

NA

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Resuelve los sistemas por el método indicado

$$-3x_1 - 6x_2 - 2x_3 = -61.5$$

$$10x_1 + 2x_2 - x_3 = 27$$

$$x_1 + x_2 + 5x_3 = -21.5$$

Factorización LU

$$A = \begin{bmatrix} -3 & -6 & -2 \\ 10 & 2 & -1 \\ 1 & 1 & 5 \end{bmatrix}, \quad x = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}, \quad b = \begin{bmatrix} -61.5 \\ 27 \\ -21.5 \end{bmatrix}$$

$A \rightarrow U$

$$\begin{bmatrix} -3 & -6 & -2 \\ 10 & 2 & -1 \\ 1 & 1 & 5 \end{bmatrix} \begin{array}{l} R_2^* = R_2 + \frac{10}{3}R_1 \\ R_3^* = R_3 + \frac{1}{3}R_1 \end{array} \rightarrow \begin{bmatrix} -3 & -6 & -2 \\ 0 & -18 & -\frac{23}{3} \\ 0 & -1 & \frac{13}{3} \end{bmatrix} \begin{array}{l} \\ R_3^* = R_3 - \frac{1}{18}R_2 \end{array}$$

$$\rightarrow \begin{bmatrix} -3 & -6 & -2 \\ 0 & -18 & -\frac{23}{3} \\ 0 & 0 & \frac{25}{54} \end{bmatrix}$$

$$l_{21} = -\frac{10}{3} \quad l_{31} = -\frac{1}{3} \quad l_{32} = \frac{1}{18}$$

$$L = \begin{bmatrix} 1 & 0 & 0 \\ -\frac{10}{3} & 1 & 0 \\ -\frac{1}{3} & \frac{1}{18} & 1 \end{bmatrix}$$

$$Ld = b$$

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & -61.5 \\ -\frac{10}{3} & 1 & 0 & 27 \\ -\frac{1}{3} & \frac{1}{18} & 1 & -21.5 \end{array} \right] \rightarrow \text{Calcular } d$$

$$d_1 = -61.5$$

$$-\frac{10}{3}d_1 + d_2 = 27$$

$$-\frac{10}{3}(-61.5) + d_2 = 27 \rightarrow d_2 = -178$$

$$d = \begin{bmatrix} -61.5 \\ -178 \\ -\frac{289}{9} \end{bmatrix}$$

$$-\frac{1}{3}d_1 + \frac{1}{18}d_2 + d_3 = -21.5 \rightarrow -\frac{1}{3}(-61.5) + \frac{1}{18}(-178) + d_3 = -21.5 \rightarrow d_3 = -\frac{289}{9}$$

$$Ux = d$$

$$\begin{bmatrix} -3 & -6 & -2 \\ 0 & -18 & -\frac{23}{3} \\ 0 & 0 & \frac{257}{54} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -61.5 \\ -178 \\ -\frac{289}{9} \end{bmatrix}$$

Sustitución hacia atrás

$$\frac{257}{54} x_3 = -\frac{289}{9} \rightarrow x_3 = -\frac{1734}{257}$$

$$-18x_2 - \frac{23}{3}x_3 = -178$$

$$18x_2 + \frac{23}{3}x_3 = 178$$

$$18x_2 + \frac{23}{3}\left(-\frac{1734}{257}\right) = 178 \rightarrow x_2 = \frac{3280}{257}$$

$$-3x_1 - 6x_2 - 2x_3 = -61.5$$

$$3x_1 + 6x_2 + 2x_3 = 61.5$$

$$3x_1 + 6\left(\frac{3280}{257}\right) + 2\left(-\frac{1734}{257}\right) = 61.5 \rightarrow x_1 = -\frac{271}{514}$$

$$\therefore x = \begin{bmatrix} -\frac{271}{514} \\ \frac{3280}{257} \\ -\frac{1734}{257} \end{bmatrix}$$



~~Gauss-Seidel~~  
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$$4x_1 + x_2 - x_3 = 9$$

$$3x_1 + 2x_2 - 6x_3 = -2$$

$$x_1 - 5x_2 + 3x_3 = 1$$

Gauss-Seidel

$P_0(3, 2, 3)$

$$4x_1 + x_2 - x_3 = 9$$

$$x_1 - 5x_2 + 3x_3 = 1$$

$$3x_1 + 2x_2 - 6x_3 = -2$$

$$x_1 = \frac{9 + x_3 - x_2}{4}$$

$$x_2 = \frac{1 - 3x_3 - x_1}{-5}$$

$$x_3 = \frac{-2 - 2x_2 - 3x_1}{-6} = \frac{2 + 2x_2 + 3x_1}{6}$$

Iteración	$x_1$	$x_2$	$x_3$	$E_{a1}$	$E_{a2}$	$E_{a3}$
0	3	2	3	No hay error	No hay error	No hay error
1	2.5	2.1	2.2833	20%	4.7619%	31.3888%
2	2.2958	1.6291	2.0243	8.8945%	28.9055%	12.7945%
3	2.3488	1.4843	2.0025	2.2563%	9.7554%	1.0886%
4	2.3796	1.4274	2.0156	1.2943%	0.467%	0.6499%
5	2.3846	1.4863	2.0211	0.2097%	0.5988%	0.2721%

$$P_5(\overbrace{2.3846}^{x_1}, \overbrace{1.4863}^{x_2}, \overbrace{2.0211}^{x_3})$$

$$E_{a1} = 0.2097\% \quad E_{a2} = 0.5988\% \quad E_{a3} = 0.2721\%$$