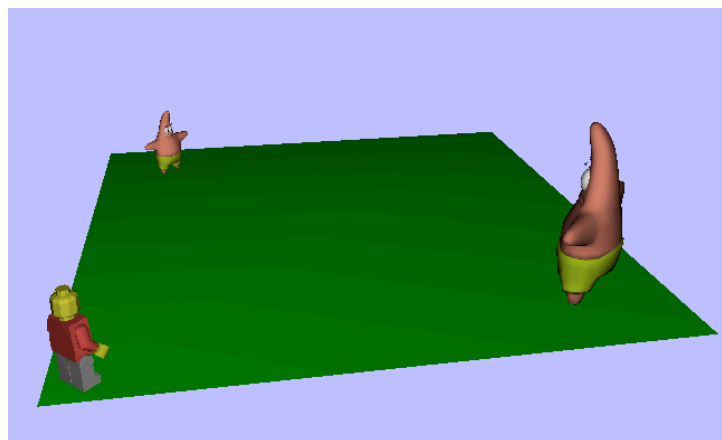
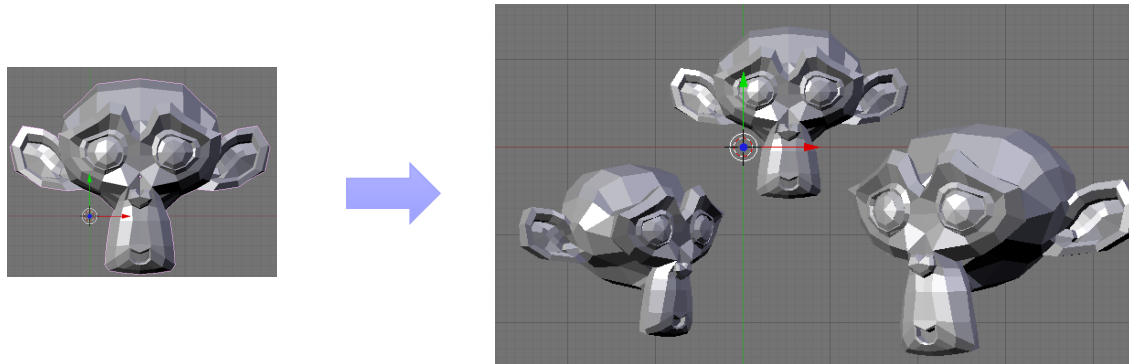




# Exercicis TG

## IDI- 2016-2017

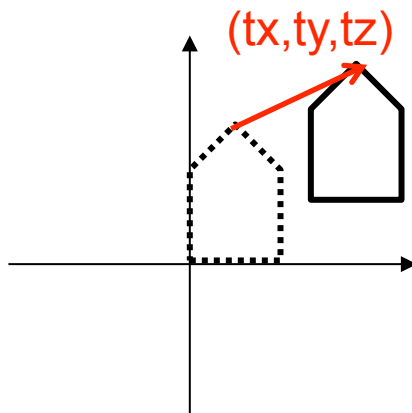
# MOTIVACIÓ: càlcul de la TG a aplicar a models



Transformació  
geomètrica

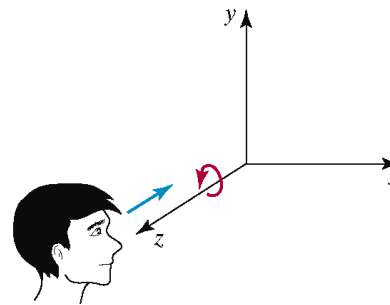


Matriu 4x4  
TG



$T(tx, ty, tz)$

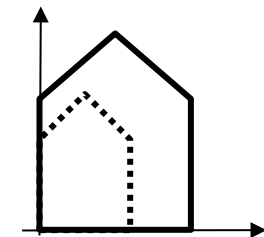
$$T(t_x, t_y, t_z) = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



(a)

$G_z(\text{angle})$

$$G_z(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 & 0 \\ \sin \alpha & \cos \alpha & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

