# SUN-AVOIDANCE SLEW PLANNING ALGORITHM WITH POINTING AND ACTUATOR CONSTRAINTS

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A sun avoidance slew maneuver is described in this paper. The algorithm finds the angular velocity, angular acceleration, and quaternion profiles needed to avoid the sun vector that lies near the plane of a sensor's FOV onboard a spacecraft.

#### INTRODUCTION

Large-angle slew maneuvers are required during any Earth-pointing or interplanetary missions. In many space missions, and for safety consideration, a sensitive payload such as imaging camera or telescope needs to be retargeted while avoiding sun vector or other bright objects in the sky. The attitude reorientation problem in the presence of attitude constrained zones has been studied in the last three decades. McInnes<sup>1</sup> addressed this problem via using an artificial potential function. He proposed a guidance law which is entirely analytical and suitable for onboard implementation. However, he uses Euler angles which are singular for large slew angles. A geometric approach was proposed by Spindle,<sup>2</sup> Hablani,<sup>3</sup> and Biggs and Colley<sup>4</sup> where a feasible attitude maneuver, or a guidance law, is precomputed based on the attitude-avoidance-zone constraints. Another approach for addressing this problem is using randomized algorithms.<sup>5</sup> However, depends on the number of constraints and initial and final attitudes, this approach is computationally expensive and not suitable for onboard implementation. Another approach for solving the time optimal reorientation maneuver subject to boundaries and path constraints is proposed by Spiller et al.<sup>6</sup> They used the particle swarm optimization (PSO) technique to find a sub-optimal solution with keep-out constraints. Another approach is to cast the problem as a convex optimization problem and use a semi-definite programming (SDP) or quadratically constrained quadratic programming (QCQP) to solve them. See for instance Kim and Mesbahi, Kim et al., Sun and Dai, and Lee and Mesbahi Recently, Ramos and Schaub<sup>11</sup> proposed a method based on the Lyapunov stability theorem and logarithmic barrier potential function to derive a steering law for attitude control of a spacecraft subject to conically constrained inclusion and exclusion regions. They also considered the control-torque constraint in their algorithm. In this paper, we present a novel geometric approach for large-angle slew planning with pointing and actuator constraints. We assume spacecraft has a single light-sensitive payload with control-torque and angular momentum constraints. Furthermore, we assume the initial and final attitudes, instrument boresight vector, and sun vector are known. Then we derive the desired quaternions, angular velocity, and angular acceleration based on the Pontryagin's minimum principle (PMP) for this maneuver. The proposed algorithm in this paper is intuitive, deterministic, easy to implement, and includes the control-torque and angular momentum constraints. The

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main drawback of the proposed algorithm is its limitation for a single payload, single-constraint region. A Monte Carlo simulation is performed to show the viability of the proposed algorithm with control-torque and angular momentum constraints.

## **Problem Justification**

$$\mathrm{Given:}_N \hat{P}_i,\,{}_N \hat{P}_f,\,{}_N \hat{S},\,{}_G \hat{P},\,\epsilon_p,\,{}^N q^G,\,{}^N_G \omega^G(t_i),\,\mathrm{and}\,{}^N_G \omega^G(t_f)\;.$$

## Find:

- 1. A sequence of slew maneuvers to avoid sun vector.
- 2. the commanded angular velocity, angular acceleration, and quaternion profiles.

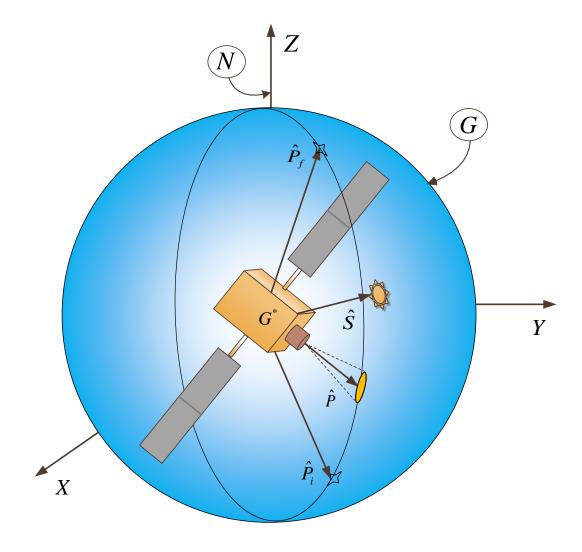


Figure 1. The spacecraft is not drawn to scale.

