

Title: Risk heterogeneity in compartmental HIV transmission models of ART as prevention in Sub-Saharan Africa: A scoping review

Running Head: Heterogeneity in HIV transmission models

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Date: July 7, 2022

Journal: Epidemics (accepted)

Funding: The study was supported by the Natural Sciences and Engineering Research Council of Canada (NSERC CGS-D); Ontario Early Researcher Award No. ER17-13-043; and the Canadian Institutes of Health Research Foundation Grant (FN-13455).

Conflicts of Interest: None declared.

Words: 3753

RISK HETEROGENEITY IN COMPARTMENTAL HIV TRANSMISSION MODELS OF ART AS PREVENTION IN
SUB-SAHARAN AFRICA: A SCOPING REVIEW

Abstract

Background. Transmission models provide complementary evidence to clinical trials about the potential population-level incidence reduction attributable to ART (ART prevention impact). Different modelling assumptions about risk heterogeneity may influence projected ART prevention impacts. We sought to review representations of risk heterogeneity in compartmental HIV transmission models applied to project ART prevention impacts in Sub-Saharan Africa. **Methods.** We systematically reviewed studies published before January 2020 that used non-linear compartmental models of sexual HIV transmission to simulate ART prevention impacts in Sub-Saharan Africa. We summarized data on model structure/assumptions (factors) related to risk and intervention heterogeneity, and explored multivariate ecological associations of ART prevention impacts with modelled factors. **Results.** Of 1384 search hits, 94 studies were included. 64 studies considered sexual activity stratification and 39 modelled at least one key population. 21 studies modelled faster/slower ART cascade transitions (HIV diagnosis, ART initiation, or cessation) by risk group, including 8 with faster and 4 with slower cascade transitions among key populations versus the wider population. In ecological analysis of 125 scenarios from 40 studies (subset without combination intervention), scenarios with risk heterogeneity that included turnover of higher risk groups were associated with smaller ART prevention benefits. Modelled differences in ART cascade across risk groups also influenced the projected ART benefits, including: ART prioritized to key populations was associated with larger ART prevention benefits. Of note, zero of these 125 scenarios considered lower ART coverage among key populations. **Conclusion.** Among compartmental transmission models applied to project ART prevention impacts in Sub-Saharan Africa, representations of risk heterogeneity and projected impacts varied considerably. Inclusion/exclusion of risk heterogeneity with turnover, and intervention heterogeneity across risk groups could influence the projected impacts of ART scale-up. These findings highlight a need to capture risk heterogeneity with turnover and cascade heterogeneity when projecting ART prevention impacts.

Words: 296

Keywords: HIV, Mathematical Model, Computer Simulation, Antiretroviral Therapy, Population Heterogeneity, Risk Factors, Healthcare Disparities

1 Introduction

As of 2019, two thirds (25.7 million) of all people living with HIV globally were in Sub-Saharan Africa (SSA), where an estimated one million new HIV infections were acquired in 2019 [1]. In SSA and elsewhere, HIV treatment via antiretroviral therapy (ART) remains a key element of combination HIV prevention [2].

Eligibility to initiate ART has seen continued expansion over the years — i.e. earlier and earlier initiation during HIV disease — following evidence of individual-level health benefits [3, 4] and partner-level prevention benefits [5, 6]. Expansion cumulated with the current recommendation of immediate ART following HIV diagnosis, or “universal test-and-treat” [2]. Parallel to ART expansion, interest has grown in estimating the population-level prevention benefits of ART, via both model-based studies [7, 8, 9, 10] and recent large-scale community-based trials [11, 12, 13]. Mixed results from these trials [11, 12, 13] have renewed interest in understanding potential determinants of population-level ART prevention benefits [14, 15].

Risk heterogeneity is a well-established determinant of HIV epidemic emergence and persistence [16, 17]. Such heterogeneity is defined by various factors affecting acquisition and onward transmission risk. Systematic model comparison studies have found that projected prevention impacts of ART scale-up were smaller when more heterogeneity was captured in the model [18, 19]. Moreover, populations experiencing barriers to viral suppression may be at highest risk for acquisition and onward transmission, including key populations such as women and men who sell sex, and men who have sex with men [20, 21]. Data also suggest that subgroups not formally described as key populations, such as youth, men who have sex with women, including clients of sex workers, may also experience barriers to engagement in ART care [22, 23, 24]. Indeed, data suggest that ART scale-up in practice has not reached subgroups equally [25].

Given the critical role of transmission modelling in estimating the prevention impacts of ART [8, 9], we sought to examine how heterogeneity in risk and ART uptake has been represented in mathematical models used to assess the prevention impacts of ART scale-up in SSA. We conducted a scoping review and ecological regression with the following objectives. Among non-linear compartmental models of sexual HIV transmission used to simulate the prevention impacts of ART in SSA:

1. In which epidemic contexts (geographies, populations, epidemic phases) have these models been applied?
2. How was the model structured to represent key factors of risk heterogeneity?
3. What are the potential influences of representations of risk heterogeneity on the projected prevention benefits of ART in the overall population?

2 Methods

We conducted a scoping review according to the PRISMA extension for scoping reviews (Appendix D).

2.1 Conceptual Framework for Risk Heterogeneity

We defined “factors of risk heterogeneity” as epidemiological phenomena and stratifications of populations, rates, or probabilities which may/not be included in transmission models. We defined 4 domains in which such factors might influence the transmission impact of ART:

- **Biological Effects:** differential transmission risk within HIV disease course that may coincide with differential ART coverage [26]
- **Behaviour Change Effects:** differential transmission risk due to behavioural changes related to engagement in the ART cascade [27, 28]
- **Network Effects:** differential transmission risk within sub-populations that increases the challenge of epidemic control through core group dynamics [17, 29, 30]
- **Cascade Effects:** differential transmission risk within sub-populations who experience barriers to ART care and achieving viral suppression, such as youth and key populations [31, 32, 20, 25]

We then compiled a list of key factors of risk heterogeneity, and their possible mechanisms of influence on ART prevention impact (Table 1).

2.2 Search

We searched MEDLINE and EMBASE via Ovid using search terms related to Sub-Saharan Africa (SSA), HIV, and transmission modelling (Table A.1). Search results were de-duplicated and screened by title and abstract in Covidence [43], followed by full-text screening using the criteria below. One reviewer (JK) conducted the search, screening, and data extraction.

2.2.1 Inclusion/Exclusion Criteria

Table A.2 lists complete inclusion/exclusion criteria and related definitions. We included peer-reviewed, primary modelling studies that used non-linear compartmental models of sexual HIV transmission to project the prevention impacts of ART in any setting within SSA. We included studies published in English anytime before Jan 1, 2020, that simulated at least one scenario with increasing ART coverage, possibly alongside

Table 1: Factors of heterogeneity in HIV transmission and their possible mechanisms of influence on the prevention impact of ART interventions

Factor	MP ^a	Definition	Possible mechanism(s) of influence on ART prevention impact
Acute Infection	β_i	Increased infectiousness immediately following infection [33, 34]	Biological: transmissions during acute infection are unlikely to be prevented by ART
Late-Stage Infection	β_i	Increased infectiousness during late-stage infection [33, 34]	Biological: transmissions during late-stage are more likely to be prevented by ART
Drug Resistance	β_i	Transmitted factor that requires regimen switch to achieve viral suppression [35]	Biological: transmissions during longer delay to achieving viral suppression will not be prevented by ART
HIV Morbidity	$c; \eta$	Reduced sexual activity during late-stage disease [36, 37]	Behaviour Change: reduced morbidity via ART could increase HIV prevalence among the sexually active population
HIV Counselling	$c; \eta; \kappa$	Reduced sexual activity and/or increased condom use after HIV diagnosis [28]	Behaviour Change: increased HIV testing with ART scale up can contribute to prevention even before viral suppression is achieved
Activity Groups	$c; \kappa$	Any stratification by rate of partnership formation [38]	Network: higher transmission risk among higher activity
Age Groups	$c; \kappa$	Any stratification by age	Network & Cascade: higher transmission risk and barriers to viral suppression among youth [39, 25]
Key Populations	$c; \kappa$	Any epidemiologically defined higher risk groups [40]	Network & Cascade: higher transmission risk and barriers to viral suppression among key populations [20]
Group Turnover	ϕ	Individuals move between activity groups and/or key populations reflecting sexual lifecourse [29]	Network & Cascade: counteract effect of stratification due to shorter periods in higher risk [41]; viral suppression may be achieved only after periods of higher risk
Assortative Mixing	m	Any degree of assortative mixing (like-with-like) by age, activity, and/or key populations	Network: assortative sexual networks compound effect of stratification [38]
Partnership Types	$\eta; \kappa$	Different partnership types are simulated, with different numbers of sex acts and/or condom usage [42]	Network: longer duration and lower condom use among main versus casual/sex work partnerships counteracts effect of stratification
ART Cascade Gaps	$\tau; \alpha$	Slower ART cascade transitions among higher activity groups or key populations [20, 25]	Cascade: ART prevention benefits may be allocated differentially among risk groups

^a MP: Model Parameters — β_i, β_s : transmission probability per act (infectiousness, susceptibility); η : number of sex acts of each type per partnership; κ : proportion of sex acts unprotected by a condom; c : partnership formation rate; m : mixing matrix (probability of partnership formation); μ : mortality rate; v : entry rate; ϕ : internal turnover between activity groups; τ : testing rate; α : ART initiation rate (and retention-related factors).

other interventions. The included studies formed Dataset A, used to complete objectives 1 and 2. A subset of Dataset A formed Dataset B, used to complete objective 3. Studies in Dataset B met three additional criteria: 1) examined scale-up of ART coverage alone (versus combination intervention); 2) examined ART intervention for the whole population (versus ART prioritized to subgroups); and 3) reported HIV incidence reduction and/or cumulative HIV infections averted relative to a base-case scenario reflecting status quo.

2.3 Data Extraction

Data extraction used the full text and all available supplementary material. Data were extracted per-study for objectives 1 and 2, and per-scenario for objective 3, possibly including multiple time horizons. Detailed variables definitions are given in Appendix B.

2.3.1 Epidemic Context

For objective 1, we extracted data on geography, epidemic phase, and key populations explicitly considered in the model. We categorized studies by country, SSA region, and scale of the simulated population (city, sub-national, national, regional). We classified epidemic size at time of ART intervention using overall HIV prevalence (low: $<1\%$, medium: $1-10\%$, high: $>10\%$), and epidemic phase using overall HIV incidence trend (increasing, increasing-but-stabilizing, stable/equilibrium, decreasing-but-stabilizing, and decreasing).

We extracted whether any of the following key populations were modelled: female sex workers (FSW); male clients of FSW (Clients); men who have sex with men (MSM); transgender individuals; people who inject drugs (PWID); and prisoners. FSW were defined as any female activity group meeting 3 criteria: $<5\%$ of the female population; $<1/3$ the client population size; and having $>50\times$ the partners per year of the lowest sexually active female activity group [44, 42]. Clients were defined as any male activity group described as clients of FSW, and being $>3\times$ the FSW population size. We also extracted whether any groups in the model were described as MSM, transgender, PWID, or prisoners.

2.3.2 Factors of Risk Heterogeneity

For objective 2, we examined if/how the factors of risk heterogeneity outlined in Table 1 were simulated in each study. We examined the number of *risk groups* defined by sex/gender and/or sexual activity, and any *turnover* of individuals between activity groups and/or key populations.

We classified how *partnership types* were defined: generic (all partnerships equal); based only on the activity groups involved; or overlapping, such that different partnership types could be formed between the same two activity groups. We extracted whether partnerships considered different numbers of sex acts and condom

use, and whether models simulated any degree of assortative *mixing* by activity groups (preference for like-with-like) versus proportionate (random) mixing. The number of *age groups* was extracted, and whether *mixing* by age groups was proportionate, strictly assortative, or assortative with age differences. We extracted whether age conferred any transmission risk beyond mixing, such as different partnership formation rates.

Finally, we extracted whether rates of HIV diagnosis, ART initiation, and/or ART discontinuation differed across risk strata (sex/gender, activity, key populations, and/or age), and if so, how they differed.

