# MAT102 - College Algebra - Polynomial and Rational Functions

## 3.1 Quadratic Functions and Applications [1]

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# Graph a Quadratic Function Written in Vertex Form

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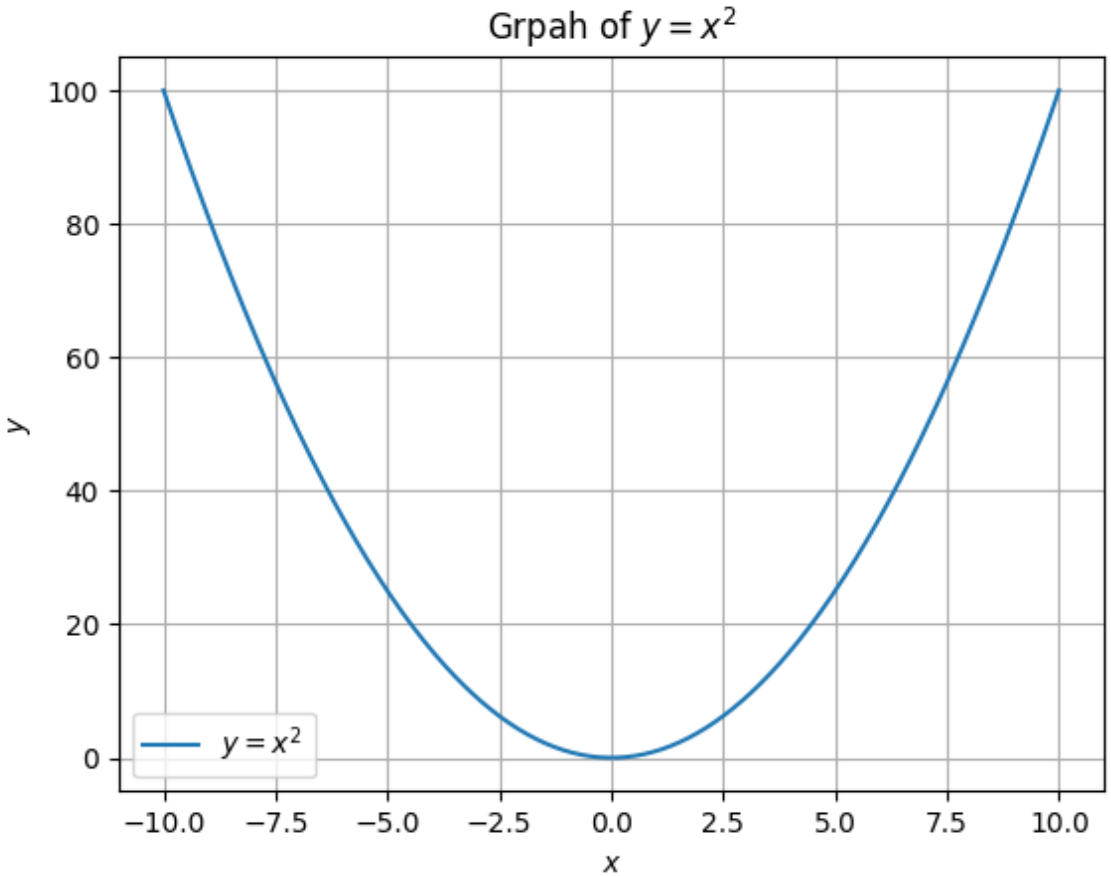

