

**Title** Adjusting for duration biases in sexual behaviour data

**Authors** Jesse Knight<sup>1,2</sup> and Sharmistha Mishra<sup>1,2</sup>

<sup>1</sup>Institute of Medical Science, University of Toronto

<sup>2</sup>MAP Centre for Urban Health Solutions, Unity Health Toronto

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**Code** [github.com/mishra-lab/duration-bias](https://github.com/mishra-lab/duration-bias)

**Abstract** Two key inputs to mathematical models of sexually transmitted infections are the average duration within epidemiological risk states (e.g., selling sex) and the average rates of sexual partnership change. These variables are often only available as aggregate estimates from published cross-sectional studies, and may be subject to distributional, sampling, censoring, and measurement biases. We explore adjustments for these biases using aggregate estimates of duration in sex work and numbers of reported sexual partners from a 2011 female sex worker survey in Eswatini. We develop adjustments from first principles, and construct Bayesian hierarchical models to reflect our mechanistic assumptions about the bias-generating processes. We show that different mechanisms of bias for duration in sex work may “cancel out” by acting in opposite directions, but that failure to consider some mechanisms could over- or underestimate duration in sex work by factors approaching 2. We also show that conventional interpretations of sexual partner numbers are biased due to implicit assumptions about partnership duration, but that unbiased estimators of partnership change rate can be defined that explicitly incorporate a given partnership duration. We highlight how the unbiased estimator is most important when the survey recall period and partnership duration are similar in length. While we explore these bias adjustments using a particular dataset, and in the context of deriving inputs for mathematical modelling, we expect that our approach and insights would be applicable to other datasets and motivations for quantifying sexual behaviour data.

**Keywords** TODO

## 1 Introduction

Epidemic modelling of sexually transmitted infections (STI) relies on quantification of sexual behaviour for model inputs (parameters) [1]. In models of STI transmission with risk heterogeneity — i.e., considering subgroups that experience differential risks — two important parameters are: the duration of time within a “risk group”, and the rate of sexual partnership change, possibly stratified by partnership type [2, 3, 4, 5]. For example, the average duration of time engaged in sex work can be used to define the modelled rate of “turnover” among sex workers [4]. Similarly, the numbers of main, casual, transactional, and/or paying sexual partners per year can be used to define the modelled rate of infection incidence [6].

Data to inform these parameters largely come from cross-sectional studies, and are often only available as crude aggregate estimates (vs individual-level data). Such estimates may be subject to distributional, sampling, censoring, and measurement biases. Our aim is therefore to explore bias adjustments for estimating:

1. duration in a risk group
2. rate of partnership change

from aggregate cross-sectional survey data, considering these factors. We explore these topics using aggregate estimates from a 2011 female sex worker survey in Eswatini [7].

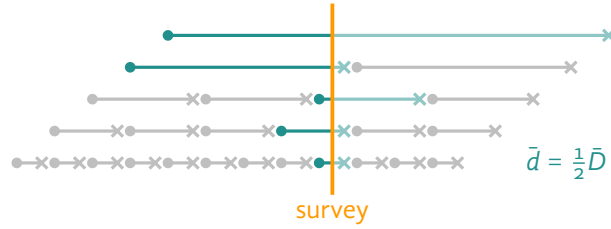
## 2 Methods

**Data Source.** Full details of the survey methodology are available in [8]. Briefly, 328 women aged 15+ who reported exchanging or selling sex for money, favors, or goods in the past 12 months were recruited via respondent-driven sampling (RDS) [9].

**Approach.** We conceptualize bias adjustments to the given data using Bayesian hierarchical models — i.e., we define explicit distributions for the unbiased data and bias-generating mechanisms, and infer the parameters of these distributions based on the available data, using Gibbs sampling [10]. Implementation details are given in Appendix A.2.

