A preliminary model for Quad-Rig catch comparison

Updated to include additional trial data

Methods for twin-rig catch comparison analysis are set out in Holst and Revill (2009). Here, this model is preliminarily extended to greater than 2 cod-ends, in particular we focus on the quad-rig with 4 cod-ends. All treatment of the data is included as in a tutorial, which can be used as a basis for capacity building in the analysis of gear technology trials.

1 Data

The data used for this example come from the July 2014 diamond cod-end mesh size trials conducted by BIM aboard MFV Celtic Warrior II on the Smalls grounds. The data are read into R and processed as follows:

```
library (gdata)
neph.dat <- read.xls("../data/Celtic Warrior Diamond mesh July 2014 Celtic Sea.xls",
                    sheet = "Nephrops Lengths",
                     stringsAsFactors = FALSE)
## remove Haul 22, as no recordings for 90mm
neph.dat <- subset (neph.dat, HAUL != 22)</pre>
## Show the first 2 rows
head(neph.dat, 2)
                     DATE HAUL COMPARTMENT Mesh.Size SPECIES
## 1 Celtic Warrior 2014-07-19 1 Control 70mm Nephrops
## 2 Celtic Warrior 2014-07-19 1 Control
                                                    70mm Nephrops
## Carapace.Length..mm.. COUNT SUBSRATIO
## 1
                       16 1
## 2
                       17
                             11
## Change the carapace length name
names (neph.dat) [names (neph.dat) == "Carapace.Length..mm.."] <- "Carapace.Length"</pre>
## Make the "HAUL" variable character
neph.dat$HAUL <- paste("H", neph.dat$HAUL, sep ="")</pre>
```

Prepare the data for a multinomial fit.

```
## get count per length bin per haul by mesh size
## using the reshape package (makes it easier to process data)
library(reshape)
## variables to keep
vars2keep <- c("fMesh.Size", "Carapace.Length", "fHAUL", "COUNT")</pre>
## melt the data frame
neph.melt <- melt(neph.dat[, vars2keep],</pre>
                  id = c("fMesh.Size", "Carapace.Length", "fHAUL"))
## re-form the dataframe in required format
neph.cast <- cast(neph.melt, Carapace.Length + fHAUL ~ fMesh.Size + variable)</pre>
neph.cast <- neph.cast[order(neph.cast$fHAUL, neph.cast$Carapace.Length), ]</pre>
neph.cast[is.na(neph.cast)] <- 0</pre>
## show the first few rows
head(neph.cast, 2)
     Carapace.Length fHAUL 70mm_COUNT 80mm_COUNT 90mm_COUNT 100mm_COUNT
## 1
                  15 H1 0 2 1
## 24
                   16
                         Н1
                                     1
                                               3
                                                           9
                                                                        1
## format the subsampling ratio similarly
vars2keep <- c("fMesh.Size", "fHAUL", "SUBSRATIO")</pre>
subs.melt <- melt(unique(neph.dat[, vars2keep]), id = c("fMesh.Size", "fHAUL"))</pre>
subs.cast <- cast(subs.melt, fHAUL ~ fMesh.Size + variable)</pre>
## merge counts and subsampling ratio back together
neph.cast <- merge(neph.cast, subs.cast, by = "fHAUL", all.x = TRUE)</pre>
## show first few lines
head(neph.cast, 2)
## fHAUL Carapace.Length 70mm_COUNT 80mm_COUNT 90mm_COUNT 100mm_COUNT
```

```
## 1 H1
## 2
                                                3
                                                           9
       Н1
                        16
                                    1
                                                                        1
## 70mm SUBSRATIO 80mm SUBSRATIO 90mm SUBSRATIO 100mm SUBSRATIO
## 1
                  1
                                1
                                                1
## 2
                  1
                                  1
                                                 1
                                                                  1
## Extract the matrix of counts
count.vars <- c("70mm_COUNT", "80mm_COUNT", "90mm_COUNT", "100mm_COUNT")
neph.count.mat <- as.matrix(neph.cast[, count.vars])</pre>
colnames (neph.count.mat) <- c("70mm_COUNT", "80mm_COUNT", "90mm_COUNT",</pre>
                               "100mm COUNT")
## Extract the matrix of subsampling ratios
subsratio.vars <- c("70mm SUBSRATIO", "80mm SUBSRATIO", "90mm SUBSRATIO",
                    "100mm SUBSRATIO")
subsratio.mat <- as.matrix(neph.cast[, subsratio.vars])</pre>
## Create the offset (NEED TO CHECK THIS)
offset.mat <- log(apply(subsratio.mat, 2, FUN =
                        function(zz){zz/subsratio.mat[,1]}))
```

