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set 4, prob 6

```
clear; clc

z = 0;

% First guess
xg0_OG = 1.5 ;
xg0 = xg0_OG ;
```

GN method

```
% no step size adjustment
a_flag = 0;
[xg0_a0, Jg_a0] = GN(a_flag, xg0, z);

% step size adjustment
a_flag = 1;
[xg0_a1, Jg_a1] = GN(a_flag, xg0, z);

% original initial guess
xg0_OG

% solution to initial guess
xg0_a1(end)

% covariance
[~, ~, H, ~] = cost_fn(xg0_a1(end), z);
Pxx = inv(H' * H)

clear Jg
x = [-6 : 0.1 : 6];
for i = 1:length(x)
    Jg(i) = cost_fn( x(i), z);
end
```

```
xg0_OG =
```

```
1.5
```

```
ans =
```

```
-1.49877953906259e-10
```

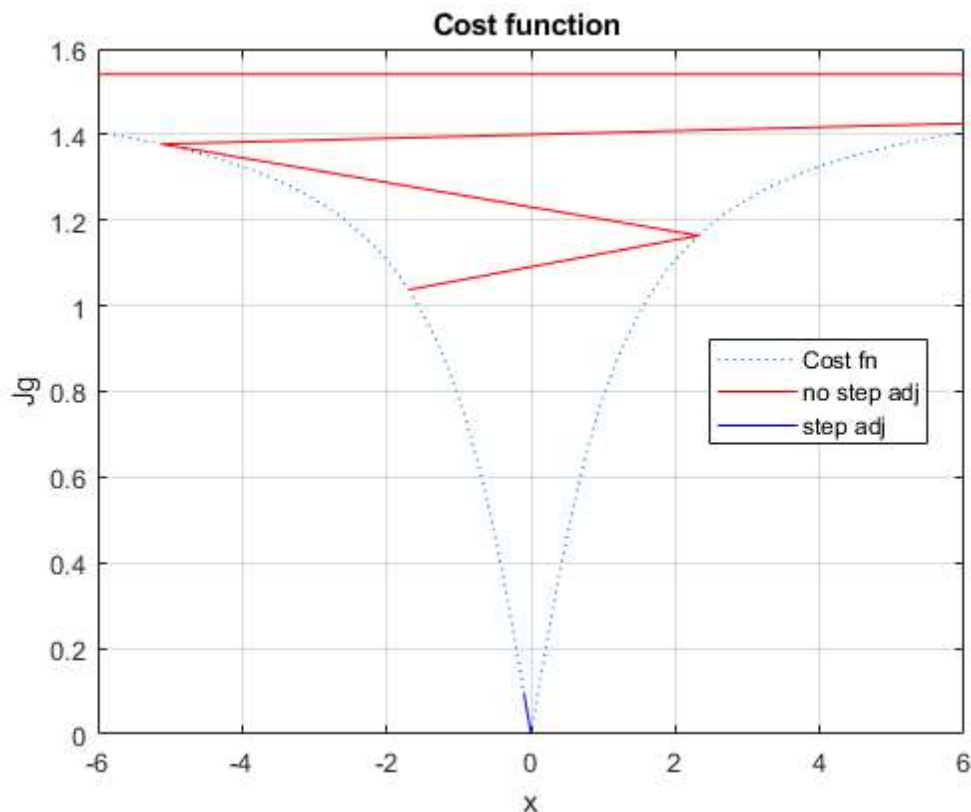
Pxx =

1

cost function plot

The cost trajectory without step size adjustment begins to diverge immediately. The cost function (norm of the difference between the measurement, z , and the measurement model, $h(x) = \text{atan}(x)$) asymptotically reaches its max value after just 5 iterations. The step-size adjusted method achieves the converged solution after just 3 iterations (of the outer loop). The crude step-size adjustment is sufficient to avoid divergence of the Gauss-Newton algorithm. To choose the step size adjustment more nearly optimally, one can take the derivative of the cost function with respect to a (the step size adjustment variable) and solve for a .

```
ftitle = 'Cost function ';  
figure('name', ftitle)  
plot(x, Jg, ':');  
hold on; grid on;  
plot(xg0_a0(1:5), Jg_a0(1:5), 'r');  
plot(xg0_a1, Jg_a1, 'b');  
legend('Cost fn', 'no step adj', 'step adj', 'location', 'best')  
xlim([-6 6])  
xlabel('x');  
ylabel('Jg');  
title(ftitle);
```



subfunctions

```
function h = h_NL(x)  
% Nonlinear measurement h
```

```

    h = atan(x);

end

function H = H_NL(x)
% Full jacobian of h

%    H = (sec(x)).^2;
    H = 1 / (1 + x^2);

end

function [Jg, h, H, dx] = cost_fn(xg, z)

% NL at guess
h = h_NL(xg);

% jacobian at guess
H = H_NL(xg);

% Cost function
Jg = norm(z - h);

% Gauss-Newton dx
dx = inv((H' * H)) * H' * (z - h);

end

function [xg0_i, Jg_i] = GN(a_flag, xg0, z)

```

First cost function and step size-adjusted cost function

```

% First NL, jacobian, and cost fn at guess
[Jg, h, H, dx] = cost_fn(xg0, z);

% first a step
a = 1;

% First new cost function
xg = xg0 + a * dx;

% First new NL, jacobian, and cost fn at guess
[Jgnew, h, H, ~] = cost_fn(xg, z);

```

The while loop

```

i_dx = 0;
i_Jg = 0;
Jg_i = [];
xg0_i = [];

% Outer loop: norm(dx) > e
while norm(dx) > 0.000001

    if a_flag == 1

        % Inner loop: Jgnew >= Jg
    end
end

```

```

while Jgnew >= Jg

    % Next a
    a = a/2;
    if a < eps
        break
    end

    % Adjust step size and update cost fn
    xg = xg0 + a * dx;
    [Jgnew, h, H, ~] = cost_fn(xg, z);

    % increase inner loop count
    i_Jg = i_Jg + 1;

end
end

% Back to outer loop: norm(idx) > e
if a < eps
    break
end

% Next guess point
xg0 = xg;
Jg = Jgnew;

% Gauss-Newton dx (H, z, and h saved from last iteration)
dx = inv((H' * H)) * H' * (z - h);

% first a step
a = 1;

% Next step-size adjusted guess
xg = xg0 + a * dx;

[Jgnew, h, H, ~] = cost_fn(xg, z);

% Increase outer loop count and populate Jg, xg0 trajectory
i_dx = i_dx + 1;
Jg_i = [Jg_i; Jg];
xg0_i = [xg0_i; xg0];

end

```

Warning: Matrix is singular to working precision.
Warning: Matrix is singular to working precision.
Warning: Matrix is singular to working precision.
Warning: Matrix is singular to working precision.
Warning: Matrix is singular to working precision.

```
end
```