### 2.1 Duration Selling Sex

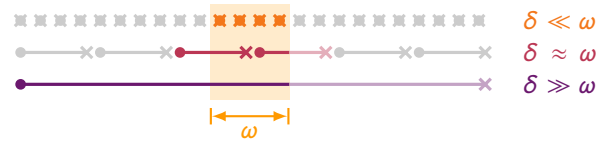
**Crude Estimates.** The survey [7] included questions about the current respondent’s age and the age of first selling sex. The difference between these ages could be used to define a crude “duration selling sex”. Using this approach, the crude median duration was  $\tilde{d} = 4$  years. However, if durations are assumed to be exponentially distributed — a implicit assumption in compartmental models [11] — then the crude mean could be estimated from the crude median as  $\bar{d} = \tilde{d}/\log(2)$  due to skewness. To move beyond crude estimates, next we develop the generative model, considering the following



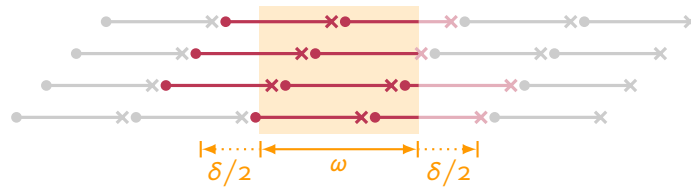
(a) Right censoring of reported durations selling sex in a steady state population



(b) Possible periods of selling sex for one individual who stopped 0, 1, or 2 times



(c) Differences in partnership duration vs recall period



(d) Fully and partially observed partnerships during a given recall period

Figure 1: Diagrams of fully observed, censored, and unobserved periods selling sex or within ongoing sexual partnerships

Guide: • : start, × : end, yellow: survey/recall period, full colour: fully observed, faded colour: right censored, grey: unobserved,  $\bar{d}$ : mean duration at survey and  $\bar{D}$ : overall,  $s$ : number of times stopped selling sex,  $g$ : relative gap length vs  $D$ ,  $\omega$ : recall period,  $\delta$ : partnership duration,  $x$ : number of reported partnerships.

potential biases.

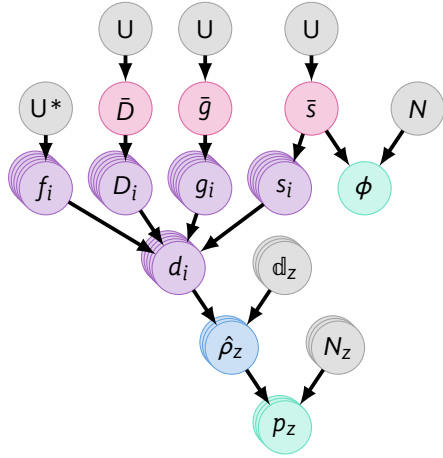
**Sampling.** Sampling bias was considered via RDS-adjustment in [7], yielding mean and 95% CI estimates of the proportions of women  $p_z$  who had sold sex starting  $d_z \in \{0-2, 3-5, 6-10, 11+\}$  years ago (Table A.1). We start by defining a model to identify distributions of reported durations  $d_i$  which are consistent with these data. We model each proportion  $p_z$  as a random variable with a beta approximation of binomial (BAB) distribution (see Appendix A.3) having parameters  $N_z$  and  $\rho_z$ . We model each  $N_z$  as a fixed value, which we fit to the 95% CI of  $p_z$  as described in § A.3. We then model each  $\rho_z$  as the proportion of reported durations  $d_i$  within the interval  $d_z$ . Since these proportions are difficult to define analytically, we estimate  $\hat{\rho}_z = \text{mean}(d_i \in d_z)$  from  $N = 100$  samples.

