

## Assignment5

```
##Q3

##(1) At iteration t, the Gibbs sampler draws  $\Theta_{tj} \sim p(\theta_{tj} | \theta_{-j}^{(t-1)}, y)$ ,
## for  $j=1, \dots, d$ , where  $\theta_{-j}^{(t-1)}$  represents all the components of  $\theta$ ,
## except for  $\theta_{tj}$ , at their current value:
##  $\Theta_{-j}^{(t-1)} = (\theta_{11}^{(t-1)}, \dots, \theta_{tj-1}^{(t-1)}, \theta_{tj+1}^{(t-1)}, \dots, \theta_{td}^{(t-1)})$ 

## Based on the lecture note, we know that  $\mu | y \sim$ 
##  $N((\mu_0/\tau_0^2) + (n\bar{y}/\text{segema}^2)) / (1/\tau_0^2 + (n/\text{segema}^2)), 1/(1/\tau_0^2 + n/\text{segema}^2))$ 

##  $\text{segema}^2 | \mu, y \sim \text{Inv-}\chi^2(v+n, ((v*\text{segema}^2 + n\bar{y})/(v+n)))$ ,  $v=1/n \sum (y_i - \mu)^2$ 

## Initializing  $(\mu^{(0)}, \text{segema}^2(0)) = (65, 16)$ 

## For each iteration/update,
##  $\mu^{(t)} \sim \mu | \text{segema}^{(t-1)}, y$ 
##  $\text{segema}^2(t) \sim \text{segema}^2 | \mu^{(t)}, y$ 

## and we have data  $y_1 = 70$ ,  $y_2 = 75$  and  $y_3 = 72$ .

## Code for sampling
library("invgamma") ## I will use rinuchisq in this package to sample
## from inverse chi-square distribution
y1<-70
y2<-75
y3<-72
ybar<-mean(c(70,75,72))
ysum<-sum(c(70,75,72))
rho<-0.8
N_iter<-9000

mu<-rep(0,N_iter)
segema<-rep(0,N_iter)
X<-rep(0,N_iter)
mu[1]<-65
segema[1]<-16

for(t in 2:N_iter){
  mu1<-((65/9+ysum/segema[t-1])/(1/9+3/segema[t-1]))
  segema1<-(1/(1/9+3/segema[t-1]))
  mu[t]<-rnorm(1,mu1,sqrt(segema1))

  VV<-function(x,x0){
    return(sum((x-x0)^2))}
}
```

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V<-VV(c(70,75,72),miu[t])

X<-rchisq(1,178)
segema2<-((175*16+V)/(178)
segema[t]<-((178*segema2)/X)

}

### Yes, the chain mixing well, there is no visual evidence of high autocorrelation.
# make a "trace plot" of the draws of theta

## Yes, the Markov Chain appear to converged after 4000 burn-in samples. (because of the
## low correlation)
## I will used first 4000 as burn-in data.
## For the trace plot at 4000:9000 iterations, there is no clear upward/downward trend
## so we conclude the chain has converged.
## The convergence is better for segema than for miu.

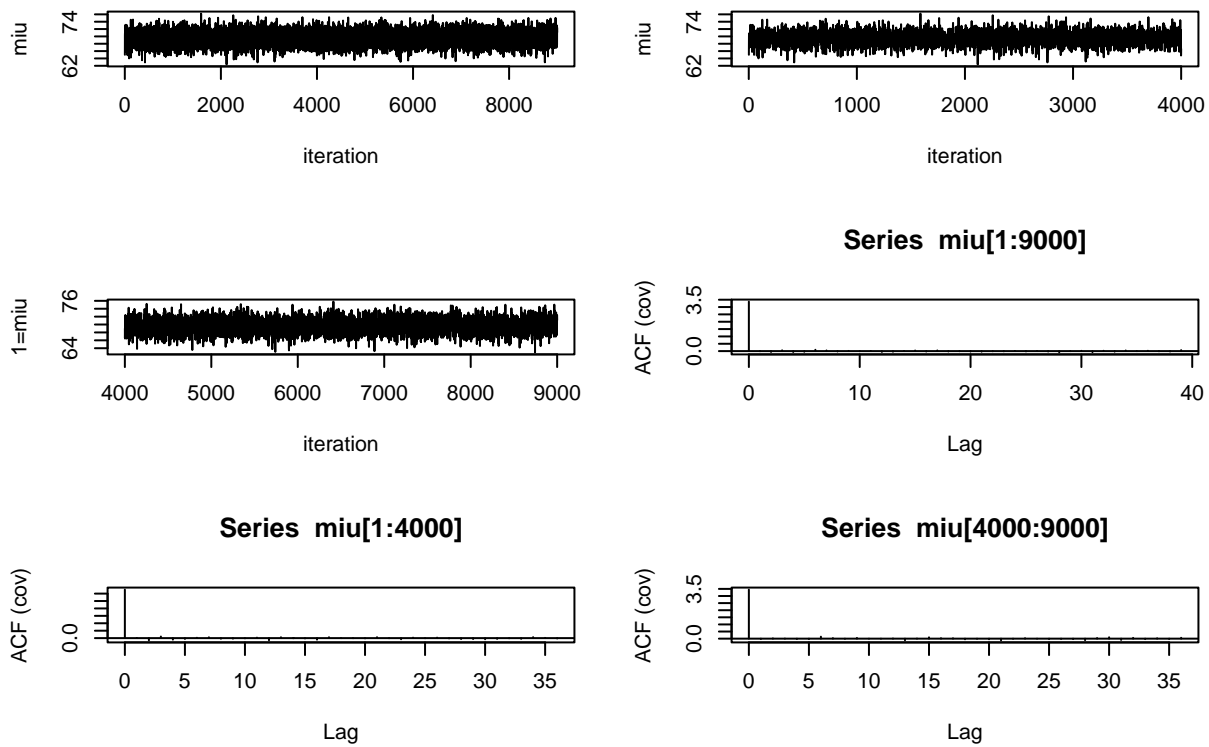
## With the zoom in of both trace and afc plot of miu and segema

