

TUTAMU Chamber Aerosol Model (TUTAMUChAM) 1.0 Manual

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LIST OF SYMBOLS AND ABBREVIATIONS

Latin symbols

\bar{c}	mean thermal velocity of a particle
D_1	the lowest particle diameter in a power law distribution
D_2	the highest particle diameter in a power law distribution
D_{coag}	cut diameter for coagulation transfer
D_p	particle diameter
\mathcal{D}_p	particle diffusion coefficient
$f(\text{Kn}_{\text{coag}})$	transition regime function
g	condensational growth rate
i	index for the distribution, PL or LN
j	index for a size section
J	new particle formation rate
k	order of the moment
k_{dep}	deposition coefficient
Kn_{coag}	Knudsen number for coagulation
l_{bg}	exponent for the coagulation losses
m	index for a vapor
$M_{i,0}$	0 th moment, i.e. the number concentration, in distribution i
$M_{i,2}$	2 th moment in distribution i
$M_{i,3}$	3 th moment in distribution i
$M_{i,k}$	k^{th} moment in distribution i
N	particle number concentration
N_{bg}	number concentration of the background distribution
n_i	mode i density function
N_j	number concentration in the size section j
n_{LN}	the density function of the LN distribution
N_{LN}	the number concentration of the LN distribution
n_{PL}	the density function of the PL distribution
N_{PL}	the number concentration of the PL distribution
t	time
T	temperature
X	index for a moment

Greek symbols

α	slope parameter of the power law distribution
β	coagulation coefficient

γ	condensational transfer factor
ΔD_j	diameter width of the size section j
ρ_p	particle density
σ	geometric standard deviation of the LN distribution

Abbreviations

CMD	count median diameter
FS	fixed-sectional representation of the distribution
GMD	geometric mean diameter
GSD	geometric standard deviation
LN	log-normal distribution
NPF	new particle formation
PL	power law distribution
PL+LN	combined power law and log-normal distribution

1. CAPABILITIES AND LIMITATIONS

TUTAMUChAM is an aerosol dynamics model used in 0-D simulations with Matlab. New particle formation, condensation (not evaporation), coagulation, coagulation losses, depositional losses, and dilution can be simulated with the model. Also interaction between vapors and their depositional losses and dilution can be modelled. Particle size distribution can be represented modally or sectionally, but many features are available only when represented sectionally. The modal representation is computationally efficient but the distribution must have a pre-defined shape. [Table 1.1](#) shows the main limitations of the model.

Table 1.1: *Limitations of TUTAMUChAM.*

Size distribution represented modally	PL (power law), LN (log-normal), PL+LN
Size distribution represented sectionally	no limitations
Number of distributions	1
Immiscible phases in a particle	1
Miscible species in a particle	1
Particle diameter D_p	no limitations
Particle morphology	spherical
Temperature T	no limitations
Pressure p	no limitations

2. THEORY

2.1 Particle size distributions

The particle size distribution can be represented as a log-normal (LN) distribution, which provides the fastest simulation. In the case of simultaneous new particle formation and growth, the combined power law (PL) and log-normal distribution (PL+LN) can also be used. Additionally, it can be represented as a power law (PL) distribution only. If the size distribution cannot be fixed to a pre-defined shape, a fixed-sectional (FS) representation can be used (default). [Figure 2.1](#) represents a sample of a LN distribution. LN distribution has

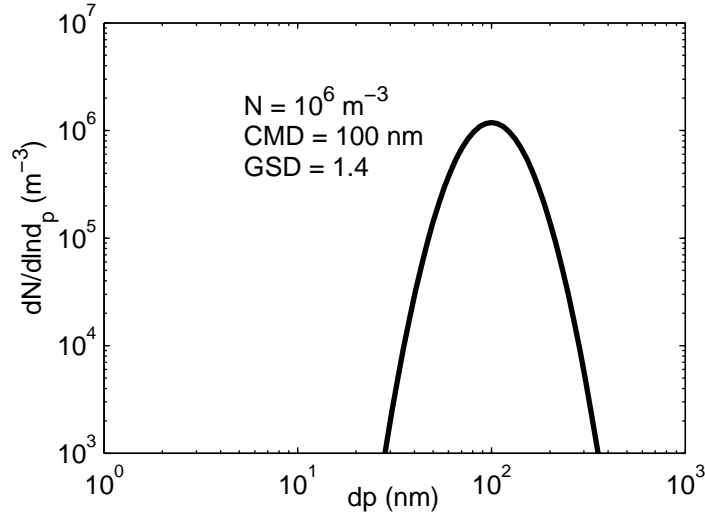


Figure 2.1: A log-normal aerosol distribution.