2.3.3 Prevention Impact of ART Scale-Up

For objective 3, we extracted the following data for each intervention scenario within Dataset B: the years that ART scale-up started (t_o) and stopped (t_f); the final overall ART coverage achieved and/or the final ART initiation rate (per person-year among PLHIV not yet in care); the criteria for ART initiation (e.g. CD4 count); and the relative reduction in transmission probability on ART. Then, we extracted the relative reduction in incidence and/or proportion of infections averted relative to the base-case scenario for available time horizons since t_o .

We conducted an ecological analyses across all modelled scenarios to examine the relationship between factors of risk heterogeneity and projected ART impacts, adjusting for other factors that could influence impacts. For each factor of risk heterogeneity, we compared projected ART impacts (incidence reduction/infections averted) across different factor levels (whether or not, and how the factor was modelled). We estimated the effect of each factor level on ART impacts using linear multivariate regression, with generalized estimating equations [45] to control for clustering due to multiple estimates per study/scenario. Time since t_o was included as a covariate, and two variables were removed due to missingness. No variable selection was used to avoid biasing effect estimates [46]. We also plotted impacts versus time since t_o , stratified by factor levels.

3 Results

The search yielded 1 384 publications, of which 94 studies were included (Figure 1). These studies (Dataset A, Appendix A.3) applied non-linear compartmental modelling to simulate ART scale-up in SSA, of which 40 reported infections averted/incidence reduction due to population-wide ART scale-up without combination intervention, relative to a base-case reflecting status quo (Dataset B).

3.1 Epidemic Context

Table 2 summarizes key features of contexts within SSA where the prevention impacts of ART have been modelled. 61 studies modelled HIV transmission at the national level; studies also explored regional (1), sub-

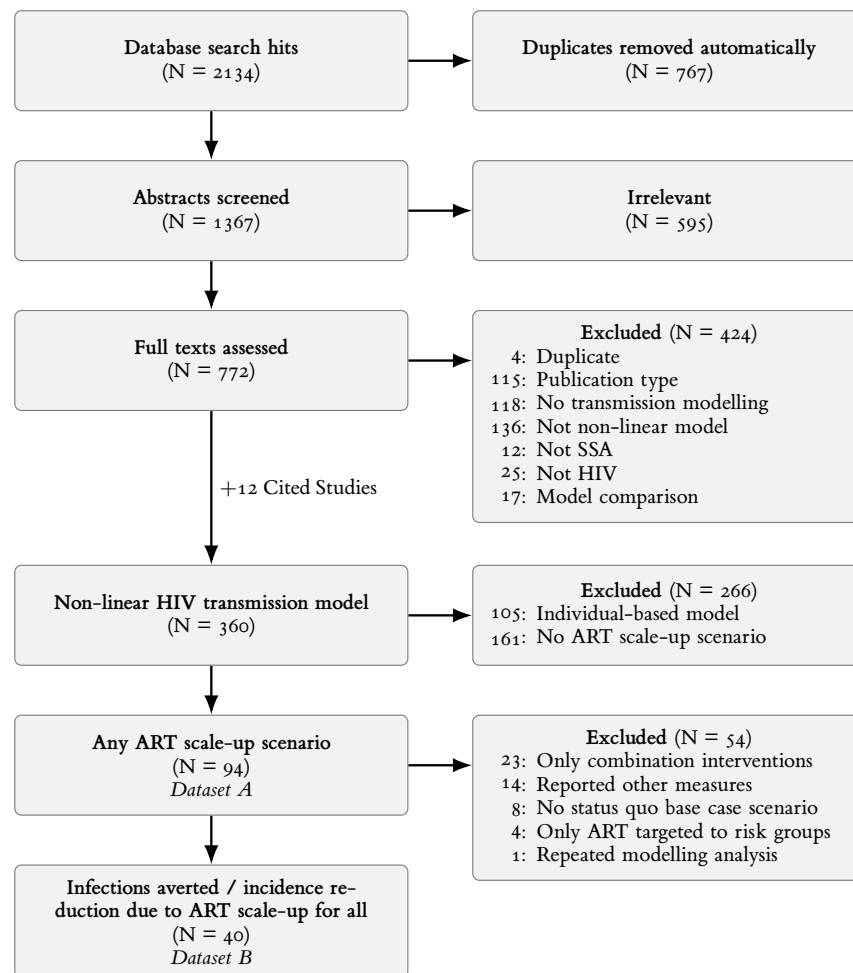


Figure 1: PRISMA flowchart of study identification

national (16), and city-level (16) epidemic scales. South Africa was the most common country simulated (52 studies); Figure C.1 illustrates the number of studies by country. East Africa was the most represented SSA region, being simulated in 77 studies, followed by Southern (72), West (28), and Central Africa (13).

ART prevention impacts were most often modelled in high-prevalence ($>10\%$) epidemics (41 studies) and medium-prevalence (1–10%) epidemics (23) (Figure C.2). No studies reported overall HIV prevalence of $<1\%$ at time of intervention, although for 30 studies, HIV prevalence was not reported or varied across simulated contexts/scenarios. The median [min, (IQR), max] year of intervention was 2014 [1990, (2010, 2015), 2040]; at which time HIV prevalence (%) was 15 [2, (6, 19), 32] (Figure C.2); and incidence (per 1000 person-years) was 14 [1, (9, 20), 50] (Figure C.3). Most reported incidence trends were decreasing or stable (45 of 48 reporting, Figure C.4).

3.1.1 Key Populations

FSW were explicitly modelled in 39 studies. Among these (of studies where it was possible to evaluate): 21 (of 25) were $<5\%$ of the female population; 14 (of 24) were $<1/3$ the size of the client population; and 15 (of 22) had $>50\times$ partners per year versus the lowest sexually active female activity group. Clients of FSW were modelled as a unique group in 31 studies, among which 8 (of 17 reporting) were $>3\times$ the size of the FSW population. In another 8 studies, clients were defined as a proportion of another group, among which 6 (of 7) were $>3\times$ the FSW population size. Studies explicitly modelled men who have sex with men (MSM) in 28 studies; transgender in 0; people who inject drugs (PWID) in 11; and prisoners in 2.

3.2 Heterogeneity Factors

3.2.1 Biological Effects

The median [min, (IQR), max] number of states used to represent HIV disease (ignoring treatment-related stratifications) was 5 [1, (3, 6), 25] (Figure C.5), and 2 studies represented HIV along a continuous dimension using partial differential equations. States of increased infectiousness associated with acute infection and late-stage disease were simulated in 68 and 74 studies, respectively.

The relative risk of HIV transmission on ART was 0.08 [0, (0.04, 0.13), 0.3] (Figure C.6), representing an average “on-treatment” state in 78 studies, versus a “virally suppressed” state in 15. Treatment failure due to drug resistance was simulated in 24 studies, including: 23 where individuals experiencing treatment failure were tracked separately from ART-naïve; and 1 where such individuals transitioned back to a generic “off-treatment” state. Another 6 studies included a similar transition that was not identified as treatment failure versus ART cessation. Transmissible drug resistance was simulated in 9 studies.

Table 2: Summary of epidemic contexts within Sub-Saharan Africa where the prevention impacts of ART have been modelled

Study Characteristic		Studies
Geographic scale	Regional	1
	National	61
	Sub-national	16
	City	16
Modelled countries ^a	South Africa	52
	Kenya	22
	Zambia	10
	Other	29
HIV prevalence	Low (<1%)	0
	Mid (1-10%)	23
	High (>10%)	41
	Unclear/Varies	30
Incidence trend at scenario divergence	Decreasing	10
	Dec-to-stable	24
	Stable	11
	Inc-to-stable	1
	Increasing	2
	Unclear/Varies	46
Key populations included	FSW ^b	39
	Clients ^c	31
	MSM	28
	Transgender	0
	PWID	11
	Prisoners	2

Total studies: 94. FSW: female sex workers; Clients: clients of sex workers; MSM: men who have sex with men; PWID: people who inject drugs. ^a Does not sum to 94 as some studies modelled multiple countries. ^b Groups described as FSW, not considering the epidemiological definitions given in Appendix B.2.1. ^c Likewise for clients, and excluding studies where clients were modelled as a proportion of another risk group.

3.2.2 Behavioural Effects

Reduced sexual activity during late-stage HIV was simulated in 25 studies, including at least one state with: complete cessation of sexual activity (14); reduced rate/number of partnerships (9); and/or reduced rate/number of sex acts per partnership (6).

Separate health states representing diagnosed HIV before treatment, and on-treatment before viral suppression were simulated in 30 and 17 studies, respectively. 22 studies modelled behaviour changes following awareness of HIV+ status, including: increased condom use (12); fewer partners per year (4); fewer sex acts per partnership (3); serosorting (1); and/or a generic reduction in transmission probability (8).

ART cessation was simulated in 35 studies, including: 16 where individuals no longer on ART were tracked separately from ART-naïve; and 19 where such individuals transitioned back to a generic “off-treatment” state. Another 6 studies included a similar transition that was not identified as treatment failure versus ART cessation.

3.2.3 Network Effects

Populations were stratified by activity (different rates and/or types of partnerships formed) in 59 studies, and by sex/gender in 64. The number of groups defined by sex/gender and/or activity was 6 [1, (2, 9), 19] (Figure C.7); and by activity alone (maximum number of groups among: women who have sex with men, men who have sex with women, MSM, or overall if sex/gender was not considered) was 3 [1, (1, 3), 18]. The highest activity groups for females and males (possibly including FSW/clients) comprised 2 [< 1 , (2, 4), 23] and 9 [< 1 , (2, 14), 35] % of female and male populations, respectively (Figures C.9 and C.10).

Turnover between activity groups and/or key populations was considered in 28 studies, of which 9 considered turnover of only one specific high-activity group or key population. Another 7 studies simulated movement only from lower to higher activity groups to re-balance group sizes against disproportionate HIV mortality.

Among 59 studies with activity groups, sexual mixing was modelled as assortative in 57 and proportionate in 2. Partnerships had equal probability of transmission in 39 studies, including all studies without activity groups. Partnerships were defined by the activity groups involved in 44 studies, among which transmission was usually lower in high-with-high activity partnerships than in low-with-low, due to fewer sex acts (31) and/or increased condom use (23). Transmission risk in high-with-low activity partnerships was defined by the: susceptible partner (9); lower activity partner (11); higher activity partner (3); or both partners' activity groups (15); yielding indeterminate, higher, lower, or intermediate per-partnership transmission risk, respectively. Partnerships were defined based on overlapping types, such that different partnership

types could be formed between the same two activity groups in 11 studies. All overlapping partnership types had differential total sex acts and condom use.

Age groups were simulated in 32 studies, among which, the number of age groups was 10 [2, (4, 34), 91] (Figure C.8), and 2 studies simulated age along a continuous dimension. Sexual mixing between age groups was assumed to be assortative either with (23) or without (3) average age differences between men and women; or proportionate (6). Differential risk behaviour by age was modelled in 29 studies.

3.2.4 Cascade Effects

Differential transition rates along the ART cascade were considered in 21 studies, including differences between genders in 15; age groups in 7; and key populations in 12. Another 2 studies did not simulate differential cascade transitions, but justified the decision using context-specific data. Differences between genders included rates of HIV diagnosis (11); ART initiation (6); and ART cessation (1), with cascade engagement higher among women, in most cases attributed to antenatal services. Differences between age groups also affected rates of diagnosis (6); ART initiation (1); but not ART cessation (0). Among key populations, *lower* rates of diagnosis, ART initiation, and retention were simulated in 0, 2, and 4 studies respectively, while *higher* rates were simulated in 8, 2, and 1.

3.3 ART Prevention Impact

Dataset B comprised 40 studies, including 125 scenarios of ART scale-up. Relative incidence reduction (IR) with ART scale-up as compared to status quo was reported in 23 studies (61 scenarios); proportion of cumulative infections averted (CIA) due to ART scale-up in 24 (75); and 7 (11) reported both. Some scenarios included multiple time horizons.

