



pencal: an R package for the dynamic prediction of survival with many longitudinal predictors

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The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `penca1`

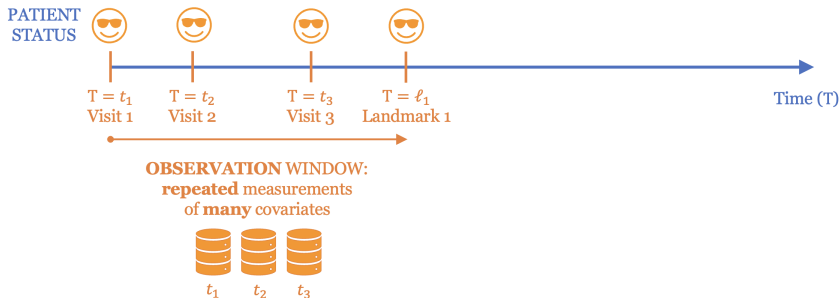
Prediction of survival

Evaluation of predictive performance

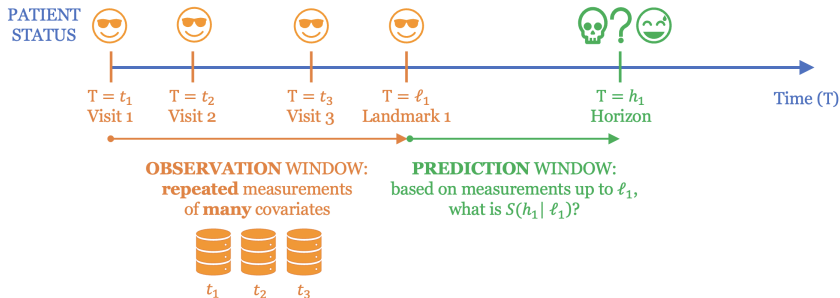
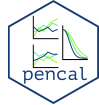
Package overview

Appendix

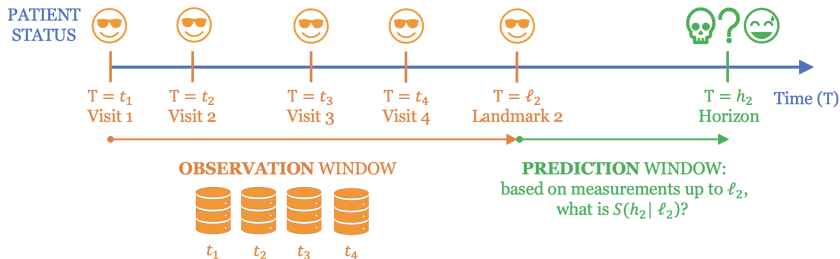
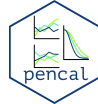
Dynamic prediction of survival



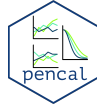
Dynamic prediction of survival



Dynamic prediction of survival



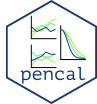
Goal of dynamic prediction



► Goals of dynamic prediction:

1. predict future survival $S(t|\ell_1)$ using repeated measurements collected over the observation period $[0, \ell_1]$
2. dynamically update predictions once more information becomes available, i.e. predict $S(t|\ell_2)$ given repeated measurements over $[0, \ell_2]$, $\ell_2 > \ell_1$

Example datasets



- ▶ Two datasets we worked with:

	ROSMAP	Mark-MD
Outcome	Alzheimer's disease diagnosis	Loss of ambulation in Duchenne patients
n	3757	157
Max follow-up	Up to 30 years	Up to 7.4 years
Baseline covariates	5	3
Longitudinal covariates	30	240 antibodies that target 118 proteins

- ▶ Datasets can differ substantially wrt n and p

- ▶ Traditional methods for dynamic prediction:
 - ▶ joint models: very **computationally-intensive**. Can't usually be estimated with more than 3-5 longitudinal predictors!
 - ▶ landmarking with LOCF¹: **no modelling of the longitudinal trajectories** + **no measurement error correction** (important for biomarkers)
- ▶ Methodological problem: how to do **dynamic prediction of survival** when the predictors are
 1. measured **longitudinally** (ROSMAP, Mark-MD)
 2. **many** - potentially **high-dimensional** setting (ROSMAP, Mark-MD)
 3. and potentially **highly-correlated** with each other (Mark-MD)

