

~~SUSY-FLAVOR~~
2.5
190.08840

Observable	SM	Experiment*	Future Thy. \oplus Exp. bound/uncertainty
$ d_e $ [e.cm]	$\lesssim \mathcal{O}(10^{-40})$ [32, 33]	$< 8.7 \times 10^{-29}$ [34]	$\lesssim 10^{-30}$ [1, 35, 36]
$ d_\mu $ [e.cm]	$\lesssim \mathcal{O}(10^{-38})$ [37]	$< 1.6 \times 10^{-19}$ [38]	$\lesssim 10^{-24}$ [1, 39]
$ d_n $ [e.cm]	$\lesssim \mathcal{O}(10^{-31})$ [40, 41]	$< 2.9 \times 10^{-26}$ [42]	$\lesssim 5 \times 10^{-28}$ [43]
a_e [10^{-12}]	1159652182.79 ± 7.71 [44]	1159652180.73 ± 28 [45]	—
a_μ [10^{-11}]	116591802 ± 49 116591828 ± 50 [46]	116592089 ± 63 [47]	± 12 [1]
$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$3.04 \pm 15.7\%$ $\times 10^{-11}$ [48]	$< 2.6 \times 10^{-8}$ [49]	$\pm 6.0\% \pm 5.1\% = 7.9\%$ [1, 50]
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$9.2 \pm 8.2\%$ $\times 10^{11}$ [48]	$17.3_{-10.5}^{+11.5}$ [51]	$\pm 5.4\% \pm 2.2\% = 5.8\%$ [1, 52]
$\text{Br}(B_d \rightarrow X_s \gamma)^\dagger$	$3.17 \pm 7.3\%$ $\times 10^4$ [53]	$3.43 \pm 6.7\%$ [54]	$\pm 6.7\% \pm 4.0\% = 7.8\%$ [55]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$	$3.74 \pm 4.1\%$ $\times 10^9$ [56]	2.9 ± 0.7 [57]	$\pm 3.2\% \pm 8.6\% = 9.2\%$ [58]
$\text{Br}(B_d \rightarrow \mu^+ \mu^-)$	$1.21 \pm 6.1\%$ $\times 10^{10}$ [56]	$3.6_{-1.4}^{+1.6}$ [57]	$\pm 3.9\% \pm 36.0\% = 36.2\%$ [58]
$\text{Br}(B_u \rightarrow \tau \nu_\tau)$	$0.779 \pm 8.6\%$ $\times 10^4$ [59]	1.14 ± 0.22 [54]	$\pm 6.0\% \pm 6.3\% = 8.7\%$ [55]
ΔM_{B_d} [ps $^{-1}$]	$0.545 \pm 16.8\%$ [60]	0.507 ± 0.005 [54]	$\pm 3.7\% \pm 0.9\% = 3.8\%$
ΔM_{B_s} [ps $^{-1}$]	$17.70 \pm 15.0\%$ [60]	17.719 ± 0.043 [54]	$\pm 3.1\% \pm 0.2\% = 3.1\%$
ΔM_K [10 $^{-3}$ ps $^{-1}$]	4.824	5.292 ± 0.009 [61]	—
ϵ_K [10 $^{-3}$]	$2.319 \pm 9.3\%$ [62]	2.228 ± 0.011 [61]	—
$\sin(2\beta)$	$0.695 \pm 5.6\%$ [62]	0.68 ± 0.02 [54]	$\pm 2.1\% \pm 1.2\% = 2.4\%$ [58]
$\sin(2\beta_s)$	$0.0375 \pm 4.0\%$ [62]	$-0.04_{-0.10}^{+0.13}$ [54]	$\pm 2.5\% \pm 15.8\% = \pm 16.0\%$ [58]

*All upper bounds are at 90% C.L., ${}^\dagger E_\gamma > 1.6$ GeV in the B -meson rest frame.