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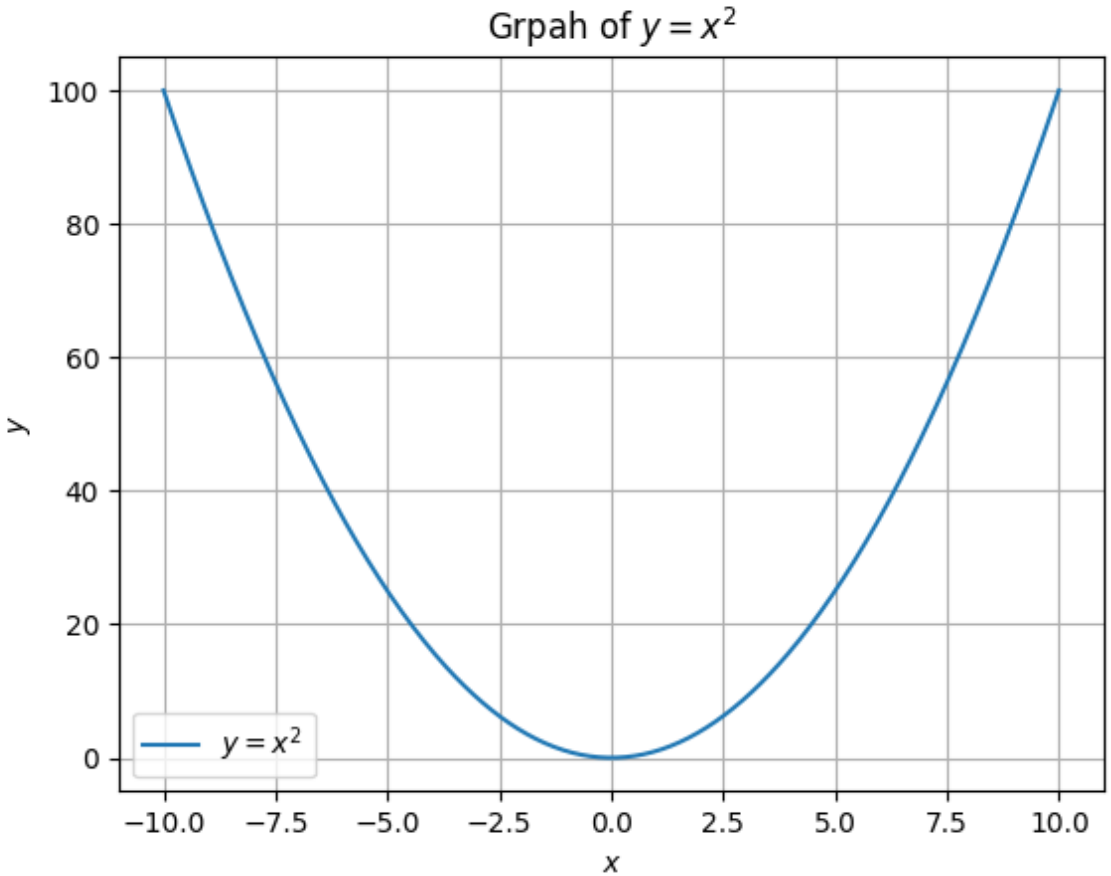

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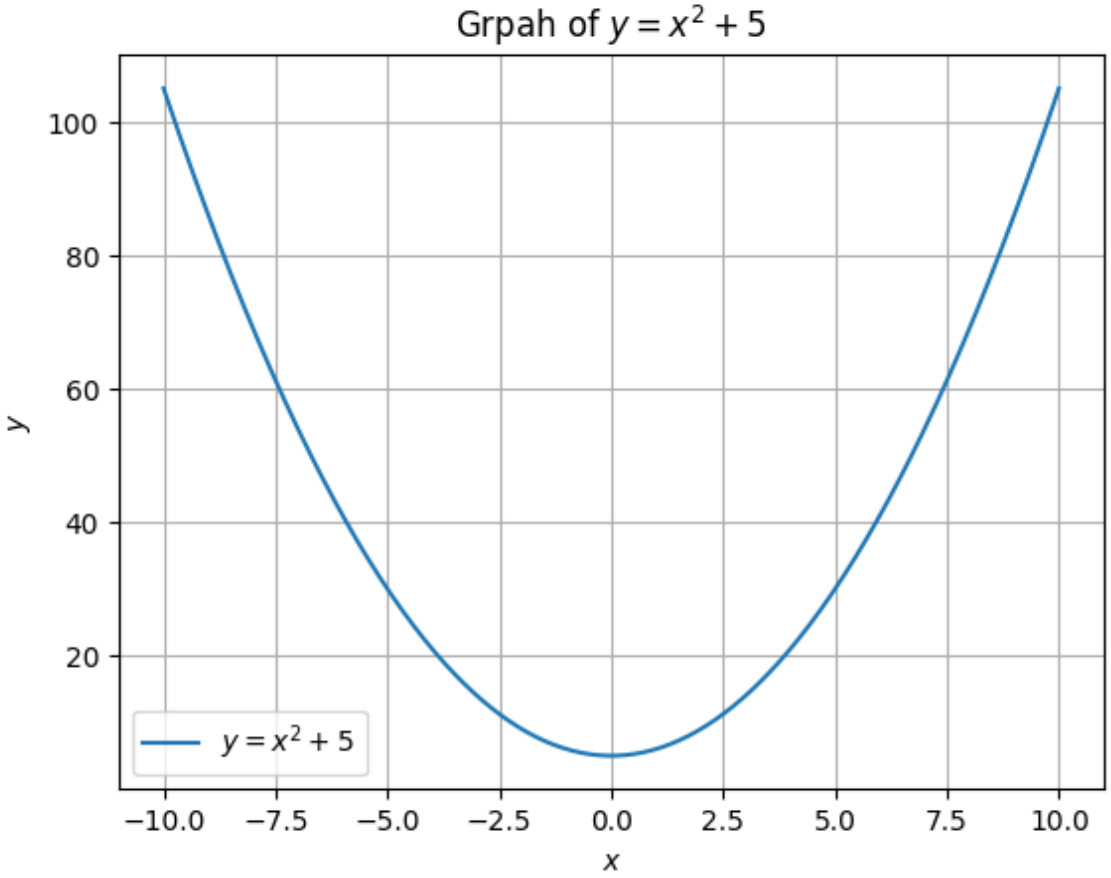

