

# Bachelor Thesis

Studies on the Different Post-Processors  
and Building a Virtual Machining  
Environment for a 5-Axis Machine Tool.

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# 1. 緒論

## 1.1 概述

近年由於複雜的曲面加工以及縮短加工時間的需求增加，傳統三軸加工的加工誤差過大與加工時間過長之缺點讓多軸加工成為目前發展的趨勢，然而複雜的多軸加工又面臨著加工門檻過高的問題，如何以有效率且彈性的方法來降低加工門檻成了重要的議題，而快速且正確的建立加工前的處理和模擬也顯得更為重要。

目前大多數商用的 CAD/CAM 軟體如 UG NX, MASTERCAM 等，只有內建的工具機機台做加工與碰撞之模擬，很難能夠建立新的機台來去做真實的碰撞預測，本文提出自行研發的軟體可以快速地建立不同工具機機台來做加工與碰撞的模擬，並可以以讀取通用的 CL 檔案來做特定機台的後處理得到真實工具機控制器可讀取的 NC 碼，以簡易的軟體輸入去預測碰撞、量測尺間，來降低多軸加工之門檻。

## 1.2 研究目的與方法

本文為提升多軸工具機加工前處理之速度與彈性，以讀取 UG NX 輸出的 CL 檔案，對特定機台，TMV 710A，做解析解後處理[1]，得到 SIEMENS 與新代 控制器可讀取之 NC 碼，並在 CL 檔案做插值來得到誤差較低的加工指令，最後使用國立成功大學李榮顯教授實驗室所研發的虛擬工具機加工環境自行建立虛擬工具機機台並模擬加工、碰撞和量測。

本文將以 NX 後處理建構器、梅可人之數值解後處理[2]以及數值解後處理所輸出之 NC 檔做比較，並比較在 CL 資料點間做插值數量對誤差影響的比較，以及用虛擬加工環境的碰撞功能去仿照三次元量床方法做加工後工件尺寸之量測。

## 2. 理論基礎與方法

### 2.1 建構虛擬工具機

#### 2.1.1 CNC 工具機構型標準

CNC 工具機的軸向運動分為線性運動以及旋轉運動。線性運動為沿著參考軸做平行於參考軸之直線運動。旋轉運動則是繞著參考軸之旋轉。因此在各軸向、參考坐標有著統一的定義[3]，本文僅介紹立式銑床之定義。

工具機軸向為由右手定則決定(如圖 2-1a)，而根據機器運動指令的需求，習慣上用刀件相對於工件來定義。[4]立式工具機之 Z 軸定義為與旋轉主軸平行之軸，而工件與刀具距離增加之方向為 Z 軸的正方向。X 軸為垂直於 Z 軸並平行於最長行程，正方向為操作者正向工具機從轉軸往機柱看時，刀具往相對工件之右邊切削之方向，Y 軸為以右手定則與已決定好之 X、Z 來定義，如圖 2-2 中之  $X'$ 、 $Y'$ 、 $Z'$ ，其中  $X'$ 、 $Y'$ 、 $Z'$  為移動工件之正方向，X、Y、Z 為刀具對工件之正方向。

三個旋轉軸為相對於 X、Y、Z 軸的旋轉軸，依序標示為 A、B、C，其中相對於 X 軸之旋轉軸為 A 軸；相對於 Y 軸之旋轉軸為 B 軸；相對於 Z 軸之旋轉軸為 C 軸，旋轉方向以右手定則做定義，大拇指為 X、Y、Z 之正方向，其他四根手指螺旋之方向即為旋轉正方向(如圖 2-1b)。

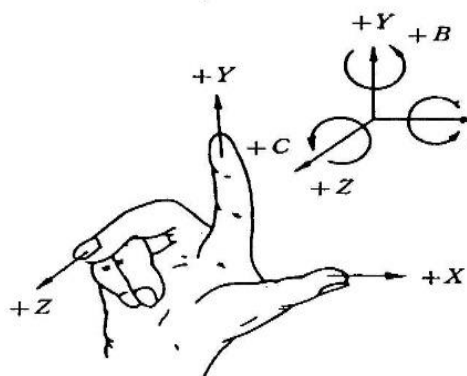


圖 2-1a

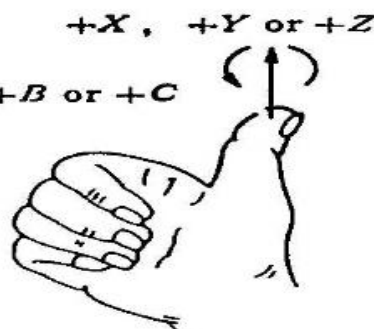


圖 2-1b

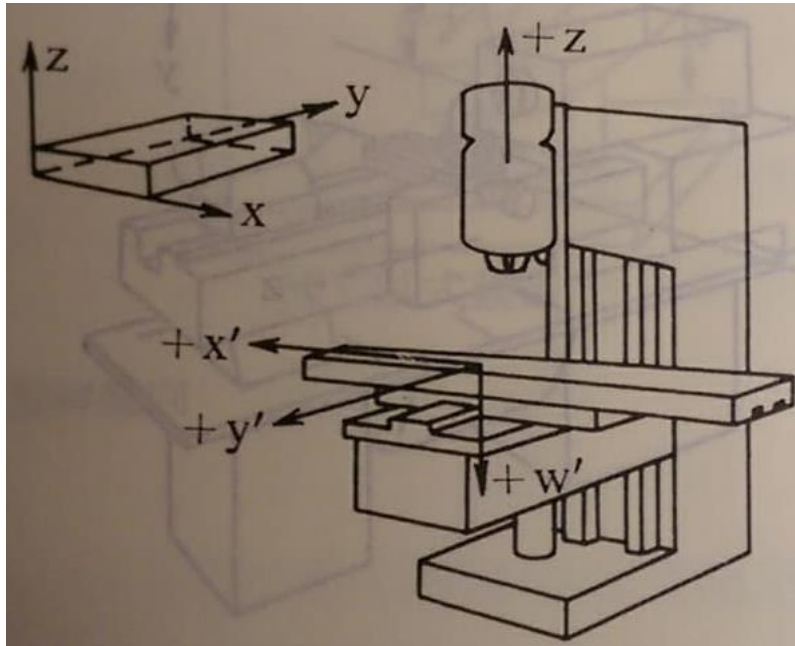


圖 2-2

## 2.1.2 虛擬工具機構型之組裝

國立成功大學李榮顯教授實驗室所開發之虛擬工具機環境中，機台構型是用機台樹狀圖來做組裝，本文以東台精機股份有限公司所開發的 TMV-710A 立式五軸工具機(A、C 軸工作檯傾斜型)之簡易構型為範例。首先須先觀察機台底座以及各軸之關聯，其中分為底座(Base)、X 軸機構、Y 軸機構、Z 軸機構、主軸(Spindle)五個部分，來繪製樹狀圖(圖 2-3)此虛擬工具機為根據機台廠商之工程圖所建構。

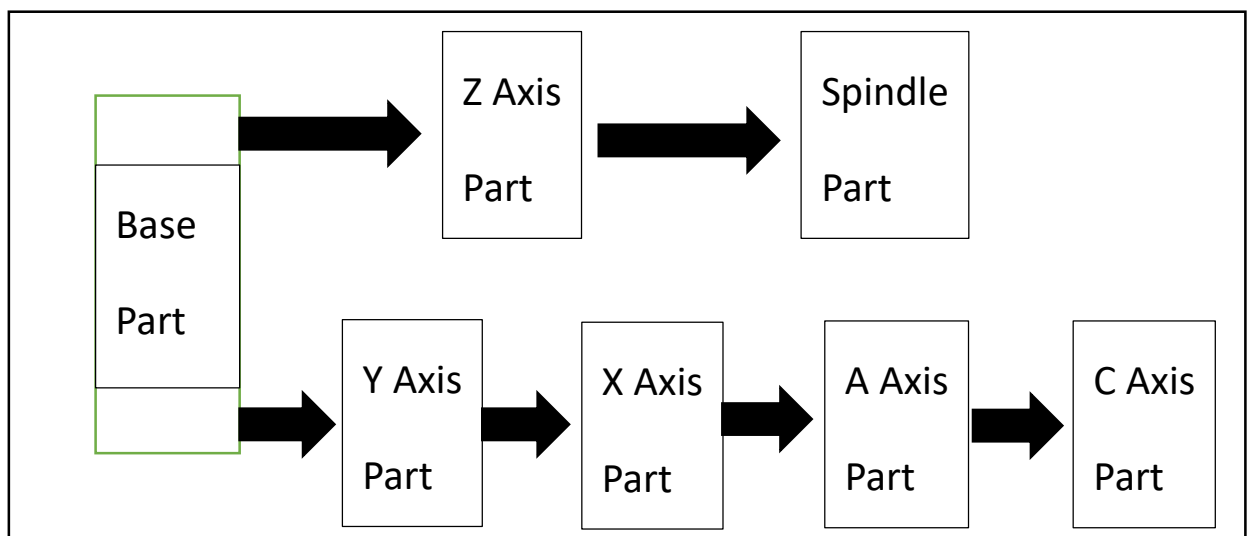


圖 2-3

各部位 STL 檔案經過虛擬工具機環境處理各個相對位置後，虛擬機台如圖 2-4 所示，其中各軸之定義方向即為如 2.1.1 章所介紹。

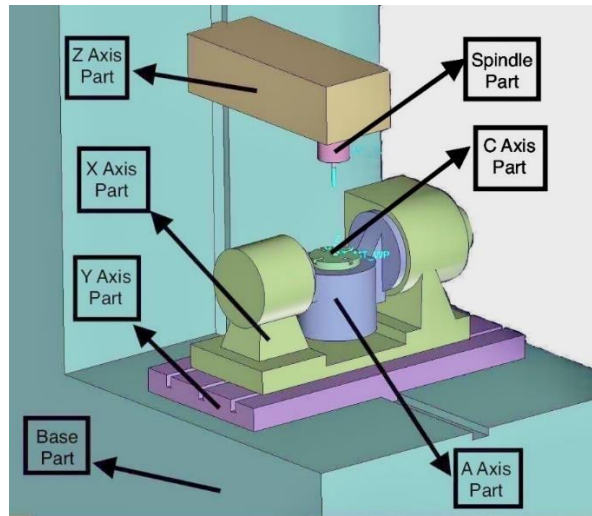


圖 2-4

## 2.2 後處理方法

### 2.2.1 後處理概述

如圖 2-5，後處理為電腦輔助製造程式設計與製造間重要的橋梁，後處理程式將通用的刀具位置(CL 檔)轉換為特定機台的加工操作資料，如此 CNC 工具機讀取這些資料後，就能依照程式加工。由於五軸工具機的種類繁多，加上各家控制器製造廠家有著不同的控制碼定義，因此五軸後處理程式通常都是個別獨立處理，即每部五軸工具機都有其專用的後處理，也因為五軸加工機具有多軸同動洗削功能，軟體所需定義的相關參數甚多，對於初次使用者而言，除非具有相當的工具機使用經驗以及學理基礎，否則往往不能定義出真實的工具機參數，也可能因此造成精密的多軸工具機損壞，所以可知準確後處理的重要性，本文將依照 TMV-710A AC 五軸加工機所搭配之新代控制器來做後處理，所探討的後處理也只針對刀具座標控制點轉作處理。



圖 2

## 2.2.2 數值解後處理流程

數值分析方法指對數學問題用遞迴趨近來得到近似解，本文數值解參考梅可人[2]使用 Broyden 方法之程式，每一行 CL 皆須一 NC 作為趨近之起動值，針對第一行的 CL，以機械原點之 NC 趨近。對每一行 CL，以上一行之 CL 相對應之 NC 趨近。若趨近失敗，則將上一次趨近之 CL 與當下欲趨近之 CL 做插值，再以插值所得之 CL 做趨近。若趨近成功，則對下一個未處理之 CL 進行如上之趨近劉程；若趨近成功且該 CL 為使用者輸入之 CL 檔案，則將其 NC 紀錄並對下一個未處理之 CL 進行如上所述之趨近，如圖 2-5。

