

# 1 Open Automaton for TCP Sliding Window

## 2 Open Automaton for Data Link Go-back- $N$

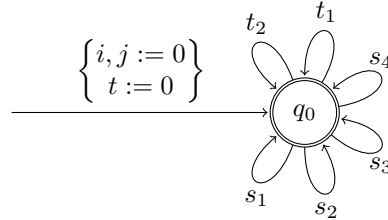
### 2.1 Specification

The sender maintains a circular buffer  $B$  of size  $N$ , where  $N$  is the window size. Let  $i$  and  $j$  denote the indices of the oldest unacknowledged frame and the next frame to send, respectively. Both range over  $[0, N - 1]$  and are interpreted modulo  $N$ . At the beginning,  $i = j = 0$ . The sender may transmit a frame  $B[j]$  if the window is not full, i.e.,  $j \neq (i - 1) \bmod N$ . After transmission,  $j$  is incremented modulo  $N$ . The receiver maintains a single expected frame index, initially set to 0. It accepts a frame if and only if its index matches the expected  $i$ , acknowledges it, and increments  $i$  modulo  $N$ . All other frames are discarded. Upon receiving an acknowledgment for frame  $i$ , the sender removes the acknowledged frame and increments  $i$  modulo  $N$ . If an acknowledgment for frame  $i$  is not received within a timeout interval  $T$  after it was sent, the sender retransmits all frames currently in the window, starting from frame  $i$  up to (but not including) frame  $j$ .

### 2.2 Open Automaton

From the specification, given that Sender and Receiver as holes, two variables  $i$  and  $j$  are required. The Sender emits observable actions **send**, **wait**, **resend** and an unobservable action **getFrame**, which fetches a packet from the network layer and converts it to a frame. The Receiver emits an observable action **ack** and an unobservable action **dispatchFrame**, which sends a frame to the network layer. In addition, let  $t \in [0, T]$  be the variable for waited time. We assume that for each time **wait** is emitted,  $t$  is incremented. The open automaton has a single state  $q_0$  and the transitions are

$$\begin{aligned}
 s_1 &= \frac{\{\text{Sender} \mapsto \text{getFrame}\}(\text{True})\{\}}{q_0 \xrightarrow{\tau} q_0} \\
 s_2 &= \frac{\{\text{Sender} \mapsto \text{send}(j)\}((j+1)\%N \neq i)\{j := (j+1)\%N\}}{q_0 \xrightarrow{\text{frameSent}} q_0} \\
 s_3 &= \frac{\{\text{Sender} \mapsto \text{wait}\}((j+1)\%N = i \wedge t < T)\{t := t+1\}}{q_0 \xrightarrow{\tau} q_0} \\
 s_4 &= \frac{\{\text{Sender} \mapsto \text{resend}(i)\}(t = T)\{t := 0\}}{q_0 \xrightarrow{\text{frameResent}} q_0} \\
 t_1 &= \frac{\{\text{Receiver} \mapsto \text{ack}(i)\}(i \neq j)\{i := (i+1)\%N; t := 0\}}{q_0 \xrightarrow{\text{frameAked}} q_0} \\
 t_2 &= \frac{\{\text{Receiver} \mapsto \text{dispatchFrame}\}(\text{True})\{\}}{q_0 \xrightarrow{\tau} q_0}
 \end{aligned}$$



## 3 Open Automaton for Data Link Selective Repeat

### 3.1 Specification

Selective repeat protocol allows the sender to only resend the oldest unacknowledged frame. In addition to a buffer  $B$  and two indices  $i$  and  $j$ , the sender needs an acknowledged array *Aked* whose values are boolean. Every time the receiver receives a frame correctly, it sends an acknowledgment. When an

acknowledgment is received, the sender either update the acknowledgment status of the corresponding frame, or when the frame is at index  $i$ , the sender rotates the sliding window and set the acknowledgment status for this frame to False.

### 3.2 Open Automaton

We need an additional array *Acked* for acknowledgment status. Let the function *oldestUnacked* return the oldest unacknowledged frame index. The transitions are

$$\begin{aligned}
s_1 &= \frac{\{\text{Sender} \mapsto \mathbf{getFrame}\}(\text{True})\{\}}{q_0 \xrightarrow{\tau} q_0} \\
s_2 &= \frac{\{\text{Sender} \mapsto \mathbf{send}(j)\}((j+1)\%N \neq i)\{j := (j+1)\%N\}}{q_0 \xrightarrow{\text{frameSent}} q_0} \\
s_3 &= \frac{\{\text{Sender} \mapsto \mathbf{wait}\}((j+1)\%N = i \wedge t < T)\{t := t+1\}}{q_0 \xrightarrow{\tau} q_0} \\
s_4 &= \frac{\{\text{Sender} \mapsto \mathbf{resend}(\mathbf{oldestUnacked}())\}(t = T)\{t := 0\}}{q_0 \xrightarrow{\text{frameResent}} q_0} \\
t_1 &= \frac{\{\text{Receiver} \mapsto \mathbf{ack}(i)\}(i \neq j)\{i := (i+1)\%N; t := 0; \text{Acked}[i] := \text{False}\}}{q_0 \xrightarrow{\text{frameAcked}} q_0} \\
t_2 &= \frac{\{\text{Receiver} \mapsto \mathbf{ack}(k)\}(i < k \neq j)\{\text{Acked}[k] := \text{True}\}}{q_0 \xrightarrow{\text{frameAcked}} q_0} \\
t_3 &= \frac{\{\text{Receiver} \mapsto \mathbf{dispatchFrame}\}(\text{True})\{\}}{q_0 \xrightarrow{\tau} q_0}
\end{aligned}$$

