1 Different Behaviors for the Holes

We build an OA serving as a prototype for connection-oriented communication protocols. Let N be the number of data units to be sent, whose index ranges from 0 to N-1. There are two holes, namely Sender and Receiver. The Sender invokes actions send, receive and process, corresponding to sending a data unit, receiving an acknowledgement and doing an internal work, such as waiting until timeout. The Receiver also invokes actions send, receive and process, but here it sends an acknowledgement and receives a data unit. A data unit or an acknowledgement may also be lost during transmission. From the environment's perspective, a data unit can be in one of the following situation

- it needs to be sent,
- it is on fly i.e. it was sent by the Sender but not arrives at the Receiver yet,
- it has been received by the Receiver, or
- it has been sent and acknowledged successfully.

Hence we use four variables of type lists D_{tosend} , D_{onfly} , D_{received} and D_{done} to store the indices of the data units in these situations. For an acknowledgement, it can also by on fly, which is store in A_{onfly} . We do not need to store received acknowledgements because the Sender processes an acknowledgement immediately when receiving it. The initial values are $D_{\text{tosend}} = [0, \dots, N-1]$ and $D_{\text{onfly}} = D_{\text{received}} = D_{\text{done}} = A_{\text{onfly}} = []$. We use two operation on a list L

- L.push(i): appending i to the list, and
- L.pop(i): removing i in its first appearance from the list or return the old list if there is no i

and a function $\min(L)$ to find the minimal element in the list. The transitions are given in the following table.

N.O.	Source	Target	Action	Hole actions	Guard	Reassignment
1	q_0	q_0	$\operatorname{sendData}(i)$	$\mathrm{Sender} \mapsto \mathtt{send}(i)$	$i = \min(D_{\text{tosend}})$	$D_{\text{onfly}}.\text{push}(i)$
2	q_0	q_0	$\operatorname{receiveAck}(i)$	$\mathrm{Sender} \mapsto \mathtt{receive}(i)$	$i \in A_{\mathrm{onfly}}$	$A_{\text{onfly}}.\text{pop}(i)$ $D_{\text{tosend}}.\text{pop}(i)$
3	q_0	q_0	au	$Sender \mapsto \mathtt{process}(opts)$	True	
4	q_0	q_0	receiveData(i)	$\text{Receiver} \mapsto \mathtt{receive}(i)$	$i \in D_{\mathrm{onfly}}$	$D_{\text{onfly}}.\text{pop}(i)$ $D_{\text{received}}.\text{push}(i)$
5	q_0	q_0	$\operatorname{sendAck}(i)$	$\operatorname{Receiver} \mapsto \mathtt{send}(i)$	$i \in D_{\text{received}}$	$D_{\text{received}}.\text{pop}(i)$
6	q_0	q_0	au	$\mathrm{Sender} \mapsto \mathtt{process}(opts)$	True	
7	q_0	q_0	loseData(i)		$i \in D_{\text{onfly}}$	$D_{\text{onfly}}.\text{pop}(i)$
8	q_0	q_0	loseAck(i)		$i \in A_{\text{onfly}}$	$A_{\text{onfly}}.\text{pop}(i)$

Table 1: Transition Table for Protocol OA

An protocol implementing the Sender and Receiver is correct if given the initial assignments of the lists, the composed OA always arrives at a terminal state with $D_{\text{done}} = [1, \dots, N]$.

Consider and example. Let $D_{\text{tosend}} = [0, 1, 2]$ and $D_{\text{onfly}} = D_{\text{received}} = D_{\text{done}} = A_{\text{onfly}} = []$. Denote by $(D_{\text{tosend}}, D_{\text{onfly}}, D_{\text{received}}, A_{\text{onfly}})$ each configuration of the OA. One possible run is

$$([0,1,2],[],[],[]) \xrightarrow{\text{sendData}(0)} ([1,2],[0],[],[],[])$$