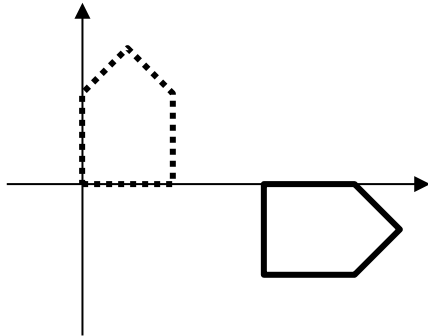


$S(s_x, s_y, s_z)$

$$S(s_x, s_y, s_z) = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

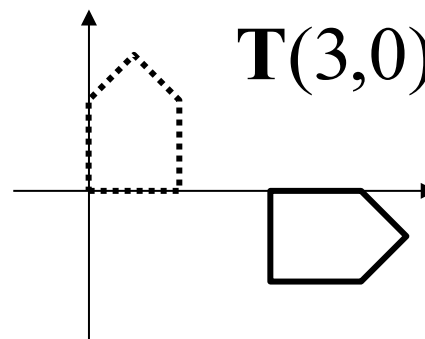
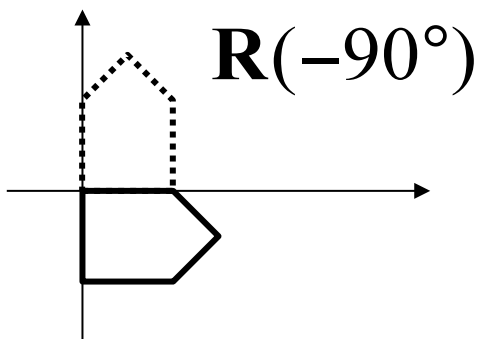
# Composició de Transformacions

- Imaginem que volem



No es pot fer amb cap de les matrius anteriors

- Cal composar/efectuar dues transformacions



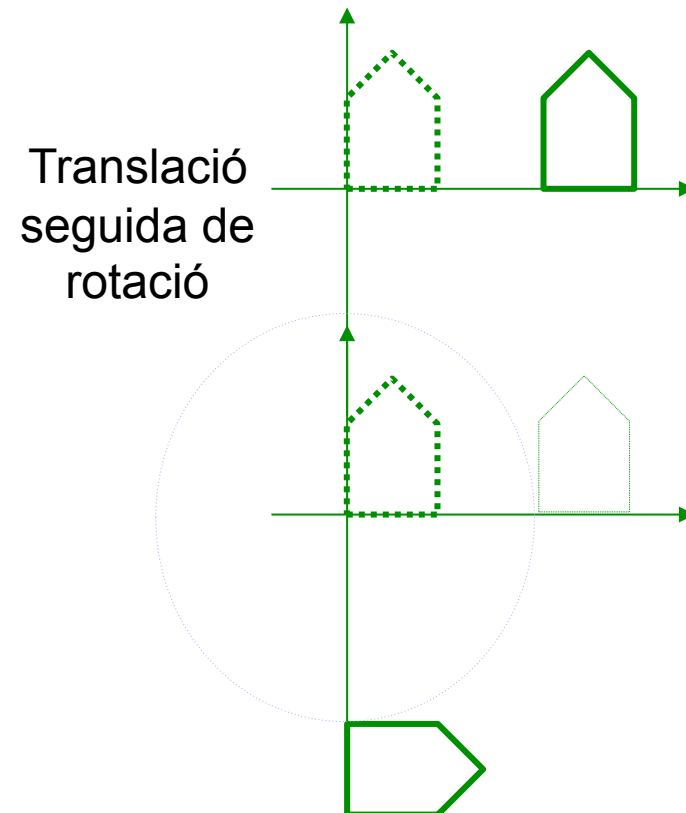
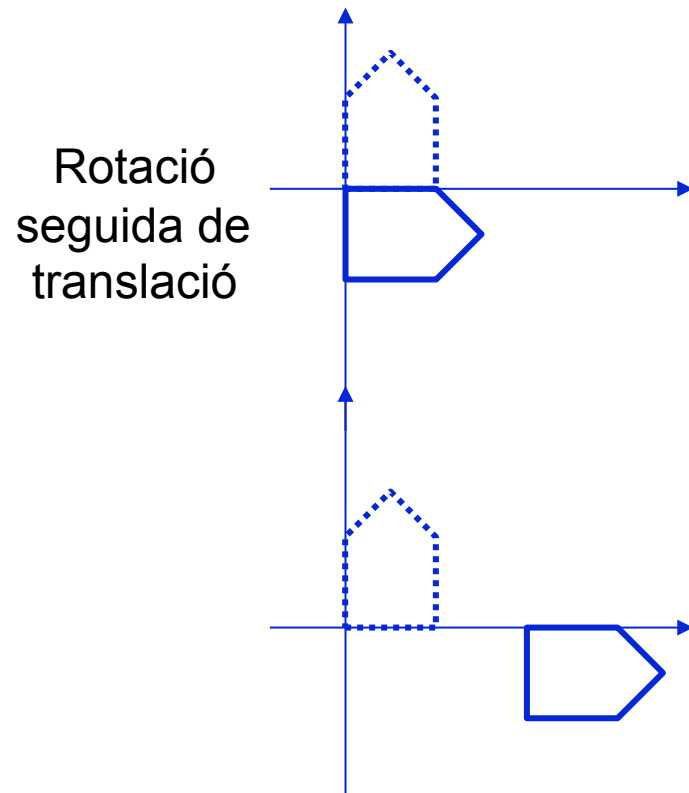
$$M = T(3,0) \cdot R(-90^\circ)$$

