1-(a) What is the size of vector w and y? (10pt)

$$W = \begin{bmatrix} w_0 \\ w_1 \\ \vdots \\ w_d \end{bmatrix}$$

1-(b) What is the size of matrix A? Write A. (10pt)

1-(c) Let d+1=n, then, A becomes a square matrix. Compute the determinant of A. (40pt in total, Derivation: 30pt, Answer: 10pt)

到至起气 复到 245的程是 观点的 当至了 是是 于例是外, 已 可哪 製 至此例 到在 好主意 到外的对。

det A = 2 + ald ap ... and there (d, B, ..., w) is permet (1,2,..., N)

t=1

인학 NXN-8102의 deste (h-1) x (h-1)와 dustermorment 3. 표현하고 숙속장 개발 법에 나에 2x2 가지 즉인 수 있고 2151만 dust = 7에서(는 수 있다.

이 분 위 (4) Cij = A UNLY I + 224 100 + JHZZM columne 지은 항전되 장전성기가 자꾸 이 경제 나는 Cij 는 + Onia, Oup ··· On only 하는 宝兰之 地位 数次分计 空外站社,

1-(d) What is the condition that makes the determinant of A non-zero? (10pt)

colons of A are linearly independent or A is invertible or Az=v have a trivial solution.

1-(e) Assume that the determinant of A is non-zero, then, what is the solution of linear equation,  $A\mathbf{w} = \mathbf{y}$ , with respect to  $\mathbf{w}$ ? (10pt)

Ais invertible this A'Aw: A'y

Iw: A'y

w: A'y

## 2. (20pt)

Suppose that n > d + 1. Then, we cannot compute the inverse of A since A is not a square matrix. In this case, how can we solve the linear equation  $A\mathbf{w} = \mathbf{y}$ ?

If columns of Ais linearly dependent, there can be. Infinite number of w,

He columns of A is treatly independent 
$$O$$
  
led  $V = Null (ATA)$   
 $= ATA V = 3$   
then  $V = ATA = V = 0$   
 $V = ATA = (AV)^T$   
 $V = ATA = (AV)^T$   
 $V = ATA = (AV)^T$   
 $V = ATA = 0$ 

because of Q. AJ=0 J=0

... NM (ATA) = NM(A) = 963

... VII (ATA) = NM(A) = 963

... VII only solution for ATAV=0

ATA B tilearly Independent.

ATA is du x du square motrix and columns of ATA is invertible.

$$A^{T}A w = A^{T}y$$

$$(A^{T}A)^{-1}(A^{T}A)w = (A^{T}A)^{-1}A^{T}y$$

$$w = (A^{T}A)^{-1}A^{T}y$$