Plot the data

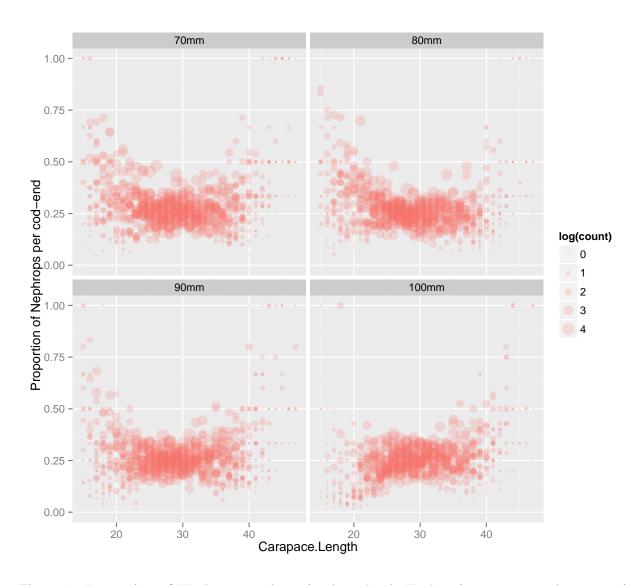


Figure 1: Proportion of Nephrops catch retained per haul. Each point represents the proportion of the Nephrops catch (in number) per haul and length class retained in a given cod-end (70mm, 80mm, 90mm, or 100mm). The size of the point is proportional to the log of the count.

2 Model

The model we focus on is the multinomial, which is a generalization of the binomial to cases with more than two categories (here 4 categories: 70mm, 80mm, 90mm, 100mm). Under the assumption that each net fishes the same, we would expect 25% of the catch to be retained in each net. We can test that hypothesis.

```
library(nnet)
## First fit is constant proportions
## not accounting for length
mnom0 <- multinom(neph.count.mat ~ 1 + offset(offset.mat))</pre>
## # weights: 24 (3 variable)
## initial value 65833.303791
## final value 65796.538161
## converged
## include carapace length
## first scale it to range between zero and one
max.length <- max(neph.cast$Carapace.Length)</pre>
neph.cast$prop.Carapace.Length <- neph.cast$Carapace.Length/max.length</pre>
## Extend to third order polynomial (based on AIC and BIC)
neph.cast$prop.Carapace.Length2 <- neph.cast$prop.Carapace.Length^2</pre>
neph.cast$prop.Carapace.Length3 <- neph.cast$prop.Carapace.Length^3</pre>
##
mnom.length <- multinom(neph.count.mat ~</pre>
                        prop.Carapace.Length + prop.Carapace.Length2 + prop.Carapace.Length
                        offset (offset.mat), data = neph.cast)
## # weights: 36 (12 variable)
## initial value 65833.303791
## iter 10 value 65574.013563
## iter 20 value 65540.974075
## final value 65538.628411
## converged
AIC (mnom0, mnom.length)
##
               df AIC
## mnom0 3 131599.1
## mnom.length 12 131101.3
```

Get predictions for the fitted model (note this is long-winded here but will be better coded for more