$$P' = T(3,0) \cdot (R(-90^\circ) P) = \underbrace{(T(3,0) \cdot R(-90^\circ))}_{\text{red arrow}} P = M \cdot P$$

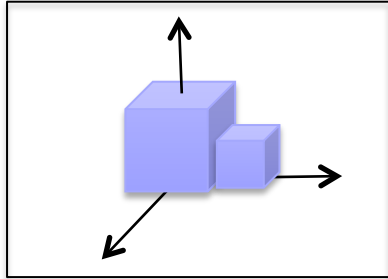
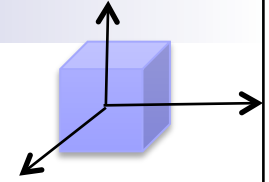
# Composició de Transformacions

$$\underset{\textcircled{2}}{T(3,0)} \cdot \underset{\textcircled{1}}{R(-90^\circ)} \neq \underset{\textcircled{2}}{R(-90^\circ)} \cdot \underset{\textcircled{1}}{T(3,0)}$$

- Multiplicació de matrius no és commutativa



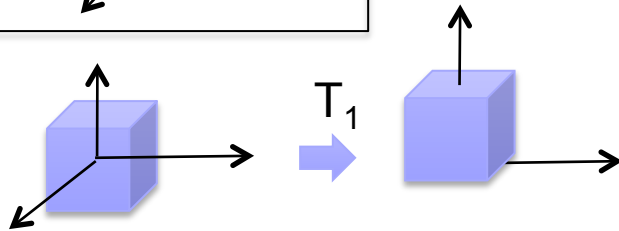
# Exemple simple de TG (1)



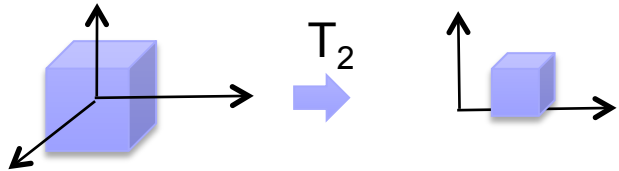
Escena a pintar utilitzant pinta\_cub()

Pseudo-codi

```
TG= Translate(0,0.5,0);  
modelMatrix(TG);  
pinta_cub ();  
TG= Translate(0.75,0.25,0);  
TG= TG*Scale(0.5,0.5,0.5);  
modelMatrix (TG);  
pinta_cub();
```



$$T_1 = \text{Trans}(0, 0.5, 0)$$



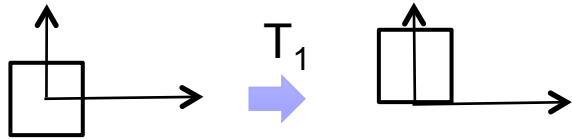
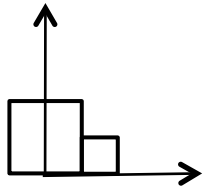
$$T_2 = \text{Trans}(0.75, 0.25, 0) * S(0.5, 0.5, 0.5)$$

```
glm::mat4 TG;  
TG= glm::translate (glm::mat4(1.f),glm::vec3(0,0.5,0));  
glUniformMatrix4fv (transLoc, 1, GL_FALSE, &TG[0][0]);  
pinta_cub ();
```

