VE311 FINAL RC - Single Stage Amplifier

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Overview

DC Calculation

Current (NMOS)
Non-saturation region:

$$\boxed{I_D = \mu_n C_{ox} \frac{W}{L_{eff}} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]}$$

Saturation region:

$$\boxed{I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})}$$

where $V_{TH} = VTO$, $\dfrac{W}{L_{eff}} = \dfrac{W_{drawn}}{L_{drawn} - 2LD}$, $C_{ox} = \dfrac{\epsilon_r \epsilon_0}{TOX}$, and $\mu_n = UO \times 10^{-4}$

gm & r_o & gmb

For NMOS,

$$\boxed{gm = \frac{\partial I_D}{\partial V_{GS}} = \frac{2I_D}{V_{GS} - V_{TH}}}$$

$$\boxed{r_o = \frac{\partial V_{DS}}{\partial I_D} \approx \frac{1}{I_D \lambda}}$$

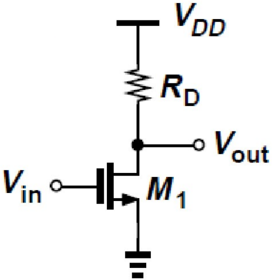
$$\boxed{gmb = \frac{\partial I_D}{\partial V_{SB}} = -\mu_n C_{ox} \frac{W}{L_{eff}} (V_{GS} - V_{TH}) \cdot \frac{\gamma}{2} \cdot \frac{1}{\sqrt{|2\phi_F + V_{SB}|}}}$$

where $\lambda = LAMBDA$, $\gamma = GAMMA$, and $2\phi_F = PHI$.

Gm & R_{out} & A_v

Common Source with Resistive Load

Basic Circuit $(\lambda, \gamma \neq 0)$



$$Gm = -gm_1$$

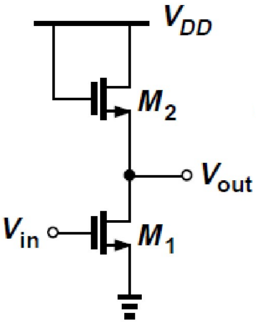
$$R_{out} = r_o || R_D$$

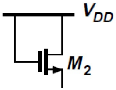
$$A_v = -gm_1(r_o || R_D)$$

* What if R_D is replaced by a DC current source? (slide page 9)
* What if M_1 is a PMOS?

Common Source with Diode-Connected Load

Basic Circuit $(\lambda, \gamma \neq 0)$





$$\Rightarrow \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2}$$

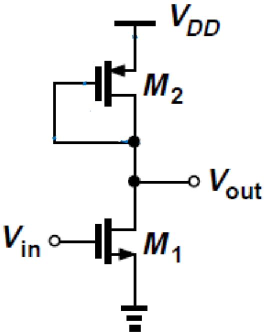
$$Gm = -gm_1$$

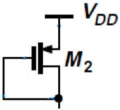
$$R_{out} = r_{o1} || \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2}$$

$$A_v = -gm_1 \left(r_{o1} || \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2} \right)$$

Common Source with Diode-Connected Load (Cont.)

Basic Circuit $(\lambda, \gamma \neq 0)$





$$\Rightarrow \frac{1}{gm_2} || r_{o2}$$

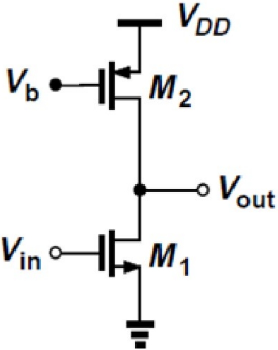
$$Gm = -gm_1$$

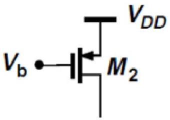
$$R_{out} = r_{o1} || \frac{1}{gm_2} || r_{o2}$$

$$A_v = -gm_1 \left(r_{o1} || \frac{1}{gm_2} || r_{o2} \right)$$

Common Source with Current-Source Load

Basic Circuit $(\lambda, \gamma \neq 0)$





$\Rightarrow r_{o2}$

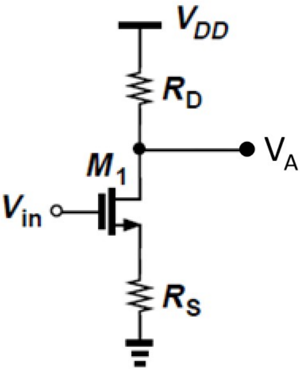
$$Gm = -gm_1$$

$$R_{out} = r_{o1} || r_{o2}$$

$$A_v = -gm_1 \left(r_{o1} || r_{o2} \right)$$

Common Source with Source Degradation

Basic Circuit $(\lambda, \gamma \neq 0)$



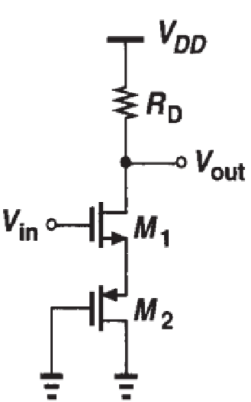
$$Gm = \frac{-gm_1 r_{o1}}{R_S + r_{o1} + (gm_1 + gmb_1)\, r_{o1} R_S}$$

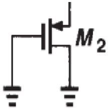
$$\begin{aligned} R_{out} = [&R_S + r_{o1} \\ &+ (gm_1 + gmb_1)\, r_{o1} R_S] \,||\, R_D \end{aligned}$$

* What if M_1 is a PMOS?