**Censoring.** These reported durations  $d_i$  are effectively right censored because they only capture engagement in sex work up until the survey, and not additional sex work after the survey (Figure 1a) [12]. If we assume that the survey reaches women at a random time point during their total (eventual) duration selling sex  $D_i$ , we can model this censoring via a random fraction  $f_i \sim \text{Unif}(0, 1)$ , such that  $d_i = f_i D_i$ . The expected means are then related by  $\bar{d}/\bar{D} = \bar{f} = \frac{1}{2}$ . If we believe that the sampling adjustment above does not fully account for delays in self-identifying as a sex worker [13], we could instead use  $f_i \sim \text{Unif}(1/4, 1)$ , or similar.

**Measurement.** Finally, women may not sell sex continuously. Reported durations  $d_i$  may therefore include multiple periods of selling sex with gaps in between, whereas we aim to model  $D_i$  as the durations of individual periods selling sex. Respondents in [7] were not asked whether they ever stopped selling sex, but a later survey [14] indicated that  $\phi = 45\%$  had stopped at least once. We model the number of times a woman stopped selling sex as a Poisson-distributed random variable  $s_i$  with mean  $\bar{s}$ . The expected value of  $\phi$  given  $\bar{s}$  is then  $P(s > 0) = 1 - e^{-\bar{s}}$ . Since  $\phi = 45\%$  is an imperfect observation, we model  $\phi$  as a random variable with a BAB distribution having parameters  $N = 328$  and  $\rho = 1 - e^{-\bar{s}}$ , which allows inference on  $\bar{s}$  given  $\phi$ .

Next, we update the model for reported durations as  $d_i = D_i (f_i + s_i (1 + g_i))$ , where  $g_i$  is the relative duration of gaps between selling sex, with the following rationale. If  $s_i = 0$ , then  $d_i = f_i D_i$  as before, reflecting the censored current period only. If  $s_i > 0$ , then  $d_i$  also includes  $s_i$  prior periods selling sex and the gaps between them (Figure 1b) — i.e.,  $s_i (D_i + g_i D_i) = D_i s_i (1 + g_i)$ . The major assumption we make here is that all successive periods are of equal length, and likewise for gaps between them. We must also assume a distribution for  $g_i$ , for which we choose  $g_i \sim \text{Exp}(1/\bar{g})$ , arbitrarily.

**Summary.** Figure 2a summarizes the proposed model graphically. The primary parameter of interest is the mean duration selling sex (for a given period)  $\bar{D}$ , but we must also infer the mean number of times women stop selling sex  $\bar{s}$ , and the mean relative duration of gaps  $\bar{g}$ . We assume uninformative priors for these 3 parameters.



$$p_z \sim \text{BAB}(N_z, \hat{\rho}_z) \quad (1)$$

$$\hat{\rho}_z = \text{mean}(d_i \in \mathbb{d}_z) \quad (2)$$

$$d_i = D_i(f_i + s_i(1 + g_i)) \quad (3)$$

$$D_i \sim \text{Exp}(1/\bar{D}) \quad (4)$$

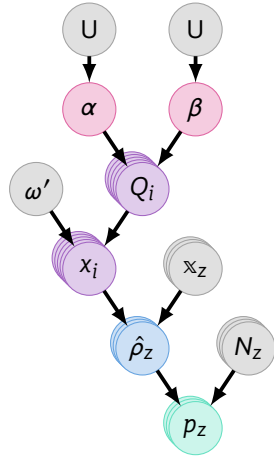
$$f_i \sim \text{Unif}(0, 1) \quad (5)$$

