

# Course Project (EE694)

Topic: Parallelize SVM Training algorithm

Group No: 33

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## SVM Algorithm:

1. For all  $x_i$  in training Data:

$$\begin{aligned} x_i \cdot w + b &\leq -1 && \text{if } y_i = -1 \text{ (belongs to -ve class)} \\ x_i \cdot w + b &\geq +1 && \text{if } y_i = +1 \text{ (belongs to +ve class)} \\ &&& \text{or} \\ &&& y_i(x_i \cdot w + b) \geq 1 \end{aligned}$$

2. For all support vectors(SV) (data points which decides margin)

$$\begin{aligned} x_i \cdot w + b &= -1 && \text{here } x_i \text{ is -ve SV and } y_i \text{ is -1} \\ x_i \cdot w + b &= +1 && \text{here } x_i \text{ is +ve SV and } y_i \text{ is +1} \end{aligned}$$

3. For decision Boundary  $y_i(x_i \cdot w + b) = 0$  here  $x_i$  belongs to point in decision boundary.

4. Our Objective is to maximize Width  $W = ((X_+ - X_-) \cdot w) / |w|$  or we can say minimize  $|w|$ .

5. Once we have found optimized  $w$  and  $b$  using algorithm

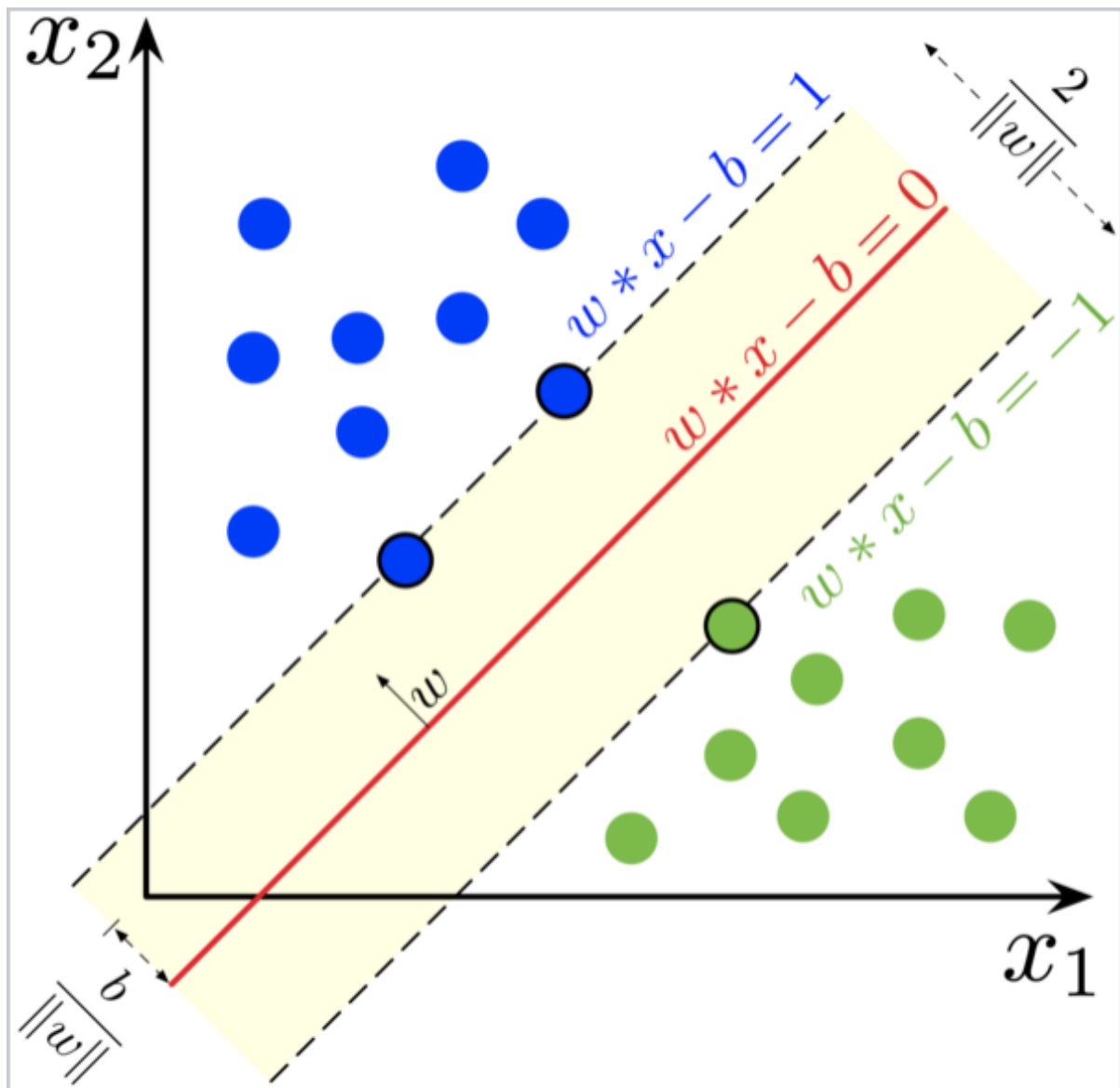
$x \cdot w + b = 1$  is line passing through +ve support vectors

$x \cdot w + b = -1$  is line passing through -ve support vectors

$x \cdot w + b = 0$  is decision boundary

6. It is not necessary that support vector lines always pass through support vectors.
7. It is a Convex Optimization problem and will always lead to a global minimum.
8. This is Linear SVM means kernel is linear.

Graphical representation:



## Algorithm in Code:

We try to fit a linear line that can separate the two classes and make the distances from either class is maximized.

The line is represented with  $w^*x + b = 0$

For label 1,  $w^*x + b \geq 1$

For label -1,  $w^*x + b \leq -1$

The distances of the gap in-between two classes is  $2/|w|$

We want to maximize this distance.

If we want to find a line that perfectly separates the two classes, we call this type of SVM cost function as Hard-Margin cost function.

If we allow some of the outliers to be misclassified, we can use Hinge-Loss when designing the cost function.

$$\max (0, 1 - y_i (\vec{w} \cdot \vec{x}_i - b)) .$$

Hinge Loss cost function

## Result:

### 1. Serial implementation of SVM

```
y = -0.411807*x1 + -0.143162*x2 + -0.176387  
Time elapsed to sequentially train a SVM is = 2.391562 seconds.
```

### 2. Parallel implementation of SVM (using OpenMP)

```
y = -0.417335*x1 + -0.154361*x2 + -0.165331  
Time elapsed to parallely train a SVM is = 1.502451 seconds.
```

### 3. Parallel implementation of SVM (using Pthreads)

```
y = -0.411807*x1 + -0.143162*x2 + -0.176387  
Time elapsed to train a SVM is = 0.923741 seconds with pthreads.
```

## Conclusion:

From the results we infer that, least time is taken by Pthread's implementation, and most time is taken by serial implementation.