than the preliminary example).

```
## get predictions manually
## CIs not defined in multinomial context but let's try
## fit coefficients
beta.mu <- c(t(coef(mnom.length)))</pre>
## fit coefficient variance covariance matrix
Sigma <- vcov(mnom.length)</pre>
## number of lengths to predict for
nlength <- 100
pred.prop.length <- seq(min(neph.cast$prop.Carapace.Length),</pre>
                         max(neph.cast$prop.Carapace.Length), length = 100)
pred.length <- seq(min(neph.cast$Carapace.Length),</pre>
                         max(neph.cast$Carapace.Length), length = 100)
## model matrix
X <- cbind(1, pred.prop.length, pred.prop.length^2, pred.prop.length^3)</pre>
## number of times to resample predictions to get CIs
nresamp <- 100
pred.array <- array(NA, dim = c(nlength, 4, nresamp))</pre>
## package to draw from multivariate normal
library (mvtnorm)
for(i in 1:nresamp){
 ## print(i)
 beta <- matrix(rmvnorm(1, mean = beta.mu, sigma = Sigma),
                 nrow = 3, byrow = TRUE)
 p80 <- exp(X %*% matrix(beta[1,]))/(1 + rowSums(exp(X %*% t(beta))))
 p90 <- exp(X %*% matrix(beta[2,]))/(1 + rowSums(exp(X %*% t(beta))))
  p100 <- exp(X %*% matrix(beta[3,]))/(1 + rowSums(exp(X %*% t(beta))))
  p70 <- 1 - p80 - p90 - p100
 pred.p <- cbind(p70, p80, p90, p100)</pre>
 pred.array[ , , i] <- pred.p</pre>
 rm(pred.p)
## mean across samples
pred.mu <- apply(pred.array, c(1, 2), mean)</pre>
## upper across samples
pred.upper <- apply (pred.array, c(1, 2), quantile, p = 0.975)
## lower across samples
pred.lower <- apply (pred.array, c(1, 2), quantile, p = 0.025)
## bring all together in a data frame for ggplot
```

Finally overlay the fit on the sample proportions

2.1 Including weight as a covariate

Make a row per observation and merge with the weight data

```
## get a row per length measurement (raise them also)
n <- nrow(neph.dat)</pre>
##neph.dat2 <- neph.dat[rep(1:n, times =</pre>
                         round(neph.dat$COUNT/neph.dat$SUBSRATIO, 0)), ]
## Note: no raising here
##neph.dat2 <- neph.dat[rep(1:n, times = neph.dat$COUNT), ]</pre>
weight.dat <- read.xls("../data/Celtic Warrior Diamond mesh July 2014 Celtic Sea.xls",
                     sheet = "Weights",
                     stringsAsFactors = FALSE)
## Show the first 2 rows
head(weight.dat, 2)
         Date Haul.. Compartment Mesh.Size Species Total.weight..kg.
TEST1
                                   90mm Haddock
## 2 2014-07-19
                                                           0.38
## Sbsample.weight..kg.
## 1
## 2
```

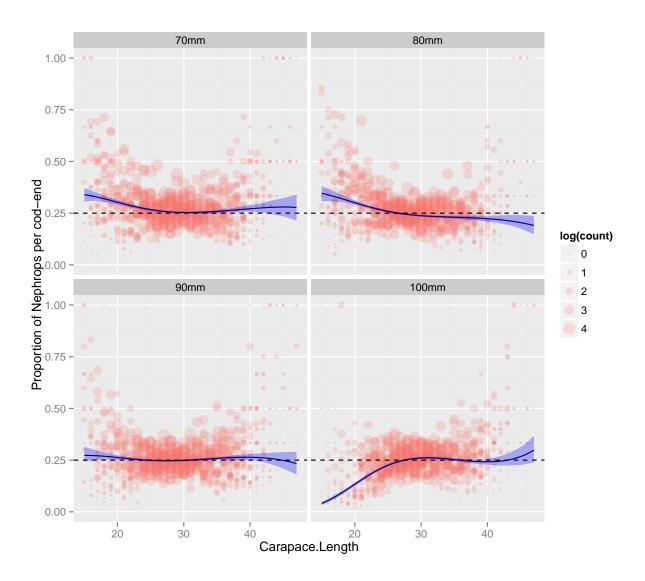
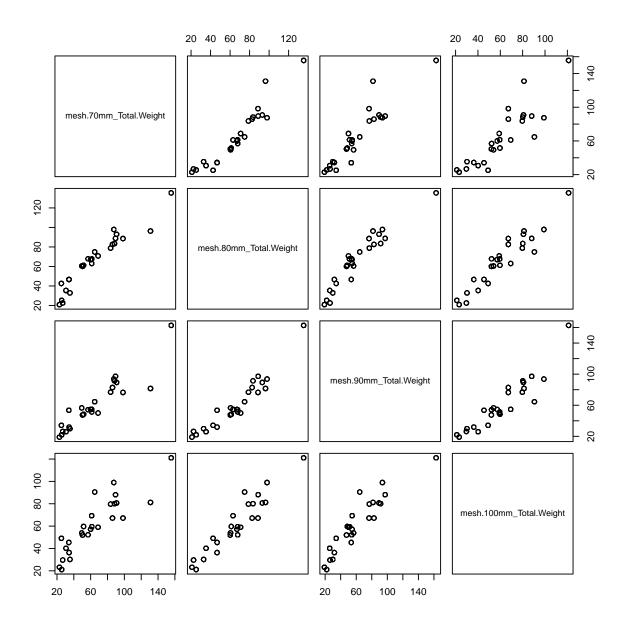


Figure 2: Proportion of Nephrops catch retained per haul with fitted multinomial model and associated re-sampled intervals. Null hypothesis of equal retention is displayed as the dashed line at 0.25.