$$s_i \sim \text{Pois}(\bar{s}) \quad (6)$$

$$g_i \sim \text{Exp}(1/\bar{g}) \quad (7)$$

$$\phi \sim \text{BAB}(N, 1 - e^{-\bar{s}}) \quad (8)$$

(a) Duration selling sex



$$p_z \sim \text{BAB}(N_z, \hat{\rho}_z) \quad (9)$$

$$\hat{\rho}_z = \text{mean}(x_i \in \mathbb{x}_z) \quad (10)$$

$$x_i \sim \text{Pois}(Q_i \omega') \quad (11)$$

$$Q_i \sim \text{Gamma}(\alpha, \beta) \quad (12)$$

(b) Rates of partnership change

Figure 2: Graphical models

TODO

## 2.2 Rates of Partnership Change

**Data & Assumptions.** The survey [7] also asked respondents to report their numbers of sexual partners ( $x$ ) in a recall period ( $\omega$ ) of 30 days. Numbers were stratified by three types of partner: new paying clients, regular paying clients, and non-paying partners. We assume that only a small proportion of new clients go on to become regular clients; thus, we conceptualize “new” clients as effectively “one-off” clients.<sup>1</sup> Since no survey questions asked about partnership durations ( $\delta$ ), we further assume that these were: 1 day with new paying clients, 4 months with regular paying clients, and 3 years with non-paying partners. We now develop the generative model to estimate the expected rate of partnership change for each type, considering the following potential biases.

**Sampling.** As before, [7] estimates RDS-adjusted proportions of respondents  $p_z$  (mean, 95% CI) reporting different numbers/ranges of partners  $x_z$  in the past 30 days (Table A.1). Thus, we take the same approach as in § 2.1 to identify distributions of reported partner numbers  $x_i$  which are consistent with the data for each partnership type.

**Interpretation.** Numbers of reported partners ( $x$ ) have generally been interpreted in two ways —  $x/\omega$  as the *rate* of partnership change ( $Q$ ) or  $x$  as the *number* of current partners ( $K$ ):

$$Q \approx \frac{x}{\omega} \quad (13a)$$

or

$$K \approx x \quad (13b)$$

Both interpretations are reasonable under certain conditions: If partnership duration is short and the recall period is long ( $\delta \ll \omega$ ), then reported partnerships mostly reflect *complete* partnerships, and thus  $x/\omega \approx Q$ . If partnership duration is long and the recall period is short ( $\delta \gg \omega$ ), then reported partnerships mostly reflect *ongoing* partnerships, and thus  $x \approx K$ . However, if partnership duration and recall period are similar in length ( $\delta \approx \omega$ ), then reported partnerships reflect a mixture of tail-ends, complete, and ongoing partnerships, and thus  $x/\omega$  overestimates  $Q$ , but  $x$  also overestimates  $K$ . These three cases are illustrated in Figure 1c.

To adjust for this bias, we again assume that survey/recall period timing is effectively random. Then, if the *end* of the recall period would intersect an ongoing partnership, the intersection point would be, on average, half-way through the partnership. The same goes for the *start* of the recall period. Thus, the recall period is effectively extended by half the partnership duration  $\delta/2$  on each end, and  $\delta$  overall, as illustrated in Figure 1d. We can therefore define unbiased estimators of  $Q$  and  $K$  as:

$$Q = \frac{x}{\omega + \delta} \quad (14a)$$

$$K = \frac{x\delta}{\omega + \delta} = Q\delta \quad (14b)$$

<sup>1</sup> The number of new clients per recall period could also be used to define a rate of partnership change [12], but we do not explore this approach here.

Returning to the generative model, we sample the true rate of partnership change from an assumed distribution  $Q_i \sim \text{Gamma}(\alpha, \beta)$ , with unknown parameters  $\alpha, \beta$ . Then, we model the numbers of reported partners  $x_i$  given  $Q_i$  and  $\omega' = (\omega + \delta)$  as:  $x_i \sim \text{Poi}(Q \omega')$ .

**Summary.** Figure 2b summarizes the proposed model graphically. The primary parameters of interest are  $\alpha, \beta$ , which govern the distribution of rates of partnership change (for a given type)  $Q$ . We assume uninformative priors for these 2 parameters.

