Significance of neural noise

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What then is time noise? If no one asks me, I know; if I want to explain it to a questioner, I do not know."

– Augustine of Hippo Gašper





■ Non-deterministic source of variability in a signal. (Faisal et al., 2008)



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- Variability of a measurement due to random or unpredictable fluctuations in the measured quantity. (McDonnell and Ward, 2011)



- Non-deterministic source of variability in a signal. (Faisal et al., 2008)
- Variability of a measurement due to random or unpredictable fluctuations in the measured quantity. (McDonnell and Ward, 2011)
- Why should philosophers care about this?

Overview



- 1 Fast and frugal heuristics (FFH)
- 2 Brains as analog computers?
- 3 Neuromorphic electronics brain analogs
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What are FFH?



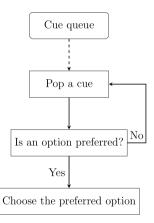
■ "Simple" decision rules evolved by "biologically constrained organisms [that] function under the uncertainty of the natural world." (Todd and Brighton, 2015).

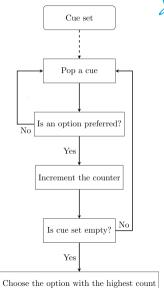
What are FFH?



- "Simple" decision rules evolved by "biologically constrained organisms [that] function under the uncertainty of the natural world." (Todd and Brighton, 2015).
- By foregoing computation (i.e. ignoring information) decision is purportedly reached faster and under less cognitive load.

TTB (left) & Tallying (right)







Empirical inadequacy of FFH



Overemphasis of executive functions.

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- Contextual effects observed in decision-making.

Empirical inadequacy of FFH



- Overemphasis of executive functions.
- Contextual effects observed in decision-making.
- Ignoring information is cognitively tasking (Glöckner et al., 2014; Söllner et al., 2014).



■ Conflation of information search & information processing.



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- Conflation of information search & information processing.
- Humans as "physical symbol systems". (Simon and Newell, 1971)
- Brains as digital computers: memory bound & sequential computation.
- Perception & motor-control imply nearly-optimal highly complex computations.



■ Perception as categorizing noisy stimuli.



- Perception as categorizing noisy stimuli.
- Motor-control as a choice of a movement trajectory.



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- Environmental noise as a similar source of risk.



- Perception as categorizing noisy stimuli.
- Motor-control as a choice of a movement trajectory.
- Environmental noise as a similar source of risk.
- Neural noise as *the common* source of uncertainty.

Dealing with uncertainty



■ Ubiquitous log odds (Zhang and Maloney, 2012) & shared neural substrates (Wu et al., 2011) for representations of probabilities.

Dealing with uncertainty



- Ubiquitous log odds (Zhang and Maloney, 2012) & shared neural substrates (Wu et al., 2011) for representations of probabilities.
- Normalization as a shared neural computation underlying decision-making & explaining cross-behavioral contextual effects (Louie et al., 2013).



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- Biological constraints?



- Perception as categorizing noisy stimuli.
- Motor-control as a choice of a movement trajectory.
- Environmental noise as a similar source of risk.
- Neural noise as the common source of uncertainty.
- Biological constraints? Ask a decision neuroscientist!

Neuromorphic computing



■ Massive parallelism, high recurrency & mutual inhibition as main computational "motifs" (Jocham et al., 2012; Hämmerer et al., 2016).

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Neuromorphic computing



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- No strong separation between memory and processing units. (Hunt and Hayden, 2017)
- Metabolic efficiency & noise mitigation before "economic rationality".



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- Theory of "naturalized rationality" should be aligned with the current best neuroscientific theories.
- Neural noise as *the common* source of uncertainty in cognitive, perceptual, and motor decision-making.
- Brains are not well-described as similar to a digital computer.
- Neuromorphic electronics as a better model of brains (Štukelj, 2019).

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Maley (2018)



- 1. Analog computation is manipulation of analog representations.
- 2. Analog representations can be continuous or discrete.
- 3. Digital representations are discrete.
- 4. Brains compute with continuous signals.

: Brains are analog computers.





- "Practically" continuous at the circuit level.
- Symbolic algebra (e.g. exact computation of $\sin(\pi/4)$).
- Real algebraic numbers and many transcendental numbers are Turing-computable.

Maley (2018)



"[T]here is no discrete 'clock' that determines when a physical change in a circuit element should count as a change in signal."

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- Temporal and rate neural codes use continuous variables.