the following density function

$$n_{\text{LN}} = \left. \frac{dN}{d \ln D_p} \right|_{\text{LN}} = \frac{N_{\text{LN}}}{\sqrt{2\pi} \ln \sigma} \exp \left[-\frac{\ln^2 \left(\frac{D_p}{\text{CMD}} \right)}{2 \ln^2 \sigma} \right], \quad (2.1)$$

where N_{LN} is the total particle number concentration, dN is the particle number concentration within a logarithmic size range $d \ln D_p$, CMD is the count median diameter, σ is the geometric standard deviation, and D_p is the particle diameter ([Hinds, 1999](#)).

[Figure 2.2](#) represents samples of PL distributions and of a combined PL+LN distribution. PL distribution has the following density function

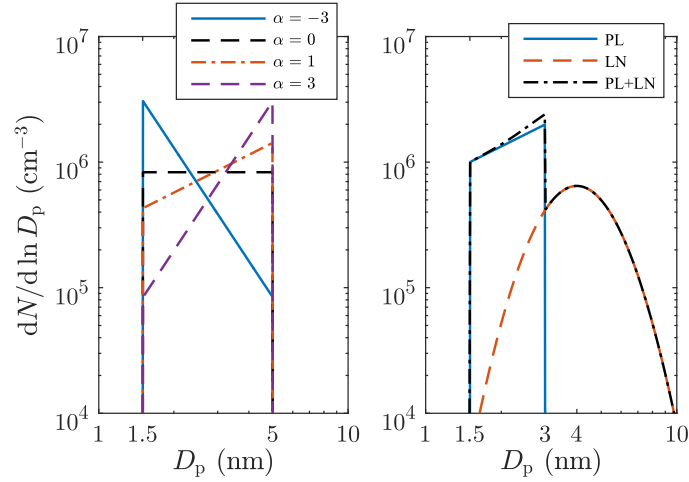


Figure 2.2: Left pane represents examples of the power law distribution with different values of α . Right pane represents the combination of power law and log-normal distributions. (Olin et al., 2016)

$$n_{\text{PL}} = \left. \frac{dN}{d \ln D_p} \right|_{\text{PL}} = \begin{cases} \frac{N_{\text{PL}} \alpha}{D_2^\alpha - D_1^\alpha} D_p^\alpha, & D_1 \leq D_p \leq D_2, \alpha \neq 0 \\ \frac{N_{\text{PL}}}{\ln(D_2/D_1)}, & D_1 \leq D_p \leq D_2, \alpha = 0 \\ 0, & \text{otherwise} \end{cases} \quad (2.2)$$

where α is the slope parameter, D_1 is the smallest diameter, and D_2 is the largest diameter of the PL distribution (Olin et al., 2016). In the PL+LN model, the total distribution is expressed with

$$n_{\text{PL+LN}} = n_{\text{PL}} + n_{\text{LN}}. \quad (2.3)$$

More information on the PL+LN model can be found in Olin et al. (2016).

Figure 2.3 represents a sample of an FS40 (fixed-sectional distribution having 40 size sections between 1.6 and 100 nm) distribution.

2.2 Moments of a distribution

A log-normal distribution function (Eq. 2.1) requires 3 parameters (N, CMD, σ) to represent the particle concentration dN for a size D_p . Therefore, modelling of a log-normal distribution requires 3 variables and 3 equations to be modelled. A power law distribution requires 4 parameters (N, α, D_1, D_2) of which D_1 has a constant value. Therefore, 3 variables are required for the PL distribution also. These variables are the k^{th} moments of a distribution that are defined as