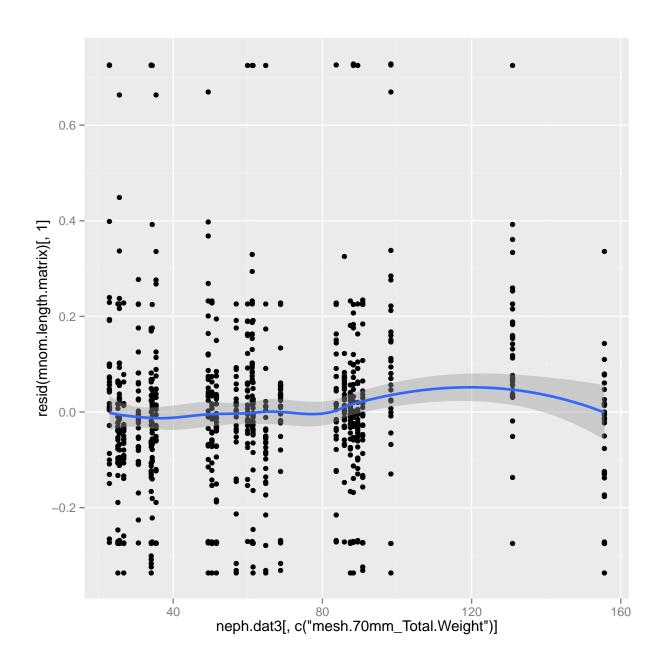
```
## create a new "HAUL" variable for the merge
weight.dat$HAUL <- paste("H", weight.dat$Haul.., sep ="")</pre>
## re-name total weight column
names (weight.dat) [names (weight.dat) == "Total.weight..kg."] <- "Total.Weight"</pre>
weight.dat <- subset(weight.dat, Species == "Bulk")</pre>
## melt the data frame
weight.melt <- melt(weight.dat[, c("HAUL", "Mesh.Size", "Total.Weight")],</pre>
                  id = c("Mesh.Size", "HAUL"))
## re-form the dataframe in required format
weight.cast <- cast (weight.melt, HAUL ~ Mesh.Size + variable)</pre>
weight.cast <- weight.cast[order(weight.cast$HAUL), ]</pre>
weight.cast[is.na(weight.cast)] <- 0</pre>
## show the first few rows
head(weight.cast, 2)
## HAUL 100mm_Total.Weight 70mm_Total.Weight 80mm_Total.Weight
                                   26.76
                       29.64
## 1 H1
                                                             22.56
## 2 H10
                       52.00
                                          50.40
                                                             60.10
## 90mm_Total.Weight
## 1
                26.28
## 2
                 47.50
weight.cast$fHAUL <- factor(weight.cast$HAUL)</pre>
names (weight.cast) [grep("^[0-9]", names (weight.cast))] <- paste("mesh.", names (weight.cast)</pre>
## merge nephrops length and total bulk weight data
neph.dat3 <- merge(neph.cast,</pre>
                   weight.cast,
                   by = c("fHAUL"),
                   sort = FALSE
max.length <- max(neph.dat3$Carapace.Length)</pre>
neph.dat3$prop.Carapace.Length <- neph.dat3$Carapace.Length/max.length</pre>
neph.dat3$prop.Carapace.Length2 <- neph.dat3$prop.Carapace.Length^2</pre>
neph.dat3$prop.Carapace.Length3 <- neph.dat3$prop.Carapace.Length^3</pre>
neph.dat3$prop.Carapace.Length4 <- neph.dat3$prop.Carapace.Length^4
```