## Nomenclature:

- $\bullet$  G frame: Unit sphere attached to the gyrostat.
- N: frame: The Newtonian frame fixed in the inertial space.
- $\bullet \ _{G}\hat{P} :$  Unit vector along the bore sight of payload in the G frame.
- ${}_{N}\hat{P}_{i}$ : Unit vector of the initial point in the G frame.
- ${}_{N}\hat{P}_{f}$ : Unit vector of the final point in the G frame.
- $_{N}\hat{S}$ : Unit vector of the sun vector in the N frame.
- $\epsilon_p$ : Payload half-cone angle.

## Literature surveyed

This is the literature surveyed.

## **Contribution of work**

This is the contribution of work.

## ALGORITHM DESCRIPTION

#### **Slew Maneuver**

Check the Sun Vector Intrusion

1. Check the angular separation between the sun vector,  $\hat{S}$ , and the  $\hat{P}_i - \hat{P}_f$  plane.

$$\alpha = \frac{\pi}{2} - \cos^{-1}(\hat{S}.\hat{e}) \tag{1}$$

where the eigenaxis is determined by

$$\hat{e} = \frac{\hat{P}_i \times \hat{P}_f}{|\hat{P}_i \times \hat{P}_f|} \tag{2}$$

2. IF  $|\alpha|<\epsilon_p$ , THEN determine the projection of the sun vector into the  $\hat{P}_i-\hat{P}_f$  plane.

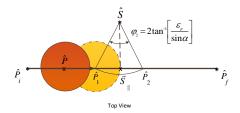
$$\vec{S}_{||} = \hat{S}\cos\alpha \tag{3}$$

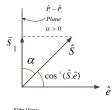
Slew Maneuvers

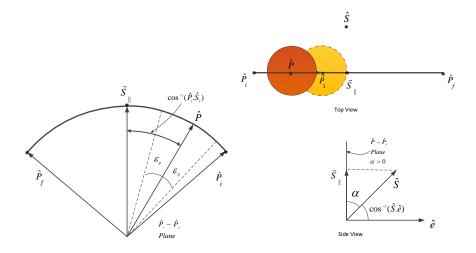
1. The  $1^{st}$  slew around the eigenaxis,  $\hat{e}$ , through angle:

$$\phi_1 = \begin{cases} \cos^{-1}(\hat{P}._G\hat{S}_{||}) - \epsilon_p & when \cos^{-1}(\hat{P}._G\hat{S}_{||}) - \epsilon_p \le \pi \\ \cos^{-1}(\hat{P}._G\hat{S}_{||}) - \epsilon_p - 2\pi & when \cos^{-1}(\hat{P}._G\hat{S}_{||}) - \epsilon_p > \pi \end{cases}$$
(4)

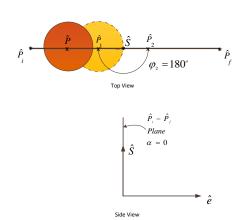
- 2. The  $2^{nd}$  slew around the unit sun vector,  $\hat{S}$ , via  $\phi_2$ .
  - (a) when  $\alpha \neq 0$





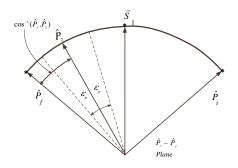


(b) when  $\alpha = 0$ 



3. The  $3^{rd}$  slew about the  $\hat{e}$  through angle:

$$\phi_3 = \begin{cases} \cos^{-1}(_G\hat{P}_f.\hat{P}_2) & when \ _G\hat{P}_f.\hat{P}_2 \ge 0\\ \cos^{-1}(_G\hat{P}_f.\hat{P}_2) - 2\pi & when \ _G\hat{P}_f.\hat{P}_2 < 0 \end{cases}$$
(5)



4. The final slew is about the instrument boresight axis to go to the final attitude.

### **Summary of Algorithm**

1. Slew around the eigenaxis,  $\hat{e}$ , through angle:

$$\phi_{1} = \begin{cases} \cos^{-1}(\hat{P}._{G}\hat{S}_{||}) - \epsilon_{p} & when \cos^{-1}(\hat{P}._{G}\hat{S}_{||}) - \epsilon_{p} \leq \pi \\ \cos^{-1}(\hat{P}._{G}\hat{S}_{||}) - \epsilon_{p} - 2\pi & when \cos^{-1}(\hat{P}._{G}\hat{S}_{||}) - \epsilon_{p} > \pi \end{cases}$$
(6)

