

MAT102 - College Algebra - Polynomial and Rational Functions

3.1 Quadratic Functions and Applications [1]

Miraj Samarakkody

Tougaloo College

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Graph a Quadratic Function Written in Vertex Form

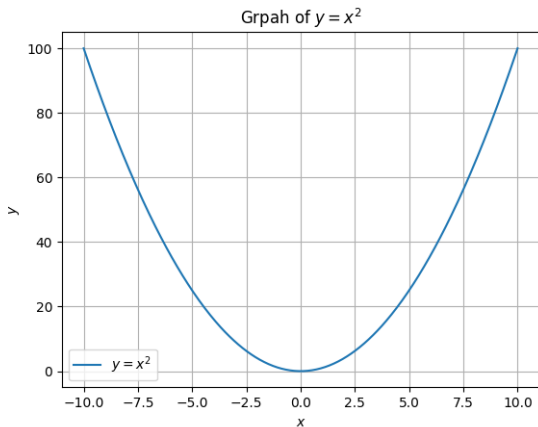
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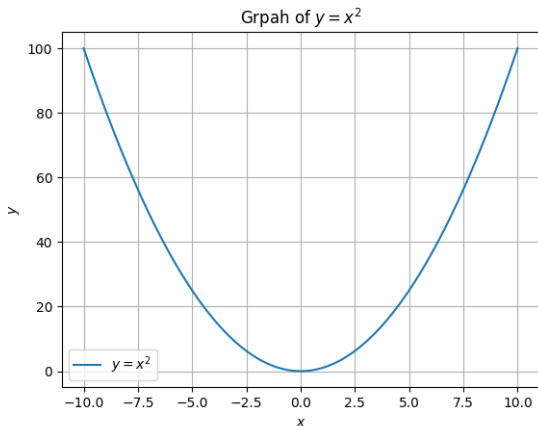
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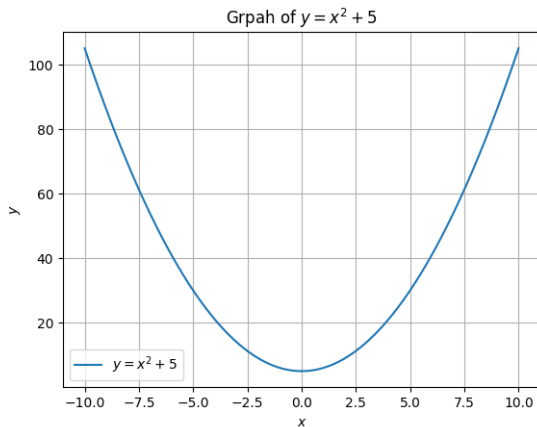


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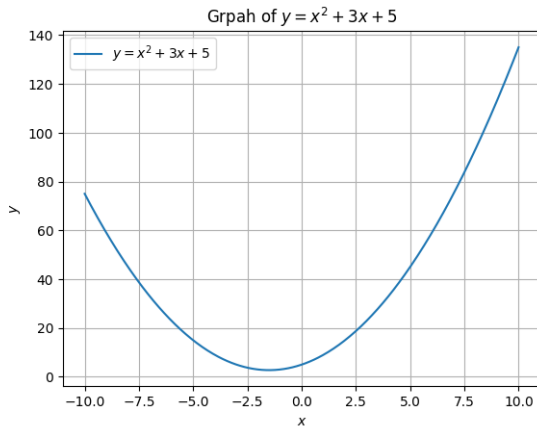
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- ▶ The axis of symmetry is $x = h$. This is the vertical line that passes through the vertex.

Example - Analyzing and Graphing a Quadratic Function

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8. Write down the domain and range in interval notation.

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References



Julie Miller and Donna Gerken.

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McGraw-Hill Education, New York, 2nd edition, 2016.