Include weight in the fit

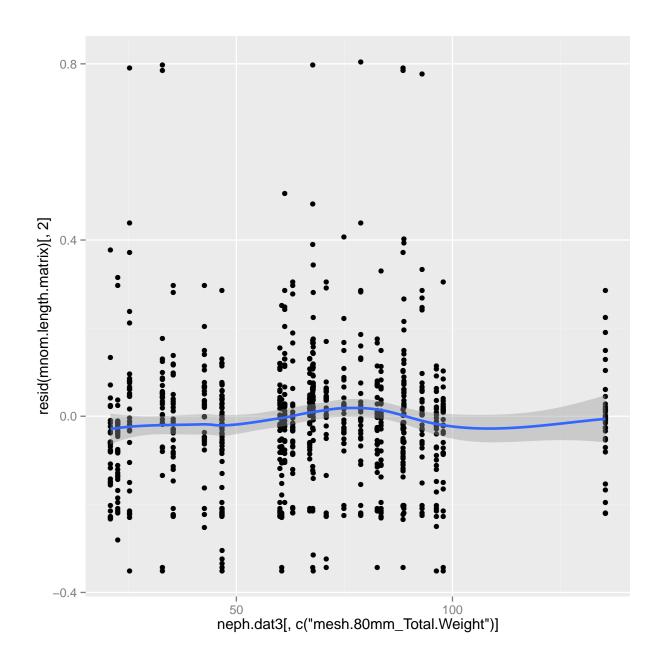
```
## compare two ways of writing same model
```



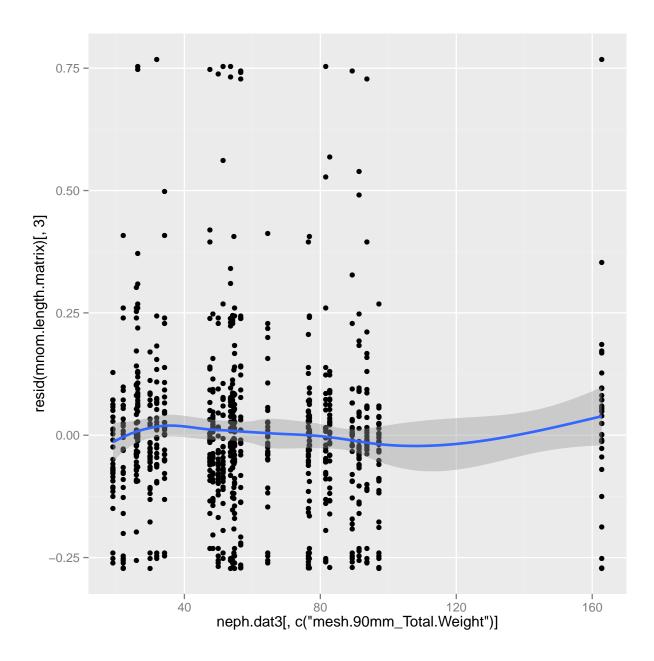
```
## very strong correlation in the counts
 round (cor (neph.dat3[, c("mesh.70mm_Total.Weight", "mesh.80mm_Total.Weight", "mesh.90mm_Total.Weight", "mesh.90mm_Total.W
 ##
                                                                                                                                                   mesh.70mm_Total.Weight mesh.80mm_Total.Weight
 ## mesh.70mm_Total.Weight
                                                                                                                                                                                                                                                1.000
                                                                                                                                                                                                                                                                                                                                                                             0.953
 ## mesh.80mm_Total.Weight
                                                                                                                                                                                                                                                0.953
                                                                                                                                                                                                                                                                                                                                                                             1.000
 ## mesh.90mm_Total.Weight
                                                                                                                                                                                                                                                0.927
                                                                                                                                                                                                                                                                                                                                                                             0.951
                                                                                                                                                                                                                                                0.882
 ## mesh.100mm_Total.Weight
                                                                                                                                                                                                                                                                                                                                                                              0.948
                                                                                                                                                   mesh.90mm_Total.Weight mesh.100mm_Total.Weight
## mesh.70mm_Total.Weight
                                                                                                                                                                                                                                                0.927
                                                                                                                                                                                                                                                                                                                                                                                  0.882
                                                                                                                                                                                                                                                0.951
                                                                                                                                                                                                                                                                                                                                                                                   0.948
## mesh.80mm_Total.Weight
```



