Radiative-convective equilibrium in a grey atmosphere

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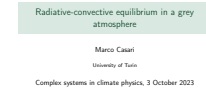

- A radiative-convective model is used to study a grey atmosphere.
- Comparison between numerical and analytical solutions is possible in radiative equilibrium.

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2. RTE describes radiative processes.
3. Fluid dynamics equations describe convective processes.

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1. Quantities do not depend on the frequency of electromagnetic radiation.

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3. Heat flux determined only by radiative and convective processes, two-stream approximation, numerical correction for convection.

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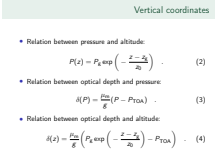

Analytical solution

Numerical solution

Radiative-convective equilibrium

Conclusion

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