

SAS Algorithm Pseudocode:

1. Find: sequence of slew maneuvers to avoid sun vector

(a) Check the sun vector intrusion

- i. Find eigenaxis $\hat{e} = \frac{\hat{P}_i \times \hat{P}_f}{|\hat{P}_i \times \hat{P}_f|}$
- ii. Compute $\alpha = \frac{\pi}{2} - \cos^{-1}(\hat{S} \cdot_{\mathcal{N}} \hat{e})$
- iii. IF $|\alpha| < \epsilon_p$, THEN find $\vec{S}_{||} = \hat{S} \cos \alpha$

(b) Compute ϕ_1 : $\phi_1 = \cos^{-1}(\hat{P}_i \cdot_{\mathcal{G}} \hat{S}_{||}) - \epsilon_p$

(c) Compute ϕ_2 :

- i. IF $\alpha \neq 0$, THEN $\phi_2 = 2 \sin^{-1} \left(\frac{\sin \epsilon_p}{\sin \theta} \right)$, $\theta = \cos^{-1}(\hat{P}_1 \cdot \hat{S})$
- ii. IF $\alpha = 0$, THEN $\phi_2 = \pi$

(d) Compute ϕ_3 : $\phi_3 = \cos^{-1}({}_{\mathcal{G}}\hat{P}_f \cdot \hat{P}_2)$

2. Find: commanded angular velocity, angular acceleration, and quaternion profiles

(a) Compute $\phi_{tt} = \frac{\dot{\phi}_{max}^2}{\ddot{\phi}_{max}}$

(b) Compute t_1 , t_2 , and t_f .

IF $\phi > \phi_{tt}$, THEN :

$$t_1 = t_0 + \frac{\dot{\phi}_{max} - \dot{\phi}_0}{\ddot{\phi}_{max}}$$

$$t_2 = t_1 + \frac{1}{\ddot{\phi}_{max}} \left[\phi_f - \dot{\phi}_0(t_1 - t_0) - \frac{1}{2} \ddot{\phi}_{max}(t_1 - t_0)^2 - \frac{\dot{\phi}_{max}(\dot{\phi}_{max} - \dot{\phi}_f)}{\ddot{\phi}_{max}} + \frac{(\dot{\phi}_{max} - \dot{\phi}_f)^2}{2\ddot{\phi}_{max}} \right]$$

$$t_f = t_1 + \frac{1}{\ddot{\phi}_{max}} \left[\phi_f - \dot{\phi}_0(t_1 - t_0) - \frac{1}{2} \ddot{\phi}_{max}(t_1 - t_0)^2 + \frac{(\dot{\phi}_{max} - \dot{\phi}_f)^2}{2\ddot{\phi}_{max}} \right].$$

ELSE:

$$t_f = \sqrt{\frac{\dot{\phi}_{max}^2}{\ddot{\phi}_{max}}}$$

$$t_2 = t_f/2$$

$$t_1 = t_2$$

(c) Find ${}^D R^N$: ${}^D R^N = [(\cos \phi) I_{3 \times 3} + (1 - \cos \phi) \hat{e} \hat{e}^T - (\sin \alpha) E^x]$

(d) Find ${}_{\mathcal{B}} \dot{\omega}^D$: ${}_{\mathcal{B}} \dot{\omega}^D = {}^D R^N \ddot{\phi}_{max} \cdot_{\mathcal{N}} \hat{e}$

(e) Solve for control torque, u : $J \cdot_{\mathcal{B}} \dot{\omega}^D = u - {}_{\mathcal{B}} \omega^C \times J \cdot_{\mathcal{B}} \omega^C$

(f) FOR each ϕ between switching times, propagate ω and q between switching times by solving above eqn and $\dot{q} = \frac{1}{2} \Omega q$

where

$$\Omega = \begin{bmatrix} 0 & \omega_3 & -\omega_2 & \omega_1 \\ -\omega_3 & 0 & -\omega_1 & \omega_2 \\ \omega_2 & -\omega_1 & 0 & \omega_3 \\ -\omega_1 & \omega_2 & -\omega_3 & 0 \end{bmatrix}$$

with correct u for each switching time interval.