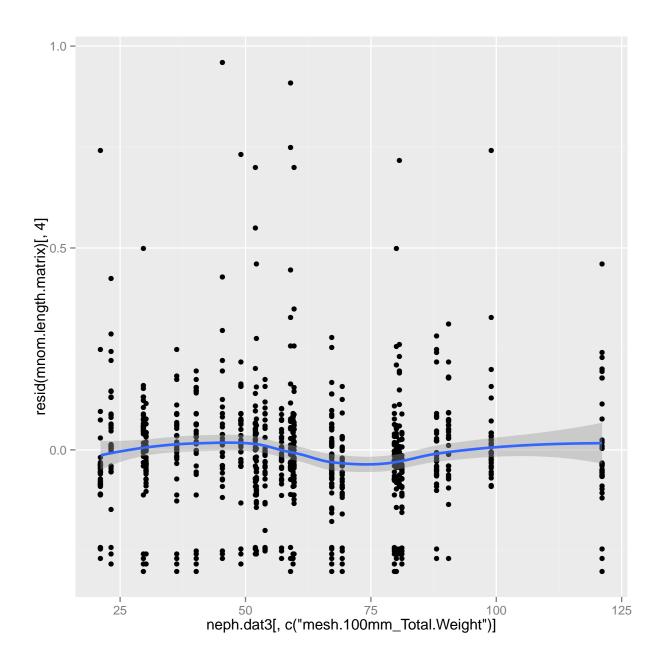
```
## geom_smooth: method="auto" and size of largest group is <1000, so using loess.
Use 'method = x' to change the smoothing method.</pre>
+ geom_smooth
+ geom_smooth
- c("mesh.80mm_Total.Weight")], resid(mnom.length.matrix)[,2])
+ geom_smooth
- geom_
```



qplot(neph.dat3[, c("mesh.90mm_Total.Weight")], resid(mnom.length.matrix)[,3]) + geom_smooth
geom_smooth: method="auto" and size of largest group is <1000, so using loess.
Use 'method = x' to change the smoothing method.</pre>



qplot(neph.dat3[, c("mesh.100mm_Total.Weight")], resid(mnom.length.matrix)[,4]) + geom_smooth
geom_smooth: method="auto" and size of largest group is <1000, so using loess.
Use 'method = x' to change the smoothing method.



```
## include bulk weight in wide format model, note only including one of the
## bulk weights as the explanatory

neph.dat3$av.Total.Weight <- apply(neph.dat3[, c("mesh.70mm_Total.Weight", "mesh.80mm_Total.
mean.wt <- mean(neph.dat3$av.Total.Weight)

neph.dat3$av.Total.Weight.scaled <- neph.dat3$av.Total.Weight - mean.wt

mnom.length.bulk <- multinom(as.matrix(neph.dat3[, c("70mm_COUNT", "80mm_COUNT", "90mm_COUNT", "00mm_COUNT", "00mm_COUNT",
```

```
(poly(av.Total.Weight.scaled, 2) + prop.Carapace.Length2)^2 +
                              (poly (av. Total. Weight.scaled, 2) + prop. Carapace. Length 3) ^ 2,
                             ##offset(offset.mat),
                             data = neph.dat3)
## # weights: 52 (36 variable)
## initial value 65846.209564
## iter 10 value 65578.319726
## iter 20 value 65497.714497
## iter 30 value 65463.674596
## iter 40 value 65455.587103
## iter 50 value 65454.225846
## iter 60 value 65453.755984
## final value 65453.493336
## converged
## cut the weights here also
wt.brks <-c(0, 44, 90, Inf)
neph.dat3$cmesh.70mm_Total.Weight <- cut (neph.dat3$mesh.70mm_Total.Weight, breaks = wt.brks
neph.dat3$cmesh.80mm_Total.Weight <- cut (neph.dat3$mesh.80mm_Total.Weight, breaks = wt.brks
neph.dat3$cmesh.90mm_Total.Weight <- cut (neph.dat3$mesh.90mm_Total.Weight, breaks = wt.brks
neph.dat3$cmesh.100mm_Total.Weight <- cut (neph.dat3$mesh.100mm_Total.Weight, breaks = wt.b</pre>
mnom.length.bulkc <- multinom(as.matrix(neph.dat3[, c("70mm_COUNT", "80mm_COUNT", "90mm_COUNT",
                              prop.Carapace.Length +
                              prop.Carapace.Length2 +
                              prop.Carapace.Length3 +
                              ##
                              cmesh.70mm_Total.Weight +
                              cmesh.80mm_Total.Weight +
                              cmesh.90mm_Total.Weight +
                              cmesh.100mm_Total.Weight,
                              ##offset(offset.mat),
                              data = neph.dat3)
## # weights: 52 (36 variable)
## initial value 65846.209564
## iter 10 value 65654.262307
## iter 20 value 65557.651822
## iter 30 value 65464.946065
## iter 40 value 65424.314033
## iter 50 value 65416.861080
## final value 65416.844867
## converged
AIC (mnom.length.matrix, mnom.length.bulk, mnom.length.bulk.order1, mnom.length.bulk.order2
## Error in lapply(list(object, ...), ll): object 'mnom.length.bulk.order1' not
found
## INCLUDE HIGHER-ORDER CARAPACE LENGTH
```

