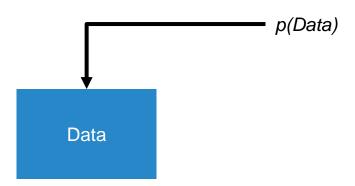
How Bitcoin works?

#### Content

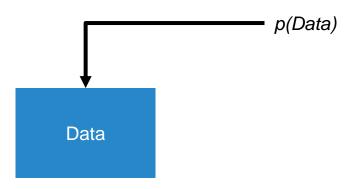
A class in data structures:

- Hash pointers
- Blockchain

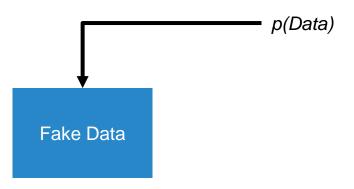
p(Data)



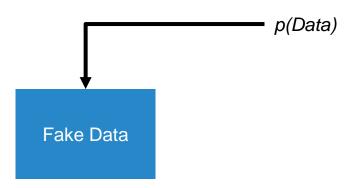
What happens if the data changes?



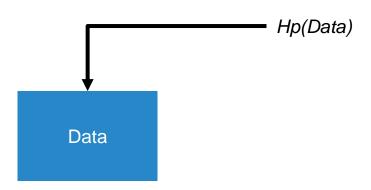
What happens if the data changes?

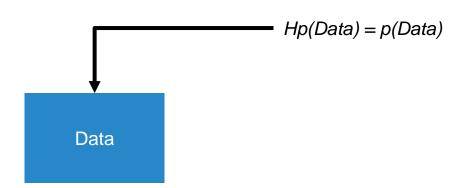


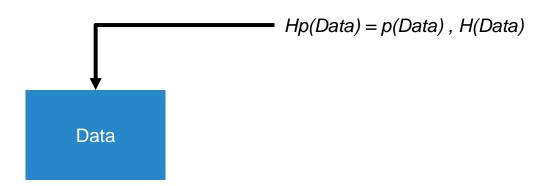
What happens if the data changes?



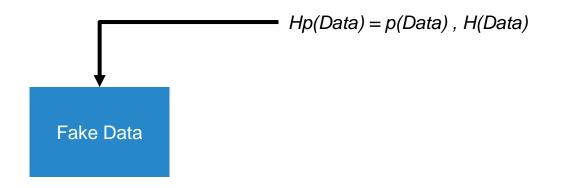
p does not reflect the change!!!



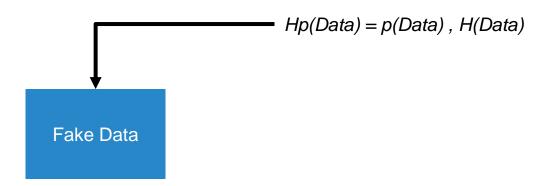




What happens if the data changes?



What happens if the data changes?



*Hp(Data)* does not point to Fake Data

What happens if the data changes?



*Hp(Data)* does not point to Fake Data

H(Fake Data) ≠ H(Data)

#### Examples of hash pointers:

- If I have a variable
- If my data is in an array
- If my data is in a dictionary (key-value) 
  show this

#### Use of hash pointers:

- In any data structure that uses pointers
- Linked lists = blockchain
- Binary trees = Merkle Trees

#### Content

#### A class in data structures:

- Hash pointers
- Blockchain



The data structure

Prev: NULL

The data structure

Prev: NULL

The data structure

Block1

Prev: NULL

The data structure



Prev: NULL

Data 1

Block2

Prev:

The data structure

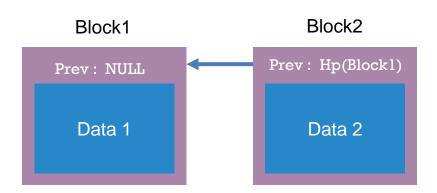
Block1

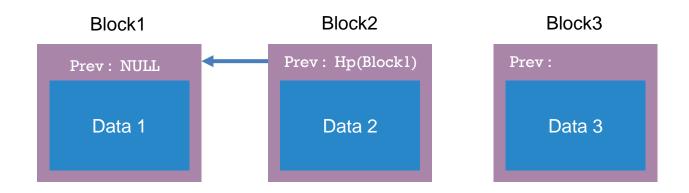
Prev: NULL

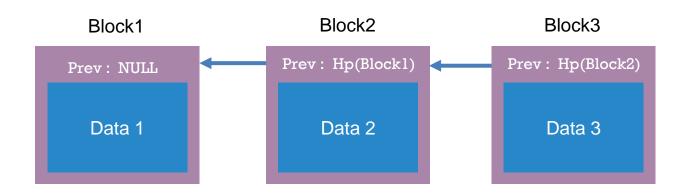
Data 1

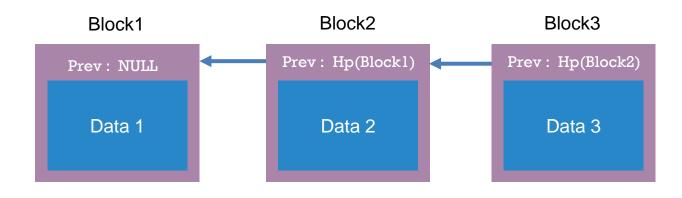
Block2

Prev: Hp(Block1)