**Comparing Assumptions.** In order to quantify the influence of using the biased vs unbiased estimators of  $Q$  and  $K$ , we fit the proposed model for each partnership type under three assumptions: assuming *short* partnerships as in (13a) with  $\omega' = \omega$ ; assuming *long* partnerships as in (13b) with  $\omega' = \delta$ ; and *no* assumption on partnership duration as in (14) with  $\omega' = \omega + \delta$ . To illustrate more general trends in the magnitude of bias, we further compared biased vs unbiased estimates of  $Q$  and  $K$  across a range of different partnership durations  $\delta \in [0.1, 10]$  and recall periods  $\omega \in [0.1, 10]$ , with fixed true rate  $Q = 1$  (arbitrary units).

## 3 Results

### 3.1 Risk Group Duration

Figure A.1 illustrates the distributions of observed proportions  $p_z$  vs inferred proportions  $\hat{p}_z$  of women reporting durations  $d_i \in \mathbb{d}_z$  selling sex, following each stage of adjustment outlined in § 2.1. Figure 3 illustrates the estimated cumulative distributions for years selling sex following each stage of adjustment, while Table A.2 provides the corresponding distribution means  $\bar{D}$  and 95% CI. Ironically, the final estimate of 4.06 (2.29, 6.34) is similar to the original median of 4, as each adjustment alternates between increasing and decreasing  $\bar{D}$ . The censoring adjustment yields the largest increase, while the measurement adjustment yields the largest decrease.

### 3.2 Rates of Partnership Change

Figure A.2 illustrates the distributions of observed proportions  $p_z$  vs inferred proportions  $\hat{p}_z$  of women reporting  $x_i \in \mathbb{x}_z$  partners in the past 30 days, under the three partnership duration assumptions. Figure 4 illustrates the inferred rates of partnership change ( $Q$ ) and numbers of current partners ( $K$ ) under each assumption, while Table A.3 provides the corresponding means and 95% CI. The biased estimates of  $Q$  and  $K$  appear equal because  $Q$  is defined as per-month. Biases are strongest for  $Q$  with long partnerships (e.g., non-paying partners) and  $K$  with short partnership (e.g., new clients). However, biases are also substantial for both  $Q$  and  $K$  with “medium-length” partnerships (e.g., regular clients). Figure 5 illustrates generalized trends in these biases.

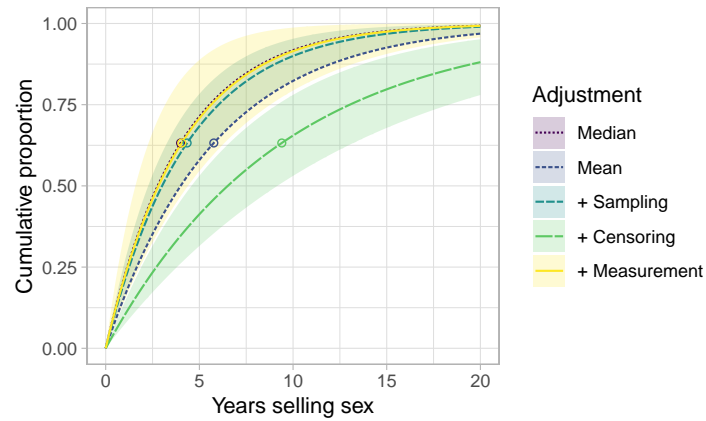


Figure 3: Estimated cumulative distribution for years selling sex following stages of adjustment

Guide: lines: cumulative distribution under posterior mean, shaded ribbon: 95% CI, circles: posterior mean.