Table 3: The complete set of observables studied in this work. All processes are computed using SUSY_FLAVOR v2.10.

calculations. The most important parameters α_i for our analysis are the CKM angle $|V_{ub}|$ and the CKM phase δ , although we include all the parameters listed in Table 4. The uncertainty in O due to the corresponding error in α_i can be estimated as

$$\sigma_i(O) = \frac{\partial O}{\partial \alpha_i} \sigma(\alpha_i). \quad (1)$$

~~+510.08840~~

Super Iso 3.4

Observable	Combined experimental value	95% C.L. Bound
BR($B \rightarrow X_s \gamma$)	$(3.43 \pm 0.21 \pm 0.07) \times 10^{-4}$ [109] 0808.1297 + UPDTE	$2.63 \times 10^{-4} \leq \text{BR}(b \rightarrow s\gamma) \leq 4.23 \times 10^{-4}$
$\Delta_0(B \rightarrow K^* \gamma)$	$(5.2 \pm 2.6) \times 10^{-2}$ (a)	$-1.7 \times 10^{-2} < \Delta_0 < 8.9 \times 10^{-2}$
BR($B_u \rightarrow \tau \nu_\tau$)	$(1.64 \pm 0.34) \times 10^{-4}$ [109]	$0.71 \times 10^{-4} < \text{BR}(B_u \rightarrow \tau \nu_\tau) < 2.57 \times 10^{-4}$
$R_{\tau \nu_\tau}$	1.63 ± 0.54 (b)	$0.56 < R_{\tau \nu_\tau} < 2.70$
BR($B \rightarrow D^0 \tau \nu_\tau$)	$(8.6 \pm 2.4 \pm 1.1 \pm 0.6) \times 10^{-3}$ [112]	$2.9 \times 10^{-3} < \text{BR}(B \rightarrow D^0 \tau \nu_\tau) < 14.2 \times 10^{-3}$
$\xi_{D \ell \nu}$	$0.416 \pm 0.117 \pm 0.052$ [112]	$0.151 < \xi_{D \ell \nu} < 0.681$
BR($B_s \rightarrow \mu^+ \mu^-$)	$(2.9 \pm 0.7) \times 10^{-9}$ [113]	$1.3 \times 10^{-9} < \text{BR}(B_s \rightarrow \mu^+ \mu^-) < 4.5 \times 10^{-9}$
BR($B_d \rightarrow \mu^+ \mu^-$)	$(3.6^{+1.6}_{-1.4}) \times 10^{-10}$ [113]	$\text{BR}(B_d \rightarrow \mu^+ \mu^-) < 1.1 \times 10^{-9}$
$\frac{\text{BR}(K \rightarrow \mu \nu)}{\text{BR}(\pi \rightarrow \mu \nu)}$	0.6358 ± 0.0011 (c)	$0.6257 < \frac{\text{BR}(K \rightarrow \mu \nu)}{\text{BR}(\pi \rightarrow \mu \nu)} < 0.6459$
$R_{\mu 23}$	0.999 ± 0.007 [104]	$0.985 < R_{\mu 23} < 1.013$ (d)
BR($D_s \rightarrow \tau \nu_\tau$)	$(5.38 \pm 0.32) \times 10^{-2}$ [97]	$4.7 \times 10^{-2} < \text{BR}(D_s \rightarrow \tau \nu_\tau) < 6.1 \times 10^{-2}$
BR($D_s \rightarrow \mu \nu_\mu$)	$5.81 \pm 0.43 \times 10^{-3}$ [97]	$4.9 \times 10^{-3} < \text{BR}(D_s \rightarrow \mu \nu_\mu) < 6.7 \times 10^{-3}$
BR($D \rightarrow \mu \nu_\mu$)	$(3.82 \pm 0.33) \times 10^{-4}$ [15]	$3.0 \times 10^{-4} < \text{BR}(D \rightarrow \mu \nu_\mu) < 4.6 \times 10^{-4}$
δa_μ	$(2.55 \pm 0.80) \times 10^{-9}$ [114]	$-2.4 \times 10^{-10} < \delta a_\mu < 5.0 \times 10^{-9}$

Table 17: Suggested limits for the observables implemented in SuperIso v3.4. The 95% C.L. bounds presented in this table include both the experimental and the theoretical uncertainties.