Common Source with Source Degradation (Cont.)

Basic Circuit $(\lambda, \gamma \neq 0)$





$$\Rightarrow \frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2}$$

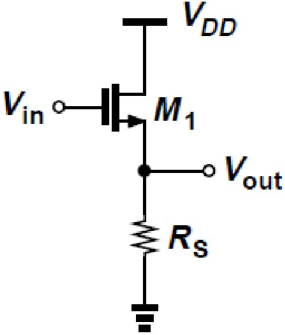
$$Gm = \frac{-gm_1 r_{o1}}{R_S + r_{o1} + (gm_1 + gmb_1)\, r_{o1} R_S}$$

$$R_{out} = [R_S + r_{o1} + (gm_1 + gmb_1)\, r_{o1} R_S] \,||\, R_D$$

with R_S replaced by $\frac{1}{gm_2} || \frac{1}{gmb_2} || r_{o2}$

Source Follower

Basic Circuit $(\lambda, \gamma \neq 0)$



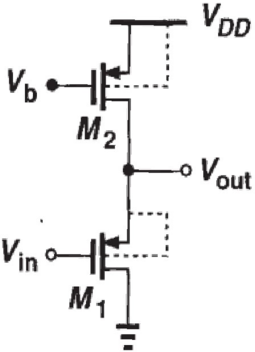
$$Gm = gm_1$$

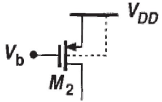
$$R_{out} = r_{o1} || R_S || (\frac{1}{gm_1 + gmb_1})$$

* What if M_1 is replaced by a PMOS?

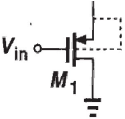
Source Follower with Current Source

Basic Circuit $(\lambda, \gamma \neq 0)$





$\Rightarrow r_{o2}$



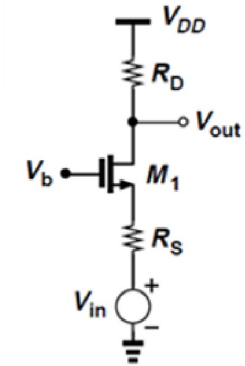
$\Rightarrow r_{o1}||\frac{1}{gm_1}$

$$R_{out} = r_o1||\frac{1}{gm_1}||r_{o2}$$

$$Gm = gm_1$$

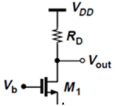
Common Gate

Basic Circuit $(\lambda, \gamma \neq 0)$



$$G_m = \frac{(gm_1 + gmb_1)r_{o1} + 1}{r_{o1} + R_S + (gm_1 + gmb_1)r_{o1}R_S}$$

$$R_{out} = R_D \| \left[r_{o1} + R_S + (gm_1 + gmb_1)r_{o1}R_S \right.$$

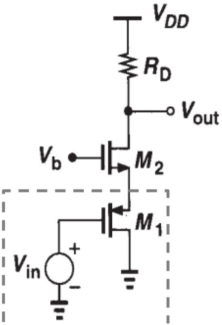


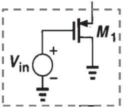
$$\Rightarrow \frac{R_D + r_{o1}}{1 + (gm_1 + gmb_1)r_{o1}}$$

* What if M_1 is replaced by PMOS?

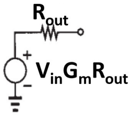
Complex Common Gate

$(\lambda, \gamma \neq 0)$



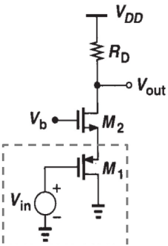
For 

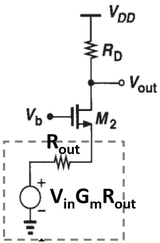
, take it as a source follower with infinity source resistance. Then we get



$$\begin{cases} G_m = gm_1 \\ R_{out} = r_{o1} \parallel \dfrac{1}{gm_1} \parallel \dfrac{1}{gmb_1} \end{cases}$$

Complex Common Gate (Cont.)

Then 

$\Rightarrow$ 

with

$$G_m = \frac{(gm_2 + gmb_2)r_{o2} + 1}{r_{o2} + R_S + (gm_2 + gmb_2)r_{o2}R_S} \cdot gm_1 \left(r_{o1} || \frac{1}{gm_1} || \frac{1}{gmb_1} \right)$$

$$R_{out} = R_D || \left[r_{o2} + R_S + (gm_2 + gmb_2)r_{o2}R_S \right]$$

$$\text{where } R_S = r_{o1} || \frac{1}{gm_1} || \frac{1}{gmb_1}$$

Some Tips qwq

- Understand all the formulas will help.
- Please write down partial steps in the exam.
- When plotting, please mark your diagram well (peak values, period. . .).

Good Luck for Your Mid!