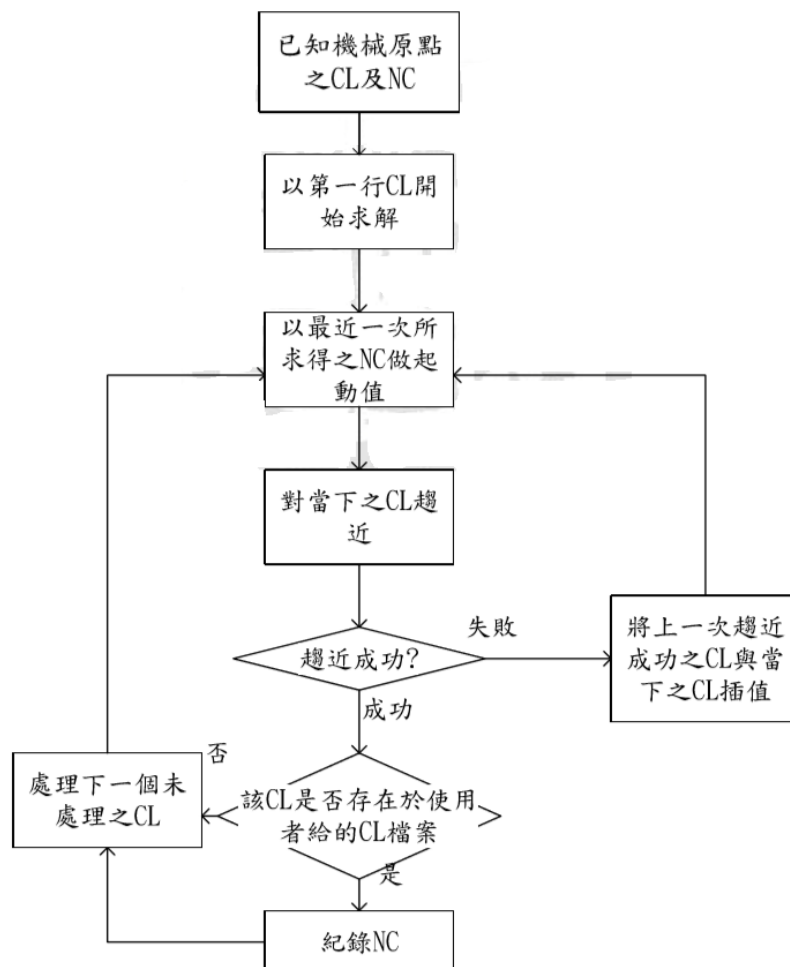


圖 2-5



## 2.2.3 五軸加工之幾何定義

一般五軸加工的刀具位置資料包含描述工件坐標系 $O_W X_W Y_W Z_W$ 中，刀具中心尖端的座標 $\tilde{Q}$ 以及刀軸方向 $\tilde{K}$ (如圖 2-6)，以矩陣的形式表示如下：

$$\begin{bmatrix} \tilde{K} & \tilde{Q} \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} K_x & Q_x \\ K_y & Q_y \\ K_z & Q_z \\ 0 & 1 \end{bmatrix} \quad (2-1)$$

其中 $K_x$ 、 $K_y$ 、 $K_z$ 為向量 $\tilde{K}$ 之方向餘弦； $Q_x$ 、 $Q_y$ 、 $Q_z$ 為位置座標 $\tilde{Q}$ 的三個座標分量，此處注意向量 $\tilde{K}$ 皆為從工件指向外的方向。

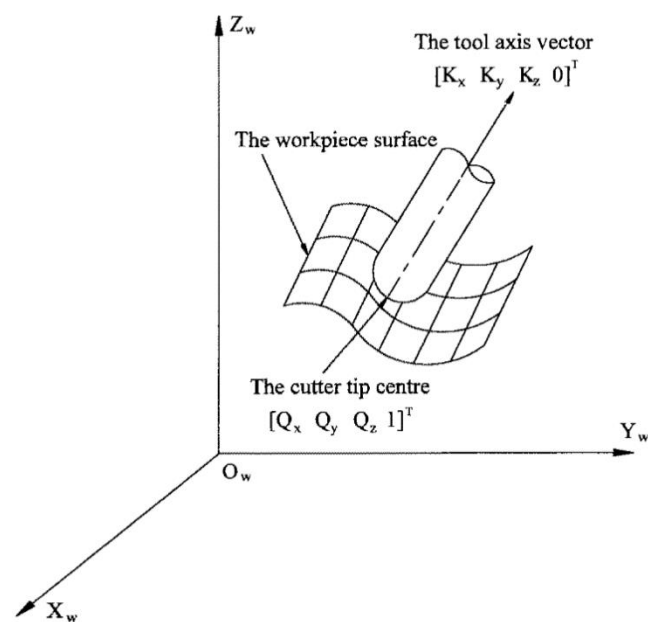


圖 2-6

## 2.2.4 解析解公式推導

解析解後處理的推導源自於逆向運動學，也就是已知末端點(刀尖)位置，來求得各軸的位置移動以及轉動角度，而逆向運動學所用到的運動齊次座標轉換矩陣如下公式(1)~(4)。(1)代表對X軸移動 $a$ 、Y軸移動 $b$ 、Z軸移動 $c$ ，(2)代表對X軸轉 $\theta$ 角度，(3)代表對Y軸轉 $\theta$ 角度，(4)代表對Z軸轉 $\theta$ 角度。座標之轉換可以經由矩陣前乘來對原有坐標系座移動或旋轉。

$$\mathbf{Trans}(a,b,c) = \begin{bmatrix} 1 & 0 & 0 & a \\ 0 & 1 & 0 & b \\ 0 & 0 & 1 & c \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (1)$$

$$\mathbf{Rot}(X,\theta) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & C\theta & -S\theta & 0 \\ 0 & S\theta & C\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (2)$$

$$\mathbf{Rot}(Y,\theta) = \begin{bmatrix} C\theta & 0 & S\theta & 0 \\ 0 & 1 & 0 & 0 \\ -S\theta & 0 & C\theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (3)$$

$$\mathbf{Rot}(Z,\theta) = \begin{bmatrix} C\theta & -S\theta & 0 & 0 \\ S\theta & C\theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (4)$$

本文僅討論 AC 軸工作台傾斜型工具機，如圖 2-7，在工作台上有兩個迴轉軸，假設兩旋轉軸相交於軸心點 R。圖 2-8 中坐標系  $O_W X_W Y_W Z_W$  及  $O_t X_t Y_t Z_t$  分別為工件及刀尖座標系統，而向量  $L_x \mathbf{i} + L_y \mathbf{j} + L_z \mathbf{k}$  為工件原點  $O_W$  至 R 點之偏移向量，此偏移向量代表實際工件架設在工具機上時，工件原點與旋轉軸心點的相對位移。

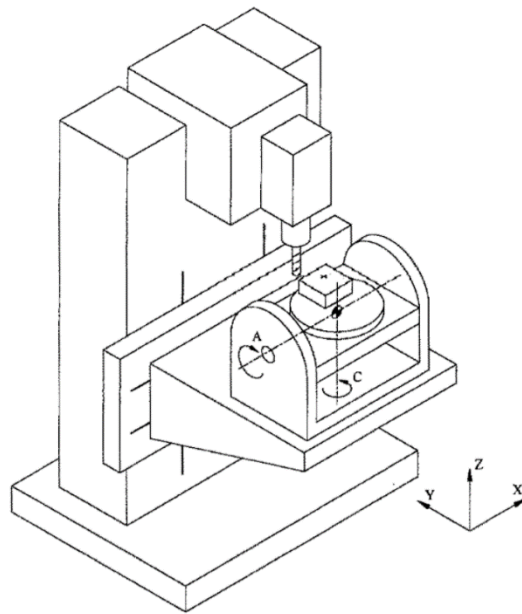


圖 2-7

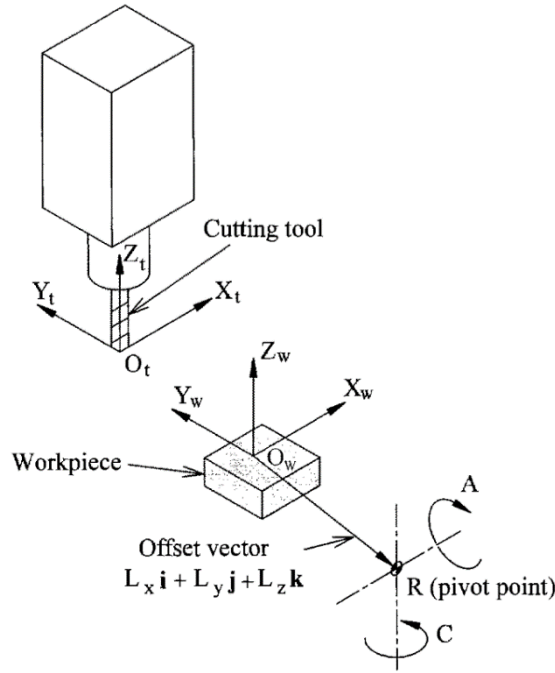


圖 2-8

由於此類型工具機實際的機構元件包含了旋轉台、線性平台、床台、主軸頭、刀具，因此可以由工件座標系開始，利用一連串的齊次座標轉換至刀具座標系，便可以得到其形狀創成函數矩陣，其轉換流程如圖 2-9 所示，以數學的表達如下：

$$\text{Trans}(L_x, L_y, L_z) \times \text{Rot}(z, \varphi_z) \times \text{Rot}(x, \varphi_x) \times \text{Trans}(P_x, P_y, P_z) \times \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} \quad (2-2)$$

其中 $\varphi_x$ 及 $\varphi_y$ 為旋轉台繞著 X 軸及 Z 軸之旋轉角度，而正方向旋轉角式沿著+X 及 +Z 軸右手螺旋方向。 $P_x$ 、 $P_y$ 、 $P_z$ 為線性平台相對於 X、Y、Z 軸之相對位移。(2-1)式為圖 2-7 構型工具機的形狀創成函數矩陣，說明工件與刀尖的相對位置和方位。對於一個已知的刀尖路徑資料，可令(2-2)式與(2-1)式相等，解出所需的工具機參數。

將(2-2)式展開，並令其與(2-1)相等，可得：

$$\begin{bmatrix} K_x & Q_x \\ K_y & Q_y \\ K_z & Q_z \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} S\varphi_x S\varphi_z & L_x + P_x C\varphi_z - P_y C\varphi_x S\varphi_z + P_z S\varphi_x S\varphi_z \\ -S\varphi_x C\varphi_z & L_y + P_x S\varphi_z + P_y C\varphi_x C\varphi_z - P_z S\varphi_x C\varphi_z \\ C\varphi_x & L_z + P_y S\varphi_x + P_z C\varphi_x \\ 0 & 1 \end{bmatrix} \quad (2-3)$$

比較(2-3)式左右兩邊所對應的第 1 行及第 2 行元素，可分別得到 6 組聯立

方程式，以解得未知數 $\varphi_x$ 、 $\varphi_z$ 及 $P_x$ 、 $P_y$ 、 $P_z$ 。其求解的過程是先解出旋轉角 $\varphi_x$ 、 $\varphi_z$ ，再解出相對位移 $P_x$ 、 $P_y$ 、 $P_z$ 值。取(2-3)式左右兩邊的第一行，雖然未知數只有 $\varphi_x$ 、 $\varphi_z$ ，卻有 3 組聯立方程式，但因 $K_x$ 、 $K_y$ 、 $K_z$ 有 $K_x + K_y + K_z = 1$ 之關係，因此實際上只有 2 組獨立的聯立方程式。