- (a) Value obtained combining the Babar measurement [110] with the results of [15, 111].
- (b) Value deduced from [109].
- (c) Value obtained combining the results of [15, 95].
- (d) See [21] for a discussion on the uncertainties.

SUSY_FLAVOR 2.53

Observable	Experiment
$\Delta F = 0$	
$\frac{1}{2}(g - 2)_e$	$(1159652188.4 \pm 4.3) \times 10^{-12}$ [51]
$\frac{1}{2}(g - 2)_\mu$	$(11659208.7 \pm 8.7) \times 10^{-10}$ [2]
$\frac{1}{2}(g - 2)_\tau$	$< 1.1 \times 10^{-3}$ [52]
$ d_e (\text{ecm})$	$< 1.6 \times 10^{-27}$ [53]
$ d_\mu (\text{ecm})$	$< 2.8 \times 10^{-19}$ [54]
$ d_\tau (\text{ecm})$	$< 1.1 \times 10^{-17}$ [55]
$ d_n (\text{ecm})$	$< 2.9 \times 10^{-26}$ [56]
$\Delta F = 1$	
$\text{Br}(\mu \rightarrow e\gamma)$	$< 5.7 \times 10^{-13}$ [57]
$\text{Br}(\tau \rightarrow e\gamma)$	$< 3.3 \times 10^{-8}$ [58]
$\text{Br}(\tau \rightarrow \mu\gamma)$	$< 4.4 \times 10^{-8}$ [58]
$\text{Br}(K_L \rightarrow \pi^0\nu\nu)$	$< 6.7 \times 10^{-8}$ [59]
$\text{Br}(K^+ \rightarrow \pi^+\nu\nu)$	$17.3^{+11.5}_{-10.5} \times 10^{-11}$ [60]
$\text{Br}(B_d \rightarrow ee)$	$< 1.13 \times 10^{-7}$ [61]
$\text{Br}(B_d \rightarrow \mu\mu)$	$< 7.4 \times 10^{-10}$ [62]
$\text{Br}(B_d \rightarrow \tau\tau)$	$< 4.1 \times 10^{-3}$ [64]
$\text{Br}(B_d \rightarrow \mu e)$	$< 3.7 \times 10^{-9}$ [63]
$\text{Br}(B_s \rightarrow ee)$	$< 7.0 \times 10^{-5}$ [65]
$\text{Br}(B_s \rightarrow \mu\mu)$	$(2.9 \pm 0.7) \times 10^{-9}$ [66]
$\text{Br}(B_s \rightarrow \tau\tau)$	--
$\text{Br}(B_s \rightarrow \mu e)$	$< 1.4 \times 10^{-8}$ [63]
$\text{Br}(B_s \rightarrow \tau e)$	$< 2.8 \times 10^{-5}$ [55]
$\text{Br}(B_s \rightarrow \mu\tau)$	$< 2.2 \times 10^{-5}$ [55]
$\text{Br}(B^+ \rightarrow \tau^+\nu)$	$(1.14 \pm 0.27) \times 10^{-4}$ [55]
$\text{Br}(B \rightarrow D\tau\nu)/\text{Br}(B \rightarrow Dl\nu)$	$(0.440 \pm 0.058 \pm 0.042)$ [67]
$\text{Br}(B \rightarrow D^*\tau\nu)/\text{Br}(B \rightarrow D^*l\nu)$	$(0.332 \pm 0.024 \pm 0.018)$ [67]
$\text{Br}(B \rightarrow X_s\gamma)$	$(3.52 \pm 0.25) \times 10^{-4}$ [68]
$\text{Br}(t \rightarrow ch, uh)$	$< 5.6 \times 10^{-3}$ [69]
$\Delta F = 2$	
$ \epsilon_K $	$(2.229 \pm 0.010) \times 10^{-3}$ [55]
ΔM_K	$(5.292 \pm 0.009) \times 10^{-3} \text{ ps}^{-1}$ [55]
ΔM_D	$(2.37^{+0.66}_{-0.71}) \times 10^{-2} \text{ ps}^{-1}$ [55]
ΔM_{B_d}	$(0.507 \pm 0.005) \text{ ps}^{-1}$ [68]
ΔM_{B_s}	$(17.77 \pm 0.12) \text{ ps}^{-1}$ [70]

Table 1: List of observables calculated by SUSY_FLAVOR v2.5 and their measured values.