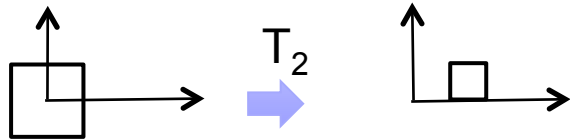
```
TG= glm::translate (glm::mat4(1.f),  
glm::vec3(0.75,0.25,0));  
TG= gml::scale(TG, glm::vec3(0.5,0.5,0.5));  
glUniformMatrix4fv (transLoc, 1, GL_FALSE, &TG[0][0]);  
pinta_cub();
```

Com faríeu per a girar els dos cubs respecte l'eix x?

## Exemple simple (2)



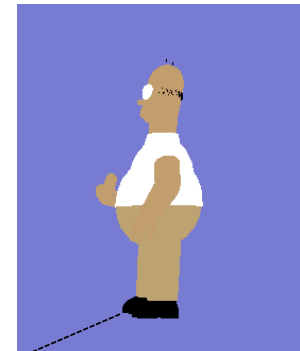
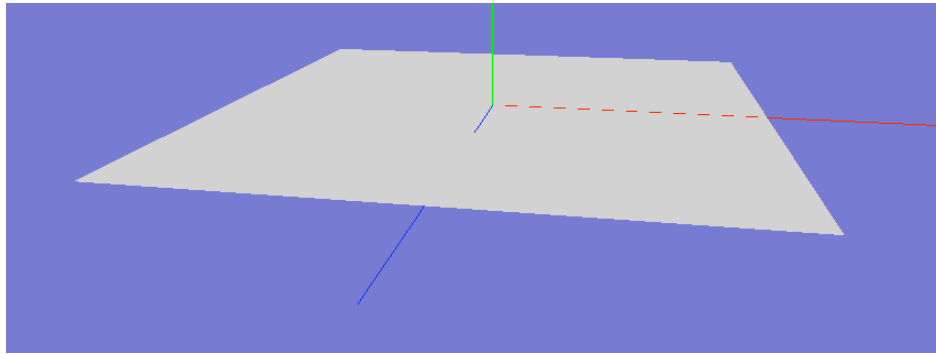
$$T_1 = G_x(\text{alfa}) * \text{Trans}(0, 0.5, 0)$$