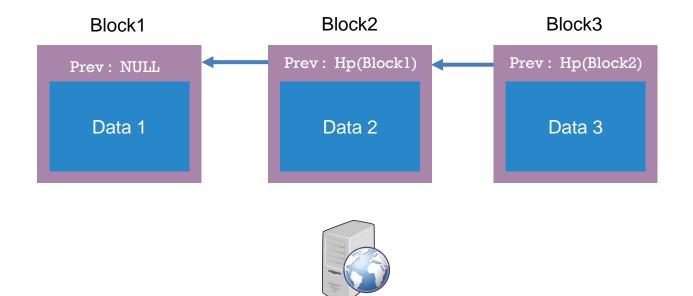




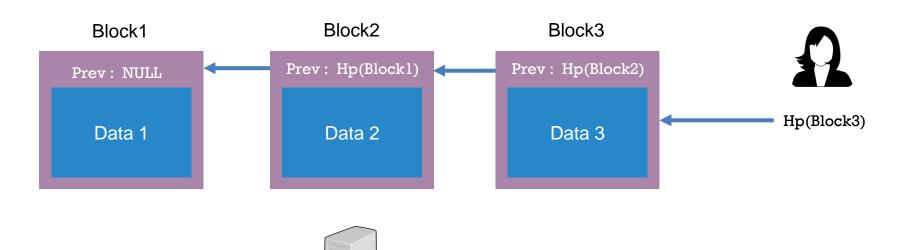


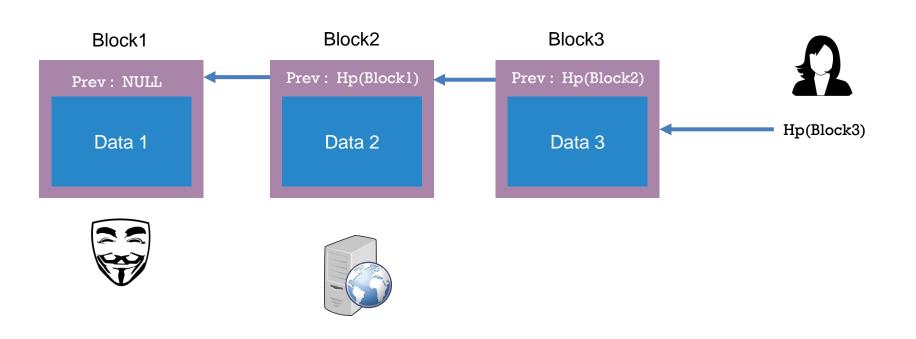


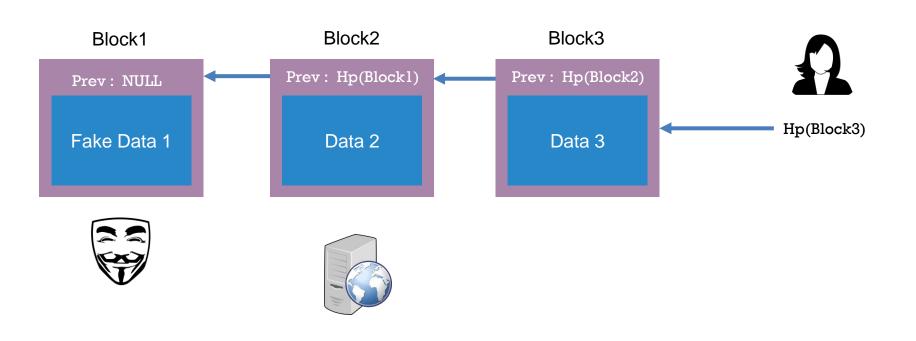


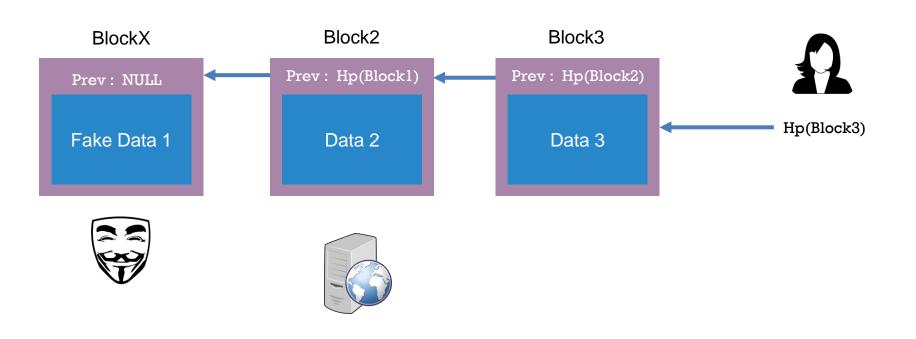


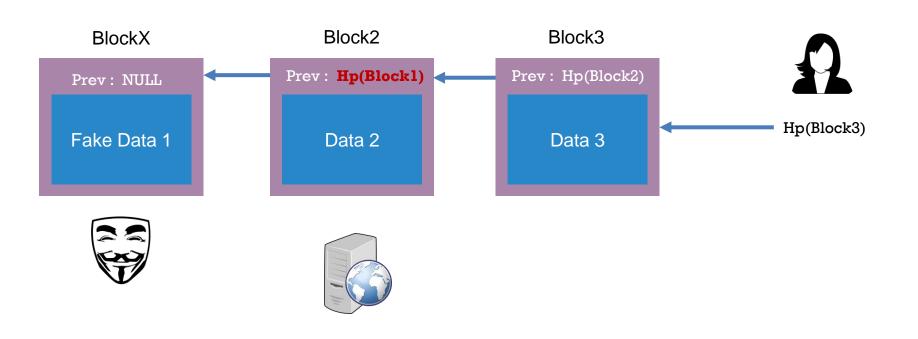


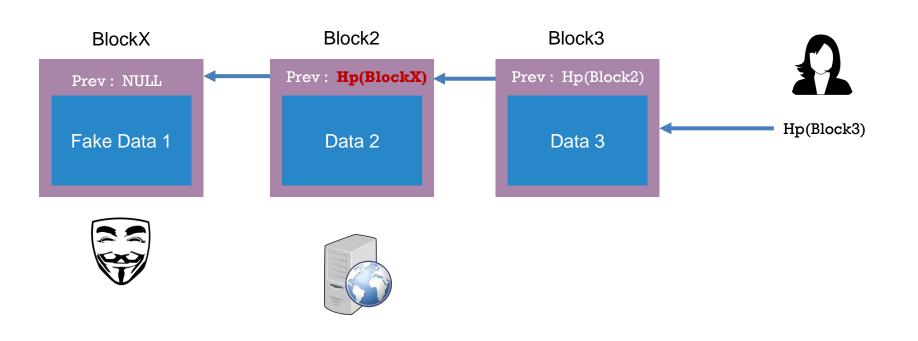


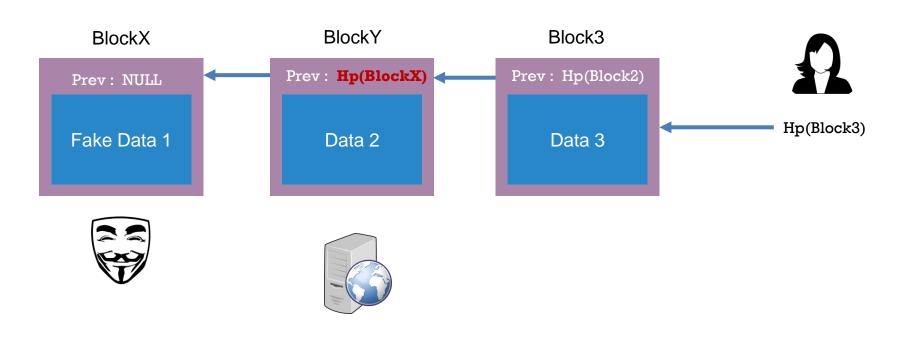


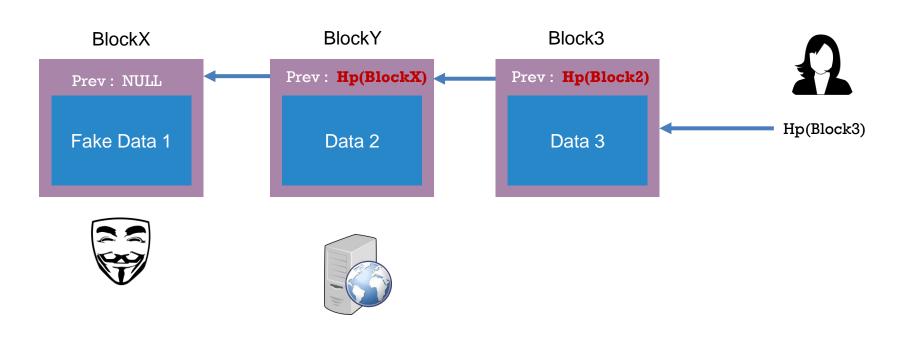


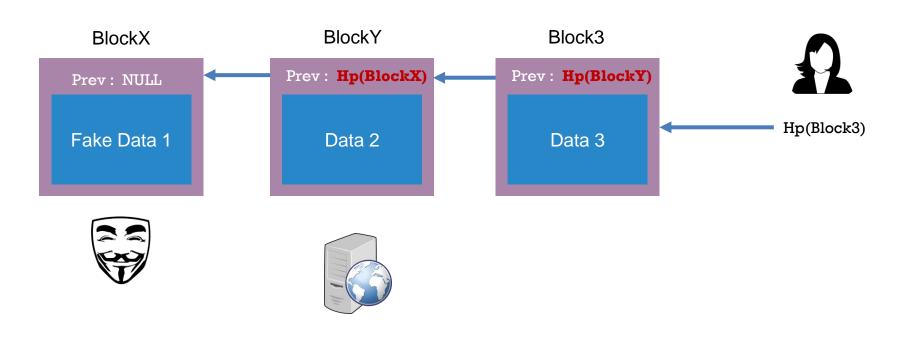


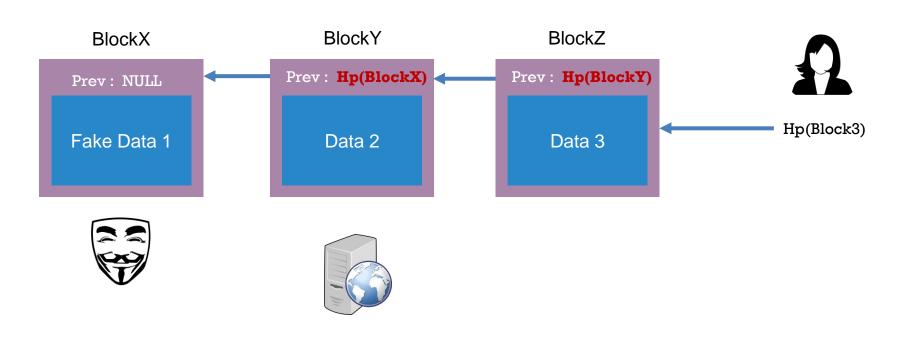


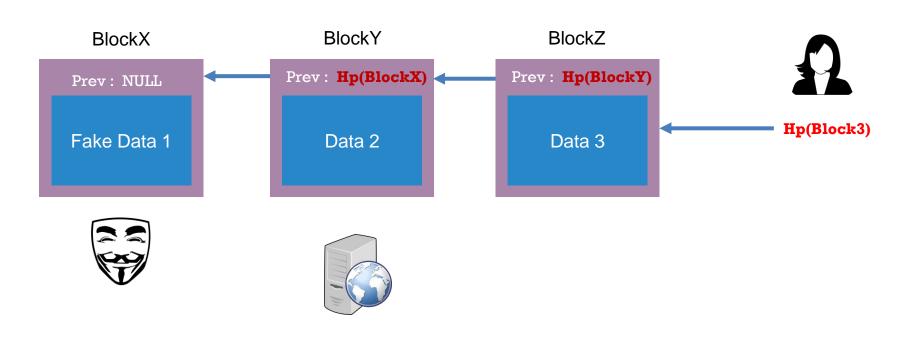


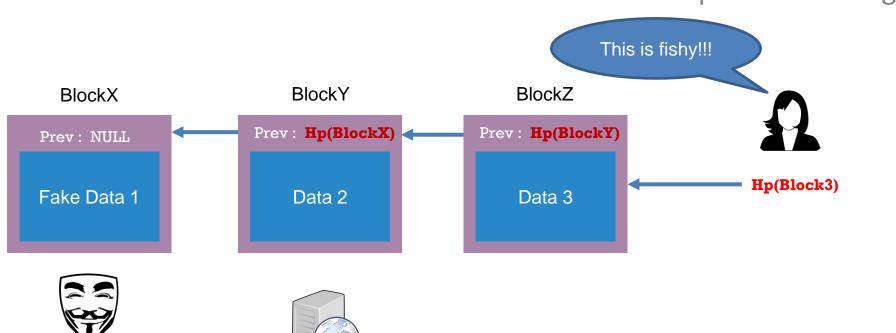




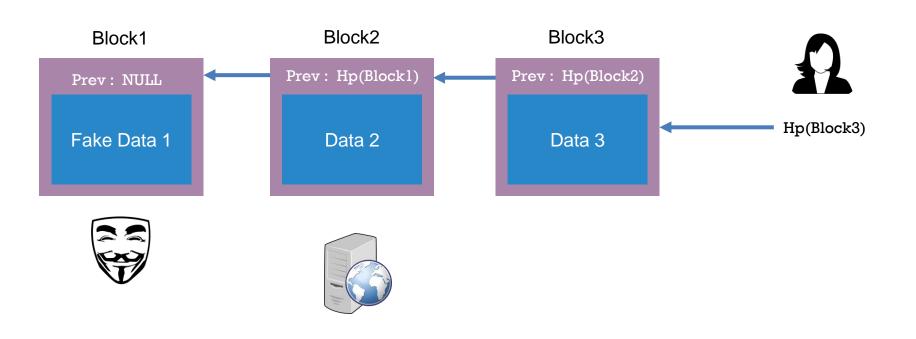








What is this is the only change?



Consistent historic data



### Ledger

Alice pays Bob \$50



Alice



Bob



Charlie

Consistent historic data



#### Ledger

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. .



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

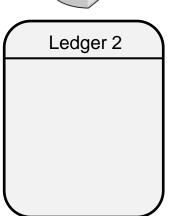
Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .





Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. .

#### Ledger 2

Bob pays Charlie \$250



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

#### Ledger 3



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

#### Ledger 3

Alice pays Bob \$20

Alice pays Charlie \$10

Bob pays Charlie \$100

Charlie pays Alice \$40



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

#### Ledger 3

Alice pays Bob \$20

Alice pays Charlie \$10

Bob pays Charlie \$100

Charlie pays Alice \$40



Alice



Bob



Charlie

Consistent historic data



#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

. . .