¹LOCF = Last Observation Carried Forward



The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `pencal`

Prediction of survival

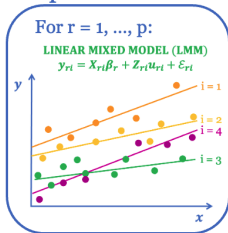
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- ▶ ℓ = landmark time
- ▶ $i \in \{1, \dots, n_\ell\}$ subjects who survived up until $t = \ell$
- ▶ Observation window - $t \in [0, \ell]$:
 - ▶ k baseline covariates x_{qi} measured at $t_i = 0$ (study entry)
 - ▶ p longitudinal covariates y_{rij} measured at $t_{i1}, \dots, t_{im_i} \in [0, \ell]$
- ▶ Prediction window - $t \in [\ell, h]$:
 - ▶ T_i^* true survival time
 - ▶ C_i censoring time
 - ▶ $T_i = \min(T_i^*, C_i)$ observed survival time
 - ▶ $\delta_i = I(T_i = T_i^*)$ event indicator

Step 1



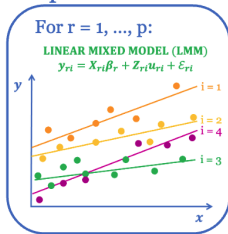
Step 2

Compute the
predicted random effects
 $\hat{u}_{ri} = \hat{W}_{ri}(y_{ri} - X_{ri}\hat{\beta}_r)$
 where
 $\hat{W}_{ri} = \hat{D}_r Z_{ri} \hat{V}_{ri}^{-1}$

Step 3

Estimate
 $h(t|\eta_i) = h_0(t)e^{\eta_i}$,
 where
 $\eta_i = x_i^T \tau + \hat{u}_i^T \gamma$,
 using **penalized maximum likelihood** (ridge / lasso / elasticnet)

Step 1



Step 2

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Step 1: model the evolution of the longitudinal covariates



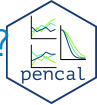
- ▶ Step 1: model longitudinal predictors with **mixed-effects models**
- ▶ Two alternatives:
 1. Linear Mixed Models (LMM)
 2. Multivariate Latent Process Mixed Model (MLPMM, Proust-Lima et al. (2013))

- ▶ Fit to each longitudinal Y_r a LMM: $y_{ri} = X_{ri}\beta_r + Z_{ri}u_{ri} + \varepsilon_{ri}$
- ▶ Example:

$$y_{rij} = \beta_{r0} + u_{r0i} + (\beta_{r1} + u_{r1i})a_{ij} + \varepsilon_{rij},$$

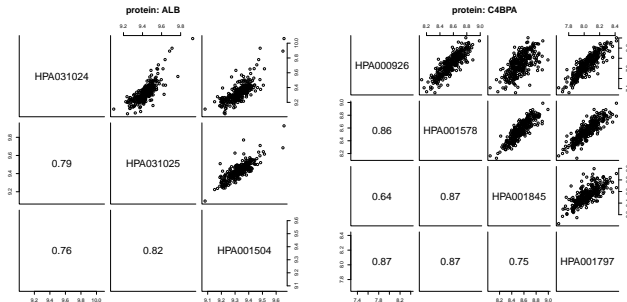
where $u_{ri} = (u_{r0i}, u_{r1i}) \sim N(0, D_r)$ and $\varepsilon_{ri} \sim N(0, \sigma_r^2 I_{m_i})$

How to handle groups of highly-correlated biomarkers?



► Issue:

1. LMM approach assumes longitudinal markers to be independent
2. what if you have groups of highly-correlated biomarkers, like in Signorelli et al. (2020)?



