The Vector problems

Coding the Matrix, 2015

For auto-graded problems, edit the file The_Vector_problems.py to include your solution.

Vector Addition Practice

Problem 1: For vectors v = [-1, 3] and u = [0, 4], find the vectors v + u, v - u, and 3v - 2u.

Problem 2: Given the vectors $\mathbf{v} = [2, -1, 5]$ and $\mathbf{u} = [-1, 1, 1]$, find the vectors $\mathbf{v} + \mathbf{u}$, $\mathbf{v} - \mathbf{u}$, $2\mathbf{v} - \mathbf{u}$, and $\mathbf{v} + 2\mathbf{u}$.

Problem 3: For the vectors $\mathbf{v} = [0, one, one]$ and $\mathbf{u} = [one, one, one]$ over GF(2), find $\mathbf{v} + \mathbf{u}$ and $\mathbf{v} + \mathbf{u} + \mathbf{u}$.

Expressing one GF(2) vector as a sum of others

Problem 4: Here are six 7-vectors over GF(2):

For each of the following vectors u, find a subset of the above vectors whose sum is u, or report that no such subset exists. You should be able to do this without the help of a computer.

- 1. u = 0010010
- 2. u = 0100010

Problem 5: Here are six 7-vectors over GF(2):

For each of the following vectors u, find a subset of the above vectors whose sum is u, or report that no such subset exists.

- 1. u = 0010010
- 2. u = 0100010

Problem 6: (You should be able to solve this problem without using a computer.) Find a vector $\mathbf{x} = [x_1, x_2, x_3, x_4]$ over GF(2) satisfying the following linear equations:

$$1100 \cdot x = 1$$

$$1010 \cdot x = 1$$

$$1111 \cdot x = 1$$

Verify for yourself that x+1111 also satisfies the equations.

Problem 7: Consider the equations

Your job is not to solve these equations but to formulate them using dot-product. In particular, come up with three vectors v1, v2, and v3 represented as lists so that the above equations are equivalent to

$$v1 \cdot x = 10$$

$$v2 \cdot x = 35$$

$$v3 \cdot x = 8$$

where x is a 4-vector over \mathbb{R} .

Practice with Dot-Product

Problem 8: For each of the following pairs of vectors u and v over \mathbb{R} , evaluate the expression $u \cdot v$:

(a)
$$u = [1, 0], v = [5, 4321]$$

(b)
$$u = [0, 1], v = [12345, 6]$$

(c)
$$u = [-1, 3], v = [5, 7]$$

(d)
$$u = [-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}], v = [\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}]$$