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$20

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

#### Ledger 3

Alice pays Bob \$20

Alice pays Charlie \$10

Bob pays Charlie \$100

Charlie pays Alice \$40



Alice



Bob



Charlie

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

Hash

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

64f3de1975fb7121411ed e2180547b8d94fcc5f7342 db03423444f528417b797

Hash

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

64f3de1975fb7121411ed e2180547b8d94fcc5f7342 db03423444f528417b797

Hash

Bob pays Charlie \$250

Ledger 2

Bob pays Alice \$20

Charlie pays Alice \$80

Alice pays Bob \$20

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

Hash

64f3de1975fb7121411ed e2180547b8d94fcc5f7342 db03423444f528417b797

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$20

Charlie pays Alice \$80

Alice pays Bob \$20



Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$20

Charlie pays Alice \$80

Alice pays Bob \$20

Alice pays Charlie \$10

64f3de1975fb7121411ed e2180547b8d94fcc5f7342 db03423444f528417b797

Hash

b4056df6691f8dc72e5630 2ddad345d65fead3ead929 9609a826e2344eb63aa4

Consistent historic data

#### Ledger 1

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

Consistent historic data

#### Ledger 1

Prev hash: NULL

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

Consistent historic data

L1

Ledger 1

Prev hash: NULL

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

Consistent historic data

#### L1

#### Ledger 1

Prev hash: NULL

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

#### Ledger 2

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Consistent historic data

L1

Ledger 1

Prev hash: NULL

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

Ledger 2

Prev hash: Hp(L1)

Bob pays Charlie \$250

Bob pays Alice \$120

Charlie pays Alice \$80

Alice pays Bob \$20

Consistent historic data

L1

Ledger 1

Prev hash: NULL

Alice pays Bob \$50

Alice pays Charlie \$20

Bob pays Charlie \$100

Charlie pays Alice \$40

Charlie pays Bob \$80

L2

Ledger 2

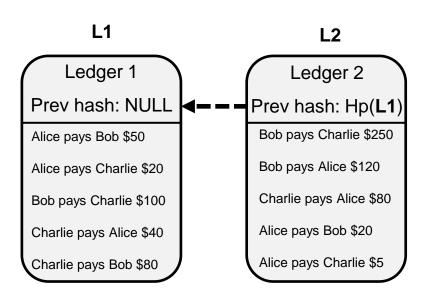
Prev hash: Hp(L1)