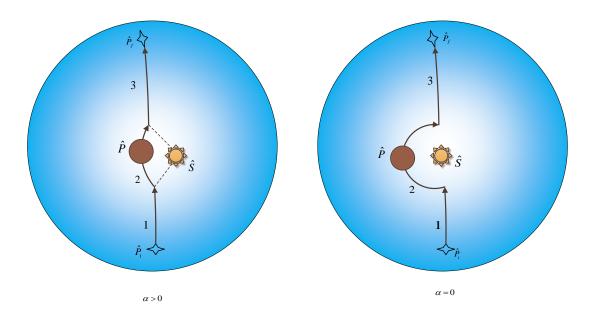
2. Slew around the  $\hat{S}$  via:

$$\phi_2 = \begin{cases} 2 \tan^{-1}(\frac{\epsilon_p}{\sin \alpha}) & when \ \alpha \neq 0 \\ \pi & when \ \alpha = 0 \end{cases}$$
 (7)

3. Slew about the  $\hat{e}$  through angle:

$$\phi_3 = \begin{cases} \cos^{-1}(_G\hat{P}_f.\hat{P}_2) & when \ _G\hat{P}_f.\hat{P}_2 \ge 0\\ \cos^{-1}(_G\hat{P}_f.\hat{P}_2) - 2\pi & when \ _G\hat{P}_f.\hat{P}_2 < 0 \end{cases}$$
(8)

4. Perform the final rotation,  $\phi_4$ , about the instrument boresight axis to adjust the attitude.



#### STEERING LAWS

# Case 1: Single-Axis, Agile Slew Maneuver with Velocity and Acceleration Constraints.

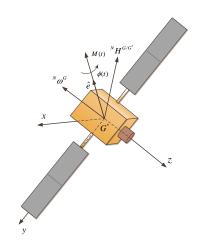
Problem Statement Consider the motion of a rigid spacecraft around a given inertially-fixed axis,  $G\hat{e} = [e_x, e_y, e_z]^T$ . The problem of minimum-time slew maneuver around the  $\hat{e}$  axis can be formulated as

$$Minimze_{u} J[x(.), u(.), t_{f}] = \int_{t_{0}}^{t_{f}} dt,$$
 (9)

subject to the following dynamic constraint

$$\Sigma : \begin{cases} \dot{x}_1 = x_2, \\ \dot{x}_2 = M/I_{\hat{e}}^{G/G*} = u, \end{cases}$$
 (10)

where  $x_1 \triangleq \phi$  and  $x_2 = \dot{\phi}$ .



Velocity and Acceleration Constraints The boundary conditions are

$$BCs: \begin{cases} \phi(t_0) = 0, \phi(t_f) = \phi_f, \\ \dot{\phi}(t_0) = \dot{\phi}_0, \dot{\phi}(t_f) = \dot{\phi}_f, \end{cases}$$
(11)

and velocity (state) and acceleration (control) constraints are

$$C_1: \begin{cases} |x_2 = \dot{\phi}| \le \dot{\phi}_{max}, \\ |u = \ddot{\phi}| \le \ddot{\phi}_{max}, \end{cases}$$
 (12)

in which

$$\dot{\phi}_{max} = [I^{w/w^*}]^{-1} [^N H^{G/G*} - (I^{G/G*} + I^{w/w*})^N \omega^G] / (e_x + e_y + e_z), \tag{13}$$

and

$$\ddot{\phi}_{max} =_B \hat{e}^T {}_B M_{max} / I_{\hat{e}}^{G/G*}, \tag{14}$$

where  ${}^NH^{G/G*}$  is the total angular momentum of the gyrostat with respect to its center of mass,  $G^*$ , in the N-frame.  $I^{G/G*}$  and  $I^{w/w*}$  represent the inertia dyadic of the gyrostat and reaction wheel with respect to their center of masses, respectively.  ${}_BM_{max}$  is the maximum generated torque along the body-axes in the body frame.