Table 3 summarizes projected ART prevention impacts (IR, CIA), stratified by heterogeneity and contextual factors, plus adjusted effect estimates for each factor from multivariate analysis. Figures C.11–C.19 illustrate unadjusted impacts stratified by factor levels, while Figures C.20 and 2 (subset) illustrate effect estimates. Compared to models with homogeneous risk, including risk heterogeneity via static activity groups but without key populations was associated with slightly higher impacts—adjusted effect (95% CI): 4 (–14, 22)% IR, 24 (12, 36)% CIA. Including key population(s) and assuming similar ART cascade across groups was also associated with higher impact: 72 (–31, 175)% IR, 20 (11, 28)% CIA. However, including turnover of one/more higher risk group(s) was associated with smaller ART prevention impacts: –82 (–153, –11)% IR, –86 (–103, –70)% CIA. Taken together, models that captured heterogeneity in risk across activity groups and/or key population(s) with turnover were associated with reduced ART prevention impacts.

Table 3: Projected ART prevention impacts, stratified by factors of risk heterogeneity and contexts

Factor	Level	Incidence Reduction (%)					Cumulative Infections Averted (%)				
		N ^a	Median	(IQR)	Effect ^b	(95% CI) ^b	N ^a	Median	(IQR)	Effect ^b	(95% CI) ^b
Risk Stratif. & Cascade Diff.	None	98	19	(7, 44)	REF		45	29	(18, 47)	REF	
	Activity (No KP)	22	35	(22, 46)	4	(-14, 22)	39	6	(3, 22)	24	(12, 36)
	+ KP (Same)	5	41	(6, 50)	72	(-31, 175)	8	10	(3, 21)	20	(11, 28)
	+ KP (Priority)	1	85	(85, 85)	136	(73, 199)	23	21	(11, 41)	131	(97, 166)
Activity Turnover	No	117	26	(8, 45)	REF		87	20	(5, 35)	REF	
	Yes	9	22	(21, 50)	-82	(-153, -11)	28	18	(7, 38)	-86	(-103, -70)
Sex/Gender Stratif. & Cascade Diff.	No	97	21	(7, 44)	REF		39	29	(18, 44)	REF	
	Yes (Same)	22	41	(30, 53)	-4	(-32, 23)	48	8	(3, 24)	-49	(-62, -36)
	Yes (Men Low)	7	21	(2, 22)	5	(-41, 50)	28	16	(4, 35)	-125	(-143, -108)
Partnership Types	Generic	107	21	(8, 44)	REF		48	28	(15, 42)	REF	
	By Groups	16	33	(22, 52)	-22	(-53, 9)	66	11	(3, 28)	34	(20, 49)
	Overlapping	3	50	(45, 62)	8	(-52, 69)	1	58	(58, 58)	-9	(-60, 43)
Time Horizon (years)	0-10	36	17	(7, 35)	REF		40	14	(3, 26)	REF	
	11-20	63	20	(8, 42)	3	(-3, 9)	60	22	(8, 38)	9	(2, 17)
	21-30	15	47	(39, 65)	3	(-7, 13)	11	23	(7, 47)	12	(6, 19)
	31+	12	46	(24, 57)	12	(5, 20)	4	34	(29, 40)	5	(1, 8)
HIV Prevalence (%)	11+	112	22	(8, 44)	REF		75	18	(4, 35)	REF	
	1-10	14	43	(36, 49)	-9	(-49, 31)	39	26	(11, 36)	-9	(-20, 2)
	0-1	0	—	(—, —)			1	49	(49, 49)	-3	(-30, 24)
HIV Incidence Trend ^c	Increasing	2	40	(38, 43)			5	32	(29, 41)		
	Inc-to-stable	1	97	(97, 97)			1	68	(68, 68)		
	Stable	17	21	(20, 29)			24	4	(2, 7)		
	Dec-to-stable	81	15	(6, 43)			11	1	(-8, 28)		
	Decreasing	1	57	(57, 57)			13	29	(19, 38)		
RR Transmission on ART	0.0-0.039	11	22	(14, 35)	REF		44	6	(2, 27)	REF	
	0.04-0.099	42	49	(34, 67)	55	(22, 89)	60	27	(15, 38)	-41	(-54, -29)
	0.1+	73	12	(5, 30)	9	(-31, 48)	11	19	(1, 33)	-20	(-26, -13)
CD4 Threshold for ART Initiation	Symptomatic	3	38	(37, 41)	47	(25, 68)	24	4	(2, 7)	-30	(-46, -15)
	200	3	28	(26, 32)	REF		4	28	(24, 30)	REF	
	350	10	29	(22, 38)	15	(3, 28)	18	18	(13, 27)	3	(-2, 7)
	500	15	29	(16, 43)	27	(8, 45)	13	29	(23, 35)	17	(10, 24)
	Any	41	56	(22, 75)	30	(14, 47)	22	51	(28, 62)	42	(37, 48)
	Mixed	54	10	(5, 31)	1	(-31, 32)	34	16	(5, 37)	63	(54, 72)
ART Coverage Target (%) ^c	0-59	3	28	(26, 31)			11	30	(13, 43)		
	60-84	13	29	(21, 41)			22	22	(8, 39)		
	85+	13	46	(36, 66)			21	36	(26, 43)		
Acute Infection	No	35	22	(10, 57)	REF		15	38	(24, 50)	REF	
	Yes	91	26	(9, 44)	52	(13, 91)	100	16	(5, 32)	51	(36, 66)
Late-Stage Infection	No	38	39	(13, 56)	REF		12	36	(20, 48)	REF	
	Yes	88	22	(8, 43)	-23	(-37, -8)	103	18	(5, 34)	-37	(-65, -9)
Trans. Drug Resist.	No	114	21	(7, 43)	REF		102	18	(5, 36)	REF	
	Yes	12	72	(39, 85)	-4	(-46, 39)	13	26	(20, 30)	-3	(-8, 3)
HIV Morbidity	No	102	21	(7, 45)	REF		73	27	(13, 42)	REF	
	Any	24	34	(22, 46)	35	(16, 54)	42	6	(3, 23)	-20	(-26, -14)
HTC Behav. Change	No	112	21	(7, 45)	REF		81	23	(11, 38)	REF	
	Any	14	41	(29, 49)	-39	(-73, -4)	34	6	(3, 22)	-13	(-18, -7)

^a N: number of unique scenarios and time horizons; sums across factor levels may be less than 126 and 115 due to missing variables.

^b Effect estimates from linear multivariate regression with generalized estimating equations [45]; effects are illustrated in Figure C.20.

^c Omitted from regression model due to missing data. RR: relative risk; HTC: HIV testing and counselling; KP: key populations. priority: modelled ART cascade transitions were faster in KP vs overall due to prioritized programs; same: cascade transitions were assumed the same in KP as overall. Factor definitions are given in Appendix B.

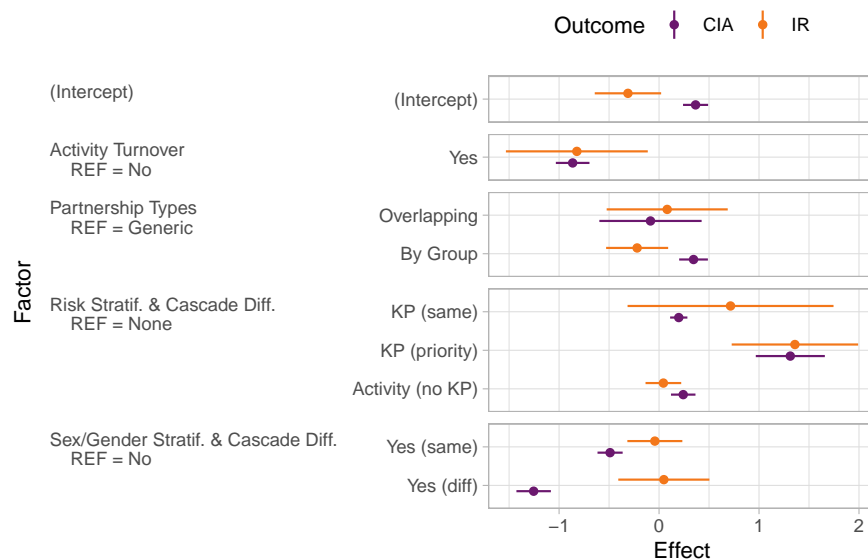


Figure 2: Effect estimates for selected factors of heterogeneity on incidence reduction (%, IR) and cumulative infections averted (%, CIA) from linear multivariate regression with generalized estimating equations.

Numerical results given in Table 3. KP: key populations. priority: modelled ART cascade transitions were faster in KP vs overall due to prioritized programs; same: cascade transitions were assumed the same in KP as overall; diff: cascade transitions were slower among men. Factor definitions are given in Appendix B.

After including risk heterogeneity, further capturing differential ART cascade across activity groups or key populations was associated with differences in projected ART prevention impacts. Models stratified by sex/gender, and those that captured lower ART cascade among men were associated with a smaller CIA: -49 (-62, -36)% and -125 (-143, -108)%, respectively; although similar effects were not observed for IR: -4 (-32, 23)% and 5 (-41, 50)%. Where key populations were explicitly modelled, including ART cascade prioritized to any key population(s) was associated with increased impact, enough to overcome reductions due to turnover: 136 (73, 199)% IR, 131 (97, 166)% CIA. No studies in Dataset B examined lower ART cascade among key population(s).

4 Discussion

Model-based evidence continues to support evaluation and mechanistic understanding of ART prevention impacts. Such evidence may be sensitive to modelling assumptions about risk heterogeneity. Via scoping review, we found that stratification by sexual activity and key population(s) was considered in approximately two-thirds and two-fifths of studies to date, respectively; one-third considered risk group turnover and one-quarter considered differential ART cascade by any risk group. In multivariate ecological analysis, we found that projected incidence reductions and proportions of infections averted were influenced by risk heterogeneity when risk group turnover and differential ART cascade were also considered.

Our findings suggest that the proportion of onward transmission prevented through ART may be reduced via turnover. Data suggest considerable within-person variability in sexual risk among key populations, including MSM, FSW, and clients of FSW [47, 48, 49], as well as in the wider population [50]. This risk variability is often reflected in compartmental models as risk group turnover. Previous modelling suggested that turnover could *increase* the prevention benefits of treatment [51]; however, the model in [51] was calibrated to overall equilibrium prevalence, allowing the reproduction number to decrease with increasing turnover. By contrast, when calibrating to group-specific prevalence with turnover, greater risk heterogeneity is inferred with versus without turnover, and the reproduction number may actually increase [41]. Turnover of higher risk groups can also reduce ART coverage in those groups through net outflow of treated individuals, and net inflow of susceptible individuals, some of whom then become infected [41]. Thus, mechanistically, turnover could reduce the transmission benefits of ART. These findings suggest that turnover is important to capture as part of modeling risk heterogeneity, and as such, models would benefit from surveys, cohorts, and repeated population size estimates that can provide data on individual-level trajectories of sexual risk, such as duration in sex work [29].

Most models assumed equal ART cascade transition rates across subgroups, including diagnosis, ART initiation, and retention. However, recent data suggest differential ART cascade by sex, age, and key populations

[32, 52, 53, 25]. These differences may stem from the unique needs of subgroups and is one reason why differentiated ART services are a core component of HIV programs [23, 54]. Moreover, barriers to ART may intersect with transmission risk, particularly among key populations, due to issues of stigma, discrimination, and criminalization [55, 14]. Our ecological analysis estimated that differences in cascade by sex (lower among men) or risk (key populations prioritized) had a large influence on projected ART prevention benefits. Thus, opportunities exist to incorporate differentiated cascade data, examine the intersections of intervention and risk heterogeneity, and to consider the impact of HIV services as delivered on the ground. Similar opportunities were noted regarding modelling of pre-exposure prophylaxis in SSA [56]. Depending on the research question, the modelled treatment cascade may need to include more cascade steps and states related to treatment failure/discontinuation.

The next generation of ART prevention impact modelling can be advanced by leveraging rapid growth in data on risk heterogeneity and its intersection with intervention heterogeneity [57, 58, 59]. Key populations often reflect intersections of risk heterogeneity with turnover, and intervention heterogeneity (cascade differences), which together suggest the unmet needs of key populations play an important role in the overall dynamics of HIV transmission in SSA [60, 61]. Although none of the models in the review considered a lower ART cascade among key populations, data suggest large cascade differences, most notably lower proportions across the cascade, among key populations in SSA [31, 20, 52]. Similarly, we found that the number of modelled clients per female sex worker, and the relative rate of partnership formation among female sex workers versus other women did not always reflect available data syntheses for sex work [29, 42]. Among studies with different partnership types, only 1/5 modelled main/spousal partnerships—with more sex acts/lower condom use—between two higher risk individuals, while 4/5 modelled only casual/commercial partnerships among higher risk individuals. However, data suggest that female sex workers form main/spousal partnerships with regular clients and boyfriends/spouses from higher risk groups [42]. Improved modelling and prioritization of services designed to reach key populations will rely on continued investment in community-led data collection for hard-to-reach populations.

