# stable tree bertsimas

### April 17, 2025

0.1 Notebook implementing the algorithm in Bertsimas et al. (ttps://arxiv.org/abs/2305.17299)

```
[1]: import numpy as np
import itertools
from sklearn.model_selection import train_test_split
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import load_breast_cancer
from sklearn.metrics import accuracy_score
```

### 0.1.1 Import dataset and split

```
[2]: data_breast_cancer = load_breast_cancer(as_frame=True)
    X_full = data_breast_cancer["data"]
    y_full = data_breast_cancer["target"]
```

```
[3]: print("X_full shape: ", X_full.shape)
X_full.head()
```

X full shape: (569, 30)

K_IUII Shape. (503, 50)					
[3]:	mean radius mean	texture mean p	perimeter	mean area	mean smoothness \
0	17.99	10.38	122.80	1001.0	0.11840
1	20.57	17.77	132.90	1326.0	0.08474
2	19.69	21.25	130.00	1203.0	0.10960
3	11.42	20.38	77.58	386.1	0.14250
4	20.29	14.34	135.10	1297.0	0.10030
	mean compactness	mean concavity	mean con	cave points	mean symmetry \
0	0.27760	0.3001		0.14710	0.2419
1	0.07864	0.0869		0.07017	0.1812
2	0.15990	0.1974		0.12790	0.2069
3	0.28390	0.2414		0.10520	0.2597
4	0.13280	0.1980		0.10430	0.1809

```
2
                       0.05999 ...
                                           23.57
                                                          25.53
                                                                           152.50
     3
                       0.09744 ...
                                           14.91
                                                          26.50
                                                                           98.87
     4
                       0.05883 ...
                                           22.54
                                                          16.67
                                                                           152.20
        worst area worst smoothness worst compactness worst concavity \
     0
            2019.0
                              0.1622
                                                  0.6656
                                                                    0.7119
            1956.0
                              0.1238
                                                  0.1866
                                                                    0.2416
     1
     2
            1709.0
                              0.1444
                                                  0.4245
                                                                    0.4504
     3
             567.7
                              0.2098
                                                  0.8663
                                                                    0.6869
            1575.0
                              0.1374
                                                  0.2050
                                                                    0.4000
        worst concave points worst symmetry worst fractal dimension
     0
                      0.2654
                                       0.4601
                                                                0.11890
     1
                      0.1860
                                       0.2750
                                                                0.08902
     2
                      0.2430
                                       0.3613
                                                                0.08758
     3
                      0.2575
                                       0.6638
                                                                0.17300
                                                                0.07678
                      0.1625
                                       0.2364
     [5 rows x 30 columns]
[4]: print("y_full shape: ", y_full.shape)
     y_full.head()
    y_full shape: (569,)
[4]: 0
          0
     1
          0
     2
          0
     3
          0
     Name: target, dtype: int64
[5]: X_train, X_test, y_train, y_test = train_test_split(X_full, y_full, test_size=0.
     →2, random_state=42)
     print("X train shape: {}, X test shape: {}".format(X train.shape, X test.shape))
     print("y_train shape: {}, y_test shape: {}".format(y_train.shape, y_test.shape))
    X_train shape: (455, 30), X_test shape: (114, 30)
    y_train shape: (455,), y_test shape: (114,)
    0.1.2 Generate first collection (T0) of trees (trained on X0)
[6]: def train_trees(X, y, depths=[3,5,7], min_samples=[5,10]):
         """Train multiple trees for different hyperparams & possibly bootstrap."""
         trees = []
         for depth, min_leaf in itertools.product(depths, min_samples):
             # need to boostrap later
```

Generated 6 trees for TO

0.1.3 Generate second collection of trees (T) (trained on full data)

```
[7]: T = train_trees(X_full, y_full)
```

0.1.4 Get global ranges of numerical features and their names

(todo: categorical features)

```
[8]: feature_names = X_full.columns
global_lower = X_full.min().values
global_upper = X_full.max().values
```

0.1.5 Compute average distance of each tree in T to the T0 collection

```
[9]: from bertsimas_stable.Paths import tree_distance
```

Distances to T0

## 0.1.6 Distances to T0 (using given method)

## 0.1.7 Compute predictive performance for each tree

/Users/adb/stuff/gitclones/Suicide\_Project/.venv/lib/python3.11/site-

Accuracies on test set: {0.974, 0.965, 0.991, 0.965, 0.991, 0.956}

packages/sklearn/utils/validation.py:2739: UserWarning: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(

```
/Users/adb/stuff/gitclones/Suicide_Project/.venv/lib/python3.11/site-packages/sklearn/utils/validation.py:2739: UserWarning: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(
/Users/adb/stuff/gitclones/Suicide_Project/.venv/lib/python3.11/site-
```

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/Users/adb/stuff/gitclones/Suicide\_Project/.venv/lib/python3.11/site-packages/sklearn/utils/validation.py:2739: UserWarning: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(

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/Users/adb/stuff/gitclones/Suicide\_Project/.venv/lib/python3.11/site-packages/sklearn/utils/validation.py:2739: UserWarning: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(

## 0.1.8 Identify Pareto frontier

Pareto indices: [2]

Number of Pareto-optimal trees: 1

### 0.2 Choose the "best" stable tree from the Pareto set

Chosen stable tree index = 2, dist=9.34090448178685, perf=0.9912280701754386