$$M_{i,k} = \int_{-\infty}^{\infty} D_p^k n_i d \ln D_p, \quad (2.4)$$

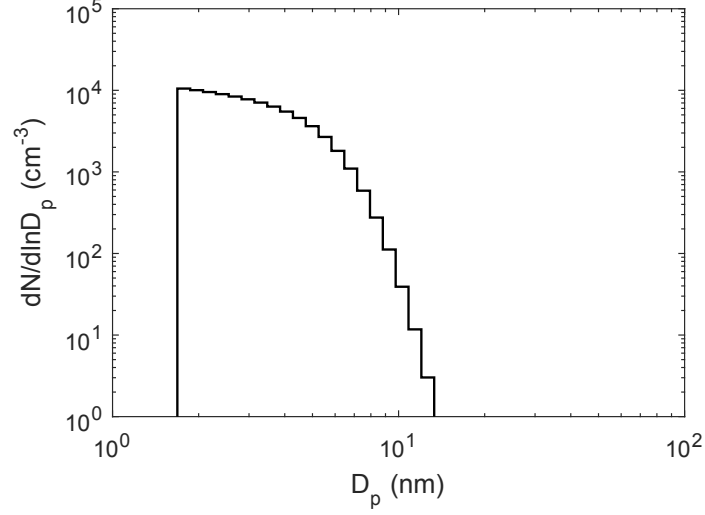


Figure 2.3: Particle size distribution represented by the FS40 model.

where i denotes the distribution, PL or LN. The 3 moments [and their units] used in TUTAMUCHAM are

$$\begin{aligned} M_{i,0} & [1/\text{cm}^3] \\ M_{i,2} & [\text{nm}^2/\text{cm}^3] \\ M_{i,3} & [\mu\text{g}^2/\text{m}^3] \end{aligned} \quad (2.5)$$

which correspond to number concentration, surface area concentration (internally without π^{-1}), and mass concentration (internally without $6\pi^{-1}\rho_p^{-1}$), respectively.

When 3 moments are known, the 3 parameters of a log-normal distribution can be calculated by (Whitby and McMurry, 1997)

$$\begin{aligned} N_{\text{LN}} &= M_{\text{LN},0} \\ \sigma &= \exp \left(\sqrt{\ln \frac{M_{\text{LN},3}^{\frac{2}{3}} M_{\text{LN},0}^{\frac{1}{3}}}{M_{\text{LN},2}}} \right) \\ CMD &= \left(\frac{M_{\text{LN},3}}{M_{\text{LN},0}} \right)^{\frac{1}{3}} e^{-1.5 \ln^2 \sigma}, \end{aligned} \quad (2.6)$$

Reconstruction of the parameters of PL distribution from 3 moments is done either using an interpolation table as described in Olin et al. (2016) or using the Levenberg-Marquardt iteration algorithm. In the PL+LN model, totally 6 moments are modelled.

2.3 General dynamic equation for the moments in modal method

Aerosol dynamics is modelled with the following equation

$$\frac{dX}{dt} = \text{dilu}_X + \text{npf}_X + \text{cond}_X + \text{coag}_X + \text{loss}_X^{\text{coag}} + \text{loss}_X^{\text{dep}} + \text{transfer}_X^{\text{coag}} + \text{transfer}_X^{\text{cond}} \quad (2.7)$$

where X denotes a particular moment.

2.3.1 Dilution

The dilution term in [Eq. 2.7](#) is

$$\text{dilu}_X = k_{\text{dilution}} X \quad (2.8)$$

where k_{dilution} is the dilution rate [1/s].

2.3.2 New particle formation

The new particle formation (NPF) term in [Eq. 2.7](#) is

$$\begin{aligned} \text{npf}_{M_{i,0}} &= J(t) \\ \text{npf}_{M_{i,2}} &= J(t) D_1^2 \\ \text{npf}_{M_{i,3}} &= J(t) D_1^3, \end{aligned} \quad (2.9)$$

where $J(t)$ is the new particle formation rate [1/cm³s] as a function of time, D_1 is the diameter of a newly formed particle. In the PL+LN model, new particles are formed only in the PL distribution.