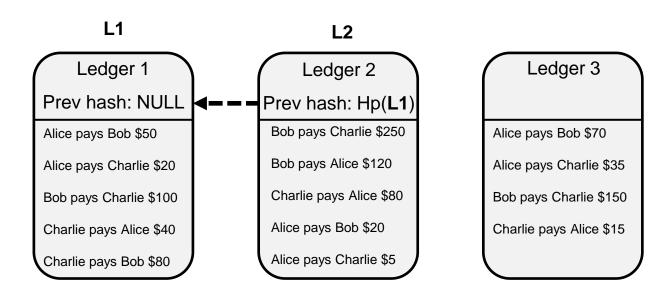
Bob pays Charlie \$250

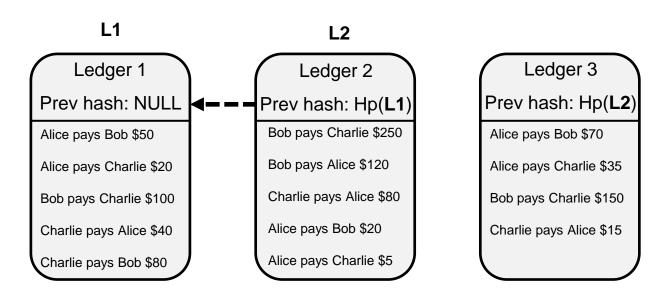
Bob pays Alice \$120

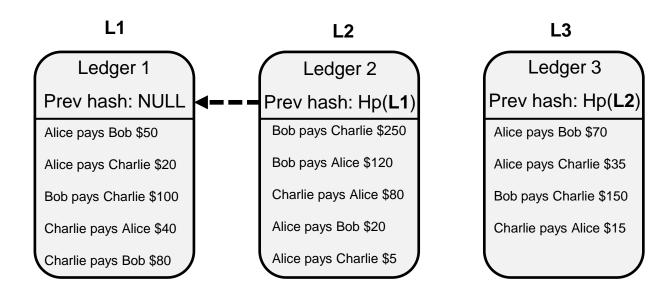
Charlie pays Alice \$80

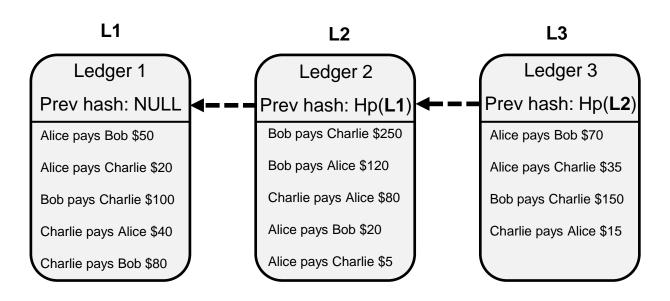
Alice pays Bob \$20



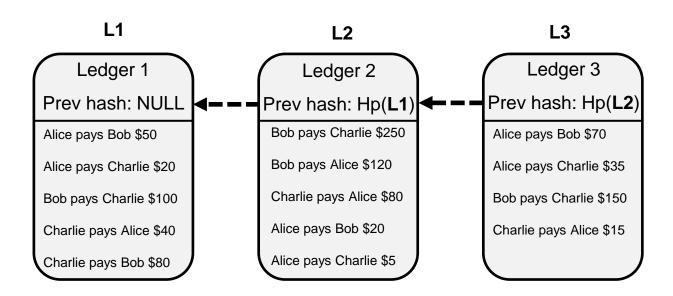






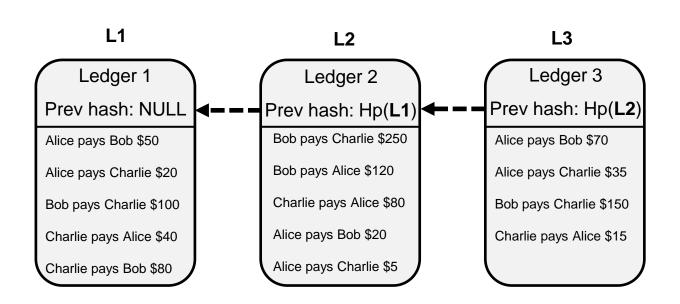


Consistent historic data

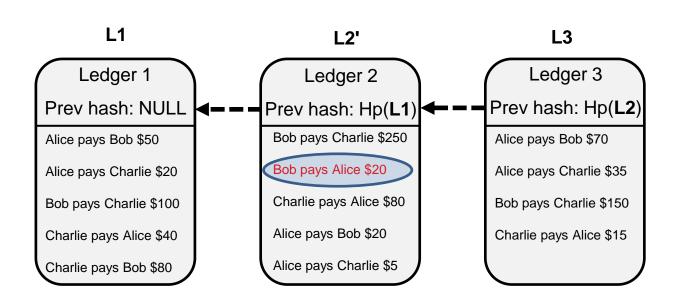


### **Blockchain**

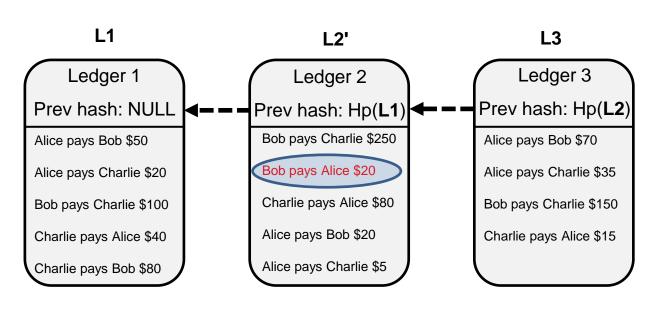
# **Immutability**



# **Immutability**



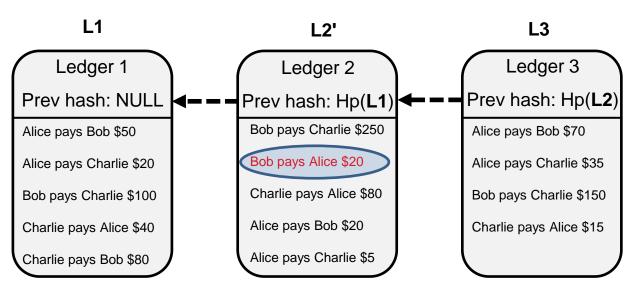
# **Immutability**



 $H(L2') \neq H(L2)$ 

# **Immutability**

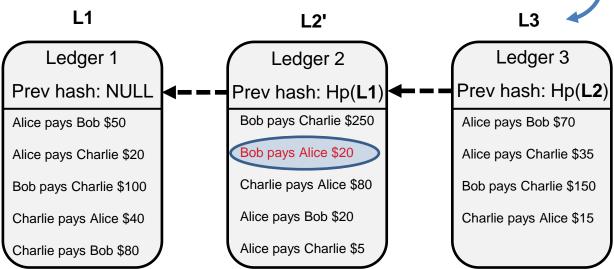




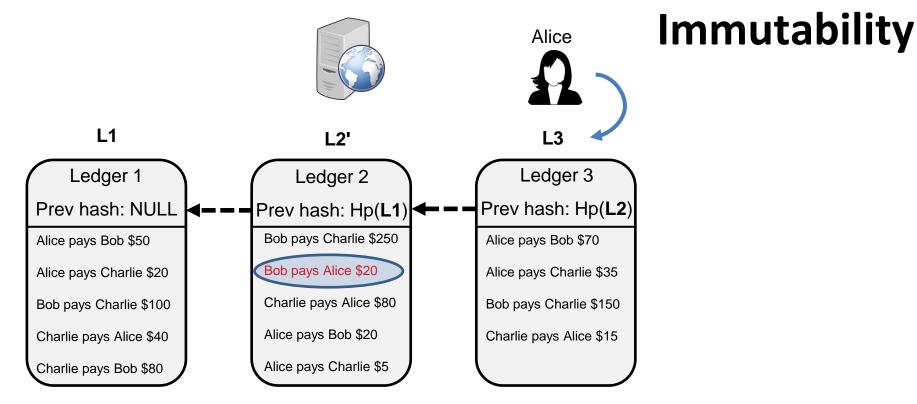
 $H(L2') \neq H(L2)$ 

# **Immutability**





 $H(L2') \neq H(L2)$ 



 $H(L2') \neq H(L2)$ 



## **Immutability**

L1 **L2'** Ledger 3 Ledger 1 Ledger 2 Prev hash: Hp(L2) Prev hash: NULL Prev hash: Hp(L1) ◀ Bob pays Charlie \$250 Alice pays Bob \$50 Alice pays Bob \$70 Bob pays Alice \$20 Alice pays Charlie \$35 Alice pays Charlie \$20 Charlie pays Alice \$80 Bob pays Charlie \$100 Bob pays Charlie \$150 Alice pays Bob \$20 Charlie pays Alice \$40 Charlie pays Alice \$15 Alice pays Charlie \$5 Charlie pays Bob \$80

 $H(L2') \neq H(L2)$ 

#### Alice L1 L2' Ledger 3 Ledger 1 Ledger 2 Prev hash: Hp(L2) Prev hash: NULL Prev hash: Hp(L1) Bob pays Charlie \$250 Alice pays Bob \$70 Alice pays Bob \$50 Bob pays Alice \$20 Alice pays Charlie \$35 Alice pays Charlie \$20 Charlie pays Alice \$80 Bob pays Charlie \$100 Bob pays Charlie \$150 Alice pays Bob \$20 Charlie pays Alice \$40 Charlie pays Alice \$15 Alice pays Charlie \$5 Charlie pays Bob \$80

**Immutability** 

 $H(L2') \neq H(L2)$ 

#### Alice L1 L2' Ledger 1 Ledger 2 Ledger 3 Prev hash: Hp(L2) Prev hash: NULL Prev hash: Hp(L1) Bob pays Charlie \$250 Alice pays Bob \$70 Alice pays Bob \$50 Bob pays Alice \$20 Alice pays Charlie \$35 Alice pays Charlie \$20 Charlie pays Alice \$80 Bob pays Charlie \$100 Bob pays Charlie \$150 Alice pays Bob \$20 Charlie pays Alice \$40 Charlie pays Alice \$15 Alice pays Charlie \$5 Charlie pays Bob \$80