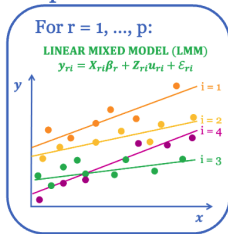
- ▶ Suppose that r_s covariates are employed to measure the same underlying phenomenon y_s that cannot be measured directly: $(\mathbf{y}_{1s}, \dots, \mathbf{y}_{r_s s})$
- ▶ Example: r_s antibodies measured as proxies for protein s
- ▶ We can specify a MLPMM for $(\mathbf{y}_{1s}, \dots, \mathbf{y}_{r_s s})$ where

$$y_{qsij} = \beta_{qs0} + u_{s0i} + b_{qsi} + (\beta_{qs1} + u_{s1i})a_{ij} + \varepsilon_{qsij} \quad (\forall q = 1, \dots, r_s),$$

with $\varepsilon_{qsij} \sim N_1(0, \sigma_{\varepsilon_{qs}}^2)$, and

- ▶ $\mathbf{u}_{si} = (u_{s0i}, u_{s1i}) \sim N_2(0, \Sigma_{us})$: shared random intercept and slope that refer to (latent) underlying quantity (\rightarrow protein)
- ▶ $b_{qsi} \sim N_1(0, \sigma_{b_{qs}}^2)$ covariate-specific random intercepts (\rightarrow antibodies)
- ▶ Latent variable interpretation (reconstruct latent protein info from measurable antibodies variables)

Step 1



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Step 3

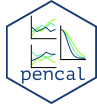
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 using **penalized maximum likelihood** (ridge / lasso / elasticnet)

Step 2: computing the predicted random effects



- ▶ Derive **subject-specific summaries of the longitudinal trajectories** from the mixed-effects models
 - ▶ random intercepts \approx different starting levels across subjects
 - ▶ random slopes \approx different progression rates between subjects

Step 2: computing the predicted random effects

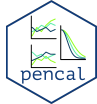


- ▶ Derive **subject-specific summaries of the longitudinal trajectories** from the mixed-effects models
 - ▶ random intercepts \approx different starting levels across subjects
 - ▶ random slopes \approx different progression rates between subjects
- ▶ For the **LMM**:

$$\hat{u}_{ri} = E(u_{ri} | Y_{ri} = y_{ri}) = \hat{D}_r Z_i^T \hat{V}_{ri}^{-1} (y_{ri} - X_i \hat{\beta}_r),$$

where $V_{ri} = Z_i D_r Z_i^T + \sigma_r^2 I_{m_i}$ is the marginal covariance matrix of subject i

Step 2: computing the predicted random effects



- For the **MLPMM**:

$$\left(\hat{u}_{si}, \hat{b}_{si} \right) = E \left(u_{si}, b_{si} | Y_{si} = y_{si} \right) = \begin{bmatrix} Z_i \Sigma_{u_s} \\ \Sigma_{b_s} I_{r_s} \otimes \mathbf{1}_{m_i, 1} \end{bmatrix} \Sigma_{y_{si}}^{-1} \dot{y}_{si},$$

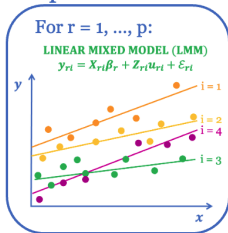
where $y_{si} = (y_{1si1}, \dots, y_{1sim_i}, \dots, y_{r_s si1}, \dots, y_{r_s sim_i})^T$, \dot{y}_{si} is the equivalent of y_{si} with $\dot{y}_{qsij} = y_{qsij} - \beta_{qs0} - \beta_{qs1} a_{ij}$ as entries, Z_i is the random-effects

design matrix associated to y_{si} , $\Sigma_{b_s} = \begin{bmatrix} \sigma_{b1s}^2 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & \sigma_{br_s s}^2 \end{bmatrix}$,

$$\Sigma_{\varepsilon_s} = \begin{bmatrix} \sigma_{\varepsilon 1s}^2 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & \sigma_{\varepsilon r_s s}^2 \end{bmatrix}, \Sigma_{u_s} = \begin{bmatrix} \sigma_{us0}^2 & \sigma_{us0, us1} \\ \sigma_{us0, us1} & \sigma_{us1}^2 \end{bmatrix} \text{ and}$$

$$\Sigma_{y_{si}} = Z_i \Sigma_{us} Z_i^T + I_{r_s} \otimes \Sigma_{\varepsilon_s} I_{m_i} + I_{r_s} \otimes \Sigma_{b_s} \mathbf{1}_{m_i, m_i}$$

Step 1



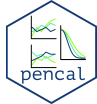
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 using **penalized maximum likelihood** (ridge / lasso / elasticnet)

