# VE311 FINAL RC - Single Stage Amplifier

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## Overview

#### **Basics**

DC  $gm \& r_o \& gmb$  $Gm \& R_{out} \& R_{in} \& A_v$ 

#### Circuits and Formulas

Common Source Source Degradation Source Follower Common Gate

#### Tips

#### DC Calculation

#### Current (NMOS)

Non-saturation region:

$$\boxed{I_D = \mu_n C_{\text{ox}} \frac{W}{L_{\text{eff}}} \left[ (V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]}$$

Saturation region:

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

where 
$$V_{TH}=VTO$$
,  $\frac{W}{L_{eff}}=\frac{W_{drawn}}{L_{drawn}-2LD}$ ,  $C_{ox}=\frac{\epsilon_r\epsilon_0}{TOX}$ , and  $\mu_n=UO\times 10^{-4}$ 

## gm & $r_o$ & gmb

For NMOS,

$$gm = \frac{\partial I_D}{\partial V_{GS}} = \frac{2I_D}{V_{GS} - V_{TH}}$$

$$r_o = \frac{\partial V_{DS}}{\partial I_D} \approx \frac{1}{I_D \lambda}$$

$$gmb = \frac{\partial I_D}{\partial V_{SB}} = -\mu_n C_{ox} \frac{W}{L_{eff}} (V_{GS} - V_{TH}) \cdot \frac{\gamma}{2} \cdot \frac{1}{\sqrt{|2\phi_F + V_{SB}|}}$$

where  $\lambda = LAMBDA$ ,  $\gamma = GAMMA$ , and  $2\phi_F = PHI$ .

## Gm & Rout

#### How to calculate Gm?

- 1. Draw small signal model.
- 2. Connect port with  $V_{out}$  to ground.
- 3. Derive *i<sub>out</sub>*.
- 4. Calculate  $Gm = \frac{i_{out}}{v_{in}}$ .

#### How to calculate R<sub>out</sub>?

- 1. Draw small signal model.
- 2. Connect port with  $V_{in}$  to ground. Connect a test voltage  $v_t$  on port with  $V_{out}$ .
- 3. Derive  $i_t$ .
- 4. Calculate  $R_{out} = \frac{v_t}{i_t}$ .

 $R_{in} \& A_{v}$ 

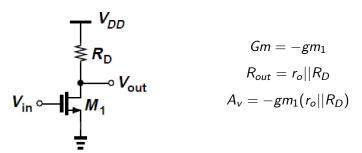
#### How to calculate Rin?

- 1. Draw small signal model.
- 2. Connect port with  $V_{out}$  to ground. Connect a test voltage  $v_t$  on port with  $V_{in}$ .
- 3. Derive  $i_t$ .
- 4. Calculate  $R_{in} = \frac{v_t}{i_t}$ .

#### How to calculate $A_{v}$ ?

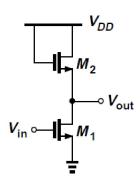
$$A_v = GmR_{out}$$

#### Common Source with Resistive Load



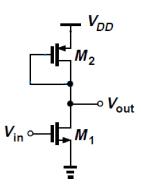
- \* What if  $R_D$  is replaced by a DC current source? (slide page 9)
- \* What if  $M_1$  is a PMOS?

## Common Source with Diode-Connected Load



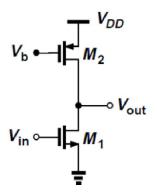
$$\begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \\ \end{array} \end{array} & \stackrel{}{\longrightarrow} \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2} \\ \\ Gm = -gm_1 \\ \\ R_{out} = r_{o1} || \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2} \\ \\ A_v = -gm_1 \left( r_{o1} || \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2} \right) \end{array}$$

# Common Source with Diode-Connected Load (Cont.)



$$V_{DD}$$
  $\Rightarrow \frac{1}{gm_2}||r_{o2}|$ 
 $Gm = -gm_1$ 
 $R_{out} = r_{o1}||\frac{1}{gm_2}||r_{o2}|$ 
 $A_v = -gm_1\left(r_{o1}||\frac{1}{gm_2}||r_{o2}\right)$ 

#### Common Source with Current-Source Load



$$V_b \longrightarrow V_{DD}$$

$$V_b \longrightarrow M_2 \Rightarrow r_{o2}$$

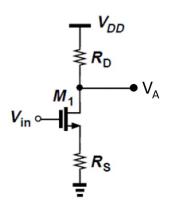
$$Gm = -gm_1$$

$$R_{out} = r_{o1}||r_{o2}$$

$$A_v = -gm_1(r_{o1}||r_{o2})$$

## Common Source with Source Degradation

Basic Circuit  $(\lambda, \gamma \neq 0)$ 

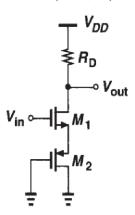


$$Gm = \frac{-gm_1r_{o1}}{R_S + r_{o1} + (gm_1 + gmb_1)r_{o1}R_S}$$

$$R_{out} = [R_S + r_{o1} + (gm_1 + gmb_1) r_{o1}R_S] ||R_D|$$

\* What if  $M_1$  is a PMOS?

