

## COMP261 Lecture 4

Graphs 3 of 3

**Victoria**  
UNIVERSITY OF VICTORIA  
Te Whare Wānanga  
o te Ōpōkai o te Haka o Māui  
CAPITAL CITY UNIVERSITY

---

---

---

---

---

---

---

---

## Traditional Adjacency Matrix

Nodes referred to by an integer, 0..n  
Array of node labels/info  
Edges represented by entries in a 2D array

- Numbers for weights, NaN or sentinel number for no edge
- Strings for labels, null for no edge

|     | 0 | 1  | 2 | 3 | 4 | 5  | 6  | 7  | 8  | 9  |
|-----|---|----|---|---|---|----|----|----|----|----|
| 0 A | 0 |    | 7 |   |   |    |    |    | 10 | 4  |
| 1 B | 1 | 7  | 5 |   |   |    | 6  |    | 3  |    |
| 2 C | 2 |    | 5 | 1 |   |    |    |    | 9  | 2  |
| 3 D | 3 |    |   | 1 | 4 |    |    |    |    | 1  |
| 4 E | 4 |    |   |   | 4 | 23 |    |    | 17 |    |
| 5 F | 5 |    |   |   |   | 23 | 25 |    | 18 |    |
| 6 G | 6 |    | 6 |   |   |    | 25 | 10 | 8  | 14 |
| 7 H | 7 | 10 |   |   |   |    |    | 10 |    | 3  |
| 8 I | 8 | 4  | 3 | 9 |   | 17 |    | 8  |    | 6  |
| 9 J | 9 |    |   | 2 | 1 | 18 | 14 | 3  | 6  |    |

What Questions are fast?  
All nodes?  
Neighbours of node?  
Neighbours to node?  
Edge exists from j to k ?

Directed or Undirected?

---

---

---

---

---

---

---

---

## Traditional Adjacency Matrix

Nodes referred to by an integer, 0..n  
Array of node labels/info  
Edges represented by entries in a 2D array

- Numbers for weights, NaN or sentinel number for no edge
- Strings for labels, null for no edge

|     | 0 | 1  | 2 | 3 | 4 | 5  | 6  | 7  | 8 |
|-----|---|----|---|---|---|----|----|----|---|
| 0 A |   |    |   |   |   |    |    |    |   |
| 1 B | 1 | 7  |   |   |   |    |    |    |   |
| 2 C | 2 |    | 5 |   |   |    |    |    |   |
| 3 D | 3 |    |   | 1 |   |    |    |    |   |
| 4 E | 4 |    |   |   | 4 |    |    |    |   |
| 5 F | 5 |    |   |   |   | 23 |    |    |   |
| 6 G | 6 |    | 6 |   |   |    | 25 |    |   |
| 7 H | 7 | 10 |   |   |   |    |    | 10 |   |
| 8 I | 8 | 4  | 3 | 9 |   | 17 |    | 8  |   |
| 9 J | 9 |    |   | 2 | 1 | 18 | 14 | 3  | 6 |

If Undirected

---

---

---

---

---

---

---

---

## Traditional Adjacency List

Nodes referred to by an integer 0..n

Array of node labels & array of lists

Lists of neighbour and edge weight/label

| node label | neighbour : weight        |
|------------|---------------------------|
| 0 A        | 1:7 7:10 8:4              |
| 1 B        | 0:7 2:5 6:6 8:3           |
| 2 C        | 1:5 3:1 8:9 9:2           |
| 3 D        | 2:1 4:4 9:1               |
| 4 E        | 3:4 5:23 8:17             |
| 5 F        | 4:23 6:25 9:18            |
| 6 G        | 1:6 5:25 7:10 8:8 9:14    |
| 7 H        | 0:10 6:10 9:3             |
| 8 I        | 0:4 1:3 2:9 4:17 6:8 9:6  |
| 9 J        | 2:2 3:1 5:18 6:14 7:3 8:6 |

What Questions are fast?

All nodes?

Neighbours of node?

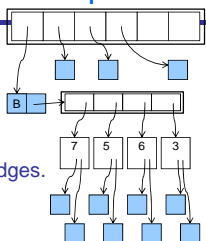
Neighbours to node?

Edge exists from j to k ?

Directed or Undirected?