由(2-3)式左右兩邊的第一行，可以解出 $\varphi_x$ 、 $\varphi_z$ 之值如下：

$$\varphi_x = \arccos(K_z) \quad 0 \leq \varphi_x \leq \pi \quad (2-4)$$

$$\varphi_z = \arctan2(K_x, K_z) \quad -\pi \leq \varphi_z \leq \pi \quad (2-5)$$

其中 $\arctan2$ 為特殊函數，可依 x、y 座標值回應角度值再 $[-\pi, \pi]$ 之值域中，其定義為

$$\theta = \begin{cases} 0 \leq \theta \leq \frac{\pi}{2} & \text{for } x \geq 0 \text{ and } y \geq 0 \\ \frac{\pi}{2} \leq \theta \leq \pi & \text{for } x \leq 0 \text{ and } y \geq 0 \\ -\pi \leq \theta \leq -\frac{\pi}{2} & \text{for } x \leq 0 \text{ and } y \leq 0 \\ -\frac{\pi}{2} \leq \theta \leq 0 & \text{for } x \geq 0 \text{ and } y \leq 0 \end{cases}$$

要注意的(2-4)式中，由於 $\arccos$ 的值域 $[0, \pi]$ ，限制了 $\varphi_x$ 角的範圍，若是 $\varphi_x$ 角在 $[-\pi, 0]$ 範圍中，則 $\varphi_x$ 及 $\varphi_z$ 之解應修正為：

$$\varphi_x = -\arccos(K_z) \quad -\pi \leq \varphi_x \leq 0 \quad (2-4)$$

$$\varphi_z = \arctan2(-K_x, -K_z) \quad -\pi \leq \varphi_z \leq \pi \quad (2-5)$$

再來由(2-3)式左右兩邊的第二行可以解出 $P_x$ 、 $P_y$ 、 $P_z$ 之值如下：

$$P_x = (Q_x - L_x)C\varphi_z + (Q_y - L_y)S\varphi_z \quad (2-6)$$

$$P_y = -(Q_x - L_x)C\varphi_x S\varphi_z + (Q_y - L_y)C\varphi_x C\varphi_z + (Q_z - L_z)S\varphi_x \quad (2-7)$$

$$P_z = (Q_x - L_x)S\varphi_x S\varphi_z - (Q_y - L_y)S\varphi_x C\varphi_z - (Q_z - L_z)C\varphi_x \quad (2-8)$$

此處所解得的 $P_x$ 、 $P_y$ 、 $P_z$ ，並不式真實的 X、Y、Z 軸 NC 碼，一般而言，NC 加工所對應的各軸運動，必須相對於一個程式座標系，這個座標細在不同的控制器則利用不同的 G 碼來設定，以 SYNTec 控制器而言，使用 G54 至 G59.9 一共 15 個座標系定義程式原點，而大部分的情況程式原點與刀尖路徑資料的工件座標系原點重合。因此假設程式原點與工件原點重合，此時可利用(2-3)式左右兩邊的第二行，當 $\varphi_x = \varphi_z = 0$ 時，

$$[Q_x \ Q_y \ Q_z \ 1]^T = [L_x + P_x \ L_y + P_y \ L_z + P_z \ 1]^T, \text{化簡得:}$$

$$[X \ Y \ Z \ 1]^T = [L_x + P_x \ L_y + P_y \ L_z + P_z \ 1]^T$$

因此本構型之五軸 NC 碼參數方程式為：

$$A = \varphi_x = \begin{cases} \arccos(K_z) & 0 \leq \varphi_x \leq \pi \\ -\arccos(K_z) & -\pi \leq \varphi_x \leq 0 \end{cases}$$

$$C = \varphi_z = \arctan2(K_x \text{sign}(S\varphi_x), K_z \text{sign}(S\varphi_x)) \quad -\pi \leq \varphi_z \leq \pi$$

$$\text{其中 } \text{sign}(S\varphi_x) = \begin{cases} 1 & \text{當 } S\varphi_x \geq 0 \\ -1 & \text{其他} \end{cases}$$

$$X = L_x + P_x = (Q_x - L_x)C\varphi_z + (Q_y - L_y)S\varphi_z + L_x$$

$$Y = L_y + P_y = -(Q_x - L_x)C\varphi_x S\varphi_z + (Q_y - L_y)C\varphi_x C\varphi_z + (Q_z - L_z)S\varphi_x + L_y$$

$$Z = L_z + P_z = (Q_x - L_x)S\varphi_x S\varphi_z - (Q_y - L_y)S\varphi_x C\varphi_z - (Q_z - L_z)C\varphi_x + L_z$$

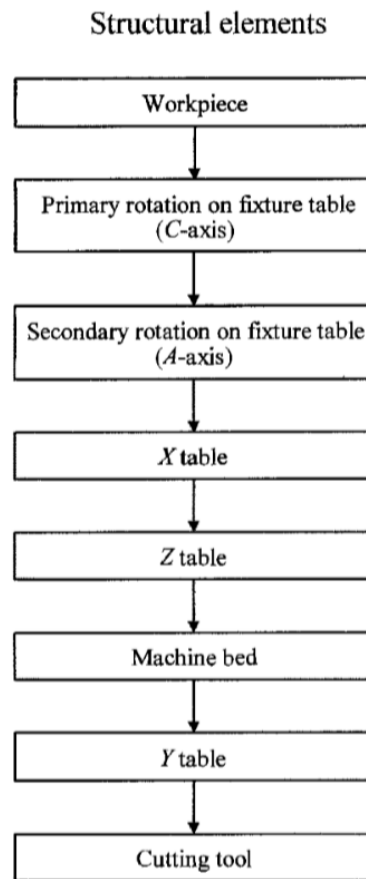


圖 2-9

## 2.2.5 解析解後處理程式流程

利用 CAD/CAM 軟體所輸出的 CL 檔(刀尖位置)，再分別用 $[-\pi, 0]$ 和 $[0, \pi]$ 兩個值域の後處理公式得到兩組 NC 碼，選擇第一行 NC 碼 C 軸需旋轉最小的 NC 碼組並紀錄之，因為兩組 NC 碼是相同 CL 檔的對偶根，加上為使加工過程刀具路徑連續，每行 NC 碼必須在兩組 NC 碼中做選擇，吾人使用選擇新的 X 軸數值與上一行 X 軸數值相差較小來繼續流程，以維持加工之連續性。如下圖

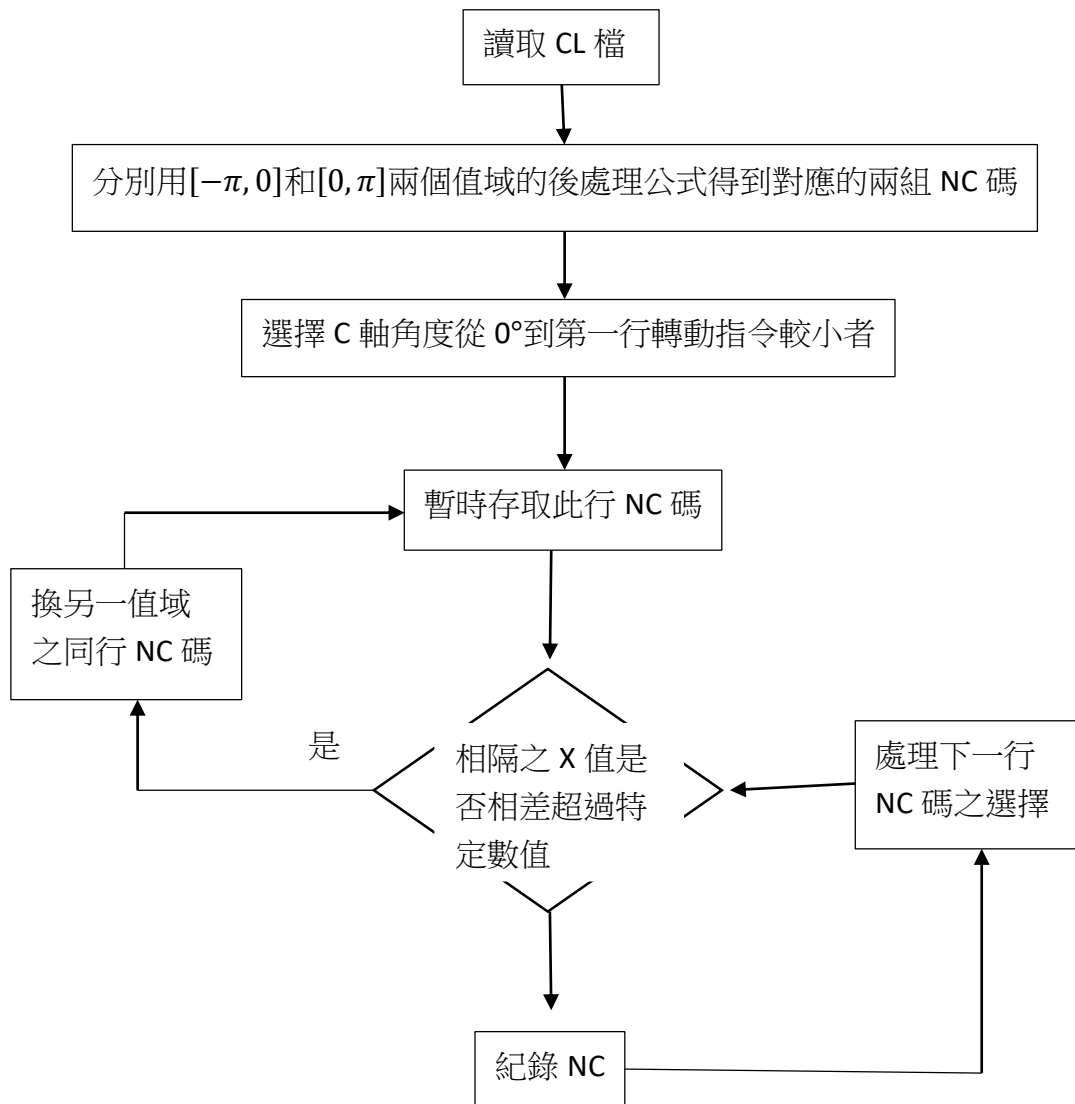


圖 2-10

## 2.3 插值目的與方法

CL 檔案為使用許多的 GOTO 指令(如圖 2-11)，也就是許多的直線小線段去趨近加工曲線路徑，在 NC 碼中為使用許多的 G01 線段做曲線的趨近。在 CL 檔案中 GOTO 後的前三個值為相對工件原點給定刀尖位置的 X、Y、Z 座標，兩個 GOTO 點座標間刀尖是以線性平均來移動到下一個 GOTO 目標座標，然後 NC 碼為各軸 G01 值的平均來做兩個 G01 值之間的移動，因此在三軸加工時，由於只有線性平台之位移，所以 CL 檔中 GOTO 間平均的移動與 NC 碼之 G01 間各軸的平均移動是等效的。然而在五軸加工，因為多了旋轉軸之指令，NC 碼之 G01 間各軸的平均移動和旋轉經過逆向後處理得到的 CL 檔，並不會等同於原先的 CL 檔指令，也就是說後處理得到的 NC 碼只有在 G01 給定的點時才會是在真實加工路徑上，G01 點間的路徑並不會等於所要求的加工路徑。

GOTO/45.1072,-50.0003,23.4884,-0.2745937,-0.2881959,0.9173557
GOTO/40.1766,-50.0000,22.1062,-0.2374081,-0.2911482,0.9267525
GOTO/37.6874,-50.0000,21.5064,-0.2096495,-0.2930564,0.9328263