2.3.3 Condensation

The condensation term in [Eq. 2.7](#) is

$$\text{cond}_X = \begin{cases} 0, & X = M_{i,0} \\ 2 g(t) \int_{-\infty}^{\infty} D_p dN_i, & X = M_{i,2} \\ 3 g(t) \int_{-\infty}^{\infty} D_p^2 dN_i, & X = M_{i,3} \end{cases} \quad (2.10)$$

where $g(t)$ is the condensational growth rate [m/s] as a function of time and dN_i is an abbreviation of $n_i d \ln D_p$. An analytical solution for the term is included in the model code.

2.3.4 Coagulation

Coagulation is modelled as intramodal coagulation within the PL distribution and within the LN distribution, and, in the PL+LN model, as intermodal coagulation from the PL distribution to the LN distribution. The coagulation terms derived from the equations of [Whitby and McMurry \(1997\)](#) are

$$\begin{aligned} \text{coag}_{M_{\text{PL},0}} = & -\frac{1}{2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{PL}} \\ & - \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{LN}} \end{aligned} \quad (2.11)$$

$$\begin{aligned} \text{coag}_{M_{\text{PL},2}} = & -\frac{1}{2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left[2D_p^2 - (D_p^3 + D_p'^3)^{\frac{2}{3}} \right] \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{PL}} \\ & - \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} D_p^2 \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{LN}} \end{aligned} \quad (2.12)$$

$$\text{coag}_{M_{\text{PL},3}} = - \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} D_p^3 \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{LN}} \quad (2.13)$$

$$\text{coag}_{M_{\text{LN},0}} = -\frac{1}{2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \beta(D_p, D'_p) dN_{\text{LN}} dN'_{\text{LN}} \quad (2.14)$$

$$\begin{aligned} \text{coag}_{M_{\text{LN},2}} = & -\frac{1}{2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left[2D_p^2 - (D_p^3 + D_p'^3)^{\frac{2}{3}} \right] \beta(D_p, D'_p) dN_{\text{LN}} dN'_{\text{LN}} \\ & + \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left[(D_p^3 + D_p'^3)^{\frac{2}{3}} - D_p^2 \right] \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{LN}} \end{aligned} \quad (2.15)$$

$$\text{coag}_{M_{\text{LN},3}} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} D_p^3 \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{LN}}, \quad (2.16)$$

where $\beta(D_p, D'_p)$ is the coagulation coefficient of particles with the diameters of D_p and D'_p calculated with the equation

$$\beta(D_p, D'_p) = 2\pi(D_p + D'_p)(\mathcal{D}_p + \mathcal{D}'_p)f(\text{Kn}_{\text{coag}}), \quad (2.17)$$

where $f(\text{Kn}_{\text{coag}})$ is the transition regime function of [Dahneke \(1983\)](#)

$$f(\text{Kn}_{\text{coag}}) = \frac{1 + \text{Kn}_{\text{coag}}}{1 + 2\text{Kn}_{\text{coag}} + 2\text{Kn}_{\text{coag}}^2}, \quad (2.18)$$

where Kn_{coag} is the Knudsen number for coagulation

$$\text{Kn}_{\text{coag}} = \frac{4(\mathcal{D}_p + \mathcal{D}'_p)}{(D_p + D'_p)\sqrt{\bar{c}^2 + \bar{c}'^2}}, \quad (2.19)$$

where \bar{c} and \bar{c}' are the mean thermal velocities of particles with the diameters of D_p and D'_p . Diffusion coefficients \mathcal{D}_p and \mathcal{D}'_p are calculated according to [Hinds \(1999\)](#) with the slip

correction coefficient.

The integrals in Eqs. (2.11) – (2.16) cannot be solved analytically in the transition regime because Eq. (2.18) cannot be presented in a polynomial form. Therefore, the integrals are calculated numerically or by using quadrature techniques. By default, in the case of the PL distribution, the integrals are solved numerically using 20 size sections, when $D_2/D_1 > 3$, and using the Gauss-Olin quadrature described in Olin et al. (2016), otherwise. In the case of the LN distribution, the Gauss-Hermite quadrature is used in calculation of the integrals.

