

yacoub: a Python package for Simulating Generalized Fading Channels

José V. de M. Cardoso, Paulo R. Lins Júnior,
Wamberto J. L. Queiroz, and Marcelo S. Alencar, *IEEE Senior Member*
Universidade Federal de Campina Grande
Instituto Federal de Educação, Ciência, e Tecnologia da Paraíba
Campina Grande, Paraíba, Brasil
{josevinicius,paulo,wamberto,malencar}@iecom.org.br

Abstract—We present a well tested Python-based library for simulating and computing generalized fading channels, named **yacoub**. We describe the applicability of **yacoub** using examples in recent communications systems challenges, namely: cooperative spectrum sensing, bit error rate computation in generalized fading channel, and parameter estimation in free space optics. The development of **yacoub** open source and its code is available at <http://github.com/mirca/yacoub>.

I. INTRODUCTION

A. Note on notation

Scalars and random variables are denoted as *italic* small-case letters *e.g.* x ; vectors and random vectors are denoted as *italic*, boldface, small-case letters *e.g.* \mathbf{x} . The n -th component of a vector \mathbf{x} is denoted as x_n . A complex vector of length n is defined as $\mathbf{x} \in \mathbb{C}^{n \times 1}$. All vectors are column vectors. Matrices are denoted as *italic*, boldface, capital letters as in \mathbf{X} ; the identity matrix of order n is denoted as \mathbf{I}_n . We define a discrete-time circularly symmetric Gaussian process \mathbf{z} as any (finite or infinite) collection of random variables $\mathbf{z} = \mathbf{x} + j\mathbf{y}$, $j \triangleq \sqrt{-1}$, such that \mathbf{x} and \mathbf{y} are iid jointly Gaussian with zero mean vector and covariance matrix given by $\mathbb{E}[\mathbf{z}\mathbf{z}^\dagger]$, in which \mathbf{z}^\dagger means the conjugate transpose of \mathbf{z} and \mathbb{E} denotes the expected value. The probability of an event A is denoted as $\mathbb{P}(A)$.

II. THE ACCEPTANCE-REJECTION SAMPLER IN LOG-SPACE

III. EXAMPLES

A. Spectrum Sensing in Complex Generalized Fading Channels

The spectrum sensing problem consists in deciding whether or not a given channel frequency band is being occupied by a licensed (primary) user and, in case that such frequency band is available, how to opportunistically allocate secondary users such that the interference on the primary user is negligible.

From a probabilistic point of view, the spectrum sensing problem may be framed as a decision theory problem, as follows

$$H_0 : \mathbf{y} = \mathbf{w}, \quad (1)$$

$$H_1 : \mathbf{y} = h\mathbf{s} + \mathbf{w}, \quad (2)$$

in which $\mathbf{y} \in \mathbb{C}^{n \times 1}$ is the decoded received vector signal, $\mathbf{w} \in \mathbb{C}^{n \times 1}$ is complex Gaussian noise process with zero mean vector and covariance matrix given as $\sigma^2 \mathbf{I}_n$, and h is the channel gain.

In [?], the authors have shown that the probability distribution of the energy statistic $\tilde{y} \triangleq \mathbf{y}^\dagger \mathbf{y}$ conditioned on the knowledge of h , in case that \mathbf{s} is an M -PSK signal such that every symbol has the same probability of occurrence, $\mathbb{P}(s_n = s) = \frac{1}{M}$, is given as

$$p(\tilde{y}|h, H_1) = 1 - Q_n \left(\sqrt{\frac{2n|h|^2 E_s}{\sigma^2}}, \sqrt{\frac{2\tilde{y}}{\sigma^2}} \right), \quad (3)$$

in which Q_n is the Marcum- Q function and E_s is the energy per symbol.

The pdf of \tilde{y} can be written using the Law of Total Expectation

$$p(\tilde{y}|H_1) = \mathbb{E}[p(\tilde{y}|h, H_1)] = \int_{-\infty}^{+\infty} p(\tilde{y}|h, H_1)p(h) dh. \quad (4)$$

Recall that the energy detection rule can be expressed as

$$d_\delta(\tilde{y}) = \begin{cases} 1, & \tilde{y} \geq \delta, \\ 0, & \tilde{y} < \delta, \end{cases} \quad (5)$$

in which δ is a strictly positive real number known as energy threshold, and $d_\delta(\tilde{y}) = j$, $j \in \{0, 1\}$ means that the detector has decided in favor of the hypothesis H_j .

As a result, the probabilities of false alarm and detection can be written as

$$p_f = 1 - p() \quad (6)$$

$$p_d = \quad (7)$$

B. Parameter Estimation in Free Space Optics

C. BER in Complex $\alpha - \mu$ Fading

IV. CONCLUSIONS

ACKNOWLEDGEMENT

The authors would like to thank the Federal University of Campina Grande (UFCG) and the Institute for Advanced Studies in Communications (Iecom) for supporting this research.