圖 2-11

為解決此問題，可以將 CL 檔先做插值，再將插值出來各點做後處理得到更符合要求之加工路徑的 NC 碼。插值的方法有許多種，像是線性插值、一次方程插值與多次方程插值，而本文使用線性插值來做測試。

假設有兩點 a、b，其座標為 $(X_a, Y_a, Z_a)$ 、 $(X_b, Y_b, Z_b)$ ，若想對其兩點間做 n 個插值，其各點之位置座標為

$$X_{a,i} = X_a + \frac{X_b - X_a}{n + 1} \times i \quad (i = 1 \sim n + 1)$$

$$Y_{a,i} = Y_a + \frac{Y_b - Y_a}{n + 1} \times i \quad (i = 1 \sim n + 1)$$

$$Z_{a,i} = Z_a + \frac{Z_b - Z_a}{n + 1} \times i \quad (i = 1 \sim n + 1)$$

而要做多少個插值，就以所需的誤差來做決定，在本文後也將討論之。

另外，為解決五軸加工機插值的不便，除了使用參數式曲線之趨近，大部分控制器廠商在工具機控制器裡有個 G43.4，刀尖點控制功能，Rotational Tool Center Point(RTCP)的指令，以新代控制器為例，在一般機台上，控制器的移動命令是下給刀柄或者主軸鼻端，開啟刀尖點控制後，移動命令會改以刀尖點所在座標來作控制，此功能是五軸加工機特有之功能。如下圖 2-12 中有兩條加工軌跡，橘色軌跡是一般加工狀況的機台路徑，控制器控制主軸鼻端的軌

跡，因此與工件表面會相差一個刀長；藍色軌跡則是 RTCP 開啟時，控制器控制刀尖點的路徑，在產出加工程式時，直接描述工件表面的座標，這樣的加工程式，可以忽略刀長的變化，以及機台之間的機構差異，可以讓程式更有效率的被使用，也可以避免上述插值的問題，圖 2-13 為 RTCP 之使用範例，未開啟 RTCP 前，直線軸與旋轉軸的動作各自獨立，開啟 RTCP 後，刀尖點的線性移動命令優先，旋轉軸需配合刀尖點來進行轉動。



圖 2-12

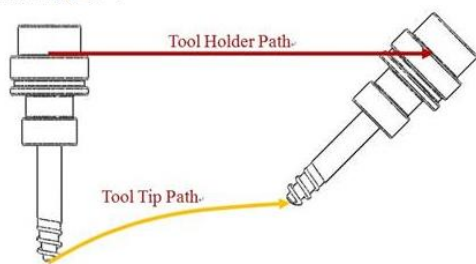
#### 使用範例

未開啟RTCP的程式：

G00 X0 Y0 Z0 B0 C0

G01 X50. Y0 Z0 B-45. C0

機台動作如下：



開啟RTCP的程式：

G43.4 H1

G00 X0 Y0 Z0 B0 C0

G01 X50. Y0 Z0 B-45. C0

機台動作如下：

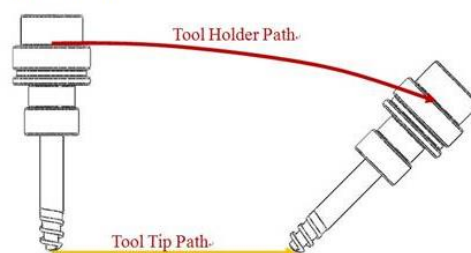


圖 2-13



## 3. 結果與討論

### 3.1 數值解與解析解比較

本文以東台精機股份有限公司所開發的 TMV-710A 立式五軸工具機(A、C 軸工作檯傾斜型)之構型來建構虛擬工具機，本構型在圖 2-8 的 $L_x$ 、 $L_y$ 、 $L_z$ 為(0、0、-20)，經過 2.2.5 章之解析解後處理流程得到的 NC 碼，與該構型在 NX 軟體中對該構型後處理之 NC 碼，以及 2.2.2 章數值解得到的 NC 碼來做比較與驗證。

吾人用 Solidworks 建構一個前基準面為一個正弦方塊對右基準面另一個正弦函數做曲線拉伸的加工件，如圖 3-1

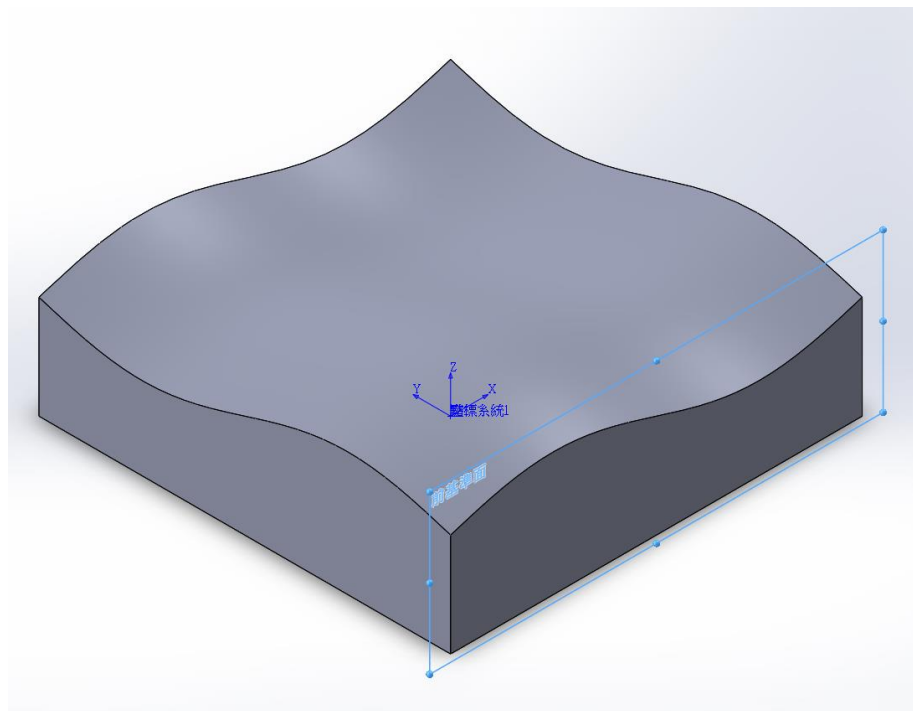


圖 3-1

其中 x 方向之正弦函數為  $z = 20 + 5\sin(\frac{2\pi x}{100})$

y 方向之正弦函數為  $z = 20 + 5\sin(\frac{2\pi y}{100})$

因此 3D 之曲面高度方程式為  $z=20 + 5\sin(\frac{2\pi x}{100})+5\sin(\frac{2\pi y}{100})$

因此只要知道 x、y 的值就可以知道 z 與該點的法向量。

將此加工件匯入 NX 去可設定要求之家工路徑以求 CL 檔與 TMV-710A 此構型之 NC 碼，這裡吾人使用刀軸垂直於驅動體此功能來用曲面之法向量作為加工路徑刀軸之向量，如圖 3-2。

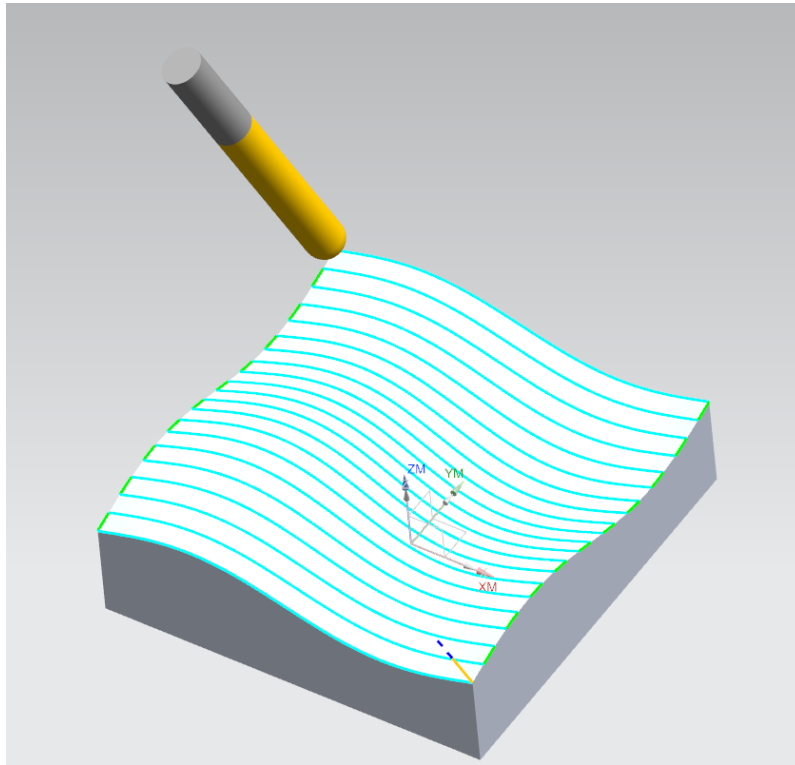


圖 3-2

而本文只探討前三條加工路徑，其完整的 CL 檔、NX 輸出之 NC 檔、本文使用之解析解後處理輸出之 NC 檔以及數值解後處理輸出之 NC 檔將放在附錄以便參考。

以 CL 檔案中的前四行來做比較

```
GOTO/50.0000,-50.0000,25.0000
GOTO/45.1072,-50.0003,23.4884,-0.2745937,-0.2881959,0.9173557
GOTO/40.1766,-50.0000,22.1062,-0.2374081,-0.2911482,0.9267525
GOTO/37.6874,-50.0000,21.5064,-0.2096495,-0.2930564,0.9328263
```

圖 3-3

解析解 NC 碼

X70.710678	Y18.270869	Z21.123902	A23.955018	C315.
X67.147925	Y12.647645	Z21.91806	A23.457486	C316.384526
X62.734816	Y3.436297	Z24.041184	A22.065882	C320.805505
X59.743114	Y-2.523146	Z25.46994	A21.120241	C324.420464

圖 3-4

數值解 NC 碼

x: 70.71068	y: 18.18607	z: -153.83853	a: 23.83692	c: -45.
x: 67.1699	y: 12.9861	z: -153.22086	a: 23.54542	c: -43.87059
x: 62.82324	y: 3.91087	z: -151.12475	a: 22.17472	c: -39.57977
x: 59.77278	y: -2.41825	z: -149.56336	a: 21.14094	c: -35.67048

圖 3-5

### NX 後處理 NC 碼

X70.711	Y18.271	Z21.124	A23.955	C315.
X67.148	Y12.648	Z21.918	A23.457	C316.385
X62.735	Y3.436	Z24.041	A22.066	C320.806
X59.743	Y-2.523	Z25.47	A21.12	C324.42

圖 3-6

以上之比較可以發現 NX 之後處理與解析解之後處理的 NC 碼一致，故可猜測 NX 為使用解析解後處理的方式來處理 NC 碼。值得注意的是，數值解得到的 NC 碼雖然與解析解以及 NX 之 NC 檔不同，但真正需要比較的為該 NC 碼命令機台移動後，刀尖相對於工件之位置，以及刀軸之方向，所以經由同方法之逆向後處理可以得知該 NC 碼所對應的 CL 檔(如圖 3-7)，與後處理前之 CL 檔(圖 3-3)誤差極小，因此該數值解仍為可行之後處理方法。

```
(49.9999999998,-50.0000000000,25.000000000035),(-0.28576646524543,-0.2857664652454,0.9146994340669)
(45.107199999999,-50.000299999999,23.4884000000002),(-0.2768495838193906,-0.2879850218105,0.9167436583647)
(40.1765999999988,-49.9999999999995,22.1061999999989),(-0.24048162071514,-0.29090140070708,0.9260372374613)
(37.687399999998,-50.000000000002,21.5064000000006),(-0.21031104607895,-0.29299720449116,0.9326960394778)
```

