



**University Institute of Engineering**  
**Department of Computer Science & Engineering**

**EXPERIMENT: 4**

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**BRANCH: BE-CSE**

**SECTION / GROUP: KRG\_2A**

**SEMESTER: 5<sup>TH</sup>**

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**SUBJECT NAME: ADBMS**

1. Consider a relation R having attributes as R(ABCD), functional dependencies are given below:

$AB \rightarrow C$

$C \rightarrow D$

$D \rightarrow A$

Identify the set of candidate keys possible in relation R. List all the set of prime and non-prime attributes.

Ans:

R (A, B, C, D)

Closure:

$A^+ \rightarrow A$

$B^+ \rightarrow B$

$C^+ \rightarrow C, D, A$

$AB^+ \rightarrow A, B, C, D$

$AC^+ \rightarrow A, C, D$

$AD^+ \rightarrow A, D,$

$BC^+ \rightarrow B, C, D, A$

$BD^+ \rightarrow B, D, A, C$

$CD^+ \rightarrow C, D, A$

Candidate Keys: AB, BC, BD

Prime Attributes: A, B, C, D

Non-prime Attributes:

Normal Form: 3NF

Explanation: We compute closures of attribute sets.  $AB^+$  covers all attributes  $\{A, B, C, D\}$ , hence AB is a candidate key. Similarly,  $BC^+$  and  $BD^+$  also cover all attributes. Since all attributes appear in candidate keys, all are prime. Non-prime attributes = None. As every FD has a prime attribute on the left-hand side, relation is in 3NF.

2. Relation R(ABCDE) having functional dependencies as:

$A \rightarrow D$

$B \rightarrow A$

$BC \rightarrow D$

$AC \rightarrow BE$

Identify the set of candidate keys possible in relation R. List all the set of prime and non-prime attributes.

Ans:

R (A, B, C, D, E)

Closure:

$A^+ \rightarrow A, D$

$B^+ \rightarrow B, A, D$

$C^+ \rightarrow C$

$AB^+ \rightarrow A, B, D$

$AC^+ \rightarrow A, C, D, B, E$

$AD^+ \rightarrow A, D$

$BC^+ \rightarrow B, C, A, D, E$

Candidate Keys: AC, BC

Prime Attributes: A, B, C

Non-prime Attributes: D, E

Normal Form: 1NF

Explanation: Closures show  $AC^+$  and  $BC^+$  determine all attributes, making them candidate keys. A, B, C are part of candidate keys, so they are prime. D, E never appear in any candidate key, so they are non-prime. The relation is only in 1NF as some FDs violate 2NF (partial dependencies).

3. Consider a relation R having attributes as R(ABCDE), functional dependencies are given below:

$B \rightarrow A$

$A \rightarrow C$

$BC \rightarrow D$

$AC \rightarrow BE$

Identify the set of candidate keys possible in relation R. List all the set of prime and non-prime attributes.

Ans:

R (A, B, C, D, E)

Closure:

$A^+ \rightarrow A, C, B, E, D$

$B^+ \rightarrow B, A, C, D, E$

$C^+ \rightarrow C$

$D^+ \rightarrow D$

$E^+ \rightarrow E$

Candidate Keys: A, B

Prime Attributes: A, B

Non-prime Attributes: C, D, E Normal Form: BCNF

**Explanation:**

- Compute closures:
  - $A^+ = \{A, C, B, E, D\} \rightarrow$  all attributes, so A is a candidate key.
  - $B^+ = \{B, A, C, D, E\} \rightarrow$  all attributes, so B is also a candidate key.
- Hence, {A, B} are candidate keys.
- Prime attributes = {A, B}.
- Non-prime attributes = {C, D, E}.
- Since all FDs have a candidate key on the left-hand side, the relation satisfies **BCNF**.

4. Consider a relation R having attributes as R(ABCDEF), functional dependencies are given below:

$A \rightarrow BCD$

$BC \rightarrow DE$

$B \rightarrow D$

$D \rightarrow A$

Identify the set of candidate keys possible in relation R. List all the set of prime and non-prime attributes.

