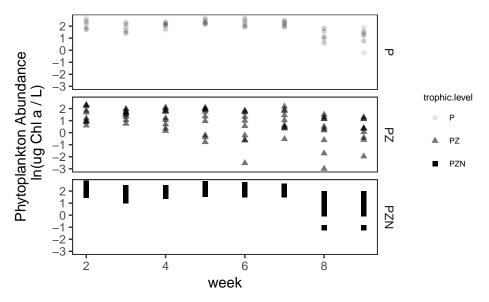
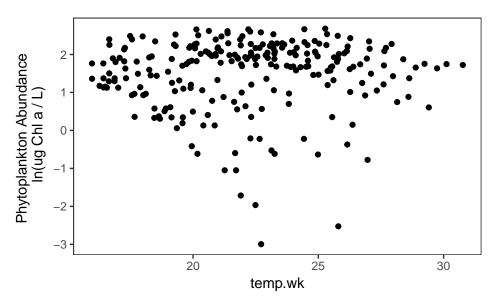
Temperature dependence of biomass and ecosystem function depend on species interactions. Supplementary File 2: Phytoplankton and oxygen flux results in main text.

0.5. Temporal Results: Chlorophyll over time (8 weeks)



```
## Model selection table
                        wek trp.lvl:wek df
                                             logLik AICc delta weight
       (Int) trp.lvl
## CT2 2.542
                   + -0.1161
                                      + 8 -194.716 406.1 0.00 0.922
## CT3 2.819
                   + -0.1665
                                          6 -199.331 411.0 4.97 0.077
## CT4 2.409
                    -0.1665
                                         4 -206.272 420.7 14.66 0.001
## Models ranked by AICc(x)
## Random terms (all models):
## '1 | Tank'
```

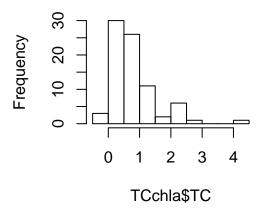
0.5. Temporal Results: Chlorophyll over temperatures



1. Trophic Cascade Results (Figure 2 Main text)

1.1 Trophic cascade (TC) is defined as $\log(\mathrm{PZN/PZ})$ for Chlorophyll a

Histogram of TCchla\$TC



1.1.2 Use nlme to compare fixed and ranefs

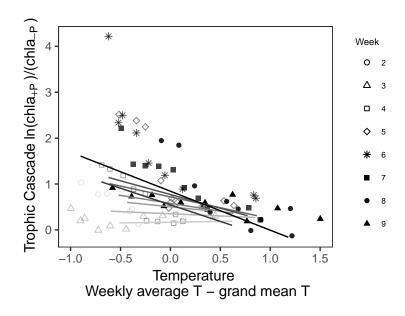
Table S2. 1: Model selection results for Trophic Cascade strength (Chl a) for linear mixed effects model

	Int	Т	Wk	T*Wk	df	logLik	AICc	d	W
TCmodb	0.18	0.03	0.13	-0.13	6	-73.17	159.50	0.00	0.749796131
TCmodc	-0.02	-0.82	0.15	NA	5	-75.55	161.91	2.41	0.224356212
TCmode	0.57	NA	0.05	NA	4	-79.67	167.88	8.39	0.011316356
TCmodf	0.57	NA	0.05	NA	4	-79.67	167.88	8.39	0.011316356
TCmodd	0.83	0.00	NA	NA	4	-80.93	170.40	10.90	0.003214947

