

Assignment 4

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Download all python codes from

[https://github.com/mirhasidheek7213/
InternshipIITH/tree/main/Assignment-4/Codes](https://github.com/mirhasidheek7213/InternshipIITH/tree/main/Assignment-4/Codes)

and latex-tikz codes from

[https://github.com/mirhasidheek7213/
InternshipIITH/blob/main/Assignment-4/
Assignment4.tex](https://github.com/mirhasidheek7213/InternshipIITH/blob/main/Assignment-4/Assignment4.tex)

Now,

$$(\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{A}) = (7 \ 14 \ 21) \begin{pmatrix} 22 \\ -47 \\ -4 \end{pmatrix} \quad (2.1.4)$$

$$\Rightarrow 154 - 658 - 17 = -588 \quad (2.1.5)$$

Hence, $(\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{A}) \neq 0$. Therefore the triangle is not right angled at A.

1 QUESTION No. 2.6 - VECTORS

Are the points $\mathbf{A} = \begin{pmatrix} 3 \\ 6 \\ 9 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} 10 \\ 20 \\ 30 \end{pmatrix}$, $\mathbf{C} = \begin{pmatrix} 25 \\ -41 \\ 5 \end{pmatrix}$,
the vertices of a right angled triangle?

2 SOLUTION

Given,

$$\mathbf{A} = \begin{pmatrix} 3 \\ 6 \\ 9 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 10 \\ 20 \\ 30 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 25 \\ -41 \\ 5 \end{pmatrix} \quad (2.0.1)$$

To check if the vertices are of a right angled triangle we have to prove $(\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{A}) = 0$, $(\mathbf{A} - \mathbf{B})^\top (\mathbf{C} - \mathbf{B}) = 0$, $(\mathbf{A} - \mathbf{C})^\top (\mathbf{B} - \mathbf{C}) = 0$. If the triangle is right angled at A, B and C respectively

2.1 Checking if $\angle A = 90^\circ$

We have to prove,

$$(\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{A}) = 0 \quad (2.1.1)$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 7 \\ 14 \\ 21 \end{pmatrix} \quad (2.1.2)$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} 22 \\ -47 \\ -4 \end{pmatrix} \quad (2.1.3)$$

2.2 Checking if $\angle B = 90^\circ$

We have to prove,

$$(\mathbf{A} - \mathbf{B})^\top (\mathbf{C} - \mathbf{B}) = 0 \quad (2.2.1)$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} -7 \\ -14 \\ -21 \end{pmatrix} \quad (2.2.2)$$

$$\mathbf{C} - \mathbf{B} = \begin{pmatrix} 15 \\ -61 \\ -25 \end{pmatrix} \quad (2.2.3)$$

Now,

$$(\mathbf{A} - \mathbf{B})^\top (\mathbf{C} - \mathbf{B}) = (-7 \ -14 \ -21) \begin{pmatrix} 15 \\ -61 \\ -25 \end{pmatrix} \quad (2.2.4)$$

$$\Rightarrow -105 + 854 + 525 = 1274 \quad (2.2.5)$$

Hence, $(\mathbf{A} - \mathbf{B})^\top (\mathbf{C} - \mathbf{B}) \neq 0$. Therefore the triangle is not right angled at B.

2.3 Checking if $\angle C = 90^\circ$

We have to prove,

$$(\mathbf{A} - \mathbf{C})^\top (\mathbf{B} - \mathbf{C}) = 0 \quad (2.3.1)$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} -22 \\ 47 \\ 4 \end{pmatrix} \quad (2.3.2)$$

$$\mathbf{B} - \mathbf{C} = \begin{pmatrix} -15 \\ 61 \\ 25 \end{pmatrix} \quad (2.3.3)$$

Now,

$$(\mathbf{A} - \mathbf{C})^\top (\mathbf{B} - \mathbf{C}) = \begin{pmatrix} -22 & 47 & 4 \end{pmatrix} \begin{pmatrix} -15 \\ 61 \\ 25 \end{pmatrix} \quad (2.3.4)$$

$$\Rightarrow 330 + 2867 + 200 = 3297 \quad (2.3.5)$$

Hence, $(\mathbf{A} - \mathbf{C})^\top (\mathbf{B} - \mathbf{C}) \neq 0$. Therefore the triangle is not right angled at B.

Since these vertices do not form right angles, they are not vertices of a right angled triangle

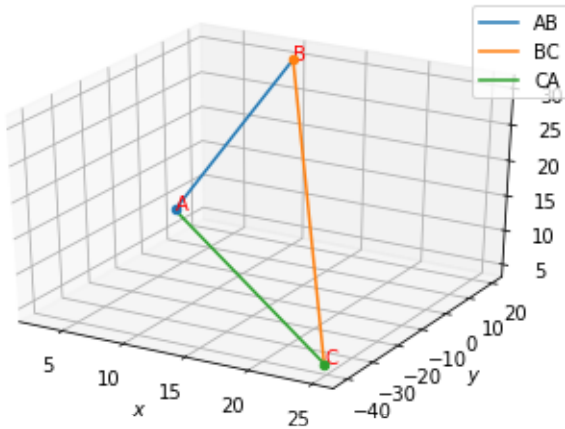


Fig. 0: Plot of the triangle