Get predictions for low, medium and high catch weights

```
## In the model we include weights by compartment
## in the predictions we fix the weights to be equal so we can see the mesh effects
## 'standardize for weight effects so we can investigate mesh effects'
## low.med.high.bulk <- quantile(weight.dat[weight.dat$Species == "Bulk",]$Total.Weight,
##
                                 p = c(0.1, 0.5, 0.9))
## low.med.high.bulk
## ## set high to 120kg
## low.med.high.bulk[3] <- 120
## get mean total weight per bin used for empirical
low.med.high.bulk <- with(neph.dat.bulk, tapply(Total.Weight, cTotal.Weight, mean))</pre>
## Error in with (neph.dat.bulk, tapply (Total.Weight, cTotal.Weight, mean)): object
'neph.dat.bulk' not found
pred.df <- expand.grid(Carapace.Length = pred.length,</pre>
                       av.Total.Weight = low.med.high.bulk)
## Error in expand.grid(Carapace.Length = pred.length, av.Total.Weight = low.med.high.bulk
object 'low.med.high.bulk' not found
pred.df$av.Total.Weight.scaled <- pred.df$av.Total.Weight- mean.wt
## Error in `$<-.data.frame`(`*tmp*`, "av.Total.Weight.scaled", value = numeric(0)):
replacement has 0 rows, data has 400
## pred.df$mesh.80mm Total.Weight <- pred.df$mesh.70mm Total.Weight
## pred.df$mesh.90mm_Total.Weight <- pred.df$mesh.70mm_Total.Weight
## pred.df$mesh.100mm_Total.Weight <- pred.df$mesh.70mm_Total.Weight
## pred.df$cmesh.70mm_Total.Weight <- cut(pred.df$mesh.70mm_Total.Weight, breaks = wt.brks
## pred.df$cmesh.80mm_Total.Weight <- cut(pred.df$mesh.80mm_Total.Weight, breaks = wt.brks
## pred.df$cmesh.90mm_Total.Weight <- cut(pred.df$mesh.90mm_Total.Weight, breaks = wt.brks
## pred.df$cmesh.100mm_Total.Weight <- cut(pred.df$mesh.100mm_Total.Weight, breaks = wt.br.
pred.df$prop.Carapace.Length <- pred.df$Carapace.Length/max.length
## Error in `$<-.data.frame`(`*tmp*`, "prop.Carapace.Length", value = numeric(0)):
replacement has 0 rows, data has 400
pred.df$prop.Carapace.Length2 <- pred.df$prop.Carapace.Length^2</pre>
## Error in `$<-.data.frame`(`*tmp*`, "prop.Carapace.Length2", value = numeric(0)):
replacement has 0 rows, data has 400
pred.df$prop.Carapace.Length3 <- pred.df$prop.Carapace.Length^3</pre>
```

```
## Error in `$<-.data.frame`(`*tmp*`, "prop.Carapace.Length3", value = numeric(0)):
replacement has 0 rows, data has 400
## Need to re-define offset here!!
## Better to set offset as cbind in data frames
##offset.mat <- matrix(0, ncol = 4, nrow = dim(pred.df)[1])</pre>
##mnom.pred <- predict(mnom.length.bulk.order3, newdata = pred.df, type = "prob")
mnom.pred <- predict(mnom.length.bulk, newdata = pred.df, type = "prob")</pre>
## Error in poly(av.Total.Weight.scaled, 2, coefs = structure(list(alpha = c(2.59920094279
: object 'av.Total.Weight.scaled' not found
m <- dim (mnom.pred) [1]
## Error in eval(expr, envir, enclos): object 'mnom.pred' not found
mnom.pred.df <- data.frame(</pre>
                  Mesh.Size = factor(rep(c("70mm", "80mm", "90mm", "100mm"),
                    each = m), levels = c("70mm", "80mm", "90mm", "100mm")),
                  Carapace.Length = rep(pred.df$Carapace.Length, times = 4),
                  prop.Carapace.Length = rep(pred.df$prop.Carapace.Length, times = 4),
                  av.Total.Weight = rep(pred.df$av.Total.Weight, times = 4),
