Congratulations! You passed!

TO PASS 80% or higher

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Week 4 Quiz

TOTAL POINTS 9

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1. Person 1 has hazard $h_1(t) = 1$, and Person 2 has hazard $h_2(t) = 2$. What is the probability of dying within the first year for each patient?

   1 / 1 point

   Hint:

   The survival function $S(t)$ in terms of the hazard function is:

   $$S(t) = e^{-\int_0^t h(s)ds}$$

   - ○ 0.6, 0.6
   - ◉ 0.63, 0.86
   - ○ 0.37, 0.14

   Correct

   Note that since the hazards are constant,

$S_1(1) = e^{(-h_1(0))} = e^{(-1)}$.

$S_2(1) = e^{(-h_2(0))} = e^{(-2)}$.

Since we want the probability of death, we take $1 - S(t)$.

This gives us for person 1: $1 - e^{(-1)} = 0.63$.

For person 2, $1 - e^{(-2)} = 0.86$.

2. Let $T > 0$.

1 / 1 point

For patient 1, let the survival function be $S_1(t)$ and the hazard function be $h_1(t)$.

For patient 2, let the survival function be $S_2(t)$ and the hazard function be $h_2(t)$

You see that $S_1(T) > S_2(T)$. The survival probability of patient 1 at time T is higher than the survival probability of patient 2 at time T.

Which of the following is true about the hazard of patient 1 and 2 at time T?

Hint:

$$S(t) = e^{-\int_0^t h(s)ds}$$

- ○ h_1(T) > h_2(T)
- ○ h_1(T) < h_2(T)
- ○ h_1(T) = h_2(T)

◉ None of the above

Correct

The answer is none of the above.

Recall that $S(t)$ decays exponentially in the integral of the hazard (it's e raised to the power of negative 1 times the integral of the hazard).

So just because you know $S(T)$ at one point does not say anything about $h(T)$ at that point, since $S(T)$ also depends on what happened from time $t = 0$ up to time $t = T$.

3. Now assume that the hazards for patient 1, h_1 and for patient 2, h_2 are proportional to each other. Also assume that $S_1(T) > S_2(T)$ for some T > 0.

1 / 1 point

Then which of the following is true about the hazards?

○ h_1(T) = h_2(T)

○ h_1(T) > h_2(T)

◉ h_1(T) < h_2(T)

Correct

Since the hazards are proportional, we know that they cannot cross each other when we vary the time T.

Therefore if the survival function of Person 1 is above the survival function of Person 2 at any point, it must be above the person 2 survival function everywhere.

Since the survival function decays exponentially with the hazards (it is e raised to the power of negative 1 times the integral of the hazard) it means that the hazard of Person 1 is LESS than the hazard of Person 2.

Since the hazards are proportional, this must be true for any time T.

In particular $h_1(T) < h_2(T)$.

4. You've fit a Cox model on 2 features: age and smoking status.

1 / 1 point

The coefficients of these features are:

β_{age} = 0.9 and β_{smoker} = 10.0.

What is the hazard ratio between Person 1, a 40 year old non-smoker, and Person 2, a 30 year old smoker?

Recall that Cox Proportional Hazards assumes a model of the form:

$$h(t) = \lambda_0(t)e^{(\beta_{age} \times Age + \beta_{smoker} \times Smoker)}$$

We're asking you to find the ratio:

$$\frac{h_1(t)}{h_2(t)}$$

- ○ 2.64
- ◉ 0.36

2.7

Correct

$$\frac{h_1(t)}{h_1(t)} = \frac{\lambda_0(t)e^{(\beta_{age} \times Age_1 + \beta_{smoker} \times Smoker_1)}}{\lambda_0(t)e^{(\beta_{age} \times Age_1 + \beta_{smoker} \times Smoker_2)}}$$

When we take the ratio, the λ_0 will drop out.

So we just compute:

$$\frac{h_1(t)}{h_2(t)} = \frac{e^{(0.9 \times 40 + 10 \times 0)}}{e^{(0.9 \times 30 + 10 \times 1)}} = e^{(36 - (27 + 10))}$$

$$\frac{h_1(t)}{h_2(t)} = e^{(-1)} = 0.36$$

5. You’ve fit a cox model and have the following coefficients:

1 / 1 point

$\beta_{female} = -1.0$

$\beta_{age} = 1.0,$

$\beta_{BP} = 0.6$

$$h(t) = \lambda_0(t)e^{((\beta_{female} \times female) + (\beta_{age} \times Age) + (\beta_{BP} \times BP))}$$

Which of the following interpretations is most correct?

- (selected) All other things held equal, being a female decreases your risk
- All other things held equal, having lower age increases your risk
- All other things held equal, having higher BP decreases your risk

Correct

Note that the effect of increasing a feature x by 1 unit will be to multiply the hazard by $e^{(\beta_x)}$.

Since $e^{(0)} = 1$, a coefficient less than 0 (a negative coefficient) reduces the hazard. A coefficient greater than 0 (positive) increases the hazard.

Therefore the only correct interpretation is that being a female decreases the hazard, since $\beta_{female} < 0$.

6. Assume h_1(t) = t, and h_2(t) = 1.0. At which time T > 0 does S_1(T) = S_2(T)?

1 / 1 point

- None of the above
- (selected) 2
- 1
- 0.5

Correct

Remember that the Cumulative hazard is the integral from 0 to t of the hazard function. Using calculus, one can see that the cumulative hazard for Person 1 is 0.5t^2 and for person 2, the cumulative hazard is t.

Since S(t) = exp(-H(t)), the survival functions are equal if and only if the cumulative hazard is equal

Since S(t) = exp(-H(t)), the survival functions are equal if and only if the cumulative hazard is equal. Setting these equal to each other, we get t = 2. A common mistake is just to set the hazards equal, which would give you t = 1.

7. Using the Nelson-Aalen estimator estimate H(7), the value of the cumulative hazard at t=7 for this dataset.

1 / 1 point

ID	Outcome
1	3
2	4
3	8
4	6+

The Nelson-Aalen estimator is:

$$H(t) = \sum_{i=0}^{t} \frac{d_i}{n_i}$$

- ( ) 8/11
- (•) 7/12
- ( ) 5/9

Correct

Evaluating this for $t = 7$, we get

$$\frac{d_3}{n_3} + \frac{d_6}{n_6} = \frac{1}{4} + \frac{1}{3} = \frac{7}{12}$$

8. Which risk assignments would make this pair **concordant**?

1 / 1 point

Patient 1 Patient 2

T 10 5+

- 0.3, 0.8
- 0.5, 0.3
- 0.5, 0.5
- (selected) The pair is not permissible

✓ **Correct**

The pair is in fact not permissible. Since Patient 2 was censored before Patient 1 had the event, we cannot say who had a worse outcome.

9. Compute the Harrell C-index for the following dataset and risk scores:

ID	Outcome	Score
1	4	1.6
2	6+	1.2
3	5	0.8
4	7	0.1

Step 1: Find all the permissible pairs

Step 2: of the permissible pairs, determine which ones are concordant.

Step 3: of the permissible pairs, determine which ones are risk ties.

Harrell's c-index = $\frac{concordant + 0.5 \times riskties}{permissible}$

- ( ) 1.0
- (•) 0.8

0.7

Correct

The permissible pairs are

(1, 2), (1, 3), (1, 4), (2, 3), (3, 4).

Of these, the concordant ones are

(1, 2), (1, 3), (1, 4), and (3, 4).

Since there are no ties, the harrell's c-index is the number of concordant pairs over the number of permissible pairs, which is $\frac{4}{5} = 0.8$.