Observable	Experiment [115–117]	SM prediction
$\text{BR}(B \rightarrow X_s \ell^+ \ell^-)_{q^2 \in [1,6]\text{GeV}^2}$	$(1.56 \pm 0.39) \times 10^{-6}$	$(1.73 \pm 0.16) \times 10^{-6}$
$\text{BR}(B \rightarrow X_s \ell^+ \ell^-)_{q^2 > 14.4\text{GeV}^2}$	$(4.79 \pm 1.04) \times 10^{-7}$	$(2.20 \pm 0.44) \times 10^{-7}$
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$(0.60 \pm 0.06 \pm 0.05 \pm 0.04 \pm 0.05) \times 10^{-7}$	$(0.70 \pm 0.81) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$0.37 \pm 0.10 \pm 0.04$	0.32 ± 0.20
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$-0.19 \pm 0.40 \pm 0.02$	-0.01 ± 0.04
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$0.03 \pm 0.15 \pm 0.01$	0.17 ± 0.02
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$0.00 \pm 0.52 \pm 0.06$	-0.37 ± 0.03
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$0.45 \pm 0.22 \pm 0.09$	0.52 ± 0.04
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$0.24 \pm 0.22 \pm 0.05$	-0.05 ± 0.04
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [0.1,2]\text{GeV}^2}$	$-0.12 \pm 0.56 \pm 0.04$	0.02 ± 0.04
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$(0.30 \pm 0.03 \pm 0.03 \pm 0.02 \pm 0.02) \times 10^{-7}$	$(0.35 \pm 0.29) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$0.74 \pm 0.10 \pm 0.03$	0.76 ± 0.20
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$-0.29 \pm 0.65 \pm 0.03$	-0.05 ± 0.05
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$0.50 \pm 0.08 \pm 0.02$	0.25 ± 0.09
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$0.74 \pm 0.58 \pm 0.16$	0.54 ± 0.07
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$0.29 \pm 0.39 \pm 0.07$	-0.33 ± 0.11
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$-0.15 \pm 0.38 \pm 0.05$	-0.06 ± 0.06
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [2,4.3]\text{GeV}^2}$	$-0.3 \pm 0.58 \pm 0.14$	0.04 ± 0.05
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$(0.49 \pm 0.04 \pm 0.04 \pm 0.03 \pm 0.04) \times 10^{-7}$	$(0.48 \pm 0.53) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$0.57 \pm 0.07 \pm 0.03$	0.63 ± 0.14
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$0.36 \pm 0.31 \pm 0.03$	-0.11 ± 0.06
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$-0.25 \pm 0.08 \pm 0.02$	-0.36 ± 0.05
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$1.18 \pm 0.30 \pm 0.10$	0.99 ± 0.03
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$-0.19 \pm 0.16 \pm 0.03$	-0.83 ± 0.05
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$0.04 \pm 0.15 \pm 0.05$	-0.02 ± 0.06
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [4.3,8.68]\text{GeV}^2}$	$0.58 \pm 0.38 \pm 0.06$	0.02 ± 0.06
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$(0.56 \pm 0.06 \pm 0.04 \pm 0.04 \pm 0.05) \times 10^{-7}$	$(0.67 \pm 1.17) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$0.33 \pm 0.08 \pm 0.03$	0.39 ± 0.24
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$0.07 \pm 0.28 \pm 0.02$	-0.32 ± 0.70
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$-0.50 \pm 0.03 \pm 0.01$	-0.47 ± 0.14
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$-0.18 \pm 0.70 \pm 0.08$	1.15 ± 0.33
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$-0.79 \pm 0.20 \pm 0.18$	-0.82 ± 0.36
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$0.18 \pm 0.25 \pm 0.03$	0.00 ± 0.00
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [14.18,16]\text{GeV}^2}$	$-0.40 \pm 0.60 \pm 0.06$	0.00 ± 0.01
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$(0.41 \pm 0.04 \pm 0.04 \pm 0.03 \pm 0.03) \times 10^{-7}$	$(0.43 \pm 0.78) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$0.38 \pm 0.09 \pm 0.03$	0.36 ± 0.13
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$-0.71 \pm 0.35 \pm 0.06$	-0.55 ± 0.59
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$-0.32 \pm 0.08 \pm 0.01$	-0.41 ± 0.15
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$0.70 \pm 0.52 \pm 0.06$	1.24 ± 0.25
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$-0.60 \pm 0.19 \pm 0.09$	-0.66 ± 0.37
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$-0.31 \pm 0.38 \pm 0.10$	0.00 ± 0.00
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [16,19]\text{GeV}^2}$	$0.12 \pm 0.54 \pm 0.04$	0.00 ± 0.04
$\langle dBR/dq^2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$(0.34 \pm 0.03 \pm 0.04 \pm 0.02 \pm 0.03) \times 10^{-7}$	$(0.38 \pm 0.33) \times 10^{-7}$
$\langle F_L(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.65 \pm 0.08 \pm 0.03$	0.70 ± 0.21
$\langle P_1(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.15 \pm 0.41 \pm 0.03$	-0.06 ± 0.04
$\langle P_2(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.33 \pm 0.12 \pm 0.02$	0.10 ± 0.08
$\langle P'_4(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.58 \pm 0.36 \pm 0.06$	0.53 ± 0.07
$\langle P'_5(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.21 \pm 0.21 \pm 0.03$	-0.34 ± 0.10
$\langle P'_6(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.18 \pm 0.21 \pm 0.03$	-0.05 ± 0.05
$\langle P'_8(B \rightarrow K^* \mu^+ \mu^-) \rangle_{q^2 \in [1,6]\text{GeV}^2}$	$0.46 \pm 0.38 \pm 0.04$	0.03 ± 0.04