Step 3: prediction of survival



- Cox model linking survival outcome to **baseline covariates** and **summaries of longitudinal covariates**:

$$h(t_i|x_i, \hat{u}_{0i}, \hat{u}_{1i}) = h_0(t_i) \exp(\eta_i), \quad (1)$$

$$\eta_i = \sum_{q=1}^k \theta_q x_{qi} + \sum_{r=1}^p \gamma_r \hat{u}_{r0i} + \sum_{r=1}^p \delta_r \hat{u}_{r1i}$$

- (θ, γ, δ) large, potentially high-dimensional \Rightarrow we estimate it using **penalized** maximum likelihood

$$\max_{\xi, \gamma, \delta} \ell(\xi, \gamma, \delta) - \lambda p(\xi, \gamma, \delta; \alpha)$$

- **Penalty functions**: ridge (ℓ^2 , recommended), elastic net, lasso (ℓ^1)
- **Predicted survival**: $\hat{S}(h|\ell) = \hat{S}(h) = e^{-\int_0^h \hat{h}_0(s) e^{\hat{\eta}_i} ds}$



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The R package: `pencal`

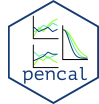
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Package overview

Appendix


Where to find the package



- ▶ Method implemented in the R package `pencal`
- ▶ Available on  **CRAN**:

pencal: Penalized Regression Calibration (PRC) for the Dynamic Prediction of Survival

Computes penalized regression calibration (PRC), a statistical method for the dynamic prediction of survival when many longitudinal predictors are available. PRC is described in Signorelli et al. (2021) <[doi:10.1002/sim.9178](https://doi.org/10.1002/sim.9178)> and Signorelli (2023) <[doi:10.48550/arXiv.2309.15600](https://doi.org/10.48550/arXiv.2309.15600)>.

Version: 2.1.1
Depends: R ($\geq 4.1.0$)
Imports: [doParallel](#), [dplyr](#), [foreach](#), [glmnet](#), [lcm](#), [magic](#), [MASS](#), [Matrix](#), methods, [nlme](#), [purrr](#), [riskRegression](#), stats, [survcomp](#), [survival](#), [survivalROC](#)
Suggests: [knitr](#), [ptmixed](#), [rmarkdown](#), [survminer](#)
Published: 2023-10-27
Author: Mirko Signorelli  [aut, cre, cph], Pietro Spitali [ctb], Roula Tsonaka [ctb], Barbara Vreede [ctb]
Maintainer: Mirko Signorelli <mignorelli.rpackages@gmail.com>
License: [GPL \(\$\geq 3\$ \)](#)
URL: <https://mirkosignorelli.github.io/r>
NeedsCompilation: no
Citation: [pencal citation info](#)
Materials: [NEWS](#)
CRAN checks: [pencal results](#)

Documentation:

Reference manual: [pencal.pdf](#)

Vignettes: [pencal: an R Package for the Dynamic Prediction of Survival with Many Longitudinal Predictors](#)

Vignette:  bit.ly/pencal-CMS

: @signormirko

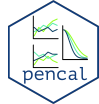
Example dataset



```
library(pencal)
data(pbc2data)
sdata = pbc2data$baselineInfo
ldata = pbc2data$longitudinalInfo
```

- ▶ Data from the PBC2 clinical trial (1974-1984)
 - ▶ $n = 312$, $k = 3$, $p = 7$
 - ▶ Outcome: time to death
 - ▶ Follow-up up to 14.3 years

Data preparation



- ▶ Let's choose $\ell = 2$ as landmark:

```
# remove subjects with event / censoring before landmark
lmark = 2
sdata = subset(sdata, time > lmark)
ldata = subset(ldata, id %in% sdata$id)

# remove repeated measurements taken after landmark
ldata = subset(ldata, fuptime <= lmark)
```

- ▶ We log-transform some highly-skewed predictors:

```
ldata$logSerBil = log(ldata$serBilir)
ldata$logSerChol = log(ldata$serChol)
ldata$logAlk = log(ldata$alkaline)
ldata$logSGOT = log(ldata$SGOT)
ldata$logProthr = log(ldata$prothrombin)
```

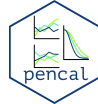
1. A dataset (ldata) with the longitudinal covariates measured up to the landmark time:

##	id	age	fuptime	logSerBil	logSerChol	albumin	logAlk
## 3	2	56.45	0.00	0.10	5.71	4.14	8.91
## 4	2	56.95	0.50	-0.22	NA	3.60	7.65
## 5	2	57.45	1.00	0.00	NA	3.55	7.44
## 16	4	54.74	0.00	0.59	5.50	2.54	8.72
## 17	4	55.26	0.51	0.47	NA	2.88	7.07
## 18	4	55.76	1.02	0.53	NA	2.80	7.05
## 19	4	56.74	2.00	1.16	NA	2.92	7.07
##	logSGOT		platelets	logProthr			
## 3	4.73		221	2.36			
## 4	4.94		188	2.40			
## 5	4.97		161	2.45			
## 16	4.10		183	2.33			
## 17	5.13		240	2.94			
## 18	5.11		251	2.45			
## 19	5.12		220	2.38			

2. A dataset (sdata) with the survival outcome, and baseline covariates:

##	id	time	event	baselineAge	sex	treatment
## 3	2	14.152338	0	56.44782	female	D-penicil
## 12	3	2.770781	1	70.07447	male	D-penicil
## 16	4	5.270507	1	54.74209	female	D-penicil
## 23	5	4.120578	0	38.10645	female	placebo
## 29	6	6.853028	1	66.26054	female	placebo
## 35	7	6.847552	0	55.53609	female	placebo

Step 1: estimating the LMMs

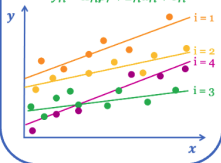


Step 1

For $r = 1, \dots, p$:

LINEAR MIXED MODEL (LMM)

$$y_{ri} = X_{ri}\beta_r + Z_{ri}u_{ri} + \varepsilon_{ri}$$



Step 2

Compute the
**predicted random
effects**

$$\hat{u}_{ri} = \hat{W}_{ri}(y_{ri} - X_{ri}\hat{\beta}_r)$$

where

$$\hat{W}_{ri} = \hat{D}_r Z_{ri} \hat{V}_{ri}^{-1}$$

Step 3

Estimate

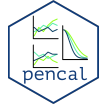
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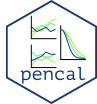
using **penalized
maximum
likelihood** (ridge /
lasso / elasticnet)

Step 1: estimating the LMMs



```
long_covs = c('logSerBil', 'logSerChol', 'albumin',  
              'logAlk', 'logSGOT', 'platelets',  
              'logProthr')  
  
step1 = fit_lmms(y.names = long_covs,  
                 fixeefs = ~ age, ranefs = ~ age | id,  
                 long.data = ldata, surv.data = sdata,  
                 t.from.base = fuptime)
```

Extracting output from the fitted LMMs



```
getlmm(step1, yname = 'logSerBil', what = 'betas') |> round(6)
```

```
## (Intercept)      age
##    0.518320   -0.001045
```

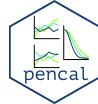
```
getlmm(step1, yname = 'logSerBil', what = 'tTable') |> round(4)
```

```
##              Value Std.Error   DF t-value p-value
## (Intercept)  0.5183    0.2788  566   1.8590  0.0636
## age         -0.0010    0.0055  566  -0.1884  0.8506
```

```
getlmm(step1, yname = 'logSerBil', what = 'variances')
```

```
## id = pdLogChol(age)
##              Variance   StdDev      Corr
## (Intercept)  7.332118e-01 0.856277849 (Intr)
## age         4.731627e-05 0.006878682 0.103
## Residual    1.437622e-01 0.379159888
```

Step 2: computing the predicted random effects

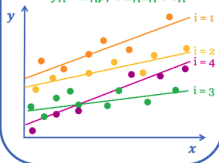


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LINEAR MIXED MODEL (LMM)

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Step 2

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Estimate

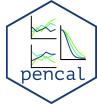
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where

$$\eta_i = x_i^T \tau + \hat{u}_i^T \gamma,$$

using **penalized
maximum
likelihood** (ridge /
lasso / elasticnet)

Step 2: computing the predicted random effects



```
step2 = summarize_lmms(step1)
```

- ▶ Handy: `summarize_lmms` automatically inherits relevant arguments from `fit_lmms` 😊

