

MISAEEL MORALES - MATH 7993 NUMERICAL OPTIMIZATION - PROJECT  
OPTIMIZATION OF MULTIVARIATE GAUSSIAN MIXTURE MODEL

Real Mu1: [-2.00, 3.00]

Real Mu2: [4.00, -5.00]

Real Sigma1: [2.00 0.00 ; 1.00 5.00]

Real Sigma2: [8.00 1.00 ; 1.00 8.00]

Real Proportions: [0.700, 0.300]

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Initial Guess Mu1: [-2.00, 2.00]

Initial Guess Mu2: [5.00, -5.00]

Initial Guess Sigma1: [50.00 5.00 ; 5.00 50.00]

Initial Guess Sigma2: [30.00 1.00 ; 0.10 3.00]

Initial Guess Proportions: [0.900, 0.100]

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EM-estimated Mu1: [-1.5617, 2.2264]

EM-estimated Mu2: [5.1835, -5.6129]

EM-estimated Sigma1: [3.261 -1.116 ; -1.116 10.350]

EM-estimated Sigma2: [6.171 2.041 ; 2.041 7.799]

EM-estimated Proportions: [0.8015, 0.1985]. Sum: 1.0000

Stopping Criteria: max iterations (5) | tolerance (1.0e-06)

Maximum number of iterations (5) was reached before convergence!

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Optimization Toolbox subroutine:

Exiting: Maximum number of iterations has been exceeded

- increase MaxIter option.

Current function value: 4823.364029

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NMS Optimization-estimated Mu1: [-1.9505, 3.0876]

NMS Optimization-estimated Mu2: [-1.9505, 3.0876]

NMS Optimization-estimated Sigma1: [1.690 -1.784 ; 0.639 5.091]

NMS Optimization-estimated Sigma2: [11.758 2.639 ; 2.164 8.681]

NMS Optimization-estimated Proportions: [0.6979, 0.3021]. Sum: 1.000

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Local minimum possible.

fminunc stopped because it cannot decrease the objective function  
along the current search direction.

<stopping criteria details>

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QN Optimization-estimated Mu1: [-1.9513, 3.1167]

QN Optimization-estimated Mu2: [3.7381, -4.9356]

QN Optimization-estimated Sigma1: [1.686 -1.116 ; 0.644 5.148]

QN Optimization-estimated Sigma2: [9.496 2.041 ; 0.085 8.211]

QN Optimization-estimated Proportions: [0.6962, 0.3038]. Sum: 1.000

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EM-estimated Negative Log-Likelihood: 5019.4828

fminsearch Negative Log-Likelihood: 4823.3640

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fminunc Negative Log-Likelihood: 4815.8169  
Original Parameters Negative Log-Likelihood: 4837.4388  
Elapsed time is 11.011121 seconds.  
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