Table 18: Experimental results and theoretical predictions for the $b \rightarrow s\ell\ell$ observables.

$$\begin{aligned} \tilde{q}_a & \text{(mass eigenstate)} & (K^+ k)_{ii} & (K^+ m^2 k)_{ii} \\ i = L1, L2, L3, R1, R2, R3 & M = q_i \rightarrow q_j & \propto \sum_a \frac{K_{ia} K_{ja}^*}{p^2 - m_a^2} = \sum_a \left[\frac{K_{ia} K_{ja}^*}{p^2 - m^2} + \frac{K_{ia} \delta m_a^2 K_{ja}^*}{(p^2 - M^2)^2} \right] \\ & K_{ia} \quad K_{ja}^* & = \frac{1}{p^2 - M^2} \left[\delta_{ij} + \sum_a \frac{\delta m_a^2}{p^2 - M^2} |K_{ia} K_{ja}^*| \right] \end{aligned}$$

$$\begin{aligned} \text{For unitary matrix w. small mixings} \quad \sum_a \delta m_a^2 K_{ia} K_{ja}^* & \approx \delta m_i^2 K_{ii} K_{jj}^* + \delta m_j^2 K_{ij} K_{ji}^* \\ K_{ij}^* K_{jj} \approx -K_{ii} K_{ji} & \approx (\delta m_i^2 - \delta m_j^2) K_{ii} K_{jj}^* = (m_i^2 - m_j^2) K_{ii} K_{jj}^* \\ \therefore M \propto 1 + \frac{m_i^2 - m_j^2}{-m^2} K_{ii} K_{jj}^* \end{aligned}$$

$$V M V^\dagger = \text{diag}$$

$$\tilde{q} = V^\dagger \tilde{q} \quad \text{mass}$$

$$-L = \tilde{q}^* M_q^2 \tilde{q} + \tilde{u}^* M_u^2 \tilde{u} + \tilde{d}^* M_d^2 \tilde{d} \quad \leftarrow \text{in our definition (B.4)}$$