**Find:**  $\phi(t)$ ,  $\dot{\phi}(t)$ , and  $\ddot{\phi}(t)$ .

Using the Pontryagin's minimum principle (PMP), we derive the necessary conditions for the optimal solution as follows:

1. State Eqs.:

$$\begin{cases} \dot{x}_1 = x_2, \\ \dot{x}_2 = u, \\ \dot{x}_3 = (x_2 + \dot{\phi}_{max})^2 \mathbb{U}(-x_2 - \dot{\phi}_{max}) + (\dot{\phi}_{max} - x_2)^2 \mathbb{U}(x_2 - \dot{\phi}_{max}), \end{cases}$$

$$(15)$$
The unit step function. It is defined as

where the unit step function,  $\mathbb{U}$ , is defined as

$$\mathbb{U}(X) = \begin{cases} 1, X > 0, \\ 0, X \le 0. \end{cases}$$
 (16)

Note:  $(x_3(t_0) = x_3(t_f) = 0 \& x_3(t) \ge 0) \to x_3(t) = 0, t \in [t_0, t_f].$ 

2. Hamiltonian:

$$H = 1 + \lambda_1 x_2 + \lambda_2 u + \lambda_3 \left[ (x_2 + \dot{\phi}_{max})^2 \mathbb{U}(-x_2 - \dot{\phi}_{max}) \right]$$

$$(\dot{\phi}_{max} - x_2)^2 \mathbb{U}(x_2 - \dot{\phi}_{max})$$
(17)

3. Costate Eqs.:

$$\begin{cases}
\dot{\lambda}_{1} = -\frac{\partial H}{\partial x_{1}} = 0, \\
\dot{\lambda}_{2} = -\frac{\partial H}{\partial x_{2}} = -\lambda_{1} - 2\lambda_{3}(x_{2} + \dot{\phi}_{max})\mathbb{U}(-x_{2} - \dot{\phi}_{max}) \\
+2\lambda_{3}(\dot{\phi}_{max} - x_{2})\mathbb{U}(x_{2} - \dot{\phi}_{max}), \\
\dot{\lambda}_{3} = -\frac{\partial H}{\partial x_{3}} = 0.
\end{cases} (18)$$

4. Applying the Pontryagin's minimum principle (PMP),

$$u^* = \underset{u \in \mathcal{U}}{argmin}H,\tag{19}$$

where  $\mathcal{U}$  defines the domain of feasible controls. The optimal control can be determined as

$$u^*(t) = \begin{cases} \ddot{\phi}_{max} & \lambda_2 < 0, \\ ? & \lambda_2 = 0, \\ -\ddot{\phi}_{max} & \lambda_2 > 0. \end{cases}$$
 (20)

This is a *singular arc* optimal control problem.

5. Determining the optimal control in the singular arc:

$$\frac{d^2}{dt^2} \left( \frac{\partial H}{\partial u} \right) = \ddot{\lambda}_2 = 0 \to \dot{x}_2 = 0 \to u^* = 0 \tag{21}$$

6. Checking the Generalized Legendre-Clebsch condition for optimality:

$$(-1)^2 \frac{\partial}{\partial u} \left[ \frac{d^2}{dt^2} \left( \frac{\partial H}{\partial u} \right) \right] = 1 \ge 0 \tag{22}$$

7. The transversality condition:

$$H|_{(*,t_f)} = 0 \text{ and } H \neq H(t) \to H = 0, \forall t \in [t_0, t_f].$$
 (23)

### Steering Profiles

• Angular acceleration profile (bang-off-bang):

$$\ddot{\phi}(t) = u = \begin{cases} \ddot{\phi}_{max} & when \ t_0 \le t \le t_1, \\ 0 & when \ t_1 \le t \le t_2, \\ -\ddot{\phi}_{max} & when \ t_2 \le t \le t_f. \end{cases}$$

$$(24)$$

• Angular velocity profile:

$$\dot{\phi}(t) = \begin{cases} \dot{\phi}_0 + \ddot{\phi}_{max}(t - t_0) & when \ t_0 \le t \le t_1, \\ \dot{\phi}_{max} & when \ t_1 \le t \le t_2, \\ \dot{\phi}_{max} - \ddot{\phi}_{max}(t - t_2) & when \ t_2 \le t \le t_f. \end{cases}$$

$$(25)$$

• Angular position profile:

$$\phi(t) = \begin{cases} \dot{\phi}_0(t - t_0) + \frac{1}{2}\ddot{\phi}_{max}(t - t_0)^2 & when \ t_0 \le t \le t_1, \\ \phi(t_1) + \dot{\phi}_{max}(t - t_1) & when \ t_1 \le t \le t_2, \\ \phi(t_2) + \dot{\phi}_{max}(t - t_2) - \frac{1}{2}\ddot{\phi}_{max}(t - t_2)^2 & when \ t_2 \le t \le t_f. \end{cases}$$
 (26)