## We could see the correlation at 4000:9000 iterations and at 1:4000 iterations
## all have very low autocorrelation and less correlation at 4000:9000 iterations.

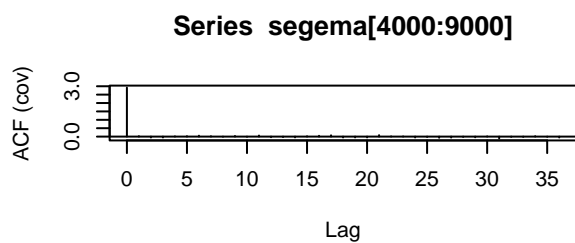
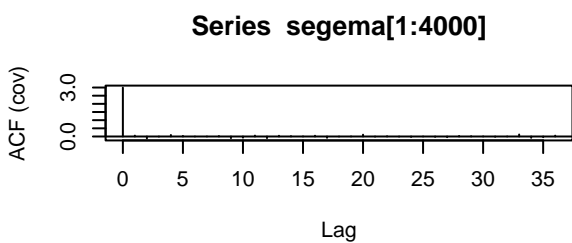
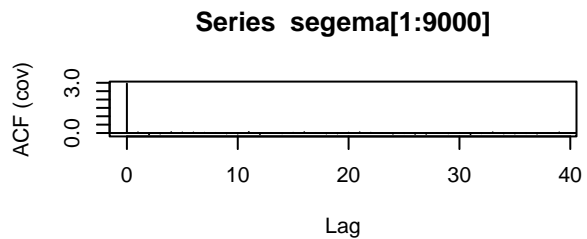
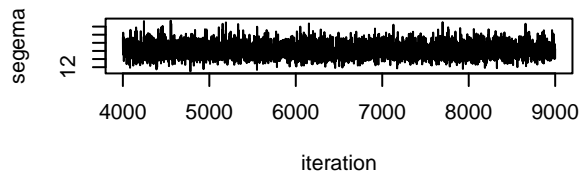
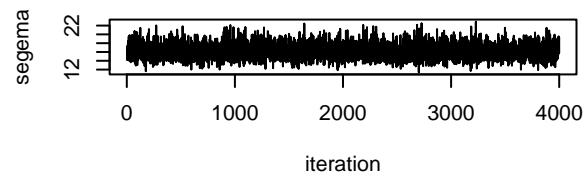
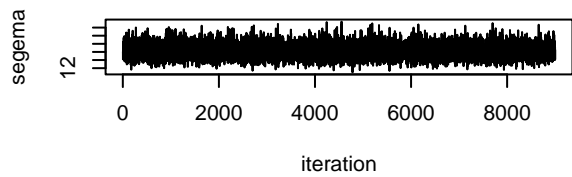
## There is no visual evidence of high autocorrelation. But somehow bit correlated
## The autocorrelation drop down with the iterations go on.

par(mfrow=c(3,2))
plot(x=c(1:9000),y=miu[1:9000],type="l",xlab="iteration",ylab="miu")
plot(x=c(1:4000),y=miu[1:4000],type="l",xlab="iteration",ylab="miu")
plot(x=c(4000:9000),y=miu[4000:9000],type="l",xlab="iteration",ylab="1=miu")
acf(miu[1:9000], type = "covariance")
acf(miu[1:4000], type = "covariance")
acf(miu[4000:9000], type = "covariance")

```



```
par(mfrow=c(3,2))
plot(x=c(1:9000),y=segema[1:9000],type="l",xlab="iteration",ylab="segema")
plot(x=c(1:4000),y=segema[1:4000],type="l",xlab="iteration",ylab="segema")
plot(x=c(4000:9000),y=segema[4000:9000],type="l",xlab="iteration",ylab="segema")
acf(segema[1:9000], type = "covariance")
acf(segema[1:4000], type = "covariance")
acf(segema[4000:9000], type = "covariance")
```



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### (3) two-dimensional plot for miu and segema.
dataa<-as.data.frame(cbind(miu,segema))
library("ggplot2")

colnames(dataa)[1] <- "miu"
colnames(dataa)[2] <- "segema"
ggplot()+geom_point(data =dataa ,aes(miu,segema, color = '1'), alpha = 0.3)
```

