

KVik metrics

$$t := |\text{Hot Files}| / (|\text{Hot Files}| + |\text{Data File}|)$$

S_k – size of key (in bytes)

S_v – size of value (in bytes)

N – number of records in KVik

M – number of keys **Log Hash Table** can hold (capacity)

f – size of offset (in bytes)

U_w – speed of write requests

E – number of write cycles (parameter of your SSD)

F – size of SSD

$$w := S_k + 2 \cdot f$$

c – **Log Hash Table** fill factor (by default, it is assumed to be 0.9)

s – **Index Hash Table** fill factor (by default, it is assumed to be 0.6)

Assumption: key and value can be placed on one memory page

$$\text{RAF} = c \cdot M/N + (N - c \cdot M)/N \cdot (1 + 1) = 2 - c \cdot M/N$$

Assuming, requests are distributed uniformly and will hit **Log Hash Table** with probability $c \cdot M/N$.

$$\text{WAF} = 1 + 1/(c \cdot M) \cdot (2 \cdot c \cdot M) + 1/(N \cdot t) \cdot (2 \cdot N \cdot t) = 5$$

First term is write operation to **Log File** that happens every time. Second term stands for situations when **Log Hash Table** is filled and needs to be merged into **Index Hash Table** (in fact it should be better because before performing modification of **Index Hash Table** we presort all keys by hash function used in there, so ones that hit same bucket will be written using only one write operation). Since it happens once in $c \cdot M$ operations we divide write operations it takes on it to take average. Each key will have two write operations (one for key written to **Index Hash Table** and one for value written to **Hot Files**). The third term is really similar to the second one but there we need one write operation to write value to **Data File** and one more write operation to update offset value in **Index Hash Table** (actually in case of update it can be done inplace so offset can remain the same but in general case it is so).

$$\begin{aligned} \text{SAF} &= (c \cdot M \cdot (S_k + S_v) + t \cdot N \cdot (S_v + S_k) + N \cdot S_v + 1.67 \cdot N \cdot w) / (N \cdot (S_v + S_k)) = \\ &= c \cdot M/N + t + 1 - S_k/(S_v + S_k) + 1.67 \cdot (S_k + 2f)/(S_v + S_k) = \\ &= t + 1 + c \cdot M/N + 0.67 \cdot S_k/(S_v + S_k) + 3.4 \cdot f/(S_v + S_k) \end{aligned}$$

Here everything is very simple: the first term in numerator is **Log File**, the second is **Hot Files**, the third is **Data File**, the fourth is **Index Hash Table** (fill factor was determined experimentally and $0.6^{-1} = 1.(6)$).

$$\text{MO} = \frac{5 \cdot N/8 + M \cdot (S_k + f)}{N} = 5/8 + M/N \cdot (S_k + f)$$

The first term in numerator is memory that we need to store **Filter**, the second term is **Log Hash Table**.