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Maley (2018)



- "[T]here is no discrete 'clock' that determines when a physical change in a circuit element should count as a change in signal."
- Temporal and rate neural codes use continuous variables.
- Membrane voltage waveforms vary continuously.

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■ Neural clocks & async digital computers.



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- Neural clocks & async digital computers.
- Falling for sloppy neuroscientific lingo?
- Strong assumptions about the "nature of things".
- Dilution of "computationally relevant".

Accommodating current best neurosci theories



■ Presence of neural noise implies discrete computation (Eliasmith, 2000).

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- Adding noise to a signal does not necessarily result in a different computation.

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- Presence of neural noise implies discrete computation (Eliasmith, 2000).
- Adding noise to a signal does not necessarily result in a different computation.
- Adding noise to a signal can result in a miscomputation the same computation performed with different outcomes.

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■ Noise as an indicator of discrete neural computation.

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- Noise as an indicator of discrete neural computation.
- Noise as an explanandum of neural miscomputation.



- Noise as an indicator of discrete neural computation.
- Noise as an explanandum of neural miscomputation.
- Computational identity is closed under noise.

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Douglas et al. (1995, p. 255)



The significance of neuromorphic systems is that they offer a method of exploring neural computation in a medium whose physical behavior is analogous to that of biological nervous systems.

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Analog as analogous



- "Analogy machines" (von Neumann, 1951)
- Representational isomorphism (Shagrir, 2010)
- Model-based computing (Beebe, 2018)



If physical system $\mathcal P$ can be described as computing a function f, and $\mathcal A$ is its analog, then I might use $\mathcal A$ to:

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- (A3) gather data about ${\mathcal A}$ that can be used to reason about a hypothesis regarding ${\mathcal P}$

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Douglas et al. (1995, p. 258)



The efficiency of neuromorphic analogue VLSI (aVLSI) rests in the power of analogy, the isomorphism between physical processes occurring in different media.

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- (A3) gather data about ${\mathcal A}$ that can be used to reason about a hypothesis regarding ${\mathcal P}$
- (A4) use \mathcal{A} to implement f^* "efficiently"

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Computing with analogs



■ Isomorphism between "physical processes" not functions describing I/O.

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Computing with analogs



- Isomorphism between "physical processes" not functions describing I/O.
- No distinction between target of analogy and target of computation/explanation.

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I/O modeling



IN_1	IN_2	OUT
HIGH	HIGH	HIGH
HIGH	LOW	LOW
LOW	HIGH	LOW
LOW	LOW	LOW

Figure: AND or OR gate?

I/O modeling



IN_1	IN_2	OUT
HIGH	HIGH	HIGH
HIGH	LOW	LOW
LOW	HIGH	LOW
LOW	LOW	LOW

Figure: AND gate!

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I/O modeling



IN_1	IN_2	OUT
HIGH	HIGH	HIGH
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LOW	HIGH	LOW
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Figure: OR gate!

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■ Energy efficiency (Mead, 1990)



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- Parallelism (Schuman et al., 2017)



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- Synchronization of isolated circuits w/ noise (Utagawa et al., 2008)

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- Energy efficiency (Mead, 1990)
- Parallelism (Schuman et al., 2017)
- Synchronization of isolated circuits w/ noise (Utagawa et al., 2008)
- Stochastic resonance (Gonzalez-Carabarin et al., 2014)

McDonnell and Ward (2011, p. 417)



[S]tochastic resonance is often described as paradoxical or counter-intuitive, because in engineered electronic systems noise is naturally seen to be only detrimental to quality. However, in a biological context, the effect is hardly counter-intuitive when thought of as the benefits of randomness, as with other constructive roles of noise in which inputs and outputs need not be readily identifiable.

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McDonnell and Ward (2011, p. 417)



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■ Analogies/isomorphisms go over and above I/O relationships.

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- Analogies/isomorphisms go over and above I/O relationships.
- Some computations are driven by non-computational goals.

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Conclusions



■ Recognition of noise as a cross-behavioral source of uncertainty has driven the unification of decision neuroscience.

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Conclusions



- Recognition of noise as a cross-behavioral source of uncertainty has driven the unification of decision neuroscience.
- The concept of noise plays an important role in neuroscientific explanations & related philosophical arguments.

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Conclusions



- Recognition of noise as a cross-behavioral source of uncertainty has driven the unification of decision neuroscience.
- The concept of noise plays an important role in neuroscientific explanations & related philosophical arguments.
- Neuromorphic computers are analog computers by virtue of physical behavior analogous to brains.

Thank you!



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