

PRACTICE MIDTERM III

ECON 103, STATISTICS FOR ECONOMISTS

Graphing calculators, notes, and text-books are not permitted.

I pledge that, in taking and preparing for this exam, I have abided by the University of Pennsylvania's Code of Academic Integrity. I am aware that any violations of the code will result in a failing grade for this course.

Name: _____

Signature: _____

Student ID #: _____ Recitation #: _____

Instructions: Answer all questions in the space provided, continuing on the back of the page if you run out of space. Show your work for full credit but be aware that writing down irrelevant information will not gain you points. Be sure to sign the academic integrity statement above and to write your name and student ID number on *each page* in the space provided. Make sure that you have all pages of the exam before starting.

Warning: If you continue writing after we call time, even if this is only to fill in your name, twenty-five points will be deducted from your final score. In addition, two points will be deducted for each page on which you do not write your name and student ID.

1. Consider a dataset of n observations x_1, x_2, \dots, x_n with sample mean \bar{x} and sample variance s_x^2 . Let z_i denote the sample z-score corresponding to the observation x_i .

(a) Write down the formula for \bar{x} .

(b) Write down the formula for s_x^2 .

(c) Write down the formula for z_i .

(d) Prove that the sample mean of the z-scores is zero.

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2. In this question you will analyze a dataset containing *last semester's* final exam scores and math diagnostic test scores. Both scores are given in points out of 100. To answer the questions given below, you will need to consult the following table of sample statistics for the dataset:

	Diagnostic	Final Exam
1st Quartile	58	51
Median	68	66
Mean	68	65
3rd Quartile	80	78
Std. Dev.	16	17
Covariance	124	

- (a) As you can see from the table, the first quartile for the diagnostic test was 58. Briefly explain what this means in terms that someone who has never taken Econ 103 would understand.
- (b) Is there any evidence of skewness in the math diagnostic or final exam scores? Explain briefly.
- (c) Were scores more variable on the final or the math diagnostic? Briefly discuss in terms of both the standard deviation and interquartile range.
- (d) Calculate the sample correlation between scores on the math diagnostic test and those on the final exam.

3. Let A be the event that it rains this Saturday, B be the event that it rains this Sunday and C be the event that it rains this weekend. In her weather forecast Molly, the local meteorologist, tells us that $P(A) = 0.5$ and $P(B) = 0.5$.
- (a) Express the event C in terms of the events A and B using set operations.
- (b) In this example, what is the meaning of the event $A \cap B$? Phrase it in a way that someone who has never taken Econ 103 would understand.
- (c) Express $P(C)$ in terms of $P(A \cap B)$ using the addition rule.
- (d) Adam, an anchorman for the local news, sees Molly's forecast and summarizes it as follows: "According to Molly we're in for a wet weekend. There's a 100% chance of rain this weekend: 50% on Saturday and 50% on Sunday." Is Adam correct? If so, briefly explain why; if not, point out the flaw in his reasoning.

4. On my desk I have 10 cups: N_B of them are *Blue Cups* and the remaining $10 - N_B$ are *Red Cups*. Each cup contains five balls: *Blue Cups* contain 4 blue balls and 1 red ball while *Red Cups* contain 4 red balls and 1 blue ball. I chose a cup at random so that each cup was equally likely to be selected. I then drew three balls at random *with replacement* from the chosen cup. In order, the balls I drew were: red, red, blue. Let C_B be the event that I chose a *Blue Cup* and let RRB be the event that represents my three draws: a red ball, followed by another red ball, followed by a blue ball.

(a) Suppose N_B is 5. Calculate $P(C_B|RRB)$.

- (b) Now suppose that we do *not* know the value of N_B . How large would N_B have to be for it to be more likely that I drew from a blue cup given that the event RRB has occurred? Prove your answer.

- (c) Suppose that I made my draws *without* replacement. What is $P(C_B|RRB)$ in this case? Briefly explain your answer.

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5. The so-called “Iris Dataset” comes pre-loaded in R in the dataframe `iris`. Here’s a description from the R documentation:

This famous (Fisher’s or Anderson’s) iris data set gives the measurements in centimeters of the variables sepal length and width and petal length and width, respectively, for 50 flowers from each of 3 species of iris. The species are *Iris setosa*, *versicolor*, and *virginica*.

A *sepal* is a part of a flower, specifically one of the small leaves found behind the petals. Here are the first few rows of the dataset:

```
> head(iris)
  Sepal.Length Sepal.Width Petal.Length Petal.Width Species
1          5.1         3.5         1.4         0.2   setosa
2          4.9         3.0         1.4         0.2   setosa
3          4.7         3.2         1.3         0.2   setosa
4          4.6         3.1         1.5         0.2   setosa
5          5.0         3.6         1.4         0.2   setosa
6          5.4         3.9         1.7         0.4   setosa
```

Note that the column `Species` is a categorical variable, aka factor, that takes on three different values: `setosa`, `versicolor`, and `virginica`.

- (a) Suppose you wanted to display only the columns `Sepal.Length` and `Petal.Width` of `iris`. What R command would you use?
- (b) What R command would you use to extract data for only flowers of the species *Iris setosa* and store it in a dataframe called `setosa`?
- (c) What R command would you use to separately calculate the sample mean `Sepal.Length` for *each species* of iris? Be sure to allow for the possibility of missing values.