Our scoping review has several limitations. First, we examined key populations based as traditionally defined [40], based on social and economic marginalization and criminalization in SSA, and future work would benefit from examining risk heterogeneity across more subgroups, such as mobile populations and adolescent girls and young women, where data suggest cascade disparities and risk heterogeneity [62, 63]. Second, our conceptual framework for risk heterogeneity did not explicitly examine heterogeneity related to anal sex, which is associated with higher probability of HIV transmission; nor did we examine structural risk factors like violence [64, 65]. Third, we did not extract whether models were calibrated, and if so, which parameters were fixed versus fitted. If certain parameters were fitted, it could explain some counterintuitive effect estimates. For example, models with versus without increased infectiousness in late-stage HIV might infer

lower earlier-stage infectiousness through model fitting, such that overall infectiousness is roughly the same. Then, when simulating ART scale-up to individuals with earlier-stage HIV, the estimated prevention benefit could be relatively lower. A similar mechanism could explain increased ART prevention impacts when including acute infection. Importantly, we conducted an ecological analysis, and within-model comparisons like [30, 18] that explore the influence of each key factor identified in this review would be an important next step.

In conclusion, model-based evidence of ART prevention impacts could likely be improved by: 1) capturing risk heterogeneity with risk group turnover, as a determinant of inferred risk heterogeneity during model calibration, and to reflect challenges to maintaining ART coverage among risk groups with high turnover; 2) integrating data on differences in ART cascade between sexual risk groups, to reflect services as delivered on the ground; and 3) capturing heterogeneity in risks related to key populations, to reflect intersections of transmission risk and barriers to HIV services that may undermine the prevention benefits of ART.

Conflicts of Interest

None declared.

Funding

The study was supported by the Natural Sciences and Engineering Research Council of Canada (NSERC CGS-D); Ontario Early Researcher Award No. ER17-13-043; and the Canadian Institutes of Health Research Foundation Grant (FN-13455).

Acknowledgements

We thank: Kristy Yiu (Unity Health Toronto) for research coordination support; Linwei Wang (Unity Health Toronto) for feedback on elements of the paper; and Kaitlin Fuller (University of Toronto) for her help designing the search strategy.

Contributions

JK and SM conceptualized and designed the study, and developed the search strategy. JK performed the search, extracted the data, conducted the analysis, and generated the results. JK and SM drafted the manuscript and appendix. All authors (JK, RK, and SM) reviewed the results and contributed to writing the manuscript.

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APPENDIX

Title: Risk heterogeneity in compartmental HIV transmission models of ART as prevention in Sub-Saharan Africa: A scoping review

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A Search Strategy

We designed our search strategy with guidance from an information specialist at our affiliate library (KF).

A.1 Search Terms

Our search strategy and step-wise results are as follows, where `term/` denotes a MeSH term, and `.mp` searches the main text fields, including title, abstract, and heading words. We searched MEDLINE and EMBASE via Ovid on 2020 March 20. Duplicate studies were removed automatically by Ovid and by Covidence; four additional duplicates with subtly different titles were later identified and removed manually.

Table A.1: Search terms and hits

	Term	Hits
M1	238,076	model, theoretical/
M2	334,921	model, biological/
M3	302,802	computer simulation/
M4	196,814	patient-specific modeling/
M5	67,459	monte carlo method/
M6	32,801	exp stochastic processes/
M7	455,312	(model* ADJ3 (math* OR transmission OR dynamic* OR epidemi* OR compartmental OR deterministic OR individual OR agent OR network OR infectious disease* OR markov OR dynamic* OR simulat*)) .mp.
M8	1,369,153	OR/ M1-M7
H1	290,863	exp HIV/
H2	651,624	exp HIV infections/
H3	753,274	(HIV OR HIV1* OR HIV2* OR HIV-1* OR HIV-2*) .mp.
H4	369,182	hiv infect* .mp.
H5	538,214	(human immunodeficiency virus OR human immun* deficiency virus) .mp.
H6	216,228	exp Acquired Immunodeficiency Syndrome/
H7	235,971	(acquired immunodeficiency syndrome OR acquired immun* deficiency syndrome) .mp.
H8	954,470	OR/ H1-H7
G1	3512	Angola/ OR Angola .mp.
G2	9273	Benin/ OR Benin .mp.
G3	5809	Botswana/ OR Botswana .mp.
G4	9983	Burkina Faso/ OR Burkina Faso .mp.
G5	2055	Burundi/ OR Burundi .mp.
G6	16,822	Cameroon/ OR Cameroon .mp.
G7	1196	Cape Verde/ OR Cape Verde .mp.
G8	15,416	Central African Republic/ OR Central African Republic .mp. OR CAR .ti.
G9	3075	Chad/ OR Chad .mp.
G10	995	Comoros/ OR Comoros .mp.
G11	13,737	Democratic Republic of the Congo/ OR Democratic Republic of the Congo .mp. OR DRC .mp.
G12	959	Djibouti/ OR Djibouti .mp.
G13	1131	Equatorial Guinea/ OR Equatorial Guinea .mp.
G14	1437	Eritrea/ OR Eritrea .mp.
G15	35,959	Ethiopia/ OR Ethiopia .mp.
G16	4500	Gabon/ OR Gabon .mp.
G17	6626	Gambia/ OR Gambia .mp.
G18	25,213	Ghana/ OR Ghana .mp.
G19	360,920	Guinea/ OR Guinea .mp.
G20	2625	Guinea-Bissau/ OR Guinea-Bissau .mp.

continued...

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	Term	Hits
G21	9730	Cote d'Ivoire/ OR Cote d'Ivoire.mp. OR Ivory Coast.mp.
G22	46,917	Kenya/ OR Kenya.mp.
G23	1649	Lesotho/ OR Lesotho.mp.
G24	4239	Liberia/ OR Liberia.mp.
G25	11,386	Madagascar/ OR Madagascar.mp.
G26	16,367	Malawi/ OR Malawi.mp.
G27	9111	Mali/ OR Mali.mp.
G28	1573	Mauritania/ OR Mauritania.mp.
G29	2373	Mauritius/ OR Mauritius.mp.
G30	8502	Mozambique/ OR Mozambique.mp.
G31	3818	Namibia/ OR Namibia.mp.
G32	35,455	Niger/ OR Niger.mp.
G33	82,192	Nigeria/ OR Nigeria.mp.
G34	13,547	Republic of the Congo/ OR Republic of the Congo.mp. OR Congo-Brazzaville.mp.
G35	1545	Reunion/
G36	7597	Rwanda/ OR Rwanda.mp.
G37	342	"Sao Tome and Principe"/ OR "Sao Tome and Principe".mp.
G38	16,674	Senegal/ OR Senegal.mp.
G39	1566	Seychelles/ OR Seychelles.mp.
G40	5456	Sierra Leone/ OR Sierra Leone.mp.
G41	4667	Somalia/ OR Somalia.mp.
G42	114,536	South Africa/ OR South Africa.mp.
G43	1193	South Sudan/ OR South Sudan.mp.
G44	21,680	Sudan/ OR Sudan.mp.
G45	2409	Swaziland/ OR Swaziland.mp. OR Eswatini/ OR Eswatini.mp.
G46	32,442	Tanzania/ OR Tanzania.mp.
G47	3749	Togo/ OR Togo.mp.
G48	37,399	Uganda/ OR Uganda.mp.
G49	13,506	Zambia/ OR Zambia.mp.
G50	15,755	Zimbabwe/ OR Zimbabwe.mp.
G51	482,060	exp africa south of the sahara/ OR sub-saharan.mp. OR south of the sahara.mp.
G52	982,505	OR/ G1-G51
X1	2190	M8 AND H8 AND G52
X2	2160	X1 NOT animal/
X3	2155	limit X2 to english language
X4	2125	limit X3 to yr="1860 - 2019"
X5	1384	remove duplicates from X4

A.2 Inclusion/Exclusion Criteria

Table A.2: Criteria for inclusion and exclusion

Include	Exclude
Publication Type	
<ul style="list-style-type: none"> • English language • published before 2020 • peer-reviewed journal article 	<ul style="list-style-type: none"> • non-English language • published in or after 2020 • non-peer-reviewed article • review article¹ • textbook, grey literature • opinions, comments, correspondence • conference abstracts and proceedings • model comparison study
Mathematical Modelling of HIV Transmission	
<ul style="list-style-type: none"> • sexual HIV transmission model • non-linear HIV transmission model² • population-level dynamics • compartmental model³ 	<ul style="list-style-type: none"> • no sexual HIV transmission modelled • HIV transmission model is linear • only within-host/cellular/protein modelling • individual-based model
Context & Objectives	
<ul style="list-style-type: none"> • any region in Sub-Saharan Africa (SSA)⁴ • assess prevention impact of ART scale-up for all⁵ 	<ul style="list-style-type: none"> • only regions outside SSA modelled • only theoretical context modelled • only individual-level benefits of ART modelled • only prevention benefits of other interventions • no base-case scenario reflecting status quo[*] • only ART-combination interventions[*] • only ART intervention targeted to some risk groups[*] • only ART prevention impacts reported for some risk groups[*] • ART prevention impacts not reported^{5*}

¹ Review articles were included if they also presented new HIV transmission modelling results fitting our criteria. ² We define a *non-linear model* as one where the number of infections projected at time t is an iterative function of the number of infections previously projected by the model before time t . ³ We define a *compartmental model* as one where the system variables represent the numbers of individuals in each state, rather than unique individuals. ⁴ SSA was defined based on the countries in the UN regions of East, South, Central, and West Africa, plus South Sudan (see Table A.1 for full country list). Studies were included if the model was parameterized/calibrated to reflect at least one context within SSA. Only model parameters & outcomes for SSA contexts were extracted. ⁵ Articles reporting HIV incidence reduction and/or cumulative HIV infections averted among the whole population due to increased coverage or initiation rate of ART for the whole population. ^{*} Used to define Dataset B only.

A.3 Included Studies

A.3.1 Dataset B

- | | |
|---|--|
| [1] 2005 Salomon et al. | [2] 2006 Abbas, Anderson, and Mellors |
| [3] 2009 Granich et al. | [4] 2009 Hallett et al. |
| [5] 2010 Bacaer, Pretorius, and Auvert | [6] 2010 Pretorius et al. |
| [7] 2011 Metzger, Lloyd-Smith, and Weinberger | [8] 2012 Yusuf and Benyah |
| [9] 2012 Andrews et al. | [10] 2012 Granich et al. |
| [11] 2012 Wagner and Blower | [12] 2013 Abbas et al. |
| [13] 2013 Long and Stavert | [14] 2013 Cremin et al. |
| [15] 2013 Alsallaq et al. | [16] 2014 Nichols et al. |
| [17] 2014 Nichols et al. | [18] 2014 Alistar, Grant, and Bendavid |
| [19] 2014 Eaton and Hallett | [20] 2015 Ying et al. |
| [21] 2015 Low et al. | [22] 2015 Khademi, Anand, and Potts |
| [23] 2015 Gilbert et al. | [24] 2015 Heaton et al. |
| [25] 2016 Rahman, Vaidya, and Zou | [26] 2016 Gilbert et al. |
| [27] 2016 Blaizot et al. | [28] 2016 Ying et al. |
| [29] 2016 Barnighausen, Bloom, and Humair | [30] 2016 Heffernan et al. |
| [31] 2017 Maheu-Giroux et al. | [32] 2017 Maheu-Giroux et al. |
| [33] 2017 Volz et al. | [34] 2017 Blaizot et al. |
| [35] 2018 Mukandavire et al. | [36] 2018 Guillon |
| [37] 2018 Akudibillah, Pandey, and Medlock | [38] 2018 Stuart et al. |
| [39] 2018 de Montigny et al. | [40] 2019 Hauser et al. |