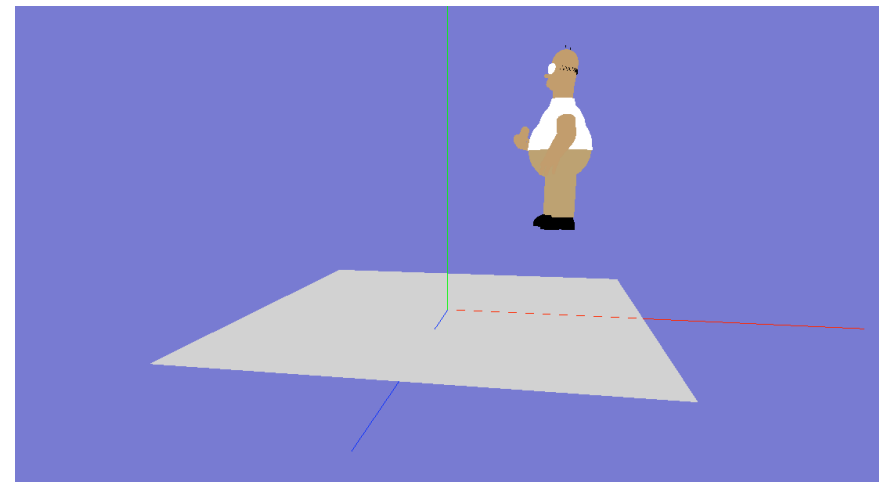
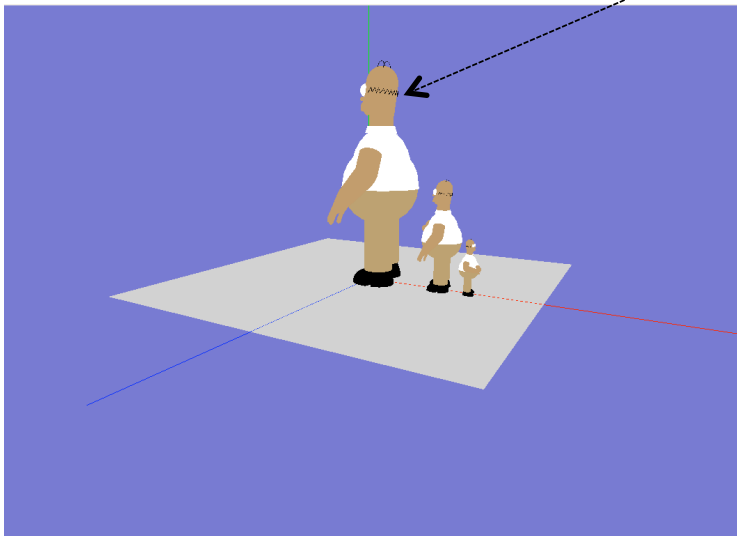
$$T_2 = G_x(\text{alfa}) * \text{Trans}(0.75, 0.25, 0) * S(0.5, 0.5, 0.5)$$

```
glm::mat4 TG, AUX;  
AUX=glm::rotate(glm::mat4(1.f), alfa, vec3(1,0,0));  
TG= glm::translate(AUX, glm::vec3(0,0.5,0));  
modelMatrix(TG); pinta_cub();  
TG= glm::translate(AUX, glm::vec3(0.75,0.25,0));  
TG= glm::scale(TG, glm::vec3(0.5,0.5,0.5));  
modelMatrix(TG);  
pinta_cub();
```

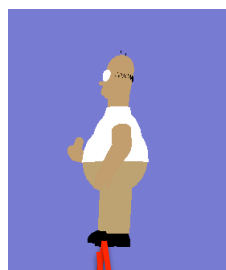
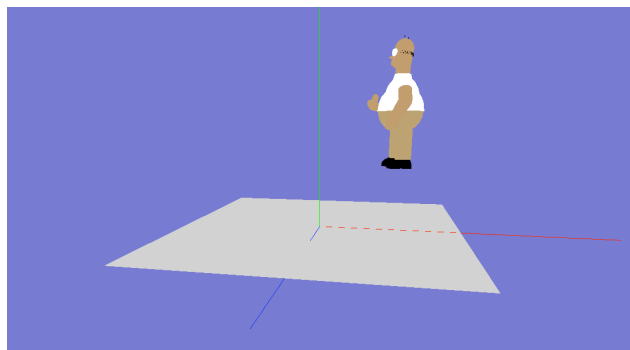
# Exercici 1