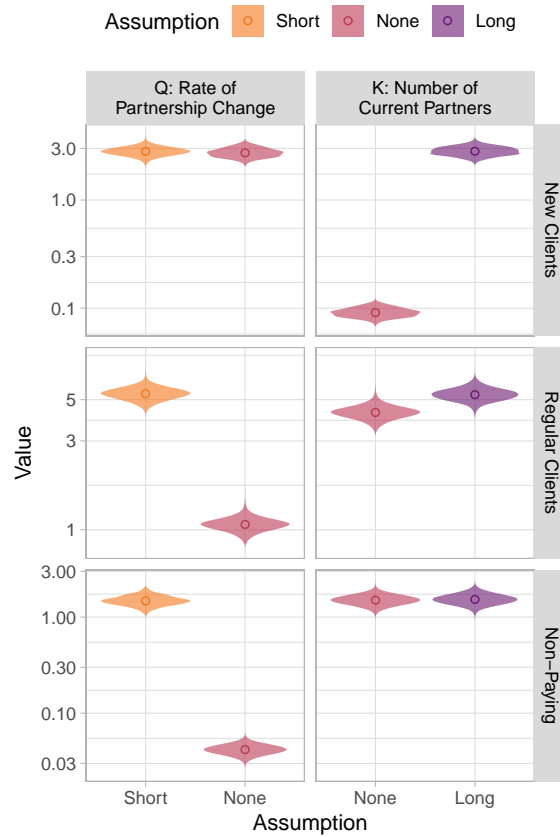


Figure 4: Estimates of rates of partnership change and numbers of current partners under different partnership duration assumptions for three partnership types reported by female sex workers

Guide: circles: posterior mean, shaded area: posterior distribution. Rates are per-month.



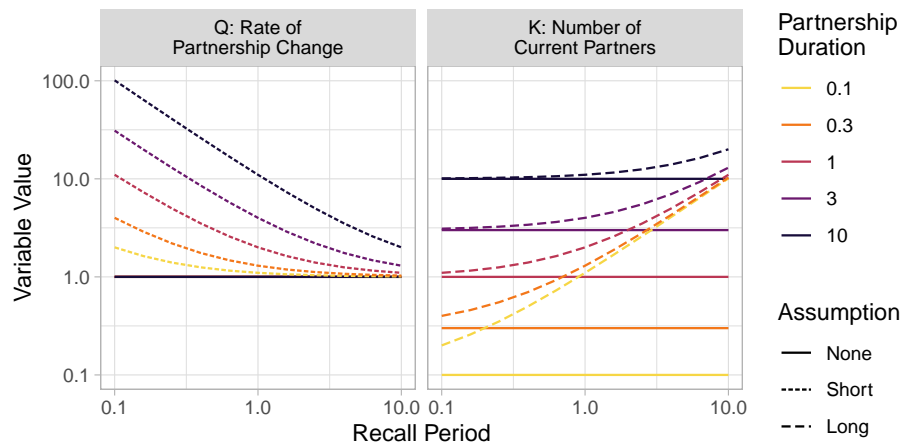


Figure 5: Estimates of rates of partnership change and numbers of current partners under different partnership duration assumptions for different recall periods and partnership durations

Units are arbitrary.

## 4 Discussion

[TODO]

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## **Appendix**

**Title** Adjusting for duration biases in sexual behaviour data

**Authors** Jesse Knight<sup>1,2</sup> and Sharmistha Mishra<sup>1,2</sup>

<sup>1</sup>Institute of Medical Science, University of Toronto

<sup>2</sup>MAP Centre for Urban Health Solutions, Unity Health Toronto

**Date** July 20, 2023

## A Supplement

### A.1 Source Data

Table A.1 gives the RDS-adjusted data from [1].