## "Modern" Data Structure for Graphs

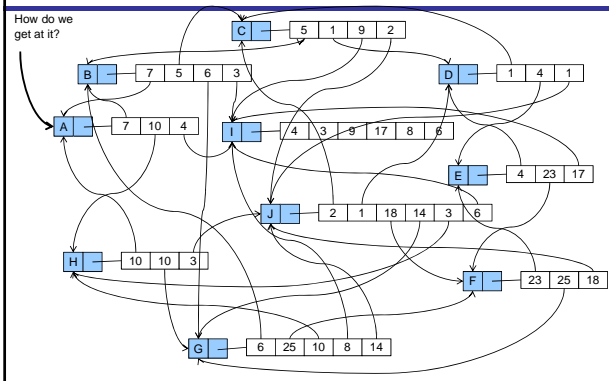
- We have a set of nodes



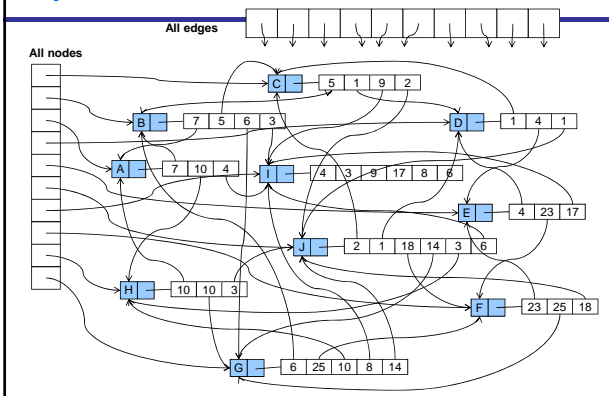
- Each node has edges out of it  
⇒ Node should contain a collection of edges.
- (Directed) Each edge has a node at the other end  
⇒ edge should contain a destination node.  
⇒ edge might contain the source node as well

## Object-based data structure.

How do we get at it?



## Object-based data structure.



## Java Type Declarations

- The graph:
 

```
Set<Node> nodes = new HashSet<Node>();
```
- Nodes:
 

```
String label;
Set<Edge> edgesOut = new HashSet<Edge>();
[ Set<Edge> edgesIn = new HashSet<Edge>(); ]
```
- Edges:
 

```
double length;
Node start;
Node end;
```

## Data Structure for the Road Map

- Road objects (homogeneous chunks of road)
  - ID#, name, one way, speed limit, type, .....
- Intersection objects
  - ID#, location, list of road segments out, [ list of road segments in? ]
- Road Segment objects
  - Road they are part of, intersection from, intersection to, geometry = list of locations for drawing

8743, 3.2, 4.8

354, High St, Warkworth, false, 0, 6, .....

3.2, 4.8 3.3, 5.0...

- Why ID#'s?
  - road segment → intersection ? via ID or direct?
  - road segment → road ? via ID or direct?

## Data structures for the Road Map

- The graph  

```
Map<Integer,Node> nodes = new HashMap<Integer,Node>();
```
- The node (intersection)  

```
List<Segment> outNeighbours = new ArrayList<Segment>(2);
List<Segment> inNeighbours = new ArrayList<Segment>(2);
```
- The Segment (the edge)  

```
Node startNode;
Node endNode;
...
```

---

---

---

---

---

---

---

---

## The Roads

```
Map<Integer,Road> roads = new HashMap<Integer,Road>()
```

Road objects

```
List<Segment> segments = new ArrayList<Segment>();
```

Segment objects

```
Node StartNode
```

```
Node EndNode
```

```
Road road
```

Note about terminology: road consists of road segments which are between two nodes each and each road segment in turn is not just a straight line but a list of coordinates that can be used to draw a segment...

---

---

---

---

---

---

---

---

## Loading data

- Read the Road data and the Intersection data
  - Remember to convert latitude/longitude to x/y coordinates (in kms).
- Put the objects into structures that gives fast access by ID.
- Read the RoadSegment data,
  - Convert the latitude/longitude data into x/y coordinates.
  - Look up the road and intersections by ID
  - Construct the road segment object(s) containing the road and intersections.
  - Add the road segment to the intersection objects
  - Add the road segment to the road objects
  - If road is not one way, you will need to create another segment object
  - Add it to the intersections

---

---

---

---

---

---

---

---