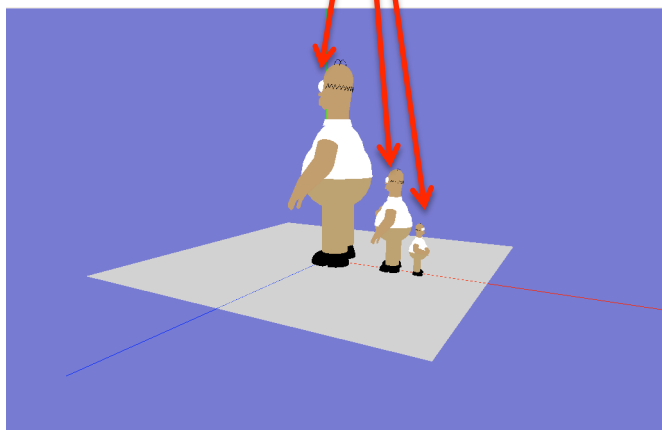
*Mateixa grandària*







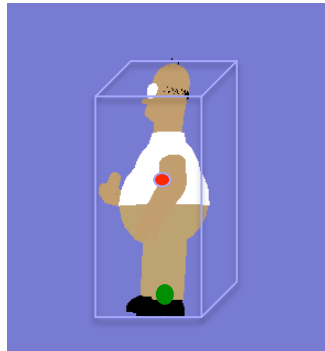
Nomes càlcul de TG



Transformació  
geomètrica



Matriu 4x4  
TG

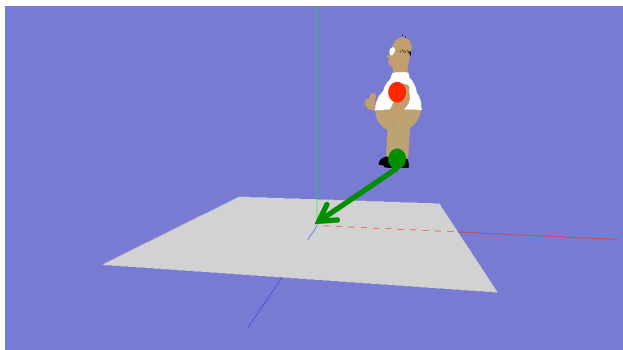


$CapsaMinCont = (xmin, ymin, zmin, xmax, ymax, zmax)$

Mides  $\Rightarrow a = (xmax - xmin)$ ,  $h = (ymax - ymin)$ ,  $f = (zmax - zmin)$

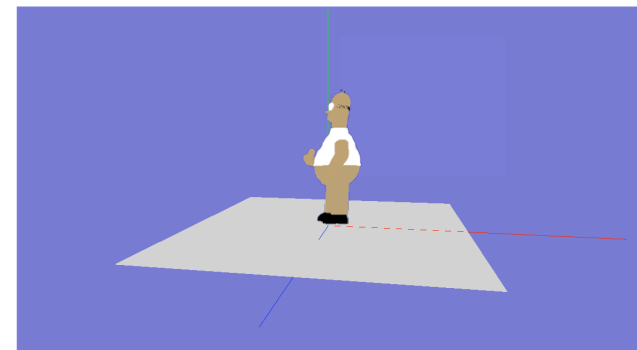
$CentBaseCapsa = (cbx, cby, cbz) = (xmin + xmax)/2, ymin, (zmin + zmax)/2)$

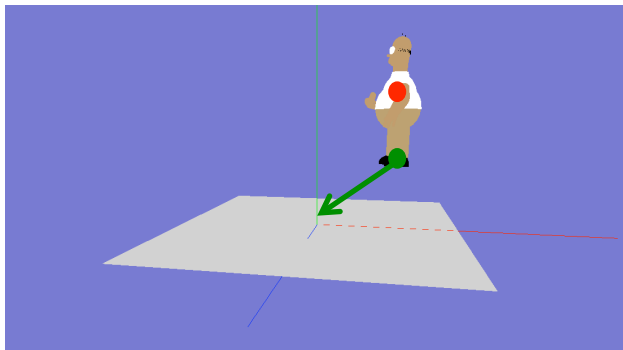
Els podem afegir com atributs al model geomètric



$TG_{H1} = \text{Trans}(t)$

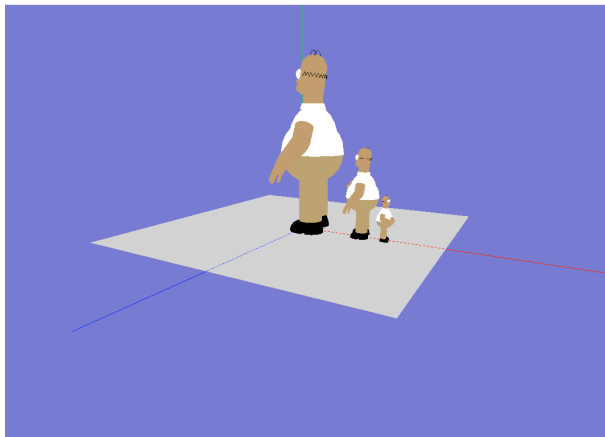
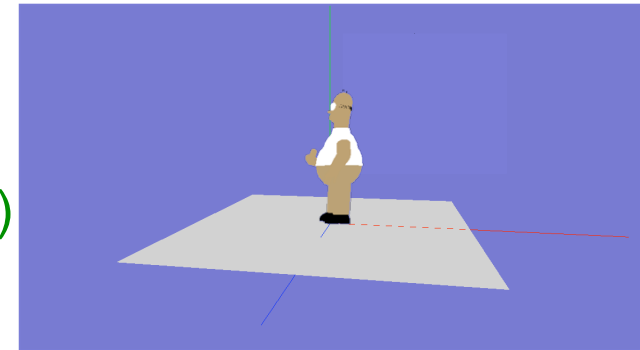
$t = (-cbx, -cby, -cbz)$