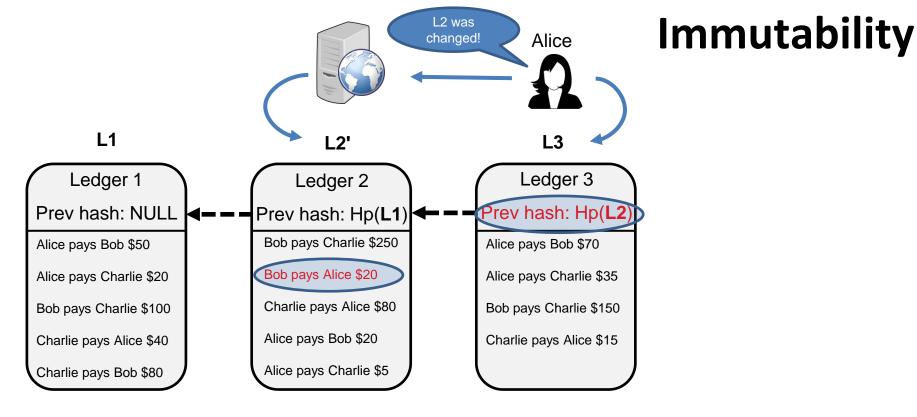
 $H(L2') \neq H(L2)$ 

# **Immutability**

#### Alice L1 L2' Ledger 1 Ledger 2 Ledger 3 Prev hash: Hp(L2 Prev hash: NULL Prev hash: Hp(L1) Bob pays Charlie \$250 Alice pays Bob \$70 Alice pays Bob \$50 Bob pays Alice \$20 Alice pays Charlie \$35 Alice pays Charlie \$20 Charlie pays Alice \$80 Bob pays Charlie \$100 Bob pays Charlie \$150 Alice pays Bob \$20 Charlie pays Alice \$40 Charlie pays Alice \$15 Alice pays Charlie \$5 Charlie pays Bob \$80

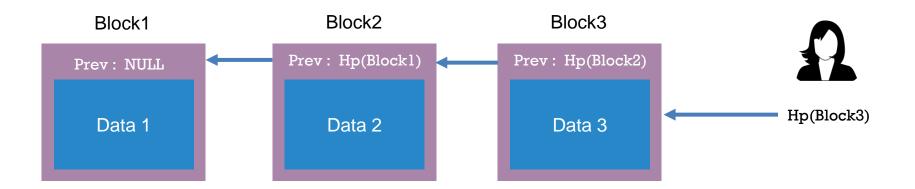
 $H(L2') \neq H(L2)$ 

# **Immutability**

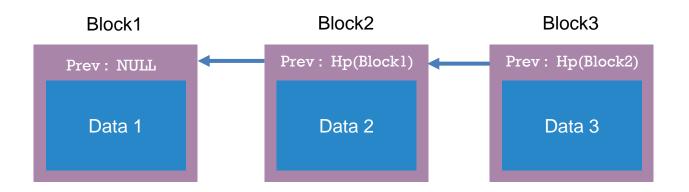


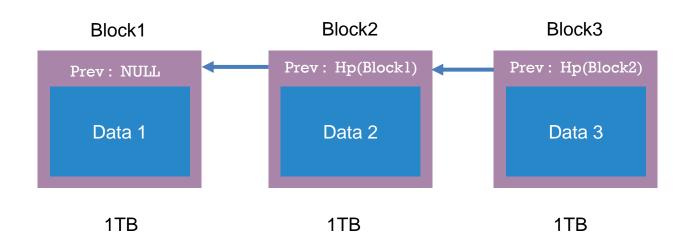
 $H(L2') \neq H(L2)$ 

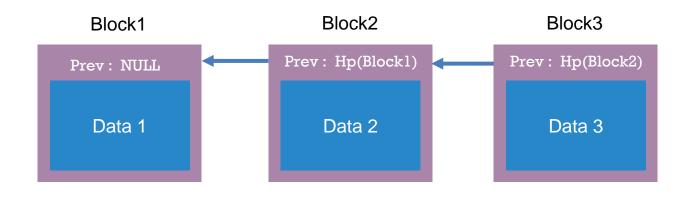
How to detect if there is a change?

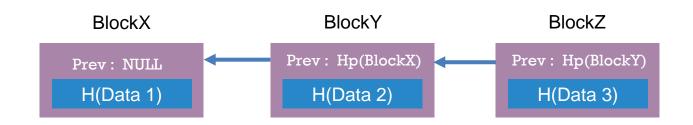


If we only have the head

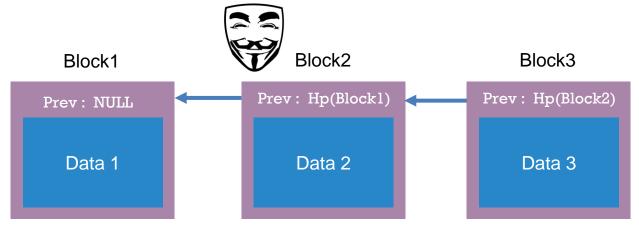


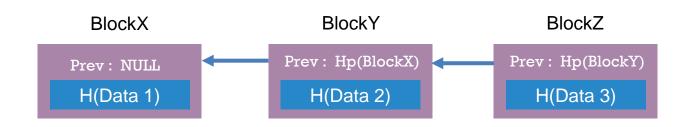




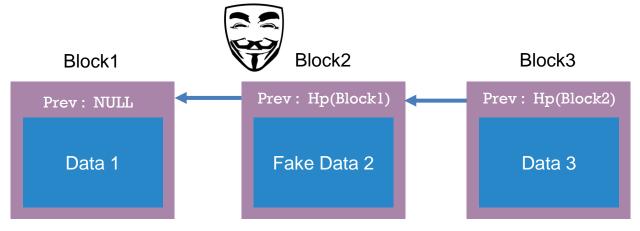


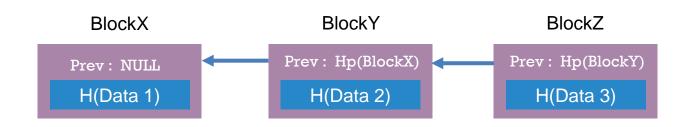






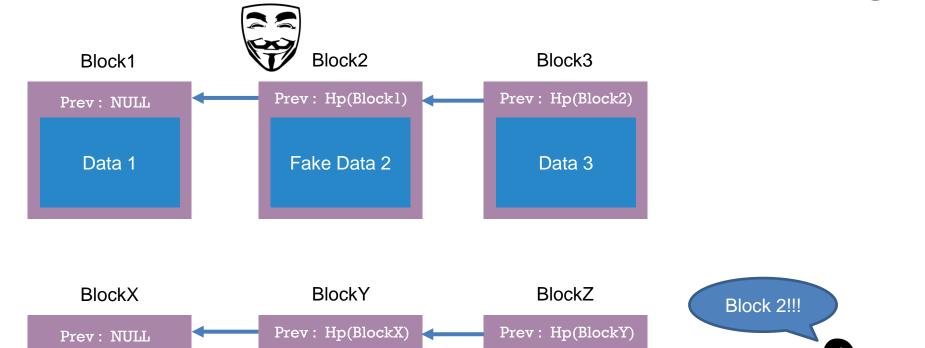








How to detect if there is a change?



