** – Streaming DB engine for large-scale network/ application monitoring
 - Optimized for high-rate data streams (“line speeds”)
 - Exploits approximate query processing tools (sampling, sketches, ...) for tracking streams at endpoints
 - Distribution issues not addressed (yet...)

Tutorial Outline

- Motivation & Streaming Applications
- Centralized Stream Processing
- Distributed Stream Processing
- Open Problems & Future Directions
- Conclusions



Basic Streaming Models & Issues

- Lots of other work on streaming data analysis problems
 - Stream mining (clustering, associations, classification, change detection,...)
 - XML stream filtering (pub/sub systems)
 - Geometric data/queries (location streams)
- Other emerging richer streaming models and problems
 - XML & text stream mining (beyond simple filtering)
 - Graph-data streams (e.g., stream of graph edges)
 - *Both bound to gain importance* with the proliferation of huge web data sets (e.g., WebGraph, social networks)
 - E.g., PageRank computation over a streaming WebGraph?

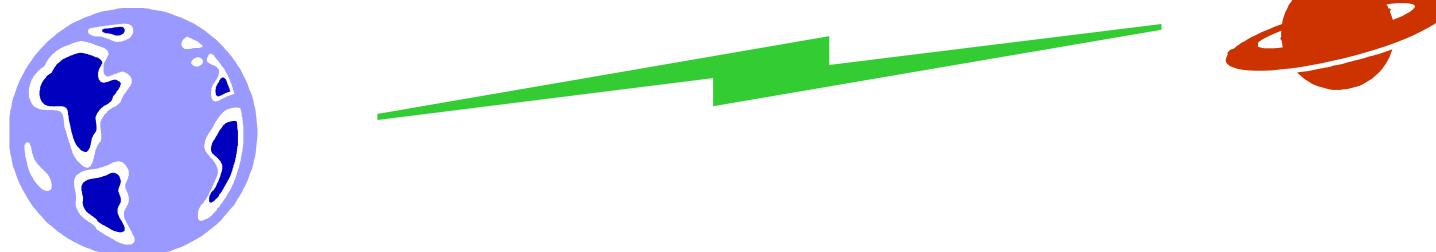
Extensions for P2P Networks

- Much work focused on specifics of sensor and wired nets
- P2P and Grid computing present alternate models
 - Structure of multi-hop overlay networks
 - “Controlled failure” model: nodes explicitly leave and join
- Allows us to think beyond model of “highly resource constrained” sensors.
- Implementations such as OpenDHT over PlanetLab [Rhea et al.’05]

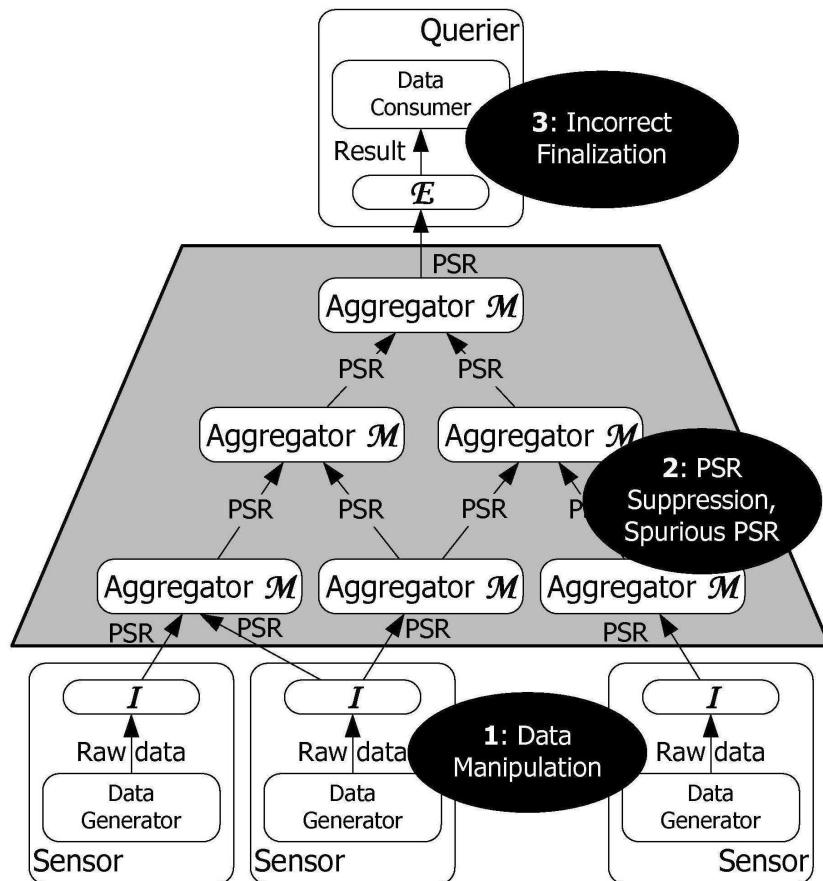


Delay-Tolerant Networks

- How to cope when connectivity is *intermittent*?
 - Roaming devices, exploring outer and inner space, network infrastructure for emerging regions (e.g., rural India), ...
 - Round trip times may be very long and varying
 - Radio to Mars is many minutes
 - Connectivity to remote villages varies [Jain, Fall, Patra '05]
- Goal is to minimize the **number** of communications and maximize **timeliness**
 - Size of communication is secondary



