Tougaloo College MAT222 - Calculus II Howework 09 - Spring, 2025

7.3 Exercises

1. Evaluate the integral.

(a)
$$\int \frac{x^2}{\sqrt{9-x^2}} dx$$

Solution: Use the substitution $x = 3 \sin \theta$

$$\frac{9}{2} \left\{ \sin^{-1}(x/3) - \frac{x\sqrt{9-x^2}}{9} \right\} + C$$

(b)
$$\int_0^{1/2} x\sqrt{1-4x^2} \, dx$$

Solution: Use the substitution $x = 2\sin\theta$. Then we have $\frac{1}{12}$