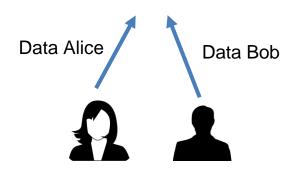
H(Data 2)

H(Data 3)

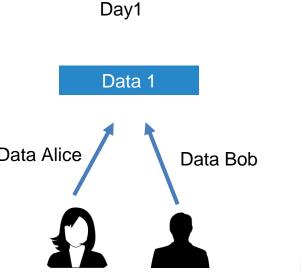
H(Data 1)



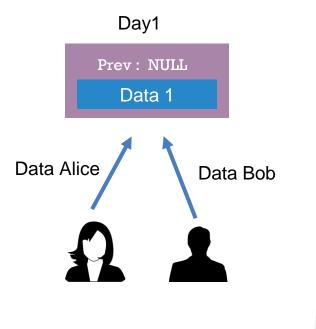
Day1



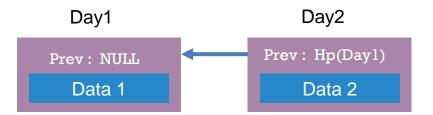








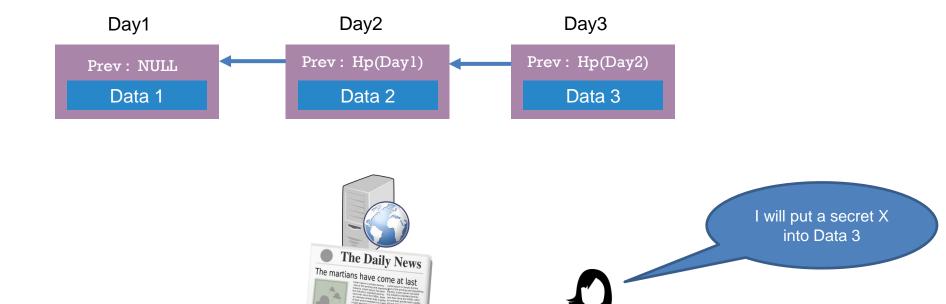


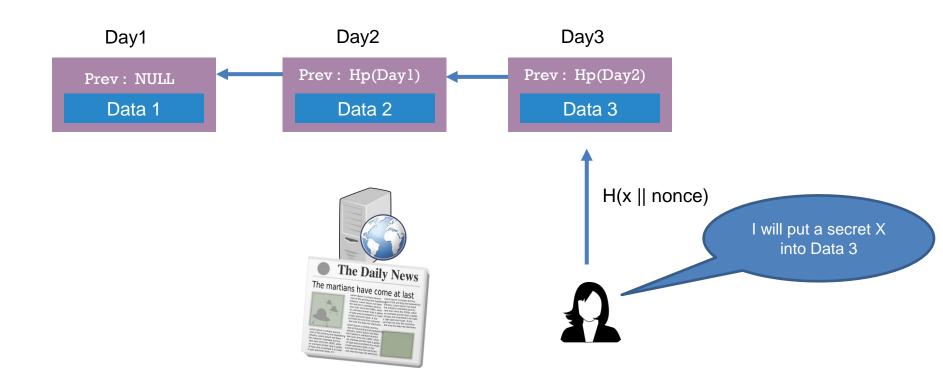


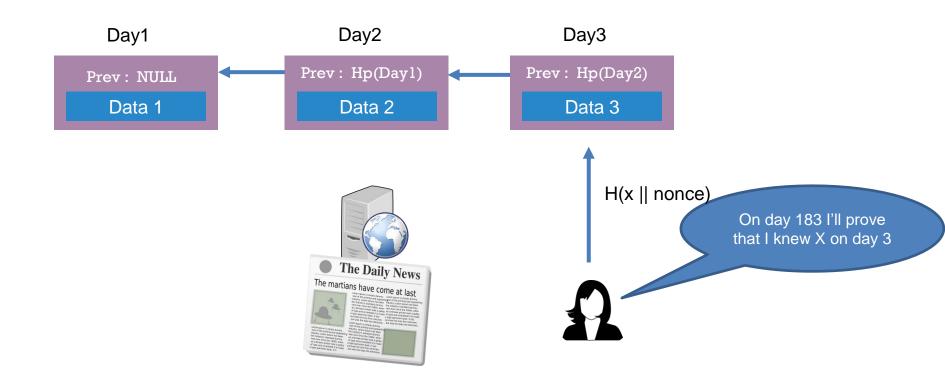


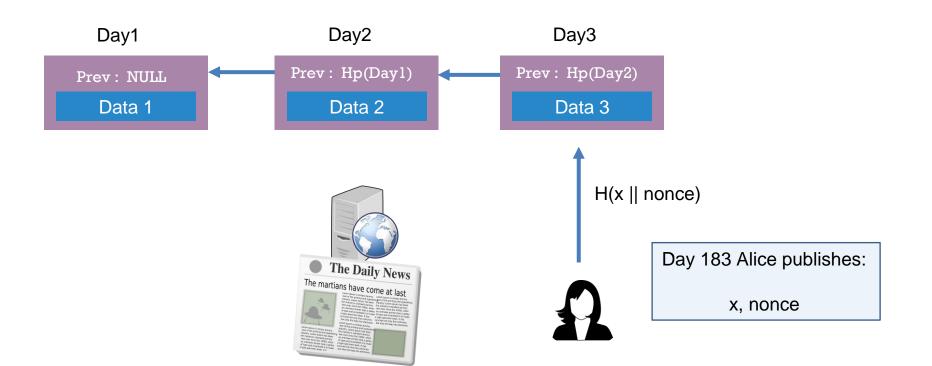


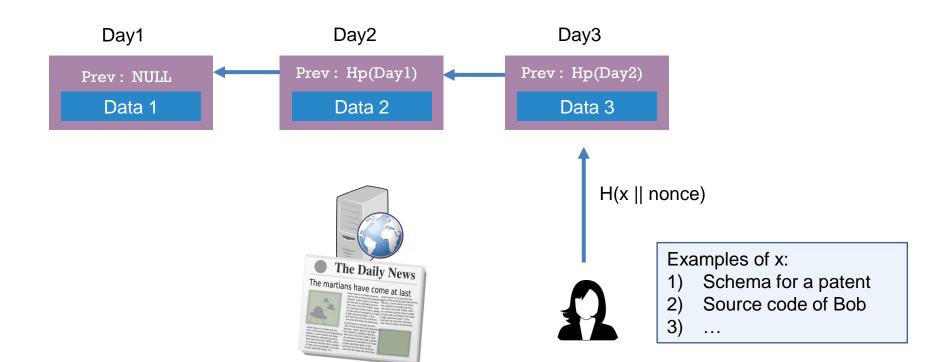


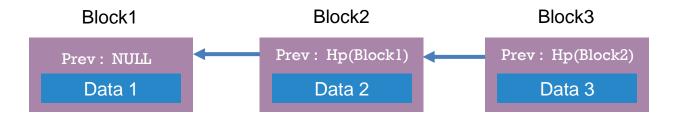


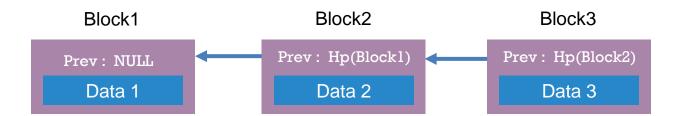






