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## Assignment - 01

1. Asymptotic notations are known as mathematical tools which are required to describe the limiting behaviour of a function as its input tends towards infinity.

(i) Big O notations ( $O$ ): This notation represents the upper bound of an algorithm's running time in the worst case. For ex:  $O(n^2)$  for a quadratic equation.

(ii) Omega notation: Represents the lower bound of an algorithm's running time in the best case scenario. ex:  $\Omega(n)$  for a linear algorithm.

(iii) Theta notation ( $\Theta$ ): Represents both the upper and lower bounds providing a tight bound on the algorithm's running time.

ex:  $\Theta(n)$  for a linear algorithm.

2. The time complexity of the given code is  $O(\log n)$ . Since the variable "i" doubles in each iteration the loop executes approximately  $\log_2(n)$  times.



3. The recurrence relation  $T(n) = 3T(n-1)$  represents the exponential growth. Therefore the time complexity is  $O(3^n)$ .
4. The recurrence relation  $T(n) = 2T(n-1) - 1$  represents exponential growth. Therefore the time complexity is  $O(2^n)$ .
5. The time complexity of the given code is  $O(n^{1/2})$ . The loop iterates until the sum "s" exceeds 'n' which happens approximately when "i" reaches  $(n^{1/2})$ .
6. The time complexity of the given code is  $O(n^{1/2})$ . The loop iterates until i is greater than which happens approximately when "i" reaches  $(n^{1/2})$ .
7. The time complexity of the given codes is  $O(n \log n)$ . The outer loop runs  $n/2$  to n times, the middle loop runs  $\log n$  times & the inner loop runs  $\log n$  times. Therefore, the total time complexity is  $O(n \log n)$ .
8. Inner loop runs n times and the outer loop runs n times, making it  $O(n^2)$ . Additionally, the function recursively calls with  $n-3$  so the no. of times it recurses can be represented as  $n/3$ .  

$$O(n^2) * O(n/3) = \cancel{O(n^2)} O(n^3)$$



9. The outer and inner loop will run  $n$  times. Therefore time complexity of second function is

$$O(n) * O(n/1 + n/2 + n/3 + \dots + n/n)$$

harmonic series is  $\log n$ .

So time complexity is  $O(n \log n)$ .

10.  $n^k$  growth rate increase polynomially with  $n$ .  
 $c^n$  growth rate increase exponentially with  $n$ .

$c^n$  grows faster than  $n^k$   
 if  $c > 1$  &  $k > 0$  then

$$\lim_{n \rightarrow \infty} \frac{c^n}{n^k}$$

Therefore for any  $c > 1$  &  $k > 0$   $c^n$  grows faster than  $n^k$ .