                  proportion = c(mnom.pred))
## Error in data.frame(Mesh.Size = factor(rep(c("70mm", "80mm", "90mm", "100mm"),
: object 'mnom.pred' not found
mnom.pred.df$Bulk.Weight <-
  ifelse (mnom.pred.df$av.Total.Weight == low.med.high.bulk[1], "Low (26kg)",
         ifelse (mnom.pred.df$av.Total.Weight == low.med.high.bulk[2], "Medium (60.5kg)", "
## Error in ifelse(mnom.pred.df$av.Total.Weight == low.med.high.bulk[1], : object
'mnom.pred.df' not found
mnom.pred.df$Bulk.Weight <- factor(mnom.pred.df$Bulk.Weight,</pre>
                                    levels = c("Low (26kg)", "Medium (60.5kg)", "High (120kg)")
## Error in factor(mnom.pred.df$Bulk.Weight, levels = c("Low (26kg)", "Medium (60.5kg)",
: object 'mnom.pred.df' not found
p + geom_line(data = mnom.pred.df,
              aes(x = Carapace.Length, y = proportion,
                  group = Bulk.Weight,
                  colour = Bulk.Weight)) +
  scale_colour_manual(values=c("#619CFF", "#00BA38", "#FF0000")) +
##scale_colour_manual(values = c("blue", "green", "red")) +
geom_hline(aes(yintercept = 0.25), linetype = "dashed") +
  geom_vline(aes(xintercept = 25), linetype = "dashed")
## Error in do.call("layer", list(mapping = mapping, data = data, stat = stat, :
object 'mnom.pred.df' not found
```

```
## draw empirical lines
## bin the weights
neph.dat.bulk <- merge(neph.dat, weight.dat)</pre>
neph.dat.bulk$cTotal.Weight <- cut (neph.dat.bulk$Total.Weight, breaks = wt.brks)</pre>
##neph.dat.bulk$cTotal.Weight <- 1</pre>
## RAISING NOT INCLUDED UNTIL OFFSET INCLUDED
##neph.dat.bulk$rCOUNT <- with(neph.dat.bulk, COUNT/SUBSRATIO)</pre>
neph.dat.bulk$rCOUNT <- with(neph.dat.bulk, COUNT)</pre>
count.array <- with (neph.dat.bulk, tapply (rCOUNT, list (cTotal.Weight, Carapace.Length, Mes)</pre>
count.array[is.na(count.array)] <- 0</pre>
prop.array <- prop.table(count.array, c(1,2))</pre>
prop.df <- expand.grid(Total.Weight = dimnames(prop.array)[[1]],</pre>
                         Carapace.Length = dimnames (prop.array) [[2]],
                        Mesh.Size = dimnames(prop.array)[[3]],
                         stringsAsFactors = FALSE)
prop.df$empirical.prop <- NA</pre>
prop.df$rCOUNT <- NA</pre>
for(i in 1:dim(prop.df)[1]){
  ## proportion
  prop.df$empirical.prop[i] <- prop.array[prop.df$Total.Weight[i],</pre>
                                             prop.df$Carapace.Length[i],
                                             prop.df$Mesh.Size[i]
  ## count
  prop.df$rCOUNT[i] <- count.array[prop.df$Total.Weight[i],</pre>
                                     prop.df$Carapace.Length[i],
                                     prop.df$Mesh.Size[i]
                                     1
prop.df$Bulk.Weight <- ifelse(prop.df$Total.Weight == "(0,44]", "Low (26kg)",
                                ifelse(prop.df$Total.Weight == "(44,90]", "Medium (60.5kg)",
prop.df$Carapace.Length <- as.numeric(prop.df$Carapace.Length)</pre>
prop.df$Mesh.Size <- factor(prop.df$Mesh.Size, levels = c("70mm", "80mm", "90mm", "100mm"))</pre>
## empirical versus modelled
##pdf("../tex/figures/")
ggplot(prop.df, aes(x = Carapace.Length, y = empirical.prop,
                 group = Bulk.Weight,
```

References

Holst, R. and Revill, A. 2009. A simple statistical method for catch comparison studies. *Fisheries Research* **95**(2–3): 254 – 259