A.3.2 Dataset A less B

- | | |
|--------------------------------------|--|
| [41] 2006 Johnson and Dorrington | [42] 2006 Baggaley, Garnett, and Ferguson |
| [43] 2006 Wilson, Kahn, and Blower | [44] 2008 Bacaer et al. |
| [45] 2009 Chigidi and Lungu | [46] 2010 Williams et al. |
| [47] 2011 Nyabadza and Mukandavire | [48] 2012 Barnighausen, Bloom, and Humair |
| [49] 2013 Wagner, Coburn, and Blower | [50] 2013 Decker et al. |
| [51] 2013 Wirtz et al. | [52] 2014 Shafer et al. |
| [53] 2014 Hove-Musekwa et al. | [54] 2014 Braithwaite et al. |
| [55] 2014 Nichols et al. | [56] 2014 Abu-Raddad and Awad |
| [57] 2014 Anderson et al. | [58] 2014 Alistar et al. |
| [59] 2014 Cori et al. | [60] 2014 Stover et al. |
| [61] 2014 Wirtz et al. | [62] 2015 Korenromp et al. |
| [63] 2015 Knight et al. | [64] 2015 Kerr et al. |
| [65] 2015 Fraser et al. | [66] 2015 Kassa and Ouhinou |
| [67] 2015 Bekker et al. | [68] 2015 Shannon et al. |
| [69] 2015 Blaizot et al. | [70] 2016 Smith et al. |
| [71] 2016 Atun et al. | [72] 2016 Shattock et al. |
| [73] 2016 McGillen et al. | [74] 2016 Johnson et al. |
| [75] 2016 Sharma et al. | [76] 2017 Akudibillah, Pandey, and Medlock |
| [77] 2017 Alsallaq et al. | [78] 2017 Anderson et al. |
| [79] 2017 Chiu et al. | [80] 2017 Johnson et al. |
| [81] 2017 Stuart et al. | [82] 2017 McGillen et al. |
| [83] 2017 Cremin et al. | [84] 2018 Ross et al. |
| [85] 2018 Anderson et al. | [86] 2018 Anderson et al. |
| [87] 2018 Omondi, Mbogo, and Luboobi | [88] 2018 Woods et al. |
| [89] 2018 Stevens et al. | [90] 2019 Stopard et al. |
| [91] 2019 Beacroft and Hallett | [92] 2019 Reidy et al. |
| [93] 2019 Omondi, Mbogo, and Luboobi | [94] 2019 Maheu-Giroux et al. |

B Definitions & Extraction

Data were obtained from (in order of precedence): article text; article tables; article figures; appendix text; appendix tables; appendix figures; and likewise for articles cited like “the model is previously described elsewhere”. Data were assessed from figures with the help of a graphical measurement tool.¹

Fitted Parameters: For the values of fitted parameters, we used the posterior value as reported, including the mean or median of the posterior distribution, or the best fitting value. If the posterior was not reported, we used the mean or median of the prior distribution, including the midpoint of uniform sampling ranges.

B.1 Epidemic Context

Let t_0 be the time of ART scale-up/scenario divergence in the model.

HIV Prevalence: As reported in the context overall at t_0 : *Low*: <1%; *Medium*: 1–10%; *High*: >10%.

Epidemic Phase: As projected in the base-case scenario in the context overall between t_0 and roughly $t_0 + 10$ years: *Increasing* (linear or exponential); *Increasing but stabilizing*; *Stable*; *Decreasing but stabilizing*; *Decreasing* (linear or exponential).

Geographic Scale: For studies of one geographic context, scale was defined as one of: *regional*: multiple countries; *national*: one country; *sub-national*: smaller than a country but greater than a city; *city*: one city or less. For studies that consider multiple geographic contexts, scale was defined as *multi-x*, where x is the smallest geographically homogeneous scale considered from the list above.

Country: The countries counted were: *Angola, Benin, Botswana, Burkina Faso, Burundi, Cameroon, Cape Verde, Central African Republic, Chad, Comoros, Democratic Republic of the Congo, Djibouti, Equatorial Guinea, Eritrea, eSwatini, Ethiopia, The Gabon, Gambia, Ghana, Guinea, Guinea-Bissau, Côte d’Ivoire, Kenya, Lesotho, Liberia, Madagascar, Malawi, Mali, Mauritania, Mauritius, Mozambique, Namibia, Niger, Nigeria, Republic of the Congo, Reunion, Rwanda, Sao Tome and Principe, Senegal, Seychelles, Sierra Leone, Somalia, South Africa, South Sudan, Sudan, Tanzania, Togo, Uganda, Zambia, Zimbabwe*. See Table A.1 for related search terms. If a study modelled multiple countries at a national scale or smaller, the counter for each country was incremented.

B.2 Risk Heterogeneity

B.2.1 Key Populations

Female Sex Workers: Any female activity group meeting 3 criteria: representing <5% of the female population; and being $< 1/3 \times$ the size of client population or highest non-MSM male activity group; and having $> 50 \times$ the partners of the lowest sexually active female activity group [Carmel2006, 95, 96]. We also noted whether the authors described any activity groups as FSW. If it was not possible to evaluate any criteria due to lack of data, then we assumed the criteria was satisfied.

Clients of FSW: Any male activity group meeting 2 criteria: described as representing clients of FSW; being $> 3 \times$ the size of the FSW population [Carmel2006]. If group sizes were not reported, then we assumed an activity group described as clients met the size criterion. We also noted whether clients were described as comprising a proportion of another male activity group.

Men who have Sex with Men: Any male activity group(s) described by the authors as MSM.

Transgender People: Any activity group(s) described by the authors as transgender.

¹WebPlotDigitizer: <https://apps.automeris.io/wpd/>

People who Inject Drugs: Any activity group(s) described by the authors as PWID.

Prisoners: Any activity group(s) described by the authors as prisoners.

B.2.2 Activity Groups

Activity groups were defined as any stratification based on sex/gender and the number and/or types of partnerships formed, including key populations, but excluding stratifications by age.

Count: We counted the number of modelled activity groups in total, and separately for women who have sex with men, men who have sex with women, and MSM.

Highest Risk Group Size: The proportion of men and women in the highest risk group.

Turnover: Turnover refers to movement of individuals between activity groups and/or key populations reflecting sexual life course. We defined four classifications of turnover if activity groups were modelled: *None*: no movement between activity groups; *High-Activity*: only movement between one high activity group or key population and other activity group(s); *Multiple*: movement between multiple pairs of risk groups; *Replacement*: only movement from low to high activity to maintain high activity group size(s) against disproportionate HIV mortality.

B.2.3 Partnerships

Approaches: How studies defined partnerships, classified into one of three approaches: *Generic*: all partnerships are equal; *By-Group*: partnership types are defined only by the activity groups involved; *Overlapping*: multiple partnership types can be formed by the same pair of activity groups. Within *By-Group*, we classified how the parameters of the partnership were defined, as based on either: the *susceptible* partner; the *lower activity* partner; the *higher activity* partner; or some consideration of *both partners*.

Characteristics: Whether any of the following varied between different partnership types: *Condom Use*: proportion of sex acts protected; *Total Sex*: total number of sex acts, possibly defined by differences in partnership duration and/or frequency of sex.

Mixing: Mixing by activity group was classified as either: *Proportionate*: proportionate to the total number of partnerships offered by each risk group; *Assortative*: any degree of preferential partnership formation between individuals of the same or similar risk groups.

B.2.4 Age Groups

Count: The number of age groups considered in the model.

Risk: Whether age groups differed in any characteristic that conferred transmission risk (binary).

Mixing: We classified whether partnership formation between age groups was assumed to be: *Proportionate*: proportionate to the number of partnerships offered by each age group; *Strictly Assortative*: any degree of preferential partnership formation between individuals of the same or similar age groups that is equal for both sexes. *Off-Diagonal*: any degree of preferential partnership formation between younger women and older men.

B.3 HIV Natural History

Count: The number of states of HIV infection considered in the model, excluding stratifications related to treatment. If states were defined by both CD4 and viral load, then the count considers all unique combinations.

Acute Infection: Whether any state represented increased infectiousness associated with acute infection (binary).

Late-Stage Infection: Whether any state(s) considered increased infectiousness associated with late-stage infection (binary).

HIV Morbidity: Whether any state(s) considered decreased sexual activity associated with late-stage disease (binary), and how that decreased was modelled: *Inactive*: complete cessation of sexual activity; *Partners*: decreased rate of partnership formation; *Sex Acts per Partnership*: decreased frequency of sex per partnership; and/or *Generic*: representative decreased probability of transmission.

B.4 Antiretroviral Therapy

B.4.1 Transmission

Transmission Reduction due to ART: The relative reduction in probability of transmission (0 is perfect prevention, 1 is no effect) among individuals who are virally suppressed; if viral suppression was not explicitly modelled, then the relative reduction among individuals who are on treatment was used.

Transmitted Resistance: Any consideration of 1+ strains of HIV which are transmitted and for which ART had reduced benefits. We did not document the number of resistant strains, or characteristics of resistance and transmissibility.

B.4.2 Treatment Cascade States

Forward Cascade: We extracted whether each of the following states were included (binary): *Diagnosed*: aware of their HIV+ status, but have not yet started ART; *Not Yet Virally Suppressed*: started ART, but are not yet virally suppressed; *Virally Suppressed*: on ART and achieved viral suppression; and *Generic On ART*: simplifications of any/all of the above.

Stopping ART: We extracted whether individuals stopped ART, either due to: *Treatment Failure*: ART is no longer efficacious due to resistance; or *ART Cessation*: ART is discontinued for other reasons, such as barriers to access or side effects. We also extracted whether individuals stopping ART for either reason were tracked separately, or whether they re-entered a generic ART-naïve state, such as “Diagnosed”.

Differential Cascade Transitions: We extracted whether rates of transitioning along the ART cascade, including: rate of *HIV diagnosis*; rate of *ART initiation*; and rate of *ART cessation*, differed by any of the following stratifications: *sex*; *age*; *activity*; and *key populations*. If the study did not mention possible differences in such rates, then we assumed that no differences were modelled.

B.4.3 Behaviour Change

HIV Counselling: Whether any sexual behaviour change associated with HIV testing and counselling was applied to individuals in the diagnosed and/or on-ART states (binary), and what changed: *Condom Use*: increased; *Serosorting*: any; *Partners*: decreased rate of partnership formation; *Sex Acts per Partnership*: decreased

frequency of sex per partnership; and/or *Generic*: representative decreased probability of transmission due to counselling.

B.5 ART Prevention Impact

The following data were extracted per scenario, rather than per-study.

B.5.1 Intervention

ART Initiation Criteria: What criteria were used for ART eligibility as part of the intervention: *Symptomatic (AIDS)*; $CD4 < 200$; $CD4 < 350$; $CD4 < 500$; *All individuals*; *Other*.

Intervention Population: Among which population sub-group(s) was the scale-up of ART coverage/initiation applied. Only scenarios with ART intervention for all individuals were included in Dataset B.

Impact Population: Among which population sub-group(s) was the ART prevention impact measured. Only scenarios measuring ART prevention impacts in all individuals were included in Dataset B.

ART Coverage Target: The proportion of people living with HIV in the intervention population who are on ART by the end of ART scale-up.

ART Initiation Rate Target: The rate at which people living with HIV in the intervention population initiate ART by the end of ART scale-up.

Intervention t_o and t_f : The years at which ART scale-up as part of the intervention started and stopped, respectively. If interventions were modelled as instantaneous, such as increasing ART initiation rate, then we considered $t_o = t_f$. Impact time horizons were measured relative to t_o .

B.5.2 Impact

For both measures of ART prevention impact, we extracted reported values from the text for any available time horizon, as well as figure data for any of the following time horizons, if available: 5, 10, 15, 20, 30, and 40 years, with the help of a graphical measurement tool. If only absolute values were reported, we calculated the relative reductions manually. Where reported, we extracted confidence intervals for each outcome.

Relative Incidence Reduction: The relative reduction in overall annual HIV incidence (per 1000 person-years) in the intervention scenario as compared to the baseline scenario, both after an equal number of years since t_o (time horizon). For example, if the baseline and intervention scenarios predicted overall HIV incidence of 1 and 0.7 per 1000 person-years 5 years after t_o , then the relative incidence reduction for the 5-year time horizon would be 30%.