Table A.1: RDS-adjusted proportions for variables of interest

| Variable                         | Stratum | Mean | (95% CI)     |
|----------------------------------|---------|------|--------------|
| Years selling sex                | 0–2     | 38.3 | (27.5, 49.1) |
|                                  | 3–5     | 32.1 | (23.6, 40.7) |
|                                  | 6–10    | 20.2 | (13.2, 27.1) |
|                                  | 11+     | 9.4  | (04.4, 14.4) |
| New clients <sup>a</sup>         | 0–1     | 16.4 | (09.8, 23.0) |
|                                  | 2       | 43.4 | (33.3, 53.5) |
|                                  | 3       | 15.2 | (09.6, 20.9) |
|                                  | 4       | 13.1 | (07.0, 19.2) |
|                                  | 5       | 11.8 | (06.0, 17.6) |
| Regular clients <sup>a</sup>     | 0–1     | 10.0 | (01.9, 18.1) |
|                                  | 2       | 8.5  | (03.2, 13.8) |
|                                  | 3       | 15.9 | (09.8, 21.9) |
|                                  | 4       | 10.0 | (04.5, 15.6) |
|                                  | 5       | 8.1  | (03.8, 12.3) |
|                                  | 6       | 10.7 | (05.8, 15.5) |
|                                  | 7+      | 36.9 | (26.4, 47.3) |
| Non-paying partners <sup>a</sup> | 0       | 12.5 | (04.8, 20.1) |
|                                  | 1       | 50.8 | (42.9, 58.7) |
|                                  | 2       | 23.6 | (16.8, 30.3) |
|                                  | 3+      | 13.2 | (07.2, 19.1) |

<sup>a</sup> Number reported in the past 30 days. Data from [1].

### A.2 Code

All analysis code is available online at: [github.com/mishra-lab/duration-bias](https://github.com/mishra-lab/duration-bias). We fit the generative models using rjags: [cran.r-project.org/package=rjags](https://cran.r-project.org/package=rjags), with 1000 adaptive iterations and 100,000 sampling iterations.

### A.3 Beta Approximation of the Binomial Distribution

The distributions of RDS-adjusted variables in [1] were reported as adjusted proportions (mean, 95% CI) for different variable value strata. For each proportion, we defined a beta approximation of

the binomial (BAB) distribution:

$$P(\rho) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} \rho^{\alpha-1}(1-\rho)^{\beta-1} \quad (\text{A.1})$$

$$\approx \binom{N}{n} \rho^n (1-\rho)^{N-n}$$

with  $\alpha = N\rho$  and  $\beta = N(1 - \rho)$ . We fixed  $\rho$  as the adjusted point estimate, and estimated  $N$  by minimizing the sum of squared differences between the 95% quantiles of (A.1) given  $N$  and the reported 95% CI for the adjusted proportion.

#### A.4 Risk Group Duration

**Fitting to RDS-Adjusted Proportions.** Figure A.1 illustrates the observed vs inferred proportions of women reporting different durations selling sex, following each stage of adjustment outlined in § 2.1.

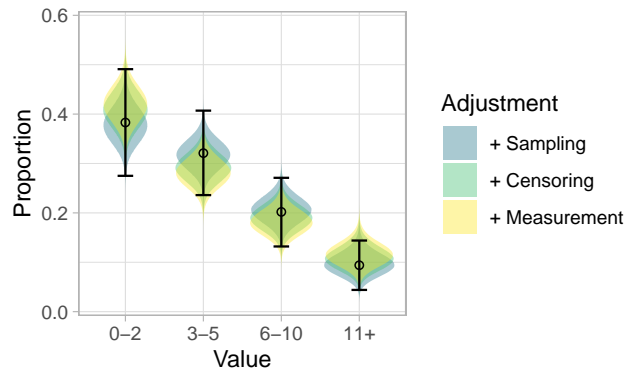


Figure A.1: Proportions of women reporting different durations selling sex: observed (points and ranges) vs inferred posterior (coloured regions) after 3 stages of adjustment

**Numeric Summary.** Table A.2 summarizes the estimated exponential distribution means (95% CI) for years selling sex following each stage of adjustment outlined in § 2.1.

Table A.2: Estimated mean durations selling sex (years) following each stage of adjustment

| Adjustment    | Mean | (95% CI)      |
|---------------|------|---------------|
| Median        | 4.00 | —             |
| Mean          | 5.77 | —             |
| + Sampling    | 4.35 | (3.27, 5.72)  |
| + Censoring   | 9.40 | (6.60, 13.22) |
| + Measurement | 4.06 | (2.29, 6.34)  |

## A.5 Rate of Partnership Change

**Fitting to RDS-Adjusted Proportions.** Figure A.2 illustrates the observed vs inferred proportions of women reporting different numbers of partners in the past 30 days, under each partnership duration assumption outlined in § 2.2.