圖 3-7

## 3.2 不同插值對誤差的比較

本章的比較也是由同上一章所使用之加工件與加工方法(圖 3-2)，比較方法為將每段 CL 檔做 N 個插值，轉為 NC 檔後將相鄰兩點 NC 檔做平均得到一個”比較 NC 檔”，將”比較 NC 檔”經過逆向後處理轉回 CL 檔，再與計算”比較 NC 檔”所用的 NC 檔所對應的 CL 檔做平均得到的”比較 CL 檔”來做誤差比較(如圖 3-8)。

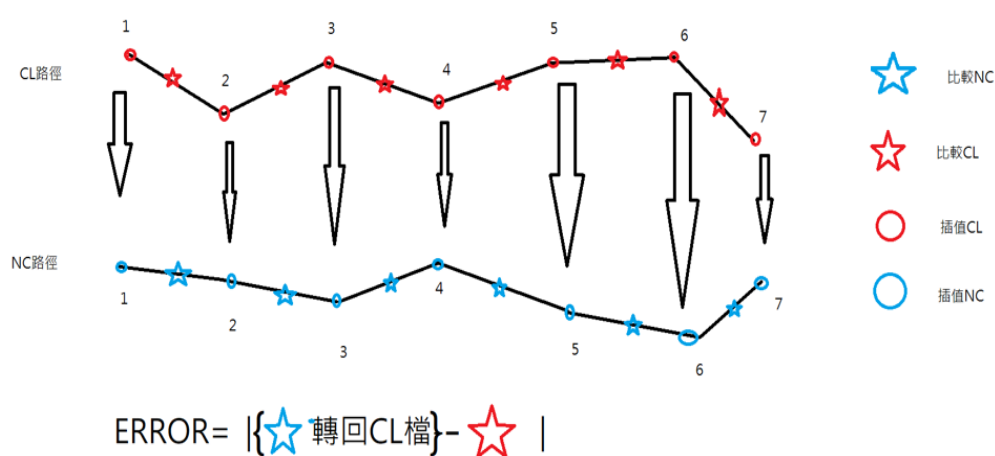


圖 3-8

比較差值數從 1 到 50 與最大加工路徑誤差關係圖(圖 3-9)

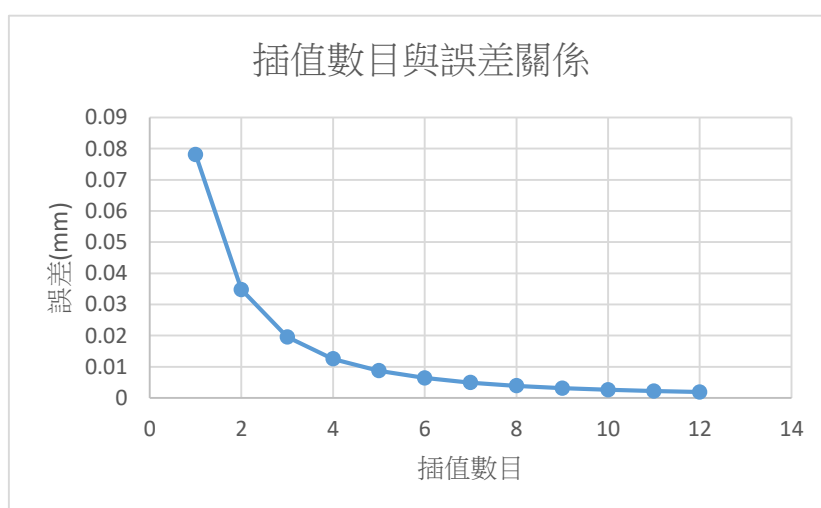
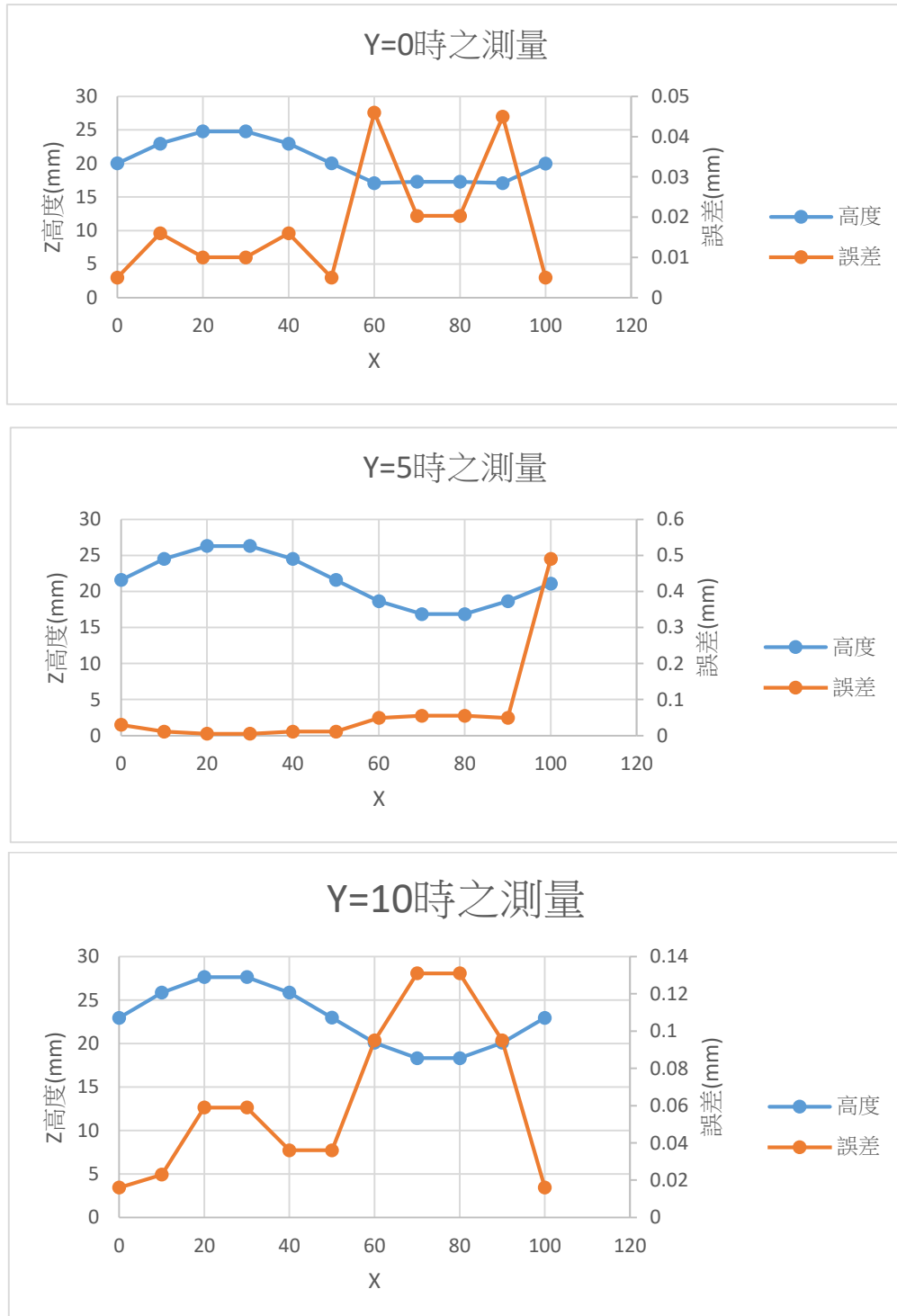


圖 3-9

由此可知若要在虛擬環境中做精度 0.01mm 之加工模擬，差值數目至少要 5 個。

### 3.3 虛擬加工誤差測量

在虛擬環境運用已有的碰撞偵測，可以仿照三次元量床(Coordinate Measuring Machine)測量工件加工後與預期尺寸之誤差。本文製作一把長75mm，尖端0.01mm的虛擬探針，來去測量用3.1章中之加工後的工件。



## 4. 結論與建議

在 3.1 章比較中，可以得知 NX 之後處理與本文所用之解析解後處理輸出的 NC 碼一致，雖然以數值解後處理所得之 NC 碼與前兩個略微不同，但由於加工所須為刀尖與工件之相對位置與角度，將數值解數值解後處理所得之 NC 碼經過逆向後處理可以得到與後處理前的 CL 檔，也就是說雖然機台各軸移動不同，仍可以得到所要求之刀尖與工件之相對位置與角度。從此可之數值解與解析解皆可以得到 TMV-710A 此構型的加工 NC 碼，但在泛用型後處理上，在解析解求解的過程，不同構型之機台需分開討論，因此缺乏一貫性的後處理流程，另外，數值解求解後處理不須求得解析解即可進行後處理，這使得組裝與後處理整合少了一項繁瑣的步驟，可以大幅增加發展銑床模擬程式的效率。

在 3.2 章比較中，可以清楚地發現當差值數目越多，可以越趨近 CL 檔中 GOTO 之線段，在要求 0.01 精度，插值五項即可達到，但這誤差是與 CL 檔線段之比較，與真實曲線還是有所誤差，因為 CL 檔的 GOTO 也是用線段去趨近真實曲線，因此不僅需要把 CL 檔線段作差值，還要將 GOTO 用更短之線段去趨近才能得到更接近真實曲線的加工路徑，不過，這會造成資料數量變得十分龐大，也會造成工具機控制器上在高速加工時的負擔。為解決此問題，許多學者提出使用參數式曲線，像是 B-SPLINE、NURBS，來做更好之曲線趨近，並減少資料的大小，少數控制器廠商也有讀取參數式曲線之指令，像是新代使用 G06.2 來讀取，但參數式曲線之計算相對於線段趨近起來複雜很多，目前能讀取該指令之控制器也是少數，因此在未來這部份來有很大空間之發展。

在 3.3 章，因為目前虛擬加工環境尚未加入測量加工後工件之功能，因此吾人用類似 CMM 三次元量床之方式來做測量，不同的是使用的探針頭並非圓球狀，也不是用曲面法向量做量測，只用與 Z 軸平行之方向來去做量測，加上虛擬環境在模擬高精度加工時因計算龐大會造成電腦之負擔，所以無法做高精度之量測，因此從 3.3 章可得知量測之誤差仍然過大。為解決此問題可以運用高速計算技術，像是 GPU 高速計算，導入目前之虛擬加工環境來得到更高精度的加工，並加入自動量測加工後工件尺寸之功能，直接用加工後工件檔案讀取之方式來得到加工後工件尺寸，避免再工件精度誤差與測量物精度誤差疊合下讓所測量的尺寸誤差更大。