## Common Source with Source Degradation (Cont.)



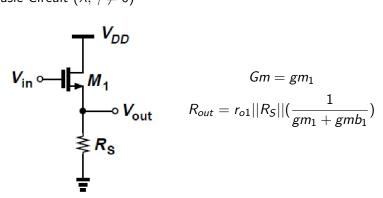
$$\int_{\Xi} M_{2} \Rightarrow \frac{1}{gm_{2}} || \frac{1}{gmb_{2}} || r_{o2}$$

$$Gm = \frac{-gm_{1}r_{o1}}{R_{S} + r_{o1} + (gm_{1} + gmb_{1}) r_{o1}R_{1}}$$

$$R_{out} = [R_{S} + r_{o1} + (gm_{1} + gmb_{1}) r_{o1}R_{S}] || R_{D}$$
with  $R_{S}$  replaced by  $\frac{1}{gm_{2}} || \frac{1}{gmb_{2}} || r_{o2}$ 

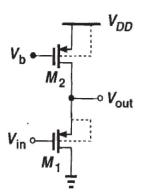
### Source Follower

Basic Circuit  $(\lambda, \gamma \neq 0)$ 



\* What if  $M_1$  is replaced by a PMOS?

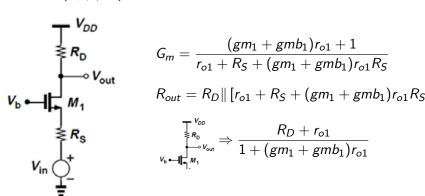
## Source Follower with Current Source



$$V_{b} \longrightarrow V_{DD}$$
  $\Rightarrow r_{o2}$ 
 $V_{in} \longrightarrow V_{in} \longrightarrow r_{o1} || \frac{1}{gm_{1}}$ 
 $R_{out} = r_{o}1 || \frac{1}{gm_{1}} || r_{o2}$ 
 $Gm = gm_{1}$ 

#### Common Gate

Basic Circuit  $(\lambda, \gamma \neq 0)$ 



\* What if  $M_1$  is replaced by PMOS?

## Complex Common Gate

$$(\lambda, \gamma \neq 0)$$

$$V_{DD}$$

$$R_{D}$$

$$V_{out}$$

$$V_{b} \leftarrow M_{2}$$

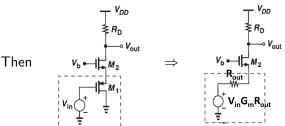
$$V_{in} \downarrow^{+}$$

For  $v_{in}$ , take it as a source follower with infinity source resistance. Then we get

$$\begin{array}{c} \begin{array}{c} \textbf{R}_{out} \\ \hline \\ \textbf{V}_{in} \textbf{G}_{m} \textbf{R}_{out} \end{array} \end{array} \quad \begin{cases} G_{m} = gm_{1} \\ \\ R_{out} = r_{o1} \parallel \frac{1}{gm_{1}} \parallel \frac{1}{gmb_{1}} \end{array}$$

# Complex Common Gate (Cont.)

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with

$$G_m = rac{(gm_2 + gmb_2)r_{o2} + 1}{r_{o2} + R_S + (gm_2 + gmb_2)r_{o2}R_S} \cdot gm_1 \left(r_{o1}||rac{1}{gm_1}||rac{1}{gmb_1}
ight) \ R_{out} = R_D \|\left[r_{o2} + R_S + (gm_2 + gmb_2)r_{o2}R_S
ight] \ ext{where } R_S = r_{o1} ||rac{1}{gm_1}||rac{1}{gmb_1}$$

## Some Tips qwq

- Derive all the *Gm* and *Rout* yourself before the final.
- Small signal model!!!
- Small signal models, equations, and explanation do matter if you cannot guarantee your final result is correct.
- When plotting, please mark your diagram well!!!(peak values, period...).

# Good Luck for Your FINAL!