• Using the conditions,  $\dot{\phi}(t_1) = \dot{\phi}_{max}$ ,  $\dot{\phi}(t_f) = \dot{\phi}_f$ ,  $\phi(t_f) = \phi_f$ , we can determine switching times  $t_1, t_2$ , and final time  $t_f$  as:

$$t_1 = t_0 + \frac{\dot{\phi}_{max} - \dot{\phi}_0}{\ddot{\phi}_{max}},\tag{27}$$

$$t_{2} = t_{1} + \frac{1}{\dot{\phi}_{max}} \left[ \phi_{f} - \dot{\phi}_{0}(t_{1} - t_{0}) - \frac{1}{2} \ddot{\phi}_{max}(t_{1} - t_{0})^{2} - \frac{\dot{\phi}_{max}(\dot{\phi}_{max} - \dot{\phi}_{f})}{\ddot{\phi}_{max}} + \frac{(\dot{\phi}_{max} - \dot{\phi}_{f})^{2}}{2\ddot{\phi}_{max}} \right],$$
(28)

and

$$t_f = t_1 + \frac{1}{\dot{\phi}_{max}} \left[ \phi_f - \dot{\phi}_0(t_1 - t_0) - \frac{1}{2} \ddot{\phi}_{max} (t_1 - t_0)^2 + \frac{(\dot{\phi}_{max} - \dot{\phi}_f)^2}{2\ddot{\phi}_{max}} \right]. \tag{29}$$

• Steering profiles:

$$^{N}q^{D}(t) = [e_x \sin\frac{\phi(t)}{2}, e_y \sin\frac{\phi(t)}{2}, e_z \sin\frac{\phi(t)}{2}, \cos\frac{\phi(t)}{2}]^{T}$$
 (30)

$${}_{G}^{N}\omega^{D}(t) = \dot{\phi}(t)_{G}\hat{e} \tag{31}$$

$${}_{G}^{N}\alpha^{D}(t) = \ddot{\phi}(t)_{G}\hat{e} \tag{32}$$

## Case 2: Single-Axis, Agile Slew Maneuver with Acceleration Constraint

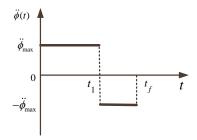
*Problem Statement* Consider the optimal control problem described by Eqs.(9), (10), (11), and subject to control constraint

$$C_2: |u = \ddot{\phi}| \le \ddot{\phi}_{max}. \tag{33}$$

**Find:**  $\phi(t)$ ,  $\dot{\phi}(t)$ , and  $\ddot{\phi}(t)$ .

• Angular acceleration about the  $\hat{e}$  axis:

$$\ddot{\phi}(t) = \ddot{\phi}_{max} \mathbb{U}(t_0) - 2\ddot{\phi}_{max} \mathbb{U}(t - t_1)$$
(34)



where the switching and the final times are given by

$$t_1 = t_0 - \frac{\dot{\phi}_0}{\ddot{\phi}_{max}} + \frac{\sqrt{\ddot{\phi}_{max}^2 (2\ddot{\phi}_{max}\phi_f + \dot{\phi}_f^2 + \dot{\phi}_0^2)}}{\sqrt{2}\ddot{\phi}_{max}^2}$$
(35)

and

$$t_f = t_0 - \frac{\dot{\phi}_f + \dot{\phi}_0}{\ddot{\phi}_{max}} + \frac{\sqrt{2}\sqrt{\ddot{\phi}_{max}^2(2\ddot{\phi}_{max}\phi_f + \dot{\phi}_{ef}^2 + \dot{\phi}_0^2)}}{\ddot{\phi}_{max}^2}$$
(36)

• Angular velocity about the  $\hat{e}$  axis:

$$\dot{\phi}(t) = \dot{\phi}_0 + \ddot{\phi}_{max}(t - t_0)\mathbb{U}(t_0) - 2\ddot{\phi}_{max}(t - t_1)\mathbb{U}(t - t_1)$$
(37)