Proportion of Infections Averted: The relative reduction in cumulative new HIV infections in the intervention scenario as compared to the baseline scenario, both after an equal number of years since t_o (time horizon). For example, if the baseline and intervention scenarios predicted 1000 and 700 new infections 5 years after t_o , then the proportion of infections averted for the 5-year time horizon would be 30%.

C Supplemental Results

Additional information on data sources, analysis, and results are available in the public repository:

<https://github.com/mishra-lab/sr-heterogeneity-hiv-models>

C.1 Map

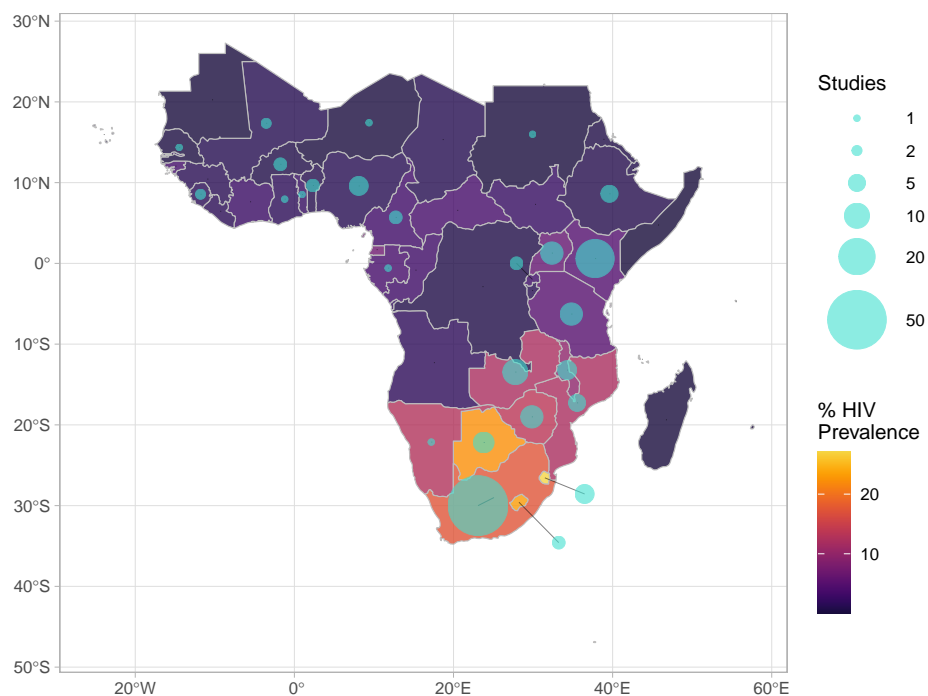


Figure C.1: Map showing number of studies (of 94 total) applying HIV transmission modelling in each country vs the number of people living with HIV (PLHIV, millions)

C.2 Risk Heterogeneity

C.2.1 Distributions

The following figures illustrate the distributions (number of studies) of various parameter values and modelling assumptions related to factors of heterogeneity and intervention contexts.

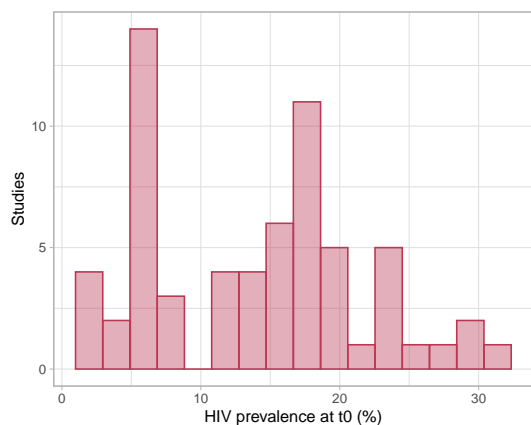


Figure C.2: HIV prevalence at t_0 (%)

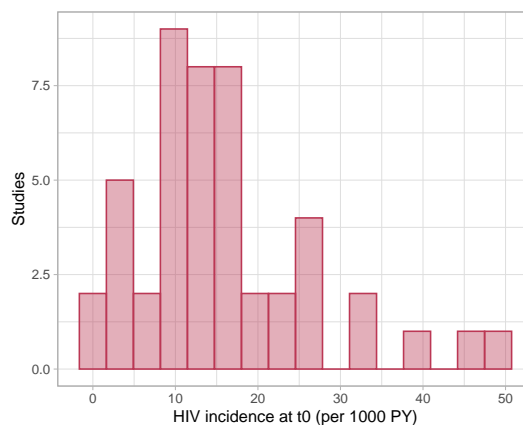


Figure C.3: HIV incidence at t_0 (per 1000 PY)

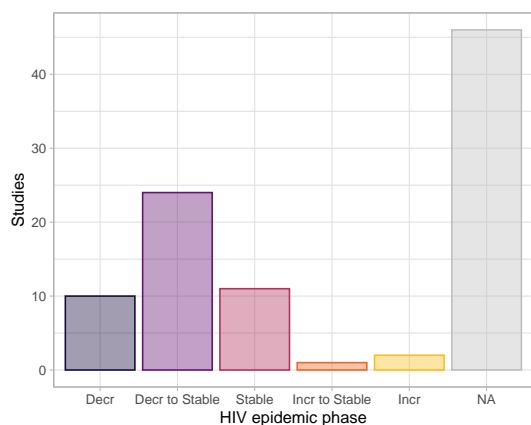


Figure C.4: HIV epidemic phase

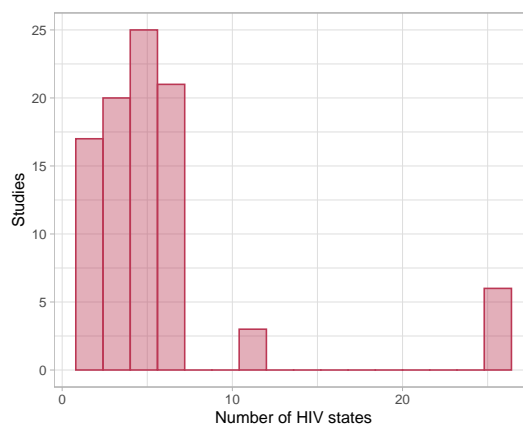


Figure C.5: Number of HIV states

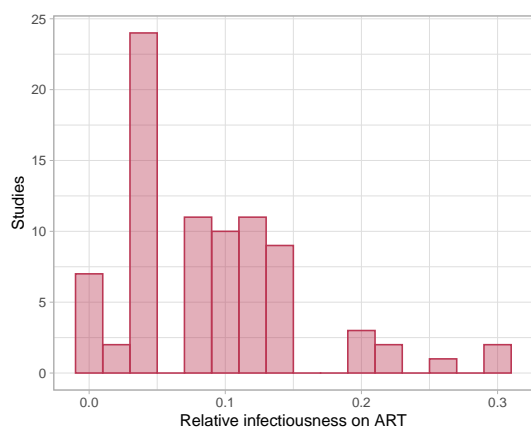


Figure C.6: Relative infectiousness on ART

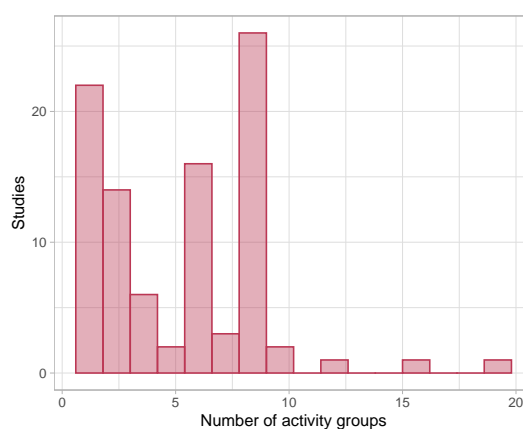


Figure C.7: Number of activity groups

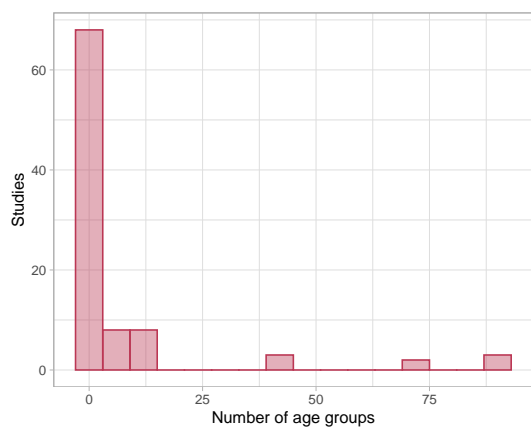


Figure C.8: Number of age groups

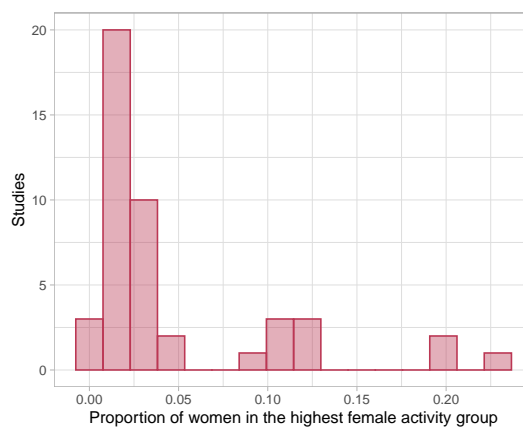


Figure C.9: Proportion of women in the highest female activity group

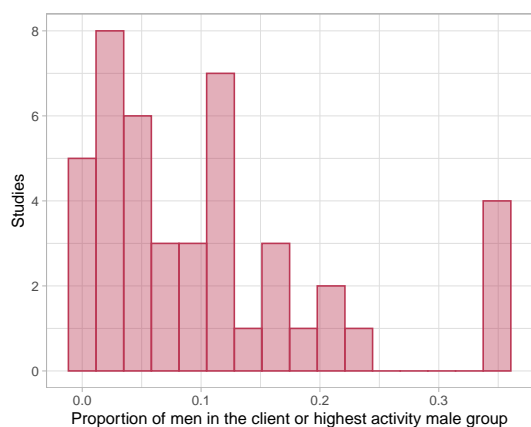


Figure C.10: Proportion of men in the client or highest activity male group

C.3 ART Prevention Impact

The following figures illustrate the projected ART prevention impact (Dataset B), stratified by various factors of heterogeneity and intervention contexts (colours). Left panels show the relative HIV incidence reduction (IR); right panels show the proportion of cumulative HIV infections averted (CIA); both as compared to a base-case scenario reflecting status quo. If any study included multiple scenarios of ART scale-up, then each scenario was included separately; if any scenario reported multiple time horizons, each time horizon was included separately. The number of studies (scenarios) reporting incidence reduction, cumulative infections averted, both, or either was: 23 (61), 24 (75), 7 (11), and 40 (125), respectively. If any factor could not be quantified due to missing data or varying values, it was omitted from that plot. In box plots, the numbers of unique scenario time-horizons contributing to each box are given above it.