2.3.5 Coagulation losses

Particles in the background distribution excluded from the modelled distribution are assumed to be significantly larger than the other particles. Therefore, the particle diameters of the background distribution can be approximated with a single diameter value, e.g., CMD_{bg} (count median diameter). According to Kerminen and Kulmala (2002), the coagulation coefficient will then become

$$\beta(D_p, \text{CMD}_{\text{bg}}) \approx \beta(D_1, \text{CMD}_{\text{bg}}) \left(\frac{D_p}{D_1} \right)^{l_{\text{bg}}}, \quad (2.20)$$

where l_{bg} is the exponent depending on CMD_{bg} . The value of l_{bg} ranges between -2 and -1 (Lehtinen et al., 2007), the default value being -1.6. The coagulation loss term for zeroth moment is

$$\text{loss}_{N_i}^{\text{coag}} = -N_{\text{bg}} \beta(D_1, \text{CMD}_{\text{bg}}) D_1^{-l_{\text{bg}}} \int_{-\infty}^{\infty} D_p^{l_{\text{bg}}} dN_i, \quad (2.21)$$

where N_{bg} is the number concentration of the background distribution (Olin et al., 2016). An analytical solution is included in the model code.

2.3.6 Depositional losses

The depositional losses are modelled with

$$\text{loss}_{N_i}^{\text{dep}} = -k_{\text{dep}} \int_{-\infty}^{\infty} D_p^{-1} dN_i \quad (2.22)$$

where k_{dep} is the deposition coefficient [m/s] (Olin et al., 2016). An analytical solution is included in the model code.

2.3.7 Coagulation transfer

Particles in the PL mode can be transferred to a LN mode using

$$\text{transfer}_{M_{\text{PL},0}} = -\text{transfer}_{M_{\text{LN},0}} = -\frac{1}{2} \int_{-\infty}^{\infty} \int_{\ln D_{\text{coag}}}^{\infty} \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{PL}} \quad (2.23)$$

$$\text{transfer}_{M_{\text{PL},2}} = -\text{transfer}_{M_{\text{LN},2}} = -\frac{1}{2} \int_{-\infty}^{\infty} \int_{\ln D_{\text{coag}}}^{\infty} (D_p^3 + D_p'^3)^{\frac{2}{3}} \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{PL}} \quad (2.24)$$

$$\text{transfer}_{M_{\text{PL},3}} = -\text{transfer}_{M_{\text{LN},3}} = -\frac{1}{2} \int_{-\infty}^{\infty} \int_{\ln D_{\text{coag}}}^{\infty} (D_p^3 + D_p'^3) \beta(D_p, D'_p) dN_{\text{PL}} dN'_{\text{PL}}, \quad (2.25)$$

where D_{coag} is the cut diameter

$$D_{\text{coag}} = (D_2^3 - D_p'^3)^{1/3} \quad (2.26)$$

which is the smallest particle that forms a particle larger than D_2 after coagulating with a particle having a diameter of D'_p , assuming full coalescence (Olin et al., 2016).

2.3.8 Condensation transfer

Some of the particles are transferred from the PL mode to the LN mode using the condensational transfer. It is modelled with

$$\text{transfer}_X^{\text{cond}} = \gamma \frac{g(t)}{D_2} n_{\text{PL}}(D_p = D_2) \cdot \begin{cases} -1, & X = M_{\text{PL},0} \\ -D_2^2, & X = M_{\text{PL},2} \\ -D_2^3, & X = M_{\text{PL},3} \\ +1, & X = M_{\text{LN},0} \\ +D_2^2, & X = M_{\text{LN},2} \\ +D_2^3, & X = M_{\text{LN},3} \end{cases}, \quad (2.27)$$

where γ is the condensational transfer factor having the value of 0.5 by default (Olin et al., 2016).

2.4 General dynamic equation in sectional method

Aerosol dynamics is modelled with the following equation

$$\frac{dN_j}{dt} = \text{dilu}_j + \text{npf}_j + \text{cond}_j + \text{coag}_j + \text{loss}_j^{\text{coag}} + \text{loss}_j^{\text{dep}} \quad (2.28)$$

where j denotes a size section.

2.4.1 New particle formation

The new particle formation (NPF) term in Eq. 2.28 is

$$\text{npf}_j = \begin{cases} J(t), & j = 1 \\ 0, & j > 1 \end{cases}. \quad (2.29)$$

2.4.2 Condensation

The condensation term in Eq. 2.28 is

$$\text{cond}_j = \begin{cases} -N_j \frac{g(t)}{\Delta D_j}, & j = 1 \\ -N_j \frac{g(t)}{\Delta D_j} + N_{j-1} \frac{g(t)}{\Delta D_{j-1}}, & j > 1 \end{cases} \quad (2.30)$$

where ΔD_j is the diameter width of the section j .