• Angular position about the  $\hat{e}$  axis:

$$\phi(t) = \dot{\phi}_0(t - t_0) + \ddot{\phi}_{max} \frac{(t - t_0)^2}{2} \mathbb{U}(t_0) - 2\ddot{\phi}_{max} \frac{(t - t_1)^2}{2} \mathbb{U}(t - t_1)$$
(38)

The First Slew Maneuver: A single-axis nonrest-to-rest maneuver around the  $\hat{e}$ 

• The BCs:

$$\dot{\phi}(t_0) = \dot{\phi}_0, \phi(t_0) = 0, \dot{\phi}(t_{f1}) = 0, \phi(t_{f1}) = \phi_1. \tag{39}$$

The switching time,  $t_{11}$ , and minimum-time,  $t_{f1}$ , are

$$t_{11} = t_0 - \frac{\dot{\phi}_0}{\ddot{\phi}_{max}} + \frac{\sqrt{\ddot{\phi}_{max}^2 (2\ddot{\phi}_{max}\phi_1 + \dot{\phi}_0^2)}}{\sqrt{2}\ddot{\phi}_{max}^2}$$
(40)

$$t_{f1} = t_0 - \frac{\dot{\phi}_0}{\ddot{\phi}_{max}} + \frac{\sqrt{2\ddot{\phi}_{max}^2(2\ddot{\phi}_{max}\phi_1 + \dot{\phi}_0^2)}}{\ddot{\phi}_{max}^2}$$
(41)

The  $\ddot{\phi}(t)$ ,  $\dot{\phi}(t)$ , and  $\phi(t)$ , can be found by substituting the boundary conditions given by (39) and  $t_{11}$  and  $t_{f1}$  in to Eqs. (34), (37), and (38), respectively.

The Second Slew Maneuver: A rest-to-rest maneuver around the sun vector

• The BCs:

$$\dot{\phi}(t_0) = 0, \phi(t_0) = 0, \dot{\phi}(t_{f2}) = 0, \phi(t_{f2}) = \phi_2. \tag{42}$$

The switching time,  $t_{12}$ , and the minimum-time,  $t_{f2}$ , are

$$t_{12} = t_0 - \frac{\sqrt{\phi_2}}{\ddot{\phi}_{max}} \tag{43}$$

$$t_{f2} = t_0 - \frac{2\sqrt{\phi_2}}{\ddot{\phi}_{max}} \tag{44}$$

The  $\ddot{\phi}(t)$ ,  $\dot{\phi}(t)$ , and  $\phi(t)$ , can be found by substituting the boundary conditions given by (42) and  $t_{12}$  and  $t_{f2}$  in to Eqs. (34), (37), and (38), respectively.

The Third Slew Maneuver: A single-axis rest-to-nonrest maneuver around the  $\hat{e}$ 

• The BCs:

$$\dot{\phi}(t_0) = 0, \phi(t_0) = 0, \dot{\phi}(t_{f3}) = \dot{\phi}_f, \phi(t_{f3}) = \phi_3. \tag{45}$$

The switching time,  $t_{13}$ , and the minimum-time,  $t_{f3}$ , are

$$t_{13} = t_0 + \frac{\sqrt{\ddot{\phi}_{max}^2 (2\ddot{\phi}_{max}\phi_3 + \dot{\phi}_f^2)}}{\sqrt{2\ddot{\phi}_{max}^2}}$$
(46)

$$t_{f3} = t_0 - \frac{\dot{\phi}_f}{\ddot{\phi}_{max}} + \frac{\sqrt{2\ddot{\phi}_{max}^2(2\ddot{\phi}_{max}\phi_3 + \dot{\phi}_f^2)}}{\ddot{\phi}_{max}^2}$$
(47)

The  $\ddot{\phi}(t)$ ,  $\dot{\phi}(t)$ , and  $\phi(t)$ , can be found by substituting the boundary conditions given by (45) and  $t_{13}$  and  $t_{f3}$  in to Eqs. (34), (37), and (38), respectively.

#### NUMERICAL SIMULATION

#### **CONCLUSION**

## **ACKNOWLEDGMENT**

APPENDIX: TITLE HERE

### **Miscellaneous Physical Dimensions**

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