Summary of best model: trophic cascade strength

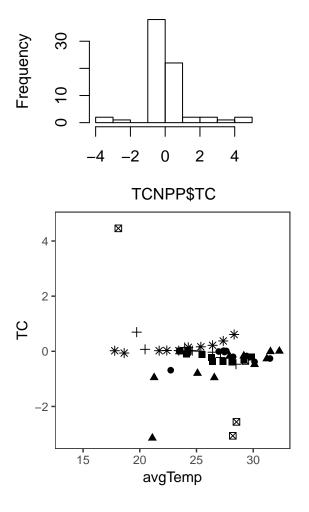
```
## Linear mixed-effects model fit by maximum likelihood
   Data: TCchla
##
         AIC
                  BIC
                         logLik
     158.345 172.6371 -73.17248
##
##
## Random effects:
   Formula: ~1 | power
##
           (Intercept) Residual
            0.1498711 0.5883612
## StdDev:
##
## Fixed effects: TC ~ 1 + I(invTavg - mean(invTavg)) * week
                                        Value Std.Error DF
                                                             t-value p-value
## (Intercept)
                                    0.1800156 0.2347745 67 0.766760 0.4459
## I(invTavg - mean(invTavg))
                                    0.0312063 0.4087578 67 0.076344 0.9394
                                    0.1334953 0.0379404 67 3.518551 0.0008
## I(invTavg - mean(invTavg)):week -0.1257280 0.0572430 67 -2.196390 0.0315
  Correlation:
                                   (Intr) I(nT-m(T)) week
## I(invTavg - mean(invTavg))
                                    0.530
                                   -0.920 -0.424
## I(invTavg - mean(invTavg)):week -0.335 -0.906
                                                      0.187
## Standardized Within-Group Residuals:
           Min
                        Q1
                                   Med
## -2.21341355 -0.48187644 -0.06052218 0.43164327
##
## Number of Observations: 80
## Number of Groups: 10
## Approximate 95% confidence intervals
##
## Fixed effects:
##
                                         lower
                                                     est.
## (Intercept)
                                   -0.27673063 0.1800157 0.63676193
## I(invTavg - mean(invTavg))
                                   -0.76401909 0.0312063
                                                          0.82643170
                                    0.05968344 0.1334953 0.20730721
## I(invTavg - mean(invTavg)):week -0.23709240 -0.1257280 -0.01436351
## attr(,"label")
## [1] "Fixed effects:"
##
##
   Random Effects:
##
    Level: power
                        lower
                                   est.
## sd((Intercept)) 0.02252525 0.1498711 0.9971638
##
   Within-group standard error:
##
       lower
                  est.
## 0.4932259 0.5883612 0.7018465
```

Figure S2. 2: Trophic Cascade strength by temperature and week



1.2. Strength of trophic cascade on NPP2

Histogram of TCNPP\$TC

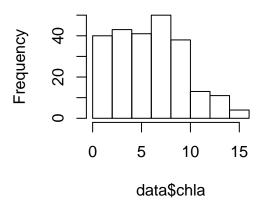


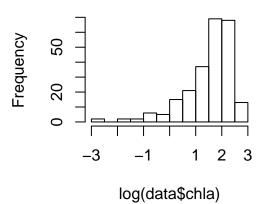
2.1 Phytoplankton abundance (for Figure 3, Table 2 main text)

Figure S2. 3: Chlorophyll a concentration

Histogram of data\$chla

Histogram of log(data\$chla)





2.1.1 Phytoplankton abundance candidate models

Table S2. 2: Model selection results for Phytoplankton (Chl a) for linear mixed effects model

	Int	TL	Tw	Tt	$\mathrm{Tw}^*\mathrm{Tt}$	$\mathrm{Tw}^*\mathrm{TL}$	$\mathrm{Tt}^*\mathrm{TL}$	df	logLik	AICc	d	W
$\overline{\mathrm{modPB8}}$	2.05	+	-0.66	1.30	NA	+	+	11	-162.86	348.87	0.00	9.528923e-01
modPB7	2.05	+	-0.96	1.30	NA	NA	+	9	-168.05	354.89	6.02	4.698179 e-02
modPBF	2.14	+	-0.52	2.16	1.34	+	NA	10	-172.89	366.74	17.86	1.259313e-04
modPB4	1.50	NA	-0.96	1.70	0.96	NA	NA	6	-207.95	428.26	79.38	5.511062e-18
modPB6	1.91	+	-0.66	NA	NA	+	NA	8	-206.58	429.79	80.92	2.557666e-18
modPB3	1.50	NA	-0.96	1.71	NA	NA	NA	5	-211.74	433.74	84.86	3.556642e-19
modPB5	1.91	+	-0.96	NA	NA	NA	NA	6	-211.45	435.27	86.40	1.653514e-19
modPB2	1.50	NA	-0.96	NA	NA	NA	NA	4	-218.40	444.98	96.11	1.286913e-21
modPB1	1.90	+	NA	NA	NA	NA	NA	5	-257.21	524.68	175.81	6.345675 e-39
modPB0	1.49	NA	NA	NA	NA	NA	NA	3	-264.15	534.41	185.54	4.902314e-41

Table S2. 3: Parameter estimates from model PB8 (Table S2.1) for Phytoplankton (Chl a) for linear mixed effects model

	Ea	lower	upper
P	1.30	0.85	1.76
PZ	3.15	2.76	3.54
PZN	1.65	1.19	2.10

2.2 Net ecosystem oxygen production

Histogram of data1\$NPP2 Histogram of log(data1\$NPP2

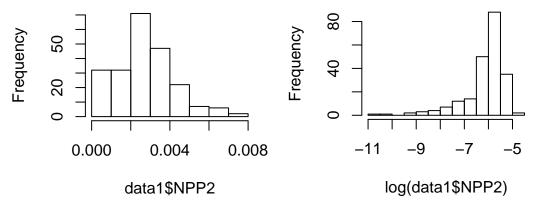


Table S2. 4: Model selection results for Net Ecosystem Oxygen Production, with 1|Tank as a random effect. Model terms are: intercept (Int), trophic treatment (TL), Temperature - weekly average (Tw), temperature - expt average (Tt), interaction terms and statistical estimates