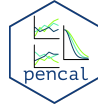
Step 2: sample output



```
round(step2$ranef.orig[1:5, 1:6], 6)
```

```
##      logSerBil_b_int logSerBil_b_age logSerChol_b_int
## 2          -0.382988          -0.001661          -0.071154
## 3          -0.117107          -0.000584          -0.598453
## 4           0.168600           0.000922          -0.370434
## 5           0.380035           0.001170          -0.291031
## 6          -0.473763          -0.002305          -0.248214
##      logSerChol_b_age albumin_b_int albumin_b_age
## 2           0.000660           0.179725           3.0e-06
## 3           0.004916           0.018124           1.0e-06
## 4           0.003468          -0.529776          -7.0e-06
## 5           0.002886          -0.148329           8.0e-06
## 6           0.002136           0.292353           1.7e-05
```

Step 3: estimate the penalized Cox model

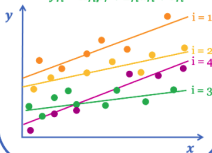


Step 1

For $r = 1, \dots, p$:

LINEAR MIXED MODEL (LMM)

$$y_{ri} = X_{ri}\beta_r + Z_{ri}u_{ri} + \varepsilon_{ri}$$



Step 2

Compute the
**predicted random
effects**

$$\hat{u}_{ri} = \hat{W}_{ri}(y_{ri} - X_{ri}\hat{\beta}_r)$$

where

$$\hat{W}_{ri} = \hat{D}_r Z_{ri} \hat{V}_{ri}^{-1}$$

Step 3

Estimate

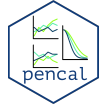
$$h(t|\eta_i) = h_0(t)e^{\eta_i},$$

where

$$\eta_i = x_i^T \tau + \hat{u}_i^T \gamma,$$

using **penalized
maximum
likelihood** (ridge /
lasso / elasticnet)

Step 3: estimate the penalized Cox model



```
step3 = fit_prc1mm(step2, surv.data = sdata,  
  baseline.covs = ~ baselineAge + sex + treatment,  
  penalty = 'ridge', standardize = T)
```

Step 3: fitted model



```
print(step3, digits = 3)
```

```
## Fitted model: PRC-LMM
## Penalty function used: ridge
## Sample size: 278
## Number of events: 107
## Bootstrap optimism correction: not computed
## Penalized likelihood estimates (rounded to 3 digits):
##   baselineAge sexfemale treatmentD-penicil logSerBil_b_int
## 1      0.051      -0.31          0.019          0.583
##   logSerBil_b_age logSerChol_b_int logSerChol_b_age
## 1      147.094          0.065          -7.513
##   albumin_b_int albumin_b_age logAlk_b_int logAlk_b_age
## 1      -1.55      34804.81          0.086          -0.217
##   logSGOT_b_int logSGOT_b_age platelets_b_int
## 1      0.164      260.291          -0.001
##   platelets_b_age logProthr_b_int logProthr_b_age
## 1      -0.043          3.053          -92.509
```



The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `penca1`

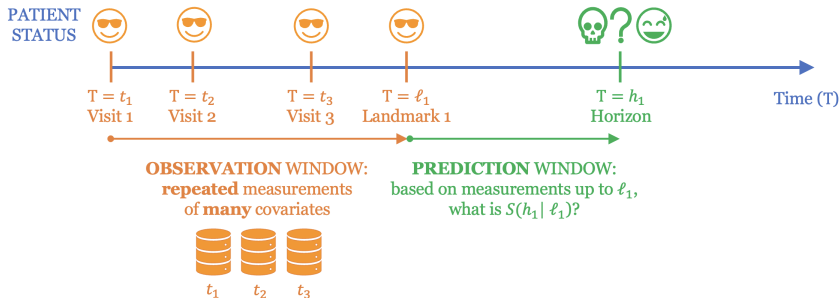
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Back to our goal: predicting survival



```
Shat = survpred_prclmm(step1, step2, step3, times = 3:5)
```

- ▶ This will compute $\hat{S}(t|2)$, $t = 3, 4, 5$:

```
head(Shat$predicted_survival, 4)
```

##	id	S(3)	S(4)	S(5)
## 2	2	0.9602048	0.9211106	0.8788494
## 3	3	0.8667790	0.7487764	0.6346572
## 4	4	0.8232941	0.6747116	0.5388305
## 5	5	0.9443086	0.8905143	0.8334098