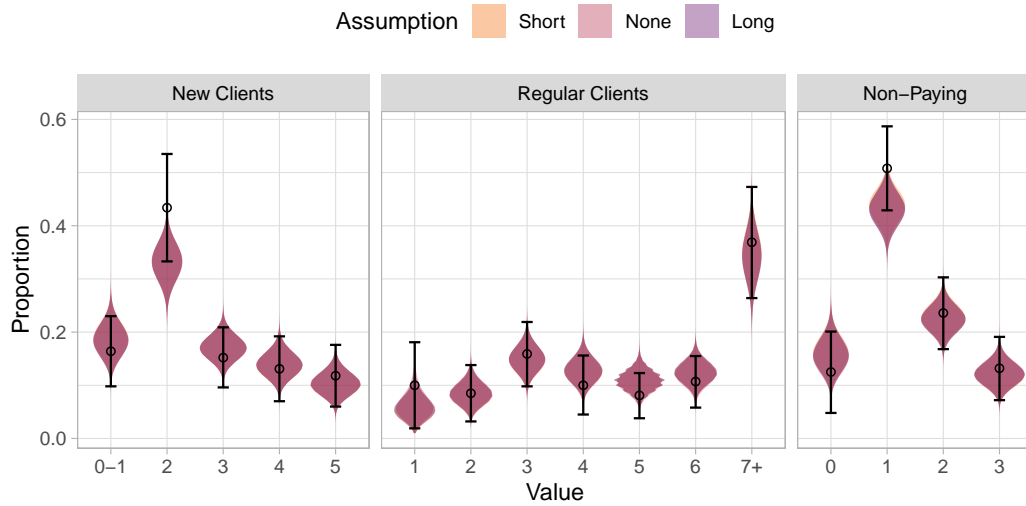


Figure A.2: Proportions of women reporting different numbers of partner in the past 30 days: observed (points and ranges) vs inferred posterior (coloured regions) under different partnership duration assumptions

**Numeric Summary.** Table A.3 summarizes the means (95% CI) for rates of partnership change and numbers of current partners estimated under each partnership duration assumption outlined in § 2.2.

Table A.3: Biased vs unbiased estimates of rates of partnership change and numbers of current partners for three partnership types

| Partnership Type | Bias <sup>b</sup> | Rate $Q^a$ |              | Number $K$ |              |
|------------------|-------------------|------------|--------------|------------|--------------|
|                  |                   | Mean       | (95% CI)     | Mean       | (95% CI)     |
| New Clients      | Biased            | 2.82       | (2.33, 3.35) | 2.84       | (2.36, 3.37) |
|                  | Unbiased          | 2.75       | (2.29, 3.31) | 0.09       | (0.08, 0.11) |
| Regular Clients  | Biased            | 5.38       | (4.60, 6.20) | 5.33       | (4.57, 6.19) |
|                  | Unbiased          | 1.07       | (0.90, 1.25) | 4.28       | (3.62, 5.02) |
| Non-Paying       | Biased            | 1.49       | (1.17, 1.86) | 1.54       | (1.20, 1.95) |
|                  | Unbiased          | 0.04       | (0.03, 0.05) | 1.51       | (1.18, 1.88) |

<sup>a</sup> Rates are per-month; <sup>b</sup> biased  $Q$  assume short partnerships as in (13a); biased  $K$  assume long partnerships as in (13b).

## References

- [1] Stefan Baral et al. "Reconceptualizing the HIV epidemiology and prevention needs of female sex workers (FSW) in Swaziland". In: *PLOS ONE* 9.12 (Dec. 22, 2014), e115465. <http://doi.org/10.1371/journal.pone.0115465>.