# 5. 附錄

## 5.1 前三行加工路徑之 CL 檔

TOOL PATH/VARIABLE_CONTOUR,TOOL,BALL_MILL	GOTO/-30.1127,-50.0015,29.7435,-0.0948647,-0.2983646,0.9497259
TLDATA/MILL,10.0000,5.0000,75.0000,0.0000,0.0000	GOTO/-32.6542,-50.0015,29.4321,-0.1366219,-0.2969060,0.9450827
MSYS/0.0000,0.0000,0.0000,1.0000000,0.0000000,0.0000000,1.0	GOTO/-35.1798,-50.0005,29.0109,-0.1747600,-0.2951041,0.9393469
000000,0.0000000	GOTO/-37.6875,-50.0000,28.4938,-0.2094767,-0.2930668,0.9328619
\$\$ centerline data	GOTO/-40.1766,-50.0000,27.8937,-0.2375673,-0.2911359,0.9267155
PAINT/PATH	GOTO/-45.1075,-50.0000,26.5126,-0.2747177,-0.2881850,0.9173220
PAINT/SPEED,10	GOTO/-50.0000,-50.0000,25.0000,-0.2870990,-0.2870990,0.9138645
LOAD/TOOL,2	PAINT/COLOR,36
PAINT/COLOR,186	GOTO/-50.0000,-45.1075,26.5126,-0.2870971,-0.2748127,0.9176346
RAPID	PAINT/COLOR,31
GOTO/44.4014,-55.5986,42.8209,-0.2870990,-0.2870990,0.9138645	GOTO/-45.1075,-45.0872,28.0251,-0.2748763,-0.2739806,0.9216168
PAINT/COLOR,211	GOTO/-40.1766,-45.0686,29.4060,-0.2378342,-0.2750865,0.9315376
RAPID	GOTO/-37.6875,-45.0606,30.0061,-0.2097638,-0.2761770,0.9379368
GOTO/47.1290,-52.8710,34.1386	GOTO/-35.1795,-45.0536,30.5215,-0.1750380,-0.2774674,0.9446552
PAINT/COLOR,42	GOTO/-32.6535,-45.0480,30.9396,-0.1368643,-0.2786515,0.9505901
FEDRAT/MMPM,250.0000	GOTO/-30.1122,-45.0438,31.2508,-0.0950463,-0.2796412,0.9553884
GOTO/50.0000,-50.0000,25.0000	GOTO/-27.5593,-45.0412,31.4451,-0.0494398,-0.2803294,0.9586298
PAINT/COLOR,31	GOTO/-25.0000,-45.0403,31.5121,0.0000096,-0.2805898,0.9598278
GOTO/45.1072,-50.0003,23.4884,-0.2745937,-0.2881959,0.9173557	GOTO/-22.4406,-45.0412,31.4453,0.0493238,-0.2803308,0.9586354
GOTO/40.1766,-50.0000,22.1062,-0.2374081,-0.2911482,0.9267525	GOTO/-19.8877,-45.0438,31.2513,0.0949627,-0.2796429,0.9553962
GOTO/37.6874,-50.0000,21.5064,-0.2096495,-0.2930564,0.9328263	GOTO/-17.3464,-45.0480,30.9401,0.1368885,-0.2786499,0.9505871
GOTO/35.1796,-50.0000,20.9905,-0.1748999,-0.2950974,0.9393229	GOTO/-14.8204,-45.0536,30.5218,0.1751701,-0.2774604,0.9446328
GOTO/32.6536,-50.0000,20.5721,-0.1366602,-0.2969053,0.9450774	GOTO/-12.3125,-45.0606,30.0060,0.2099457,-0.2761661,0.9378993
GOTO/30.1123,-50.0000,20.2609,-0.0947925,-0.2983677,0.9497321	GOTO/-9.8234,-45.0686,29.4060,0.2378252,-0.2750872,0.9315397
GOTO/27.5594,-50.0000,20.0669,-0.0492267,-0.2993540,0.9528714	GOTO/-4.8925,-45.0872,28.0250,0.2747613,-0.2739902,0.9216483
GOTO/25.0000,-50.0000,20.0000,0.0000023,-0.2997173,0.9540281	GOTO/0.0000,-45.1075,26.5126,0.2871064,-0.2748119,0.9176319
GOTO/22.4407,-50.0000,20.0669,0.0492272,-0.2993539,0.9528714	GOTO/4.8926,-45.1278,25.0003,0.2744401,-0.2777567,0.9206160
GOTO/19.8878,-50.0000,20.2609,0.0947899,-0.2983678,0.9497324	GOTO/9.8235,-45.1464,23.6193,0.2372722,-0.2823552,0.9295039
GOTO/17.3464,-50.0000,20.5721,0.1366558,-0.2969055,0.9450779	GOTO/12.3126,-45.1545,23.0193,0.2093419,-0.2849896,0.9353913
GOTO/14.8205,-50.0000,20.9905,0.1748949,-0.2950977,0.9393238	GOTO/14.8205,-45.1614,22.5035,0.1745995,-0.2876440,0.9416878
GOTO/12.3126,-50.0000,21.5063,0.2096454,-0.2930567,0.9328272	GOTO/17.3464,-45.1670,22.0851,0.1363971,-0.2899528,0.9472715
GOTO/9.8236,-50.0001,22.1068,0.2375525,-0.2911376,0.9267188	GOTO/19.8878,-45.1712,21.7740,0.0945957,-0.2917893,0.9517934
GOTO/4.8928,-50.0002,23.4882,0.2746055,-0.2881949,0.9173524	GOTO/22.4407,-45.1738,21.5799,0.0491214,-0.2930091,0.9548470
GOTO/0.0000,-50.0000,25.0000,0.2871083,-0.2870982,0.9138618	GOTO/25.0000,-45.1747,21.5131,0.0000023,-0.2934528,0.9559736
GOTO/-4.8925,-50.0000,26.5125,0.2746028,-0.2881949,0.9173533	GOTO/27.5594,-45.1738,21.5799,-0.0491209,-0.2930091,0.9548470
GOTO/-9.8234,-50.0000,27.8936,0.2375583,-0.2911366,0.9267176	GOTO/30.1123,-45.1712,21.7740,-0.0945982,-0.2917892,0.9517932
GOTO/-12.3125,-50.0000,28.4937,0.2096583,-0.2930552,0.9328248	GOTO/32.6536,-45.1670,22.0851,-0.1364015,-0.2899526,0.9472709
GOTO/-14.8201,-50.0005,29.0110,0.1748919,-0.2950970,0.9393245	GOTO/35.1796,-45.1614,22.5035,-0.1746045,-0.2876437,0.9416870
GOTO/-17.3457,-50.0014,29.4322,0.1366461,-0.2969050,0.9450795	GOTO/37.6874,-45.1545,23.0193,-0.2093461,-0.2849893,0.9353905
GOTO/-19.8872,-50.0014,29.7436,0.0947813,-0.2983670,0.9497335	GOTO/40.1766,-45.1464,23.6191,-0.2371279,-0.2823656,0.9295375
GOTO/-22.4405,-50.0006,29.9349,0.0492251,-0.2993529,0.9528718	GOTO/45.1075,-45.1278,25.0002,-0.2744283,-0.2777578,0.9206192
GOTO/-25.0000,-50.0000,29.9999,0.0000096,-0.2997163,0.9540284	GOTO/50.0000,-45.1075,26.5126,-0.2870971,-0.2748127,0.9176346
GOTO/-27.5594,-50.0006,29.9349,-0.0493409,-0.2993512,0.9528664	PAINT/COLOR,36

