Ukulelor Formulation

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The statement of the use case is on Mip Wise's website: www.mipwise.com/use-cases/use-case-name.

For a beginner-friendly formulation, see ukulelor.ipynb.

Input Data Model

Indices

• *I*: Collection of retailers.

Parameters

- pu: Production upper bound (units), i.e., production capacity of the factory.
- *sl*: Shipment lower bound (units), i.e., minimum shipment quantity to avoid penalty.
- pn: Penalty (num. of units) paid for each order that has less than S ukuleles shipped.
- p_i : Unit price at which ukuleles are sold to retailer i.
- d_i : Demand (units) of ukuleles from retailer i.

Decision Variables

- x_i : The number of ukuleles shipped to retailer i.
- z_i : Equals 1 if Ted ships to retailer i, 0 otherwise.

Constraints

· C1) Production capacity:

$$\sum_i x_i \leq pu.$$

• C2) If ship to retailer i, then ship at least 50:

$$sl \cdot z_i \leq x_i, \quad orall i.$$

• C3) If no shipping to retailer i, then $x_i = 0$:

$$x_i \leq d_i \cdot z_i, \quad \forall i.$$

Objective

The objective is to maximize total profit, which is total revenue minus penalty.

revenue =
$$\sum_{i} p_i \cdot x_i$$
.

penalty =
$$\sum_{i} pn \cdot p_i \cdot (1 - z_i)$$
.

Final Formulation

Putting everything together, we obtain:

$$egin{aligned} \min & \sum_{i} p_{i} \cdot x_{i} - \sum_{i} pn \cdot p_{i} \cdot (1 - z_{i}) \ \mathrm{s.t.} & \sum_{i} x_{i} \leq pu, \ & sl \cdot z_{i} \leq x_{i}, \quad orall i, \ & x_{i} \leq d_{i} \cdot z_{i}, \quad orall i, \ & x_{i} \geq 0, z_{i} \in \{0, 1\} \quad orall i. \end{aligned}$$