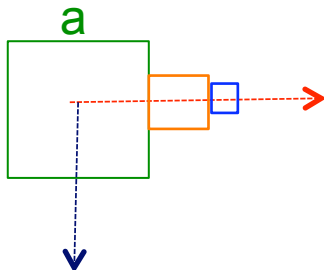


$$TG_{H1} = \text{Trans}(t)$$

$$t = (-cbx, -cby, -cbz)$$



$$TG_{H2} = \text{Trans}(3a/4, 0, 0) S(1/2, 1/2, 1/2) \text{Trans}(t)$$

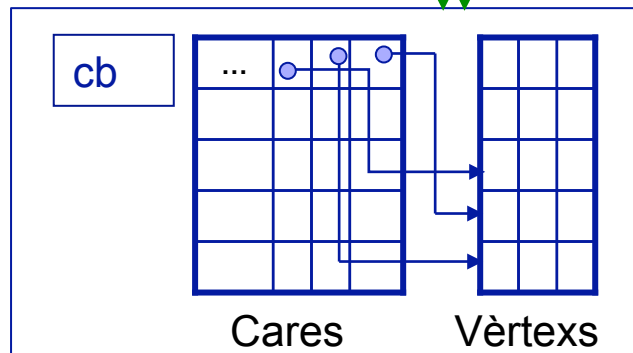
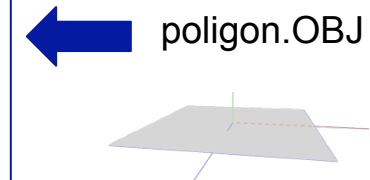
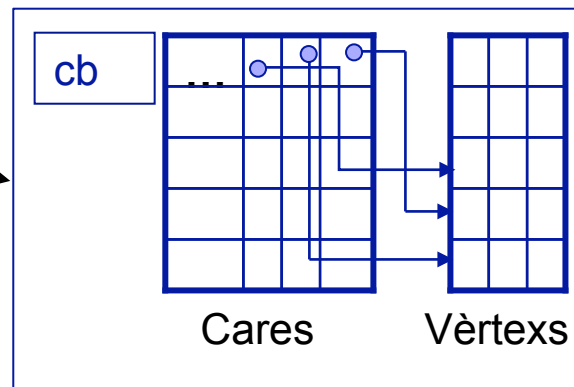


$$TG_{H3} = \text{Trans}(9a/8, 0, 0) S(1/4, 1/4, 1/4) R_y(-180) \text{Trans}(t)$$

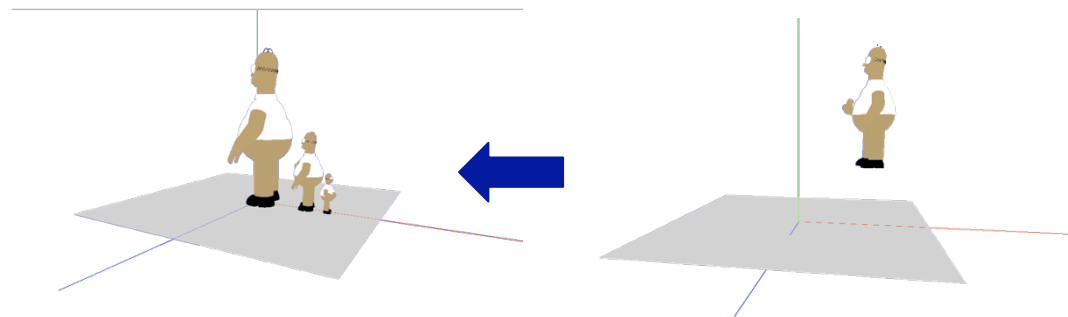
$$TG_{H3} = \text{Trans}(9a/8, 0, 0) R_y(-180) S(1/4, 1/4, 1/4) \text{Trans}(t)$$