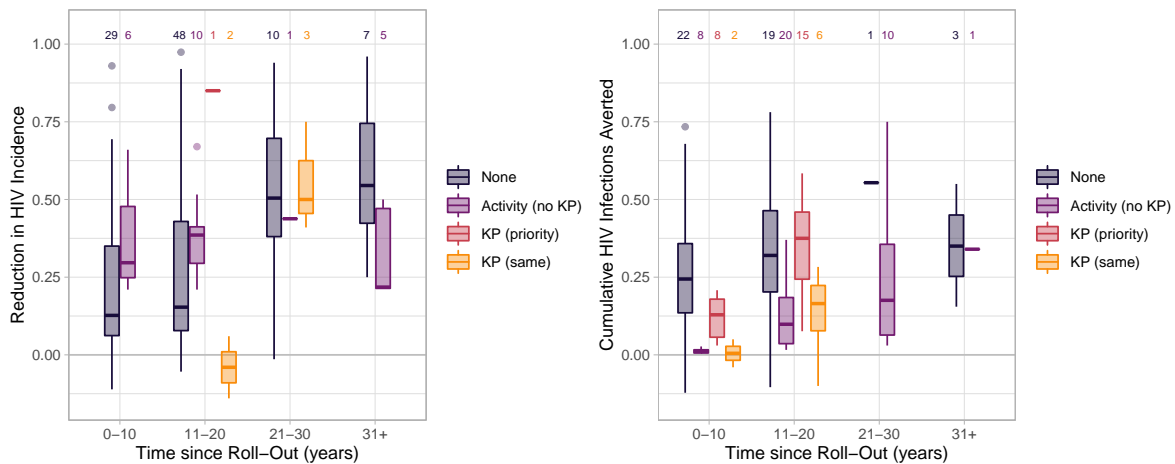


Figure C.11: Risk Stratification & ART cascade differences

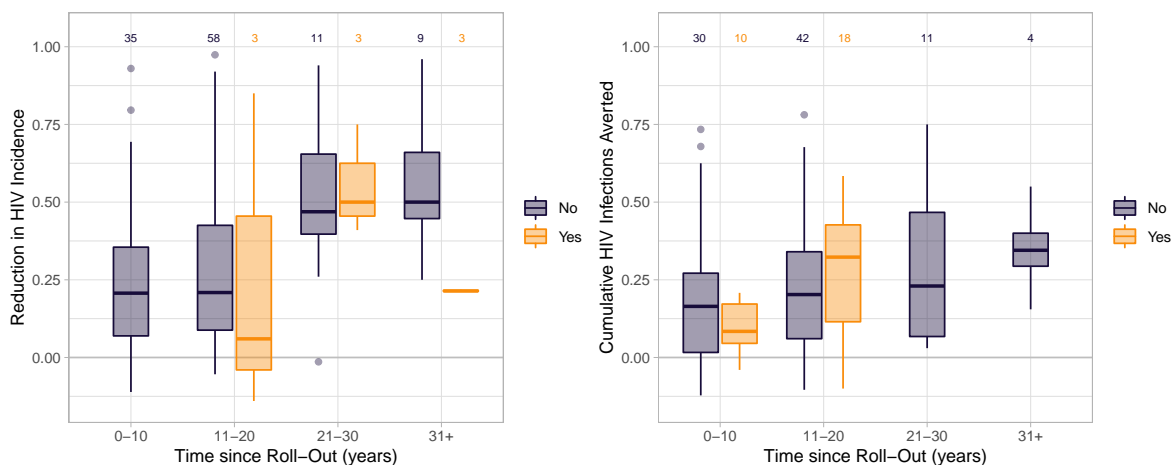


Figure C.12: Any activity group turnover

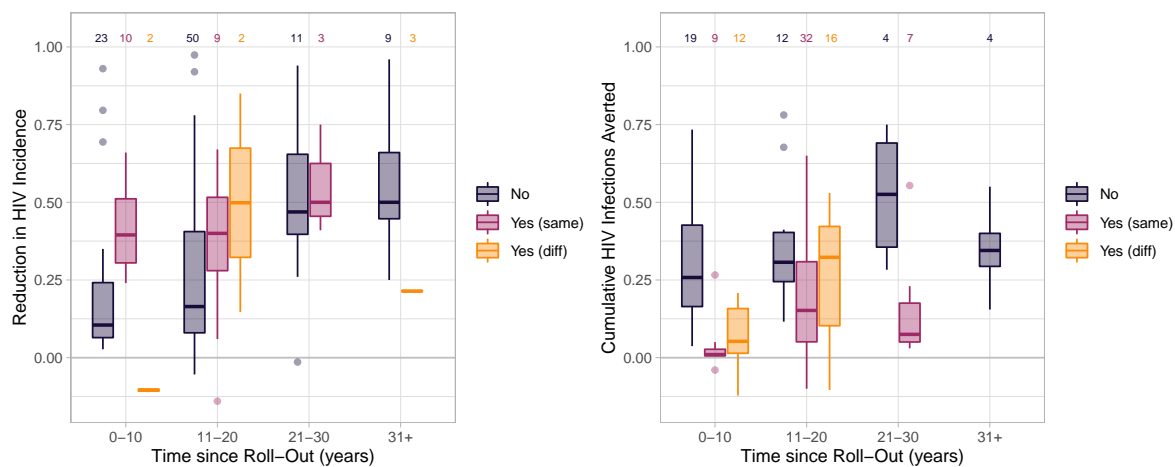


Figure C.13: Sex stratification & any ART cascade differences

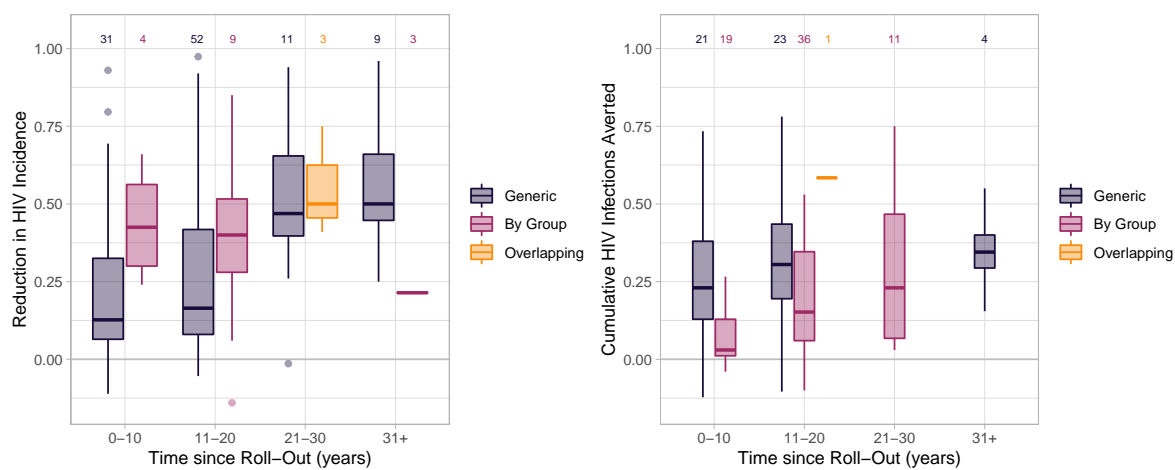


Figure C.14: Type of partnership definition

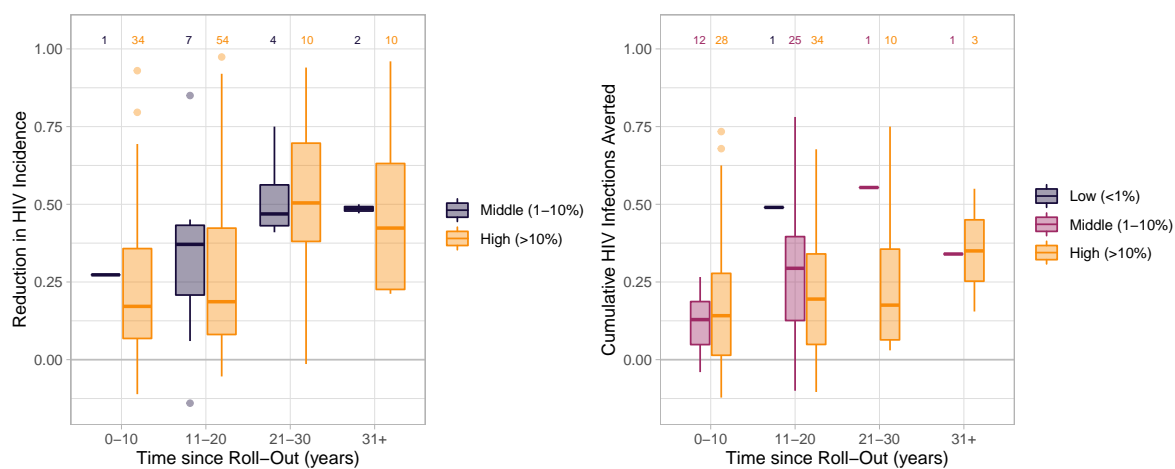
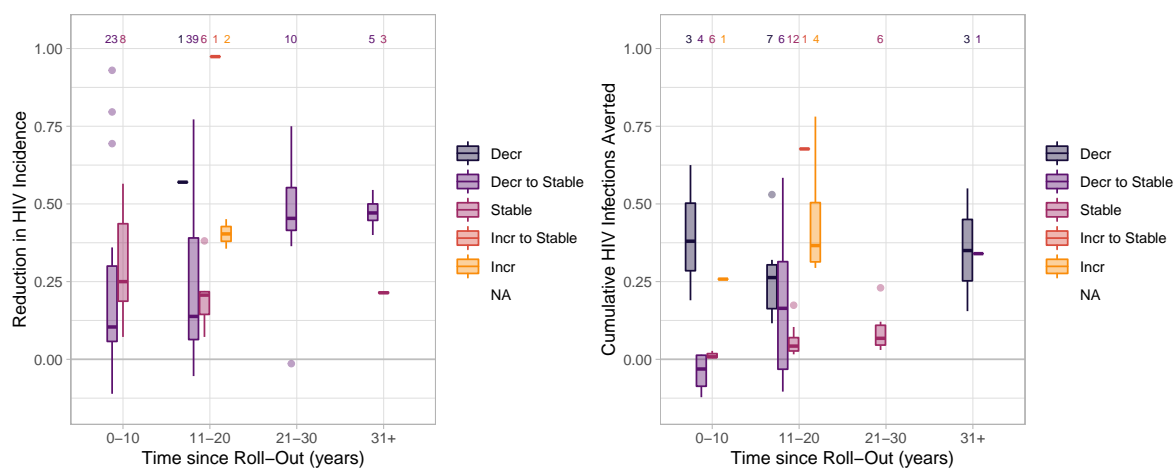
Figure C.15: HIV prevalence at t_0 (%)