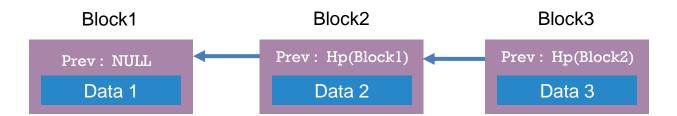




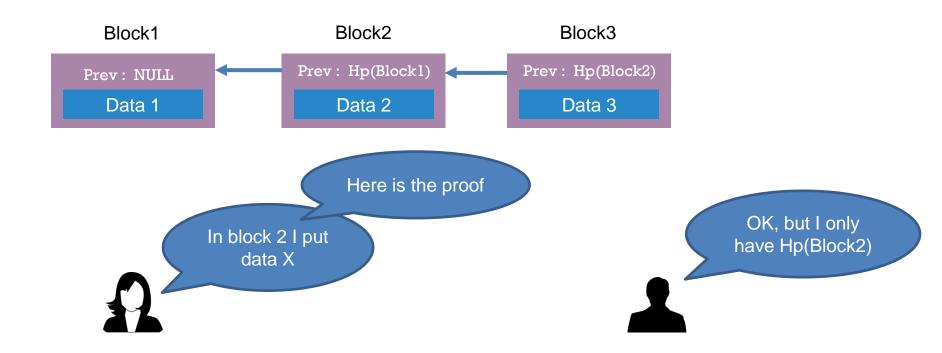


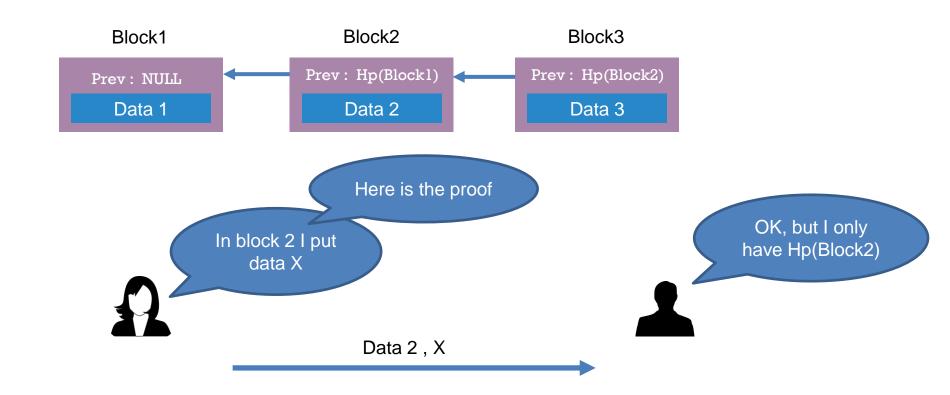


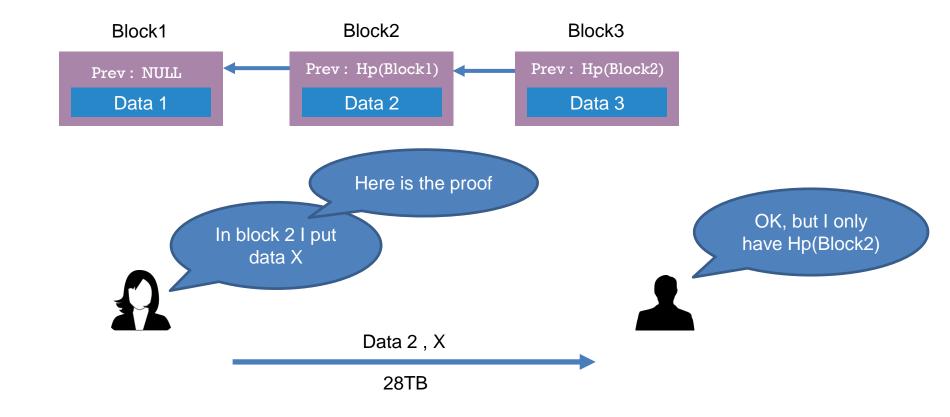


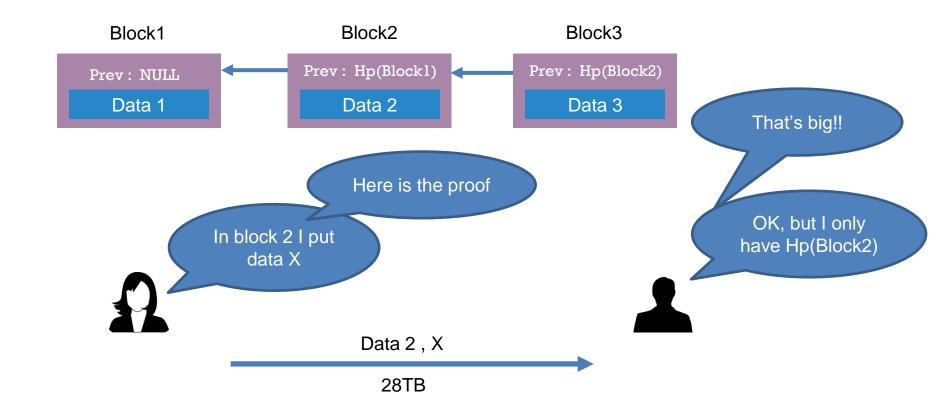


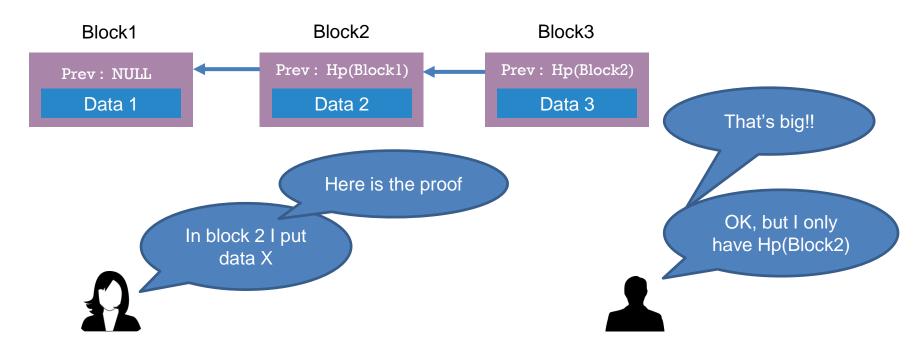












How to make the proof more efficient???

# reading

#### Narayanan et. Al:

- Chapter 1.2
- Chapter 9.1

#### Practice time!!!

#### Exercizes!!!

- Implement blockchain
- Run against the test data
- Different ways of implementing this

Let's see the two class we need to implement!!!