Ans:

R (A, B, C, D, E, F)

Closure:

$A^+ \rightarrow A, B, C, D, E$

$B^+ \rightarrow B, D, A, C, E$

$C^+ \rightarrow C$

$D^+ \rightarrow D, A, B, C, E$

$E^+ \rightarrow E$

$F^+ \rightarrow F$

$AF^+ \rightarrow A, B, C, D, E, F$

$BF^+ \rightarrow B, F, D, A, C, E$

$CF^+ \rightarrow C, F$

$DF^+ \rightarrow D, F, A, B, C, E$

Candidate Keys: AF, BF, DF

Prime Attributes: A, B, D, F

Non-prime Attributes: C, E

Normal Form: 1NF

**Explanation:**

- Compute closures:
  - $AF^+ = \{A, B, C, D, E, F\} \rightarrow$  all attributes, so AF is a candidate key.
  - $BF^+ = \{B, D, A, C, E, F\} \rightarrow$  all attributes, so BF is also a candidate key.
  - $DF^+ = \{D, A, B, C, E, F\} \rightarrow$  all attributes, so DF is also a candidate key.
- Candidate Keys = {AF, BF, DF}.
- Prime attributes = {A, B, D, F}.
- Non-prime attributes = {C, E}.
- Because of transitive and partial dependencies, the relation only satisfies **1NF**.

5. Designing a student database involves certain dependencies which are listed below:

$X \rightarrow Y$

$WZ \rightarrow X$

$WZ \rightarrow Y$

$Y \rightarrow W$

$Y \rightarrow X$

$Y \rightarrow Z$

The task here is to remove all the redundant FDs for efficient working of the student database management system.

Ans:

$R(W, X, Y, Z)$

Closure:

$X^+ \rightarrow X, Y, W, Z$

$Y^+ \rightarrow Y, X, W, Z$

$WZ^+ \rightarrow W, Z, X, Y$

Candidate Keys:  $X, Y, WZ$

Prime Attributes:  $X, Y, W, Z$

Non-prime Attributes:

Normal Form: BCNF

**Explanation:**

- Compute closures:
  - $X^+ = \{X, Y, W, Z\} \rightarrow$  all attributes, so  $X$  is a candidate key.
  - $Y^+ = \{Y, X, W, Z\} \rightarrow$  all attributes, so  $Y$  is also a candidate key.
  - $WZ^+ = \{W, Z, X, Y\} \rightarrow$  all attributes, so  $WZ$  is also a candidate key.
- Candidate Keys =  $\{X, Y, WZ\}$ .
- Since all attributes are part of some candidate key, all are **prime**.
- No non-prime attributes exist.
- Each FD has a candidate key on the left-hand side  $\rightarrow$  relation is in **BCNF**.

6. Debix Pvt Ltd needs to maintain database having dependent attributes ABCDEF.

These attributes are functionally dependent on each other for which functionally dependency set F given as:

$A \rightarrow BC$

$D \rightarrow E$

$BC \rightarrow D$

$A \rightarrow D$

Consider a universal relation  $R1(A, B, C, D, E, F)$  with functional dependency set F, also all attributes are simple and take atomic values only. Find the highest normal form along with the candidate keys with prime and non-prime attribute.

Ans:

$R(A, B, C, D, E, F)$

Closure:

$A^+ \rightarrow A, B, C, D, E$

$B^+ \rightarrow B$

$C^+ \rightarrow C$

$D^+ \rightarrow D, E$

$AF^+ \rightarrow A, B, C, D, E, F$

Candidate Keys: AF

Prime Attributes: A, F

Non-prime Attributes: B, C, D, E Normal Form: 1NF

**Explanation:**

- $A^+ = \{A, B, C, D, E\}$ . Missing F  $\rightarrow$  not a key.
- $AF^+ = \{A, B, C, D, E, F\} \rightarrow$  covers all attributes  $\rightarrow$  Candidate Key.
- No smaller set works, so **Candidate Key** = {AF}.
- Prime attributes = {A, F}. Non-prime attributes = {B, C, D, E}.
- The relation is only in **1NF**, since  $A \rightarrow BC$  and  $A \rightarrow D$  create partial dependencies (violating 2NF).