Figure C.16: HIV epidemic phase

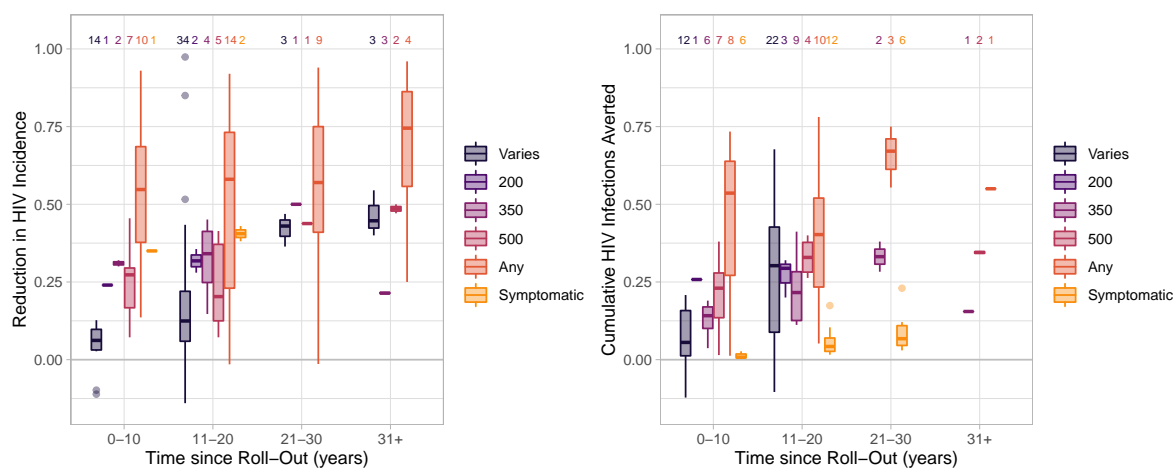


Figure C.17: CD4 initiation criteria

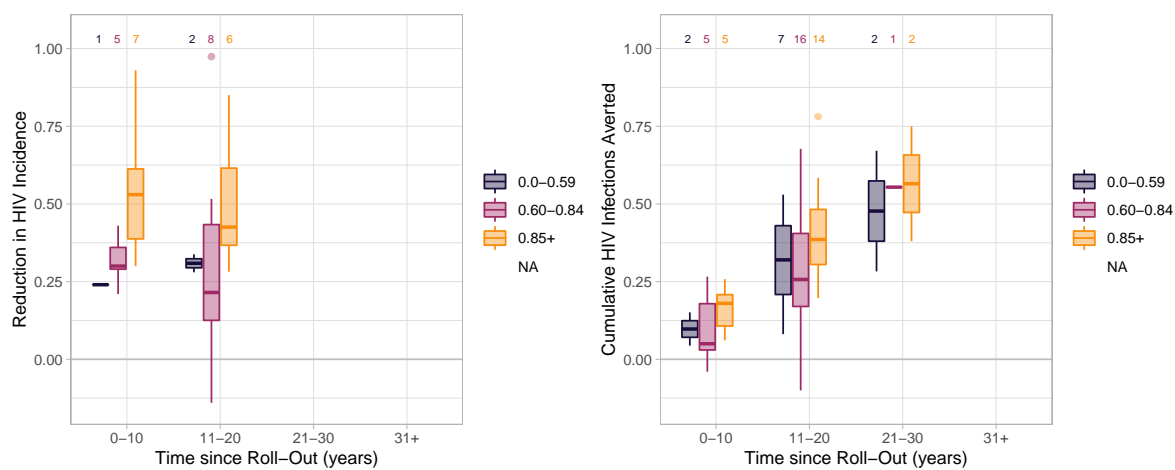


Figure C.18: ART intervention coverage target

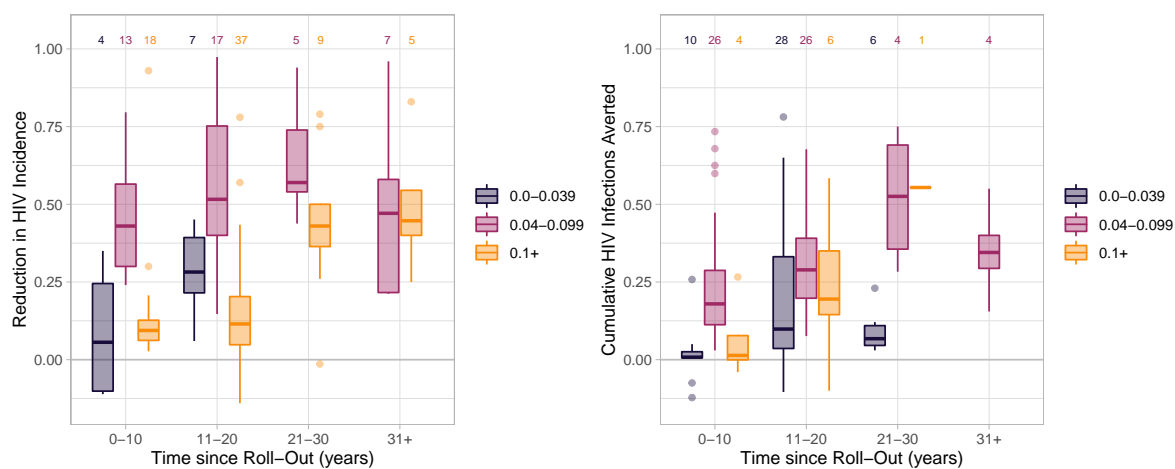


Figure C.19: Relative infectiousness on ART

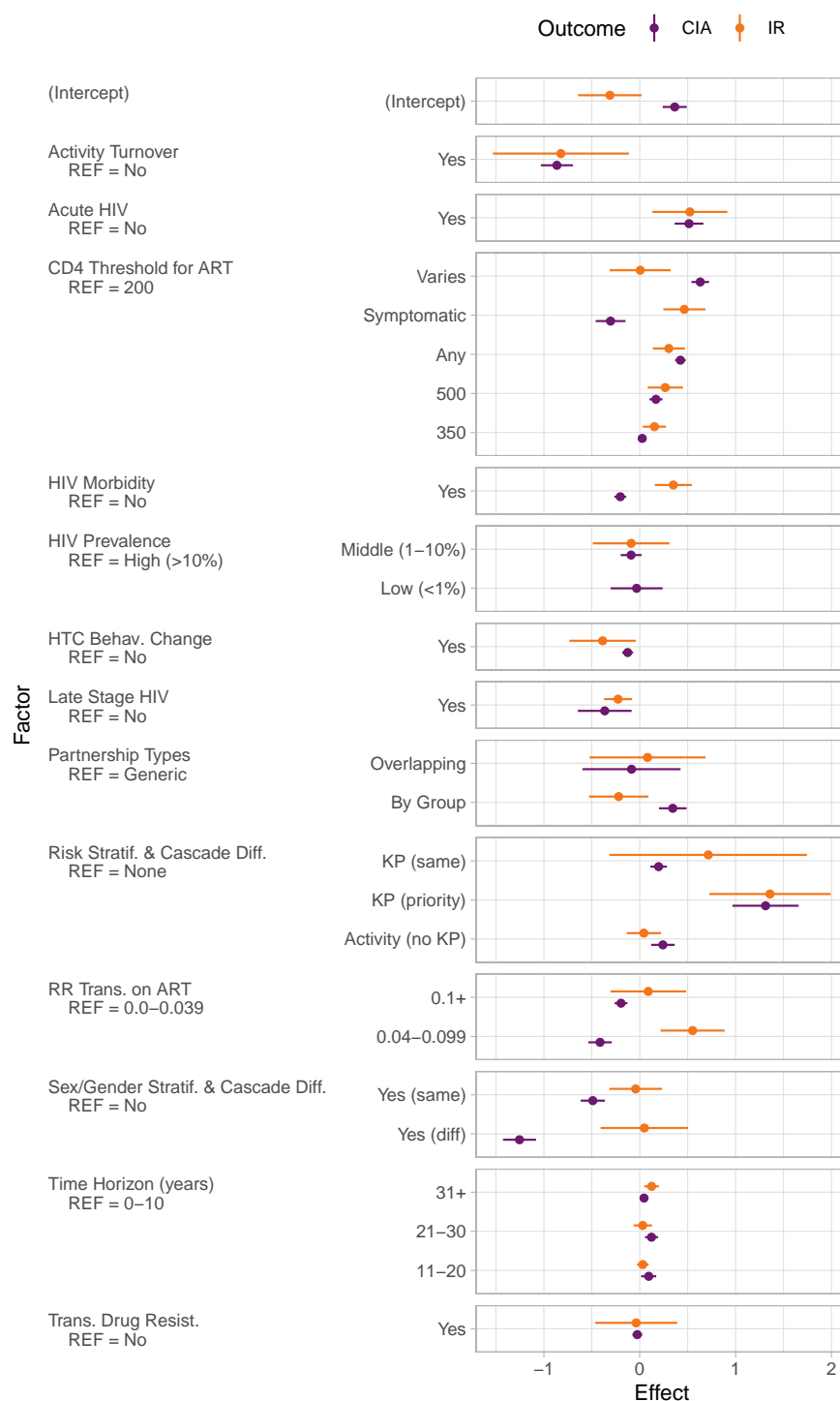


Figure C.20: Effect estimates for factors of heterogeneity on incidence reduction (%, IR) and cumulative infections averted (%, CIA) from linear multivariate regression with generalized estimating equations.

Numerical results given in Table 3. RR: relative risk; HTC: HIV testing and counselling; KP: key populations. priority: modelled ART cascade transitions were faster in KP vs overall due to prioritized programs; same: cascade transitions were assumed the same in KP as overall. Factor definitions are given in Appendix B.

D PRISMA-ScR Checklist

Preferred Reporting Items for Systematic reviews and Meta-Analyses extension for Scoping Reviews (PRISMA-ScR) Checklist

SECTION	ITEM	PRISMA-ScR CHECKLIST ITEM	REPORTED ON PAGE #
TITLE			
Title	1	Identify the report as a scoping review.	1
ABSTRACT			
Structured summary	2	Provide a structured summary that includes (as applicable): background, objectives, eligibility criteria, sources of evidence, charting methods, results, and conclusions that relate to the review questions and objectives.	Abstract
INTRODUCTION			
Rationale	3	Describe the rationale for the review in the context of what is already known. Explain why the review questions/objectives lend themselves to a scoping review approach.	Introduction
Objectives	4	Provide an explicit statement of the questions and objectives being addressed with reference to their key elements (e.g., population or participants, concepts, and context) or other relevant key elements used to conceptualize the review questions and/or objectives.	Introduction
METHODS			
Protocol and registration	5	Indicate whether a review protocol exists; state if and where it can be accessed (e.g., a Web address); and if available, provide registration information, including the registration number.	N/A
Eligibility criteria	6	Specify characteristics of the sources of evidence used as eligibility criteria (e.g., years considered, language, and publication status), and provide a rationale.	Methods 2.2 Appendix A.2
Information sources*	7	Describe all information sources in the search (e.g., databases with dates of coverage and contact with authors to identify additional sources), as well as the date the most recent search was executed.	Methods 2.2 Appendix A.1
Search	8	Present the full electronic search strategy for at least 1 database, including any limits used, such that it could be repeated.	Methods 2.2 Appendix A.1
Selection of sources of evidence†	9	State the process for selecting sources of evidence (i.e., screening and eligibility) included in the scoping review.	Methods 2.2 Appendix A.2
Data charting process‡	10	Describe the methods of charting data from the included sources of evidence (e.g., calibrated forms or forms that have been tested by the team before their use, and whether data charting was done independently or in duplicate) and any processes for obtaining and confirming data from investigators.	Methods 2.3 Appendix B
Data items	11	List and define all variables for which data were sought and any assumptions and simplifications made.	Meth 2.3 App B
Critical appraisal of individual sources of evidence§	12	If done, provide a rationale for conducting a critical appraisal of included sources of evidence; describe the methods used and how this information was used in any data synthesis (if appropriate).	N/A
Synthesis of results	13	Describe the methods of handling and summarizing the data that were charted.	Meth 2.3 App B

SECTION	ITEM	PRISMA-ScR CHECKLIST ITEM	REPORTED ON PAGE #
RESULTS			
Selection of sources of evidence	14	Give numbers of sources of evidence screened, assessed for eligibility, and included in the review, with reasons for exclusions at each stage, ideally using a flow diagram.	Results Figure 1
Characteristics of sources of evidence	15	For each source of evidence, present characteristics for which data were charted and provide the citations.	Results Appendix A.3
Critical appraisal within sources of evidence	16	If done, present data on critical appraisal of included sources of evidence (see item 12).	N/A
Results of individual sources of evidence	17	For each included source of evidence, present the relevant data that were charted that relate to the review questions and objectives.	Results Appendix C
Synthesis of results	18	Summarize and/or present the charting results as they relate to the review questions and objectives.	Results App C
DISCUSSION			
Summary of evidence	19	Summarize the main results (including an overview of concepts, themes, and types of evidence available), link to the review questions and objectives, and consider the relevance to key groups.	Discussion
Limitations	20	Discuss the limitations of the scoping review process.	Discussion
Conclusions	21	Provide a general interpretation of the results with respect to the review questions and objectives, as well as potential implications and/or next steps.	Discussion
FUNDING			
Funding	22	Describe sources of funding for the included sources of evidence, as well as sources of funding for the scoping review. Describe the role of the funders of the scoping review.	Funding

JB1 = Joanna Briggs Institute; PRISMA-ScR = Preferred Reporting Items for Systematic reviews and Meta-Analyses extension for Scoping Reviews.

* Where *sources of evidence* (see second footnote) are compiled from, such as bibliographic databases, social media platforms, and Web sites.

† A more inclusive/heterogeneous term used to account for the different types of evidence or data sources (e.g., quantitative and/or qualitative research, expert opinion, and policy documents) that may be eligible in a scoping review as opposed to only studies. This is not to be confused with *information sources* (see first footnote).

‡ The frameworks by Arksey and O'Malley (6) and Levac and colleagues (7) and the JB1 guidance (4, 5) refer to the process of data extraction in a scoping review as data charting.

§ The process of systematically examining research evidence to assess its validity, results, and relevance before using it to inform a decision. This term is used for items 12 and 19 instead of "risk of bias" (which is more applicable to systematic reviews of interventions) to include and acknowledge the various sources of evidence that may be used in a scoping review (e.g., quantitative and/or qualitative research, expert opinion, and policy document).

From: Tricco AC, Lillie E, Zarin W, O'Brien KK, Colquhoun H, Levac D, et al. PRISMA Extension for Scoping Reviews (PRISMA-ScR): Checklist and Explanation. *Ann Intern Med*. 2018;169:467–473. doi: 10.7326/M18-0850.



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