#### MT222: Calculus II

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# 7.3 - Trigonometric Substitution

## Table of Trigonometric Substituution

#### **Table of Trigonometric Substitutions**

Expression	Substitution	Identity
$\sqrt{a^2-x^2}$	$x = a \sin \theta,  -\frac{\pi}{2} \le \theta \le \frac{\pi}{2}$	$1 - \sin^2 \theta = \cos^2 \theta$
$\sqrt{a^2+x^2}$	$x = a \tan \theta,  -\frac{\pi}{2} < \theta < \frac{\pi}{2}$	$1 + \tan^2\theta = \sec^2\theta$
$\sqrt{x^2-a^2}$	$x = a \sec \theta$ , $0 \le \theta < \frac{\pi}{2}$ or $\pi \le \theta < \frac{3\pi}{2}$	$\sec^2\theta - 1 = \tan^2\theta$

Find

$$\int \frac{1}{x^2 \sqrt{x^2 + 4}} \ dx$$

Find

$$\int \frac{x}{\sqrt{x^2 + 4}} dx$$

Evaluate

$$\int \frac{dx}{\sqrt{x^2 - a^2}},$$

where a > 0.

#### Evaluate

$$\int \frac{dx}{\sqrt{x^2 - a^2}},$$

where a > 0. (Use Hyperbolic functions)