-	Int	TL	Tw	Tt	Tw*Tt	Tw*TL	Tt*TL	df	logLik	AICc	d	W
$\overline{\mathrm{modNPP8}}$	-6.42	+	0.29	-1.41	NA	+	+	11	-266.46	556.20	0.00	3.880444e-01
$\operatorname{modNPPF}$	-6.42	+	0.37	-1.42	0.84	+	+	12	-265.54	556.59	0.39	3.199070e-01
modNPP7	-6.41	+	0.03	-1.39	NA	NA	+	9	-269.68	558.21	2.01	1.421772e-01
modNPP3	-6.15	NA	0.02	-0.96	NA	NA	NA	5	-274.37	559.02	2.81	9.506575 e-02
modNPP4	-6.15	NA	0.02	-0.96	0.61	NA	NA	6	-273.87	560.13	3.92	5.458021 e-02
modNPP0	-6.15	NA	NA	NA	NA	NA	NA	3	-283.15	572.41	16.20	1.177095e-04
modNPP2	-6.15	NA	0.03	NA	NA	NA	NA	4	-283.13	574.44	18.24	4.256459 e - 05
modNPP1	-6.26	+	NA	NA	NA	NA	NA	5	-282.25	574.78	18.58	3.589977e-05
modNPP6	-6.26	+	0.27	NA	NA	+	NA	8	-279.83	576.34	20.14	1.642404 e - 05
modNPP5	-6.26	+	0.03	NA	NA	NA	NA	6	-282.23	576.85	20.65	1.275902 e-05

NPP Coefficients

Table S2. 5: Parameter estimates from model NPP8 (Table S2.3) for Net Ecosystem Oxygen Productivity (NEP) for linear mixed effects model (For MS Figure 3)

	Ea	lower	upper
P	-1.41	-2.25	-0.58
PZ	-1.21	-2.36	-0.07
PZN	-0.99	-2.10	0.12

2.2 Net ecosystem oxygen consumption (ER)

Histogram of data\$ER2 Histogram of log(data\$ER2)

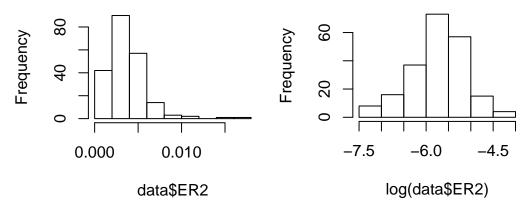


Table S2. 6: Model selection results for Net Ecosystem Respiration, with 1|Tank as a random effect. Model terms are: intercept (Int), trophic treatment (TL), Temperature - weekly average (Tw), temperature - expt average (Tt), interaction terms and statistical estimates

•	Int	TL	Tw	Tt	Tw*Tt	Tw*TL	Tt*TL	df	logLik	AICc	d	W
$\overline{\mathrm{modER7}}$	-6.03	+	0.26	-1.32	NA	NA	+	9	-158.72	336.33	0.00	8.117512e-01
modER8	-6.03	+	0.19	-1.32	NA	+	+	11	-158.19	339.72	3.39	1.492212e-01
modERF	-5.98	+	0.25	-0.81	0.57	+	NA	10	-160.65	342.41	6.08	3.885201 e- 02
modER3	-5.74	NA	0.26	-0.68	NA	NA	NA	5	-172.34	354.98	18.64	7.257027e-05
modER4	-5.74	NA	0.26	-0.64	0.60	NA	NA	6	-171.28	354.98	18.65	7.255858e-05
modER5	-5.89	+	0.26	NA	NA	NA	NA	6	-172.51	357.43	21.09	2.134098e-05
modER6	-5.89	+	0.19	NA	NA	+	NA	8	-172.00	360.71	24.38	4.134606e-06
modER1	-5.90	+	NA	NA	NA	NA	NA	5	-175.56	361.42	25.09	2.892592e-06
modER2	-5.74	NA	0.26	NA	NA	NA	NA	4	-177.02	362.24	25.90	1.927201 e-06
modER0	-5.76	NA	NA	NA	NA	NA	NA	3	-180.12	366.35	30.02	$2.461395 \mathrm{e}\text{-}07$

ER coefficients

Table S2. 7: Confidence intervals for model ER7 (Table S2.5) (For MS Figure 3

	Ea	lower	upper
P	-1.3163396	-1.8455347	-0.7871445
PZ	-0.8777488	-1.3246951	-0.4308026
PZN	-0.3295142	-0.8562013	0.1971728

Figure 3 (Full)

Figure S2. 5: Manuscript figure 3: Effects of temperature on oxygen flux and phytoplankton standing stock