GOTO/50.0000,-40.1766,27.8937,-0.2871092,-0.2379072,0.9278839

PAINT/COLOR,31

GOTO/45.1075,-40.2571,26.3832,-0.2742280,-0.2431946,0.9304060

GOTO/40.1766,-40.3307,25.0039,-0.2367696,-0.2498239,0.9388973

GOTO/37.6874,-40.3626,24.4050,-0.2089520,-0.2532968,0.9445527

GOTO/35.1796,-40.3901,23.8898,-0.1742164,-0.2566616,0.9506700

GOTO/32.6536,-40.4124,23.4721,-0.1360588,-0.2595479,0.9560977

GOTO/30.1123,-40.4289,23.1613,-0.0943392,-0.2618125,0.9604969

GOTO/27.5594,-40.4393,22.9675,-0.0489792,-0.2632963,0.9634709

GOTO/25.0000,-40.4428,22.9008,0.0000023,-0.2638293,0.9645694

GOTO/22.4407,-40.4393,22.9675,0.0489797,-0.2632962,0.9634709

GOTO/19.8878,-40.4289,23.1613,0.0943366,-0.2618125,0.9604972

GOTO/17.3464,-40.4124,23.4720,0.1360544,-0.2595481,0.9560983

GOTO/14.8205,-40.3901,23.8898,0.1742114,-0.2566619,0.9506709

GOTO/12.3126,-40.3626,24.4049,0.2089478,-0.2532971,0.9445535

GOTO/9.8235,-40.3307,25.0041,0.2369137,-0.2498143,0.9388635

GOTO/4.8926,-40.2571,26.3833,0.2742398,-0.2431934,0.9304029

GOTO/0.0000,-40.1766,27.8936,0.2871185,-0.2379066,0.9278812

GOTO/-4.8925,-40.0960,29.4040,0.2749718,-0.2345603,0.9324012

GOTO/-9.8234,-40.0225,30.7832,0.2381618,-0.2331454,0.9428267

GOTO/-12.3125,-39.9905,31.3824,0.2103030,-0.2330525,0.9494520

GOTO/-14.8204,-39.9630,31.8975,0.1755123,-0.2332849,0.9564380

GOTO/-17.3464,-39.9408,32.3153,0.1371843,-0.2335914,0.9626087

GOTO/-19.8877,-39.9242,32.6260,0.0951828,-0.2339100,0.9675879

GOTO/-22.4406,-39.9138,32.8197,0.0494430,-0.2341662,0.9709385

GOTO/-25.0000,-39.9103,32.8865,0.0000096,-0.2342728,0.9721709

GOTO/-27.5593,-39.9139,32.8195,-0.0495593,-0.2341653,0.9709328

GOTO/-30.1122,-39.9242,32.6255,-0.0952666,-0.2339094,0.9675798

GOTO/-32.6535,-39.9408,32.3147,-0.1371600,-0.2335937,0.9626116

GOTO/-35.1795,-39.9631,31.8971,-0.1753799,-0.2332914,0.9564607

GOTO/-37.6875,-39.9905,31.3825,-0.2101208,-0.2330616,0.9494901

GOTO/-40.1766,-40.0225,30.7832,-0.2381709,-0.2331447,0.9428246

GOTO/-45.1075,-40.0960,29.4042,-0.2750869,-0.2345518,0.9323694

GOTO/-50.0000,-40.1766,27.8937,-0.2871092,-0.2379072,0.9278839

PAINT/COLOR,36

GOTO/-50.0119,-37.6867,28.4903,-0.2872523,-0.2066629,0.9352949

GOTO/-50.0000,-35.1795,29.0092,-0.2870992,-0.1752055,0.9417415



## 5.2 前三行加工路徑之解析解後處理 NC 碼

X70.711	Y18.271	Z21.124	A23.955	C315	X-19.317562	Y-32.466015	Z43.305708	A16.538273	C349.997985
X70.710678	Y18.27087	Z40.624495	A23.955018	C315.	X-25.001541	Y-28.776345	Z42.080351	A16.295405	C0.00196
X70.710678	Y18.270838	Z31.123867	A23.955018	C315.	X-29.906147	Y-24.15383	Z40.836864	A16.537146	C9.97897
X70.710678	Y18.270869	Z21.123902	A23.955018	C315.	X-33.315387	Y-19.503631	Z39.672889	A17.177153	C18.756747
X67.147925	Y12.647645	Z21.91806	A23.457486	C316.384526	X-35.431918	Y-15.349408	Z38.601097	A18.086833	C26.162866
X62.734816	Y3.436297	Z24.041184	A22.065882	C320.805505	X-36.583498	Y-11.935814	Z37.62905	A19.155274	C32.265598
X59.743114	Y-2.523146	Z25.46994	A21.120241	C324.420464	X-37.072041	Y-9.30801	Z36.759846	A20.298288	C37.242653
X55.756553	Y-9.493415	Z27.105278	A20.061845	C329.3454	X-36.906703	Y-7.808786	Z36.085193	A21.323888	C40.844882
X50.568162	Y-16.761068	Z28.726589	A19.077489	C335.28423	X-35.380888	Y-7.514278	Z35.271341	A22.831746	C45.080511
X43.838238	Y-23.99386	Z30.301036	A18.243966	C342.374759	X-32.585885	Y-10.135822	Z35.077524	A23.417699	C46.253404
X35.307357	Y-30.595754	Z31.789646	A17.660397	C350.66168	X-28.237636	Y-15.147465	Z35.305272	A22.983696	C44.655875
X24.999616	Y-35.712901	Z33.14704	A17.440617	C0.00044	X-21.52387	Y-21.913596	Z35.622471	A21.642386	C40.041421
X14.030023	Y-38.326619	Z34.250993	A17.660397	C9.338416	X-16.808611	Y-25.646262	Z35.685986	A20.708546	C36.299507
X3.815155	Y-38.372371	Z35.040625	A18.243911	C17.624782	X-10.76452	Y-29.294515	Z35.603087	A19.66304	C31.257691
X-5.147847	Y-36.518866	Z35.559563	A19.077401	C24.715055	X-3.529641	Y-32.224701	Z35.328306	A18.689056	C25.192828
X-12.742983	Y-33.439991	Z35.850261	A20.061694	C30.653856	X4.98809	Y-33.921931	Z34.821989	A17.862867	C17.962269
X-19.077217	Y-29.66093	Z35.95232	A21.120098	C35.578978	X14.662934	Y-33.729867	Z34.041093	A17.283384	C9.516832
X-23.998654	Y-25.83492	Z35.911691	A22.071021	C39.212581	X24.999646	Y-31.003877	Z32.942122	A17.064777	C0.000449
X-30.949494	Y-18.991539	Z35.647402	A23.457961	C43.616803	X34.648952	Y-25.836313	Z31.585035	A17.283384	C350.483263
X-35.355961	Y-14.038183	Z35.478694	A23.955399	C45.001008	X42.57526	Y-19.245343	Z30.092105	A17.862904	C342.037281
X-38.033454	Y-11.595479	Z35.734643	A23.457831	C43.616521	X48.774	Y-12.062959	Z28.508278	A18.689163	C334.806445
X-39.221642	Y-12.149139	Z36.607043	A22.071204	C39.213362	X53.506985	Y-4.862165	Z26.872868	A19.663176	C328.741554
X-39.106219	Y-13.776598	Z37.307465	A21.120479	C35.580785	X57.105421	Y2.042253	Z25.218682	A20.708675	C323.699916
X-38.241724	Y-16.494148	Z38.200319	A20.061577	C30.653485	X59.800152	Y7.964149	Z23.766387	A21.637166	C319.976785
X-36.661675	Y-19.917065	Z39.192802	A19.077121	C24.713547	X63.804746	Y17.203455	Z21.583872	A22.983227	C315.34547
X-34.092164	Y-23.968212	Z40.276991	A18.24371	C17.623326	X67.159479	Y23.007911	Z20.72283	A23.41731	C313.747607
X-30.256182	Y-28.394299	Z41.444752	A17.660322	C9.338056	X62.838186	Y29.795796	Z19.642637	A21.89268	C309.646153
X-25.001602	Y-32.714875	Z42.686896	A17.440559	C0.001835	X60.048275	Y23.548522	Z20.575777	A21.501808	C311.567689
X-19.060811	Y-36.13062	Z43.90883	A17.661342	C350.640313	X56.90386	Y13.954549	Z22.817016	A20.132811	C316.536759
X-13.546539	Y-38.346992	Z45.017997	A18.245101	C342.361994	X54.756824	Y7.824142	Z24.291722	A19.169256	C320.479773
X-8.762709	Y-39.673252	Z46.024444	A19.07656	C335.290381	X51.791303	Y0.627607	Z25.962441	A18.071528	C325.832179
X-4.792321	Y-40.442453	Z46.941604	A20.057836	C329.366076	X47.683784	Y-6.986721	Z27.609722	A17.04053	C332.335815
X-1.585413	Y-40.921131	Z47.786015	A21.114579	C324.443779	X42.034498	Y-14.716456	Z29.200318	A16.158214	C340.184329
X0.483055	Y-41.442717	Z48.48528	A22.071524	C320.785507	X34.490358	Y-21.941599	Z30.695611	A15.534171	C349.462112
X1.850024	Y-43.23041	Z49.468105	A23.462336	C316.370525	X24.999647	Y-27.691612	Z32.05085	A15.297398	C0.000499
X0.	Y-46.34911	Z49.833803	A23.955018	C315.	X14.666366	Y-30.751896	Z33.144583	A15.534171	C10.537998
X-1.988809	Y-43.281357	Z49.432538	A23.41731	C313.747607	X5.005394	Y-30.996699	Z33.917243	A16.158152	C19.815168
X0.089726	Y-40.139565	Z49.01275	A22.836397	C314.906497	X-3.398986	Y-29.182164	Z34.412523	A17.040412	C27.663405
X-0.916239	Y-38.270382	Z47.976681	A21.324219	C319.153973	X-10.420835	Y-26.068449	Z34.673249	A18.071362	C34.167026
X-2.757557	Y-37.694576	Z47.252734	A20.292094	C322.78236	X-16.186418	Y-22.229518	Z34.739229	A19.169116	C39.519629
X-5.715556	Y-37.15286	Z46.38406	A19.151362	C327.754563	X-20.624631	Y-18.326687	Z34.655216	A20.138436	C43.481746
X-9.449169	Y-36.30635	Z45.444468	A18.08628	C333.841273	X-26.873712	Y-11.25566	Z34.287161	A21.502293	C48.433675
X-14.015008	Y-34.866091	Z44.422576	A17.178666	C341.22779	X-30.936403	Y-5.926866	Z33.997846	A21.893095	C50.354829

X-33.680171	Y-2.936329	Z34.123978	A21.187734	C49.534693
X-35.471648	Y-2.853094	Z34.87126	A19.468185	C45.60981
X-35.932289	Y-4.227456	Z35.515655	A18.29516	C42.06261
X-35.868776	Y-6.870554	Z36.358341	A16.973869	C36.956037
X-35.184098	Y-10.52496	Z37.309337	A15.717574	C30.425
X-33.468815	Y-15.238393	Z38.365984	A14.62754	C22.142421
X-30.202294	Y-20.775265	Z39.521613	A13.846948	C11.922592
X-25.001635	Y-26.408768	Z40.764374	A13.54876	C0.002348
X-18.697657	Y-30.81187	Z41.996454	A13.848313	C348.050124
X-12.828687	Y-33.474971	Z43.126703	A14.629377	C337.839919
X-7.934617	Y-34.898874	Z44.167413	A15.716961	C329.579679
X-4.105891	Y-35.624906	Z45.130356	A16.969413	C323.0655
X-1.21312	Y-36.038828	Z46.026361	A18.288204	C317.963202
X0.495766	Y-36.539506	Z46.779576	A19.468546	C314.38901
X1.244344	Y-38.398525	Z47.876032	A21.192774	C310.452443
X-0.966259	Y-41.651221	Z48.35355	A21.89268	C309.646153
X1.384655	Y-41.396212	Z47.507207	A20.72416	C305.733027
X3.983294	Y-40.968237	Z46.672602	A19.653894	C301.394097

### 5.3 前三行加工路徑之數值解後處理 NC 碼

x: 70.71068	y: 18.14587	z: -134.33797	a: 23.83692	c: -45	x: -24.50313	y: -29.03883	z: -132.8432	a: 16.29506	c: -0.63015
x: 70.71068	y: 18.16542	z: -143.83858	a: 23.83692	c: -45	x: -29.74416	y: -24.28146	z: -134.13454	a: 16.52457	c: 9.74998
x: 70.71068	y: 18.18607	z: -153.83853	a: 23.83692	c: -45	x: -32.98059	y: -19.84909	z: -135.25508	a: 17.12515	c: 18.22989
x: 67.1699	y: 12.9861	z: -153.22086	a: 23.54542	c: -43.87059	x: -35.34006	y: -15.47063	z: -136.37531	a: 18.06034	c: 26.00256
x: 62.82324	y: 3.91087	z: -151.12475	a: 22.17472	c: -39.57977	x: -36.58535	y: -11.93479	z: -137.37191	a: 19.15419	c: 32.26911
x: 59.77278	y: -2.41825	z: -149.56336	a: 21.14094	c: -35.67048	x: -36.92675	y: -9.56078	z: -138.18748	a: 20.2217	c: 36.95071
x: 55.75765	y: -9.49188	z: -147.89571	a: 20.06093	c: -30.65711	x: -36.90827	y: -7.80768	z: -138.91569	a: 21.32302	c: 40.84814
x: 50.78467	y: -16.38684	z: -146.37139	a: 19.13171	c: -25.10842	x: -35.33571	y: -7.6022	z: -139.71178	a: 22.79436	c: 44.98936
x: 43.95743	y: -23.8521	z: -144.73558	a: 18.2583	c: -17.80277	x: -32.43718	y: -10.41333	z: -139.88648	a: 23.27674	c: 45.98091
x: 35.72403	y: -30.25787	z: -143.29766	a: 17.68525	c: -9.8724	x: -28.36047	y: -15.00791	z: -139.71954	a: 23.03489	c: 44.85418
x: 25.19289	y: -35.62152	z: -141.8829	a: 17.43926	c: -0.22125	x: -21.81	y: -21.67117	z: -139.39401	a: 21.74671	c: 40.44317
x: 14.56047	y: -38.21647	z: -140.81111	a: 17.63246	c: 8.76397	x: -16.88035	y: -25.60061	z: -139.31471	a: 20.72888	c: 36.39364
x: 3.98998	y: -38.37839	z: -139.97597	a: 18.22508	c: 17.43814	x: -10.76661	y: -29.29497	z: -139.39756	a: 19.6621	c: 31.26028
x: -5.151	y: -36.51999	z: -139.44147	a: 19.07594	c: 24.71848	x: -3.86726	y: -32.14864	z: -139.65002	a: 18.74242	c: 25.59381
x: -12.43304	y: -33.57934	z: -139.16349	a: 19.99304	c: 30.30296	x: 4.83259	y: -33.92325	z: -140.1649	a: 17.87695	c: 18.14369
x: -18.98759	y: -29.72115	z: -139.04915	a: 21.09249	c: 35.47166	x: 14.2036	y: -33.83783	z: -140.90375	a: 17.30776	c: 10.06136
x: -23.72199	y: -26.06979	z: -139.07926	a: 21.96963	c: 38.86051	x: 24.82164	y: -31.099	z: -142.02992	a: 17.06328	c: 0.22598
x: -30.93952	y: -19.00504	z: -139.35166	a: 23.45143	c: 43.60236	x: 34.23839	y: -26.19782	z: -143.32324	a: 17.25525	c: -8.93117
x: -35.18921	y: -14.28753	z: -139.47896	a: 23.85463	c: 44.73141	x: 42.46327	y: -19.3961	z: -144.871	a: 17.84406	c: -17.77261
x: -38.03451	y: -11.5949	z: -139.26596	a: 23.45727	c: 43.61837	x: 48.77567	y: -12.06134	z: -146.493	a: 18.68769	c: -25.19711
x: -39.28527	y: -12.04783	z: -138.41543	a: 22.10166	c: 39.32557	x: 53.37867	y: -5.23283	z: -148.02087	a: 19.59495	c: -30.90014
x: -39.24546	y: -13.56786	z: -137.73794	a: 21.17699	c: 35.81951	x: 57.07838	y: 1.91851	z: -149.74178	a: 20.68135	c: -36.19048
x: -38.24328	y: -16.49351	z: -136.80052	a: 20.06066	c: 30.656	x: 59.76584	y: 7.70188	z: -151.1399	a: 21.57598	c: -39.80109
x: -36.92253	y: -19.62267	z: -135.87105	a: 19.13136	c: 25.10641	x: 63.801	y: 16.75149	z: -153.2263	a: 22.86706	c: -44.29625
x: -34.22145	y: -23.8522	z: -134.75026	a: 18.25811	c: 17.80148	x: 67.16513	y: 22.92271	z: -154.23846	a: 23.3977	c: -46.18615
x: -30.68122	y: -28.09678	z: -133.62929	a: 17.68519	c: 9.87264	x: 62.88059	y: 29.6455	z: -155.31194	a: 21.95546	c: -50.16347
x: -25.19498	y: -32.62366	z: -132.343	a: 17.43921	c: 0.22365	x: 60.00884	y: 23.89717	z: -154.56998	a: 21.56245	c: -48.74606
x: -19.60089	y: -35.97671	z: -131.16775	a: 17.63327	c: -8.78366	x: 56.90455	y: 13.9806	z: -152.1924	a: 20.13714	c: -43.4877
x: -13.73185	y: -38.32613	z: -130.00858	a: 18.22621	c: -17.45092	x: 54.7888	y: 8.10353	z: -150.79815	a: 19.22631	c: -39.78089
x: -8.75919	y: -39.67541	z: -128.97639	a: 19.07511	c: -24.71303	x: 51.79206	y: 0.62955	z: -149.03844	a: 18.07055	c: -34.171
x: -5.16501	y: -40.49384	z: -128.1172	a: 19.98934	c: -30.28348	x: 47.8387	y: -6.59402	z: -147.48978	a: 17.09697	c: -28.09819
x: -1.70273	y: -40.9509	z: -127.23481	a: 21.08699	c: -35.44883	x: 42.03631	y: -14.71537	z: -145.80091	a: 16.15642	c: -19.81941
x: 0.08637	y: -41.56629	z: -126.588	a: 21.96945	c: -38.86014	x: 34.85303	y: -21.56787	z: -144.39213	a: 15.56012	c: -11.13959
x: 1.83301	y: -43.23877	z: -125.53665	a: 23.45579	c: -43.615	x: 25.17625	y: -27.58744	z: -142.97896	a: 15.29559	c: -0.25004
x: -0.32949	y: -46.46996	z: -125.24733	a: 23.85523	c: -44.73302	x: 15.15955	y: -30.6186	z: -141.91688	a: 15.50334	c: 9.89253
x: -2.05635	y: -43.25238	z: -125.55137	a: 23.43968	c: -46.1949	x: 5.16706	y: -30.99821	z: -141.09888	a: 16.13779	c: 19.60826
x: 0.37968	y: -39.98677	z: -125.89959	a: 22.96235	c: -45.35399	x: -3.40244	y: -29.18338	z: -140.58835	a: 17.03886	c: 27.66792
x: -0.89406	y: -38.2646	z: -127.01977	a: 21.32935	c: -40.86708	x: -10.14354	y: -26.20218	z: -140.33853	a: 17.99922	c: 33.78672
x: -2.35888	y: -37.59317	z: -127.67538	a: 20.39232	c: -37.60686	x: -16.10803	y: -22.28762	z: -140.26128	a: 19.1404	c: 39.40443
x: -5.58888	y: -37.13683	z: -128.59619	a: 19.17546	c: -32.37304	x: -20.47685	y: -18.46672	z: -140.33635	a: 20.07454	c: 43.24697
x: -9.44591	y: -36.30831	z: -129.55615	a: 18.08504	c: -26.16213	x: -26.87477	y: -11.2553	z: -140.71329	a: 21.50175	c: 48.43568
x: -13.56853	y: -34.92621	z: -130.51444	a: 17.22502	c: -19.26043	x: -30.91698	y: -5.958	z: -140.99446	a: 21.88311	c: 50.31144
x: -19.13313	y: -32.52472	z: -131.66842	a: 16.54769	c: -10.21689	x: -33.69492	y: -2.88709	z: -140.88255	a: 21.21786	c: 49.57261