SCKM basis

$$\tilde{q}^* M_q^2 \tilde{q} = (\tilde{q}^\dagger V^\dagger) M_q^2 \text{diag} (V \tilde{q}) \quad (Q^\dagger U) \begin{pmatrix} M_q & A^\dagger \\ A & M_u \end{pmatrix} (U^\dagger)$$

$$\tilde{q}_i^* \tilde{q}_j \tilde{q} + \tilde{q}_i \tilde{q}_j \tilde{q} = \tilde{q}_i^* V_{ij} q_j \tilde{q} + \bar{q}_i \bar{q} (V^\dagger)_{ij} q_j$$

$$\rightarrow \text{in this definition } K = \sqrt{I}$$

$$\text{In 0812.0511 } \delta_{ij} \equiv \frac{m_j^2 - m_i^2}{m_q^2} K_{ij} K_{ji}^* = \frac{m_i^2 - m_j^2}{m_q^2} K_{ii} K_{jj}^*$$

and $K \equiv V_{\text{quark}} V_{\text{squark}}^\dagger$ (B.4)

$$\therefore \delta_{ij} \equiv \frac{j-i}{m_q^2} V_{ji}^* V_{jj} = \frac{i-j}{m_q^2} V_{ii}^* V_{ij} = (-M)^*$$

$$\text{ie. } K = V^\dagger$$

$$\frac{1}{p^2 - m_a^2} = \frac{1}{p^2 - M^2} + \frac{\delta m_a^2}{(p^2 - M^2)^2} \quad \left| \begin{array}{l} (m_j^2 - m_i^2) K_{ij} K_{ji}^* = (m_j^2 - m_i^2) (-K_{ii} K_{ji}^*) \\ = -(m_j^2 - m_i^2) K_{ii} K_{ji}^* \end{array} \right.$$

$$\delta m_a^2 = m_a^2 - M^2$$

$$\begin{aligned} \text{Mass insertion: } M & \sim \tilde{q}_i \tilde{q}_j^* \sim (m^2)_{ij} / M \\ \therefore \delta_{ij} & \approx -\frac{(m^2)_{ij}^*}{\text{mass}} \end{aligned}$$

No. _____

Sho Iwamoto

Date _____

0812.0511

H

1001.1513

II

1002.0900

H

1306.6631

D-system update δ_{iz}^n
Nir + Hochberg

Nir - Perez + Ishidori $\text{Im } \delta = 0.3 \text{ Re } \delta$

←

Perez Shandini

$\text{Im } \delta \sim \text{Re } \delta$

Perez Ishidori

$$Y_d^+ V_{CKM} \bar{y} y^+ V_{CKM} Y_d$$

Write down anything in form one obs.

$$S m_q^2 = \textcircled{1} \bar{y} y^+$$

$$\rightarrow \bar{y}' y'^+$$

$$S m_d^2 = \textcircled{1} \bar{y} Y_d^+ y^+ Y_d$$

$$\rightarrow \bar{Y}_d^{\text{diag}} \bar{y} y^+ Y_d$$

$$A_u \sim \bar{y} y^+ Y_u$$

$$\rightarrow \bar{y}' y'^+ Y_u^{\text{diag}}$$

$$\rightarrow (A_u)_{\parallel} = (\bar{y}' y'^+)_{\parallel} (Y_u^{\text{diag}})_{\parallel}$$

in form one obs

$$\rightarrow \begin{matrix} \tilde{U}_L & (A_u)_{\parallel} & \tilde{U}_R \\ \hline U_L & : & U_R \end{matrix}$$

is Real
→ NO EDM

Note that we can have

$$A_d^* = V_{dL} \bar{y} y^+ Y_d V_{dR}^+$$

$$= V_{CKM} \bar{y}' y'^+ V_{CKM}^+ Y_d^{\text{diag}}$$

$$\begin{matrix} \tilde{U}_L & -x- & \tilde{U}_R \\ \hline \tilde{U}_L & x & \tilde{U}_R \end{matrix}$$

$$A_d^*_{12} = (V \bar{y}' y'^+ V^+)_{12} Y_d^{\text{diag}}_2$$

(Non zero

and anti C)