- ▶ Prediction for **new** subjects? Possible through additional arguments `new.longdata` and `new.basecovs`



The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `pencl`

Prediction of survival

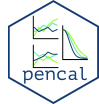
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- ▶ Performance measures: time-dependent AUC, C index, Brier score
- ▶ Internal validation of predictive performance:
 - ▶ cluster bootstrap optimism correction procedure (Signorelli et al. (2021)) → appendix
 - ▶ repeated cross-validation also possible as an alternative

Computing the CBOCP

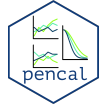


- ▶ To compute the cluster bootstrap optimism correction procedure, rerun steps 1, 2 and 3 specifying $nboots = B > 0$ inside `fit_lmms`:

```
step1b = fit_lmms(y.names = long_covs,
                  fixefs = ~ age, ranefs = ~ age | id,
                  long.data = ldata, surv.data = sdata,
                  t.from.base = fuptime,
                  n.boots = 50, n.cores = 8)
step2b = summarize_lmms(step1b, n.cores = 2)
step3b = fit_prclmm(step2b, surv.data = sdata,
                    baseline.covs = ~ baselineAge + sex + treatment,
                    penalty = 'ridge', standardize = T, n.cores = 8)
```

- ▶ NB: `n.boots` needs to be specified just in step 1, but it is used also in steps 2 and 3
- ▶ `n.cores` allows you to parallelize computations within each step!

Computing the performance measures



```
predPerf = performance_prc(step2 = step2b, step3 = step3b,  
    metric = c('tdauc', 'brier'), times = 3:5,  
    n.cores = 8)
```

Predictive performance



```
predPerf
```

```
## $call
## performance_prc(step2 = step2b, step3 = step3b, metric = c("tdauc",
##      "brier"), times = 3:5, n.cores = 8)
##
## $tdAUC
##   pred.time tdAUC.naive optimism.correction tdAUC.adjusted
## 1         3      0.9434          -0.0064          0.9370
## 2         4      0.9348          -0.0160          0.9188
## 3         5      0.9273          -0.0134          0.9139
##
## $Brier
##   pred.time Brier.naive optimism.correction Brier.adjusted
## 1         3      0.0556           0.0127          0.0683
## 2         4      0.0679           0.0239          0.0918
## 3         5      0.0823           0.0286          0.1109
```



The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `pencl`

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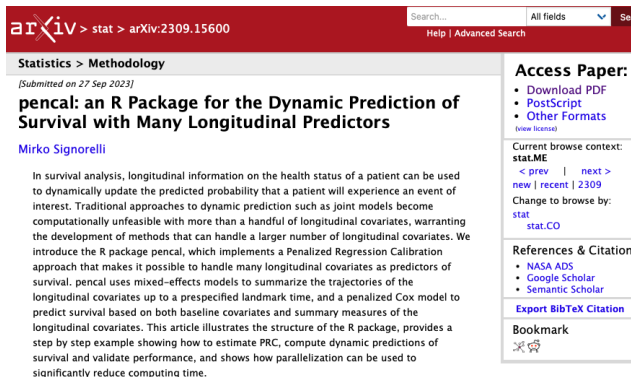
Package overview table



Table 1: Overview of the `pencal` functions that implement the different modelling steps for the PRC LMM and PRC MLPMM approaches.

Task	PRC LMM	PRC MLPMM
Step 1: estimate the mixed-effects models	<code>fit_lmms</code>	<code>fit_mlpmms</code>
Step 2: compute the predicted random effects	<code>summarize_lmms</code>	<code>summarize_mlpmms</code>
Step 3: estimate the penalized Cox model	<code>fit_prclmm</code>	<code>fit_prcmlpmm</code>
Computation of predicted survival probabilities	<code>survpred_prclmm</code>	<code>survpred_prcmlpmm</code>
Evaluation of predictive performance	<code>performance_prc</code>	<code>performance_prc</code>

- Vignette (Signorelli (2023)) available at [arXiv:2309.15600](https://arxiv.org/abs/2309.15600):