# Visualització OpenGL: models en SCM i paràmetres

nom	s, pos,...	
Terra		
Homer-1		
Homer-2		
Homer-3		



Homer.OBJ



$$TG_{H1} = \text{Trans}(t) \quad t = (-cbx, -cby, -cbz)$$

$$TG_{H2} = \text{Trans}(3a/4, 0, 0) S(1/2, 1/2, 1/2) \text{Trans}(t)$$

$$TG_{H2} = \text{Trans}(9a/8, 0, 0) S(1/4, 1/4, 1/4) R_y(-180^\circ) \text{Trans}(t)$$

4

3

2

1

## Visualització OpenGL: models en SCM

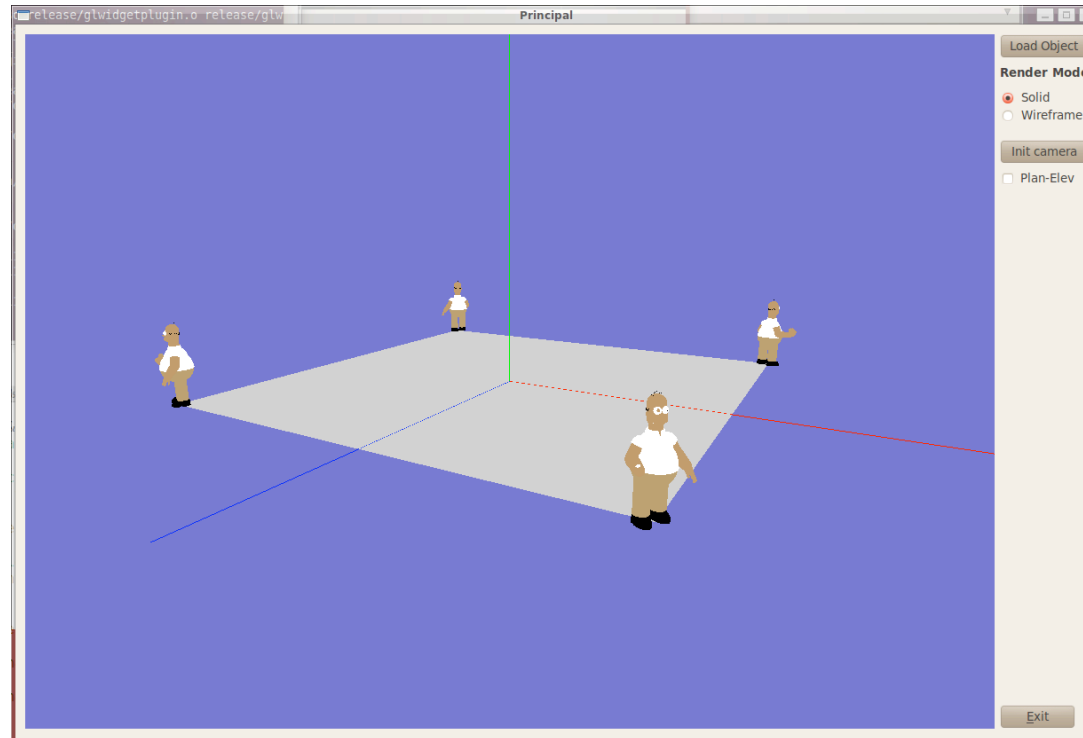
```
per cada objectei  
  //Càlcul TGi i enviar a OpenGL  
  modelTransformi()  
  pinta_modeli();  
fper
```

4                      3                      2                      1 →

$$TG_{H3} = \text{Trans}(7a/8, 0, 0) S(1/4, 1/4, 1/4) R_y(-180^\circ) \text{Trans}(t)$$

```
modelTransform()  
  //tercer homer  
  {  
    TG=I;  
    TG= TG*Translate(posx, posy, posz);  
    TG= TG*Scale(s, s, s);  
    TG= TG*Rotate(-180, (0, 1, 0));  
    TG= TG*Translate(-cb.x, -cb.y, -cb.z);  
    modelMatrix(TG); //enviar uniform  
  }  
  
  pinta_homer();
```

# Exercicis



Mireu la col·lecció de problemes del racó.  
Proposta de mínims: 16, 19, 24, 25