x: -35.53955	y: -2.67589	z: -140.16376	a: 19.53981	c: 45.79578
x: -35.93395	y: -4.22567	z: -139.48529	a: 18.29426	c: 42.06706
x: -36.00771	y: -6.58585	z: -138.69629	a: 17.05152	c: 37.30343
x: -35.2611	y: -10.39745	z: -137.71472	a: 15.74312	c: 30.59732
x: -33.47174	y: -15.23709	z: -136.63535	a: 14.62566	c: 22.1481
x: -30.60428	y: -20.39306	z: -135.55159	a: 13.88127	c: 12.59529
x: -25.19977	y: -26.28898	z: -134.26554	a: 13.5473	c: 0.28724
x: -19.26326	y: -30.6185	z: -133.08095	a: 13.81117	c: -11.22385
x: -13.01685	y: -33.4533	z: -131.90033	a: 14.60483	c: -21.93691
x: -7.92918	y: -34.9014	z: -130.83329	a: 15.71543	c: -30.42643
x: -4.4517	y: -35.69541	z: -129.931	a: 16.88388	c: -36.56115
x: -1.31591	y: -36.07522	z: -128.99549	a: 18.25467	c: -41.92959
x: 0.16007	y: -36.68585	z: -128.29906	a: 19.34448	c: -45.27182
x: 1.23187	y: -38.40781	z: -127.12899	a: 21.18514	c: -49.53572
x: -1.01973	y: -41.70316	z: -126.6789	a: 21.84849	c: -50.30608

## 5.4 前三行加工路徑之 NX 後處理 NC 碼

X70.711 Y18.271 Z21.124 A23.955 C315.	X-33.315 Y-19.504 Z39.673 A17.177 C18.757
X67.148 Y12.648 Z21.918 A23.457 C316.385	X-35.432 Y-15.349 Z38.601 A18.087 C26.163
X62.735 Y3.436 Z24.041 A22.066 C320.806	X-36.584 Y-11.936 Z37.629 A19.155 C32.266
X59.743 Y-2.523 Z25.47 A21.12 C324.42	X-37.072 Y-9.308 Z36.76 A20.298 C37.243
X55.757 Y-9.493 Z27.105 A20.062 C329.345	X-36.907 Y-7.809 Z36.085 A21.324 C40.845
X50.568 Y-16.761 Z28.727 A19.077 C335.284	X-35.381 Y-7.514 Z35.271 A22.832 C45.081
X43.838 Y-23.994 Z30.301 A18.244 C342.375	X-32.586 Y-10.136 Z35.078 A23.418 C46.253
X35.307 Y-30.596 Z31.79 A17.66 C350.662	X-28.238 Y-15.147 Z35.305 A22.984 C44.656
X25. Y-35.713 Z33.147 A17.441 C0.0	X-21.524 Y-21.914 Z35.622 A21.642 C40.041
X14.03 Y-38.327 Z34.251 A17.66 C9.338	X-16.809 Y-25.646 Z35.686 A20.709 C36.3
X3.815 Y-38.372 Z35.041 A18.244 C17.625	X-10.765 Y-29.295 Z35.603 A19.663 C31.258
X-5.148 Y-36.519 Z35.56 A19.077 C24.715	X-3.53 Y-32.225 Z35.328 A18.689 C25.193
X-12.743 Y-33.44 Z35.85 A20.062 C30.654	X4.988 Y-33.922 Z34.822 A17.863 C17.962
X-19.077 Y-29.661 Z35.952 A21.12 C35.579	X14.663 Y-33.73 Z34.041 A17.283 C9.517
X-23.999 Y-25.835 Z35.912 A22.071 C39.213	X25. Y-31.004 Z32.942 A17.065 C0.0
X-30.95 Y-18.992 Z35.647 A23.458 C43.617	X34.649 Y-25.836 Z31.585 A17.283 C350.483
X-35.356 Y-14.038 Z35.479 A23.955 C45.001	X42.575 Y-19.245 Z30.092 A17.863 C342.037
X-38.033 Y-11.595 Z35.735 A23.458 C43.617	X48.774 Y-12.063 Z28.508 A18.689 C334.806
X-39.222 Y-12.149 Z36.607 A22.071 C39.213	X53.507 Y-4.862 Z26.873 A19.663 C328.742
X-39.106 Y-13.777 Z37.307 A21.12 C35.581	X57.105 Y2.042 Z25.219 A20.709 C323.7
X-38.242 Y-16.494 Z38.2 A20.062 C30.653	X59.8 Y7.964 Z23.766 A21.637 C319.977
X-36.662 Y-19.917 Z39.193 A19.077 C24.714	X63.805 Y17.203 Z21.584 A22.983 C315.345
X-34.092 Y-23.968 Z40.277 A18.244 C17.623	X67.159 Y23.008 Z20.723 A23.417 C313.748
X-30.256 Y-28.394 Z41.445 A17.66 C9.338	X62.838 Y29.796 Z19.643 A21.893 C309.646
X-25.002 Y-32.715 Z42.687 A17.441 C.002	X60.048 Y23.548 Z20.576 A21.502 C311.568
X-19.061 Y-36.131 Z43.909 A17.661 C350.64	X56.904 Y13.955 Z22.817 A20.133 C316.537
X-13.547 Y-38.347 Z45.018 A18.245 C342.362	X54.757 Y7.824 Z24.292 A19.169 C320.48
X-8.763 Y-39.673 Z46.024 A19.077 C335.29	X51.791 Y.628 Z25.962 A18.072 C325.832
X-4.792 Y-40.442 Z46.942 A20.058 C329.366	X47.684 Y-6.987 Z27.61 A17.041 C332.336
X-1.585 Y-40.921 Z47.786 A21.115 C324.444	X42.035 Y-14.717 Z29.2 A16.158 C340.184
X.483 Y-41.443 Z48.485 A22.072 C320.786	X34.49 Y-21.942 Z30.696 A15.534 C349.462
X1.85 Y-43.23 Z49.468 A23.462 C316.371	X25. Y-27.692 Z32.051 A15.297 C.001
X0.0 Y-46.349 Z49.834 A23.955 C315.	X14.666 Y-30.752 Z33.145 A15.534 C10.538
X-1.989 Y-43.281 Z49.433 A23.417 C313.748	X5.005 Y-30.997 Z33.917 A16.158 C19.815
X.09 Y-40.14 Z49.013 A22.836 C314.906	X-3.399 Y-29.182 Z34.413 A17.04 C27.663
X-.916 Y-38.27 Z47.977 A21.324 C319.154	X-10.421 Y-26.068 Z34.673 A18.071 C34.167
X-2.758 Y-37.695 Z47.253 A20.292 C322.782	X-16.186 Y-22.23 Z34.739 A19.169 C39.52
X-5.716 Y-37.153 Z46.384 A19.151 C327.755	X-20.625 Y-18.327 Z34.655 A20.138 C43.482
X-9.449 Y-36.306 Z45.444 A18.086 C333.841	X-26.874 Y-11.256 Z34.287 A21.502 C48.434
X-14.015 Y-34.866 Z44.423 A17.179 C341.228	X-30.936 Y-5.927 Z33.998 A21.893 C50.355
X-19.318 Y-32.466 Z43.306 A16.538 C349.998	X-33.68 Y-2.936 Z34.124 A21.188 C49.535
X-25.002 Y-28.776 Z42.08 A16.295 C.002	X-35.472 Y-2.853 Z34.871 A19.468 C45.61
X-29.906 Y-24.154 Z40.837 A16.537 C9.979	X-35.932 Y-4.227 Z35.516 A18.295 C42.063

X-35.869 Y-6.871 Z36.358 A16.974 C36.956  
X-35.184 Y-10.525 Z37.309 A15.718 C30.425  
X-33.469 Y-15.238 Z38.366 A14.628 C22.142  
X-30.202 Y-20.775 Z39.522 A13.847 C11.923  
X-25.002 Y-26.409 Z40.764 A13.549 C.002  
X-18.698 Y-30.812 Z41.996 A13.848 C348.05  
X-12.829 Y-33.475 Z43.127 A14.629 C337.84  
X-7.935 Y-34.899 Z44.167 A15.717 C329.58  
X-4.106 Y-35.625 Z45.13 A16.969 C323.065  
X-1.213 Y-36.039 Z46.026 A18.288 C317.963  
X.496 Y-36.539 Z46.78 A19.469 C314.389  
X1.244 Y-38.399 Z47.876 A21.193 C310.452  
X-.966 Y-41.651 Z48.354 A21.893 C309.646  
X1.385 Y-41.396 Z47.507 A20.724 C305.733  
X3.983 Y-40.968 Z46.673 A19.654 C301.394

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