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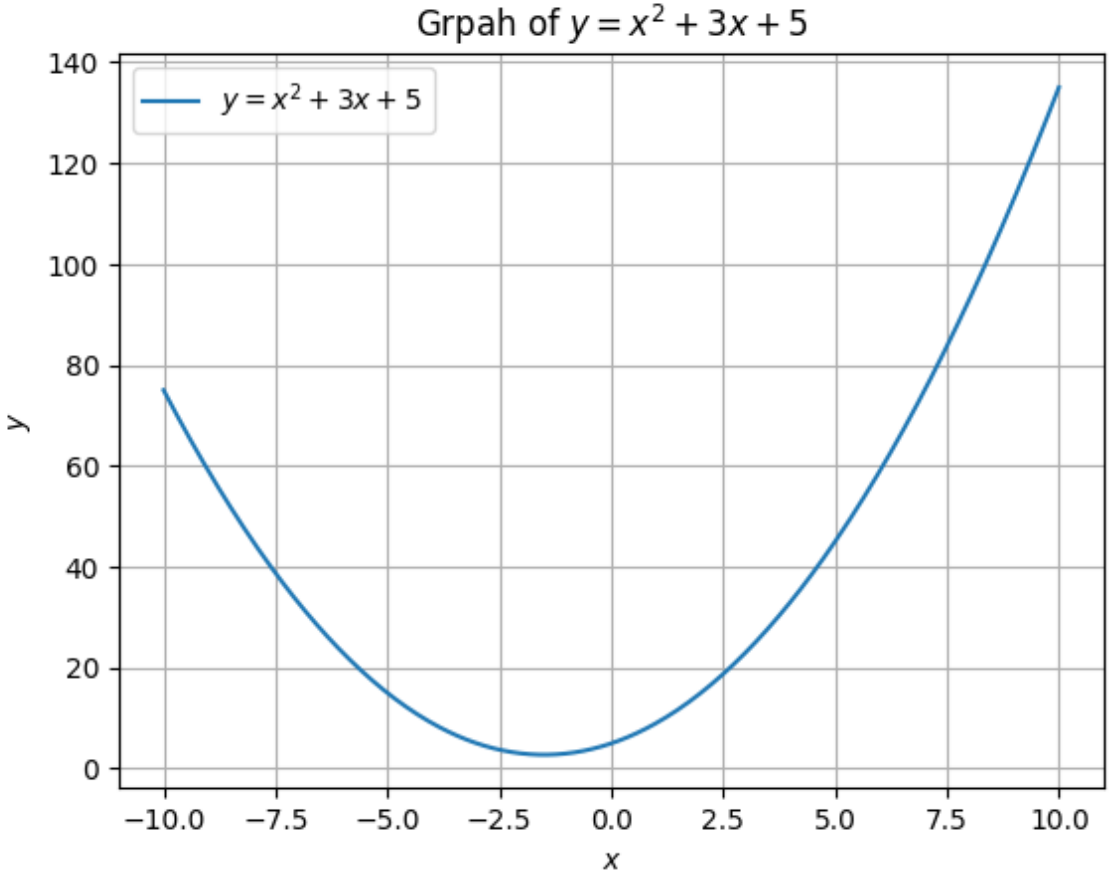

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- The axis of symmetry is $x = h$. This is the vertical line that passes through the vertex.

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7. Determine the maximum or minimum value of $f$.

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8. Write down the domain and range in interval notaion.

# References


Julie Miller and Donna Gerken.
*College Algebra*.
McGraw-Hill Education, New York, 2nd edition, 2016.