

Week 2 Homework

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Task 1

You should find:

1. simulate this mechanism (obtain all positions.)
2. velocities for A, B, C, E, F, D. Find angular velocities for all links.
3. acc. for A and B and ang. vel for AB
4. draw plots for previous statements.

Needed variables:

$$\omega_{O_1A} = 2 \text{ rad/s};$$

$$\phi = 60^\circ; a = 56; b = 10; c = 26; d = 16; e = 25;$$

$$O_1A = 21; O_2B = 25; O_3F = 20; AB = 54; BC = 52;$$

$$CD = 69; CE = 35; EF = 32.$$

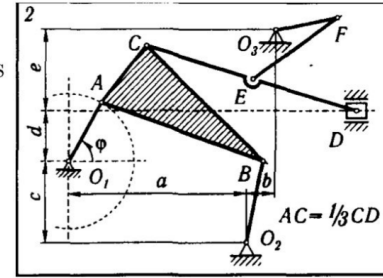


Figure 3: HW 2, task 1
(Yablonskii (rus) K4)

Let O1 be the origin

$$x_A = O_1A \begin{bmatrix} \cos(\phi(t)) \\ \sin(\phi(t)) \end{bmatrix}$$

Writing the equations of intersections of two circles to find XB

$$\begin{cases} (x_B - x_A)^2 + (y_B - y_A)^2 = (AB)^2 \\ (x_B - x_{o_2})^2 + (y_B - y_{o_2})^2 = (O_2B)^2 \end{cases}$$

From the triangle ABC, we can find Xc in the intersection of two circles:

$$\begin{cases} (x_C - x_A)^2 + (y_C - y_A)^2 = (AB)^2 \\ (x_C - x_B)^2 + (y_C - y_B)^2 = (BC)^2 \end{cases}$$

point D slides horizontally over axis x, thus

$$X_D = \begin{bmatrix} x_D(t) \\ d \end{bmatrix}$$

$$|X_c - X_D| = CD$$

We know that D is on CD, hence

$$X_E = X_C + CE \frac{\overrightarrow{CD}}{|\overrightarrow{CD}|}$$

F can also be found from the equation of intersection of two circles:

$$\begin{cases} (x_F - x_E)^2 + (y_F - y_E)^2 = (EF)^2 \\ (x_F - x_{o_3})^2 + (y_F - y_{o_3})^2 = (O_3F)^2 \end{cases}$$

let us use Instantaneous Velocity Centre to find the angular velocity for AB

$$\omega_{AB} = V_A r_{AB}$$

r can be found with the intersection of two lines O1A and O2B

$$r_{AB} = \begin{cases} y = \left(\frac{y_A - y_{o1}}{x_A - y_{o1}} \right) x + \left(y_A - \frac{y_A - y_{o1}}{x_A - y_{o1}} x_A \right) \\ y = \left(\frac{y_B - y_{o2}}{x_B - y_{o2}} \right) x + \left(y_B - \frac{y_B - y_{o2}}{x_B - y_{o2}} x_B \right) \end{cases}$$

Now after finding all positions, we can obtain velocities and accelerations by differentiating once and twice in order.

Task 2

Body B is static, A – moves. No friction. You should find:

1. angular vel. and angular acc. for A;
2. vel. and acc. for M point;
3. draw plots for previous statements.

Needed variables:

$$OM_0 = 40; \omega_1 = 2; \varepsilon_1 = 3.7; M_0M = 5.$$

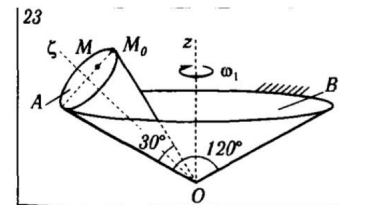


Figure 4: HW 2, task 2
(Yablonskii (rus) K6)

$$O = (0; 0; 0), Z = (0; 0; ZO), S = (0; 0; SO) A = (SA, 0, SO),$$

$$P = (PZ \cdot \cos(\phi(t)), PZ \cdot \sin(\phi(t)), ZO)$$

$$AO = M_0O$$

$$OP = AO \cdot \cos(15)$$

$$AP = AO \cdot \sin(15) = PM_0$$

$$AE = PE = AP \cdot \cos(45)$$

$$PZ = AS - AE$$

$$SO = AO \cdot \sin(30)$$

$$ZO = SO + PE$$

Point p is on a circle where

$$z = ZO$$

$$X_P(t) = \begin{bmatrix} PZ \cdot \cos(\phi(t)) \\ PZ \cdot \sin(\phi(t)) \\ ZO \end{bmatrix}$$

$$V_P(T) = w_1(t) \times OP$$

Rolling happens without slipping, then:

$$\phi(t) \cdot AS = \phi_M(t) \cdot AP$$

$$\phi_M(t) = \frac{AS}{AP} \cdot \phi(t)$$

$$v_M = v_P + w_2 \times r_{PM}$$

$$a_M = a_{M_t} + a_{M_n} + a_{P_t} + a_{P_n}$$

tangential and normal accelerations can be obtained from the equations

$$a_n = \frac{v^2}{r}$$

$$a_t = \alpha \cdot r$$