Authenticated Stream Aggregation



- Wide-area query processing
 - Possible *malicious aggregators*
 - Can suppress or add spurious information
- Authenticate query results at the querier?
 - Perhaps, to within some approximation error
- Initial steps in [Garofalakis et al.'07]

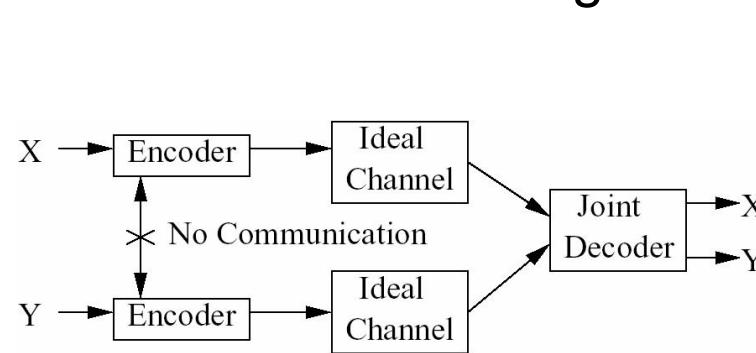
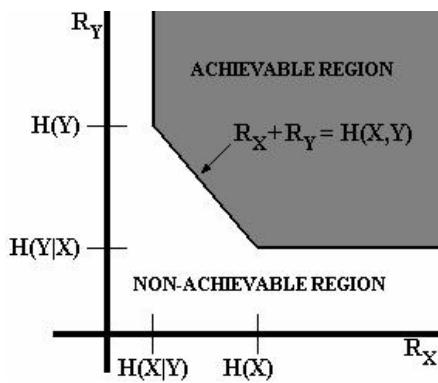
Other Classes of Queries

- Mostly talked about specific, well-defined aggregates
- What about *set-valued* query answers?
 - No principled, “universal” approximation error metric
- A general distributed query language (dist-streamSQL?)
 - Define a language so a query optimizer can find a plan that guarantees good performance, small communication?
- Other tasks, e.g., data mining, machine learning, over distributed streams?
 - ML/AI communities are already starting to consider communication-efficient distributed learning

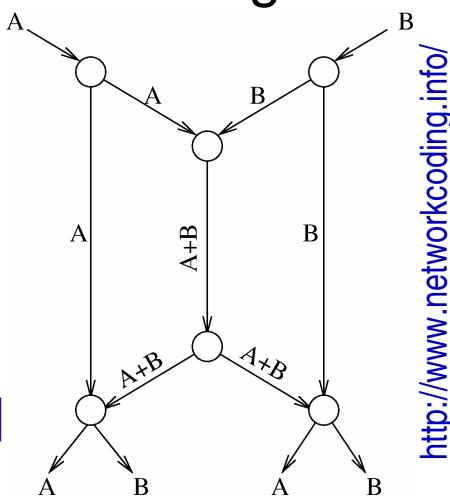
Theoretical Foundations

“Communication complexity” studies lower bounds of distributed **one-shot** computations

- Gives lower bounds for various problems, e.g., **count distinct** (via reduction to abstract problems)
- Need new theory for continuous computations
 - Based on info. theory and models of how streams evolve?
 - Link to distributed source coding or network coding?



Slepian-Wolf theorem [Slepian Wolf 1973]



Richer Prediction models

- The better we can capture and anticipate future stream direction, the less communication is needed
- So far, only look at predicting each stream alone
- Correlation/anti-correlation across streams should help?
 - But then, checking validity of model is expensive!
- Explore tradeoff-between power (expressiveness) of model and complexity (number of parameters)
 - Optimization via Minimum Description Length (MDL)?
[Rissanen 1978]

Conclusions

- Data Streaming: Major departure from traditional persistent database paradigm
 - Fundamental re-thinking of models, assumptions, algorithms, system architectures, ...
- Many new streaming problems posed by developing technologies
- Simple tools from approximation and/or randomization play a critical role in effective solutions
 - Sampling, sketches (AMS, CM, FM, ...), Exponential histograms, ...
 - Simple, yet powerful, ideas with great reach
 - Can often “mix & match” for specific scenarios

Conclusions

- **Distributed Streams:** Common features allow for general techniques/principles instead of “point” solutions
 - In-network query processing
Local filtering at sites, trading-off approximation with processing/network costs, ...
 - Models of “normal” operation
Static, dynamic (“predictive”), probabilistic, ...
 - Exploiting network locality and avoiding global resyncs
- Many new directions unstudied, more will emerge as new technologies arise
- *Lots of exciting research to be done! ☺*

Thank you!



<http://www.cs.berkeley.edu/~minos/>

minos@acm.org

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