No EDM also fin

down q

? → Real

W(?)

$$\begin{aligned} S m^2_{d_{RR}} &= Y_d^+ \gamma \gamma^+ Y_d \\ &= Y_d^{\text{diag}+} V^+ \gamma' \gamma'^+ V Y_d^{\text{diag}} \end{aligned}$$

$$[S m^2_{d_{RR}}]_{ab} = Y_d^d \alpha (V^+ \gamma' \gamma'^+ V)_{ab} Y_d^d \beta$$

SARAH
Sphere

Calibbi
Paradisi
Zojer

CP viol in Slv dgm?

$$W = Y_{uij} H_u Q_i \bar{U}_j + Y_{dij} H_d Q_i \bar{D}_j$$

$$Y_u^{\text{diag}} = V_{uL} Y_u V_{uR}^+ \quad ; \quad Y_d^{\text{diag}} = V_{dL} Y_d V_{dR}^+$$

$$= H_u Q V_{uL}^+ Y_u^{\text{diag}} V_{uR} \bar{U} + H_d Q V_{dL}^+ Y_d^{\text{diag}} V_{dR} \bar{D}$$

◦ HAT - BASIS : down-sector diagonalized

◦ Tilde - BASIS : up-sector diagonalized

$$= H_u \tilde{Q} Y_u^{\text{diag}} \tilde{\bar{U}} + H_d \tilde{Q} V_{uL} V_{dL}^+ Y_d^{\text{diag}} V_{dR} \bar{D}$$

$$= H_u \hat{Q} V_{uL} V_{uR}^+ Y_u^{\text{diag}} V_{uR} \bar{U} + H_d \hat{Q} Y_d^{\text{diag}} \hat{\bar{D}}$$

$$m_i^2; Q_i Q_i^* = Q^T m^2 Q \xrightarrow{\text{omitted}} = Q^T m^2 Q^*$$

$$= \tilde{m}_i^2 \tilde{Q}_{ik} V_{ki} \tilde{Q}_k^* (V^+)_jl = \tilde{Q} V_{uL} m^2 V_{uR}^+ \tilde{Q}^*$$

$$= \hat{Q} V_{dL} m^2 V_{dR}^+ \hat{Q}^*$$

$$m_{ii}^2 \bar{U}_i \bar{U}_i^* = \tilde{\bar{U}}_i^* V_{dR} (m^2)^* V_{uR}^+ \tilde{\bar{U}}_i$$

$$m_{ii}^2 \bar{D}_i \bar{D}_i^* = \tilde{\bar{D}}_i^* V_{dR} (m^2)^* V_{dR}^+ \tilde{\bar{D}}_i$$

$$G = T^\alpha \tilde{g}^\alpha$$

$$\hat{G} = -(T^\alpha)^T \tilde{g}^\alpha$$

$$\bar{G} = T^\alpha \tilde{\bar{g}}^\alpha$$

$$\mathcal{L} \supset -\sqrt{2} g_3 \left(\overset{\text{up}}{q}_i^* G \overset{\text{down}}{Q}_i + \overset{\text{up}}{u}_i^* \hat{G} \overset{\text{up}}{\bar{U}}_i + \overset{\text{down}}{d}_i^* \hat{G} \overset{\text{down}}{\bar{D}}_i + \overset{\text{up}}{G} \overset{\text{down}}{Q}_i q_i + \dots \right)$$

is diagonal (F.C.) at this stage., i.e. before defining
"squark mass eigenstates".