This is a screenshot of the arXiv website page for the paper 'pencial: an R Package for the Dynamic Prediction of Survival with Many Longitudinal Predictors' by Mirko Signorelli. The page has a red header with the arXiv logo and navigation links. The main content area is white and contains the title, author, submission date, and abstract. On the right side, there is a sidebar with links to download the paper in various formats, a 'Current browse context' section, and a 'References & Citation' section. The abstract text is visible in the main content area.

arXiv > stat > arXiv:2309.15600

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Statistics > Methodology

[Submitted on 27 Sep 2023]

pencial: an R Package for the Dynamic Prediction of Survival with Many Longitudinal Predictors

Mirko Signorelli

In survival analysis, longitudinal information on the health status of a patient can be used to dynamically update the predicted probability that a patient will experience an event of interest. Traditional approaches to dynamic prediction such as joint models become computationally infeasible with more than a handful of longitudinal covariates, warranting the development of methods that can handle a larger number of longitudinal covariates. We introduce the R package pencial, which implements a Penalized Regression Calibration approach that makes it possible to handle many longitudinal covariates as predictors of survival. pencial uses mixed-effects models to summarize the trajectories of the longitudinal covariates up to a prespecified landmark time, and a penalized Cox model to predict survival based on both baseline covariates and summary measures of the longitudinal covariates. This article illustrates the structure of the R package, provides a step by step example showing how to estimate PRC, compute dynamic predictions of survival and validate performance, and shows how parallelization can be used to significantly reduce computing time.

Subjects: **Methodology** (stat.ME); Computation (stat.CO)

Cite as: [arXiv:2309.15600](https://arxiv.org/abs/2309.15600) [stat.ME]
(or [arXiv:2309.15600v1](https://arxiv.org/abs/2309.15600v1) [stat.ME] for this version)
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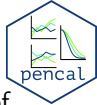
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References I



- Proust-Lima, C., Amieva, H., & Jacqmin-Gadda, H. (2013). Analysis of multivariate mixed longitudinal data: A flexible latent process approach. *British Journal of Mathematical and Statistical Psychology*, 66(3), 470–487.
- Signorelli, M. (2023). pencal: an R Package for the Dynamic Prediction of Survival with Many Longitudinal Predictors. *arXiv Preprint arXiv:2309.15600*.
- Signorelli, M., Ayoglu, B., Johansson, C., Lochmüller, H., Straub, V., Muntoni, F., Niks, E., Tsonaka, R., Person, A., Aartsma-Rus, A., Nilsson, P., Al-Khalili Szigartyo, C., & Spitali, P. (2020). Longitudinal serum biomarker screening identifies MDH2 as candidate prognostic biomarker for Duchenne muscular dystrophy. *Journal of Cachexia, Sarcopenia and Muscle*, 11(2), 505–517.
- Signorelli, M., Spitali, P., Al-Khalili Sgyziarto, C., The Mark-MD Consortium, & Tsonaka, R. (2021). Penalized regression calibration: A method for the prediction of survival outcomes using complex longitudinal and high-dimensional data. *Statistics in Medicine*.



The problem: dynamic prediction of survival

The method: Penalized Regression Calibration

The R package: `penca1`

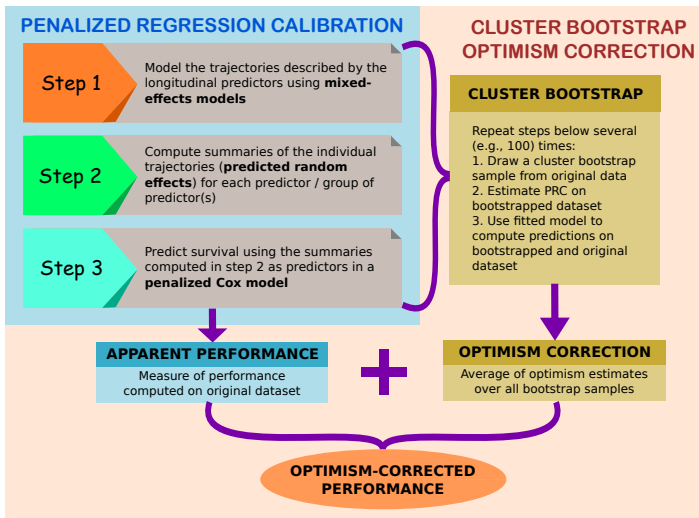
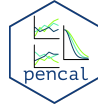
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Cluster-bootstrap optimism correction



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