MFV-like

$$m_{\tilde{q}}^2 = m_{\text{diag}}^2 + \begin{pmatrix} 0 & \lambda^3 & \lambda^3 \\ \lambda^3 & \lambda^4 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

off-diag
 δm $\sim O(\lambda)$

$$m_{\tilde{\mu}}^2 = \dots \begin{pmatrix} 0 & \lambda^4 & \lambda^3 \\ \lambda^4 & \lambda^2 & \lambda \\ \lambda^3 & \lambda & 1 \end{pmatrix} \sim O(\lambda^2)$$

$\rightarrow \tilde{C}_L$ and \tilde{U}_R : degenerate but $O(1)$ mixing
 \tilde{C}_R , \tilde{M}_D : small and small mixing.

this means that, for "usual" mediation

$\Delta m^2 \gg$ large \rightarrow mix

square mixing from CKM

$\Delta m^2 \ll$ small \rightarrow off-diagonal correction
 can yield
 large mix!!

Gilad et al
 studied for
 t-c mixing
 where oscillation
 does not play
 an important role

MFV-like

$$\tilde{m}_{d_L}^2 = \text{diag.} + A^\dagger A \quad A = \gamma^{\text{diag}} V_{CKM}$$

$$= V^\dagger \tilde{m}^2 \text{diag} V = K \tilde{m}^2 \text{diag} K^\dagger \quad k = 1+x$$

$$= (1+x)(\text{diag} + A^\dagger A)(1-x) \quad KK^\dagger = 1 - x - x^\dagger$$

$$= \text{diag} + A^\dagger A + x \text{id}$$

$$-L \supset Q \overset{M_Q}{\underset{m_Q^2 T}{\sim}} Q^\dagger + \bar{U}^\dagger \overset{M_U}{\underset{m_U^2 T}{\sim}} \bar{U} + Q A_U \bar{U} + \bar{U}^\dagger A_U^\dagger Q^\dagger$$

$$(Q \bar{U}^\dagger) \begin{pmatrix} M_Q & A_U \\ A_U^\dagger & M_U \end{pmatrix} \begin{pmatrix} Q^\dagger \\ \bar{U} \end{pmatrix}$$

$\gamma_0 \gamma_0^\dagger \gamma_0 \gamma_0^\dagger$ $\gamma_\alpha^\dagger \gamma_0 \gamma_\alpha^\dagger \gamma_0$ $\gamma_0 \gamma_0^\dagger \gamma_0$ $\gamma_0^\dagger \gamma_0 \gamma_0^\dagger \gamma_0$
 $\gamma_0 \gamma_0^\dagger \gamma_0$ $\gamma_\alpha^\dagger \gamma_0 \gamma_\alpha^\dagger$

$$\tilde{u}_c \xrightarrow{x} \tilde{u}_R$$

\tilde{u}_c \tilde{u}_R
 $\gamma_0 \gamma_0^\dagger \gamma_0 \gamma_0^\dagger$ $\gamma_\alpha^\dagger \gamma_0 \gamma_\alpha^\dagger \gamma_0$
 $\gamma_0 \gamma_0^\dagger \gamma_0$ $\gamma_\alpha^\dagger \gamma_0 \gamma_\alpha^\dagger$

$$Y = V_L^{-1} Y^d V_R$$

$$\begin{aligned} \tilde{u}_c \rightarrow \tilde{u}_R &= (A_U)_{11} \rightarrow (V_{dL} A_U V_{dR}^\dagger)_{11} = V_L \gamma_0 \gamma_0^\dagger V_L^\dagger \gamma^d + Y^d V_R \gamma_0 \gamma_0^\dagger V_R^\dagger \\ \tilde{u}_c \rightarrow \tilde{u}_p &= (M_Q A_U \oplus A_U M_U)_{11} \\ &= V_L M_Q V_L^\dagger V_L \gamma_0 \gamma_0^\dagger V_L^\dagger \gamma^d + V_L M_Q V_L^\dagger Y^d V_p \gamma_0 \gamma_0^\dagger V_R^\dagger \oplus V_R M_U V_R^\dagger \\ &= (H_1 H_2) \gamma^d \quad H_2 \gamma^d H_4 \\ &\quad H_1 \gamma^d H_3 \quad Y^d (H_3 + H_4)_{11} \end{aligned}$$