2.4.3 Coagulation

The coagulation term is

$$\text{coag}_j = -N_j \sum_{j'=1}^{\infty} \beta(D_j, D_{j'}) N_{j'} + \frac{1}{2} \sum_{j'=1}^{j-1} \beta(D_{j'}, D_{j-j'}) N_{j'} N_{j-j'}. \quad (2.31)$$

2.4.4 Coagulation losses

The coagulation loss term is

$$\text{loss}_j^{\text{coag}} = -N_{\text{bg}} \beta(D_1, \text{CMD}_{\text{bg}}) D_1^{-l_{\text{bg}}} D_j^{l_{\text{bg}}} N_j. \quad (2.32)$$

2.4.5 Depositional losses

The depositional loss term is

$$\text{loss}_j^{\text{dep}} = -\frac{k_{\text{dep}}}{D_j} N_j. \quad (2.33)$$

3. USING TUTAMUCHAM

The TUTAMUChAM model is used with Matlab. It has been tested with Matlab R2023a but should work with other versions as well.

3.1 Launching the model

The model uses two structs, **p** and **out**, which denote input parameter setup and the output of the simulation, respectively. If **p** does not exist in the workspace, it needs to be created by typing the command `initialize`, which loads the default parameter setup, asks your own setup file, and creates **p** struct into the workspace.

You can make your own setup file in `.m` format that contains at least the input variables that do not have the default values. You can use `defaultSetupFile.m` file as a model in making your own setup file. The parameters and their default values are described next.

p.model How the distribution is modelled: power law ('PL'), log-normal ('LN'), combination ('PLLN'), fixed-sectional with *n* size sections ('FSn'). The LN model is the fastest model and it can be used in the most cases. The PL+LN model provides more accuracy especially in the cases of simultaneous new particle formation and growth. The most accurate model is the FS model, but the computational cost is significantly higher.

p.PLEquations How the system of equations in the PL model is solved: interpolation table (1), Levenberg-Marquardt iteration algorithm (2, default).

p.JMatrix New particle formation rate, $J(t)$ [$1/\text{cm}^3 \text{ s}$], in a matrix form. The top row denotes the times [s] and the bottom row the rates at those times. The default matrix

$$\begin{bmatrix} 0 & 3600 \\ 0 & 1 \end{bmatrix} \quad (3.1)$$

denotes the following function

$$J(t) = \begin{cases} 0 \text{ cm}^{-3} \text{ s}^{-1}, & t \leq 0 \text{ s} \\ 1 \text{ cm}^{-3} \text{ s}^{-1}, & t \leq 3600 \text{ s} \end{cases} \quad (3.2)$$

Make sure that the highest time in the matrix is not less than the highest simulation time. The number of columns in the matrix is not limited, and it can also be one. E.g.,

the matrix

$$\begin{bmatrix} \text{inf} \\ 1 \end{bmatrix} \quad (3.3)$$

denotes that J has a constant value of $1 \text{ cm}^{-3} \text{ s}^{-1}$.

p.dCluster The diameter of a newly formed particle [m]. It also describes the smallest diameter that is modelled in the FS model. The default value is 1 nm.

p.highestDiameter The highest diameter in the FS model. The default value is 100 nm.

p.GRModel If growth rates are modelled (1) or just inputted as a matrix (0). If they are modelled, also new particle formation becomes modelled and vapor transport equation will be used.

p.GRMatrix Condensational growth rate if (p.GRModel is 0), $g(t)$ [m/s], in a matrix form. The default matrix

$$\begin{bmatrix} 0 & 3600 \\ 0 & 3\text{e-}12 \end{bmatrix} \quad (3.4)$$

denotes the following function

$$g(t) = \begin{cases} 0 \text{ m s}^{-1}, & t \leq 0 \text{ s} \\ 3 \cdot 10^{-12} \text{ m s}^{-1}, & t \leq 3600 \text{ s} \end{cases}. \quad (3.5)$$

p.nVapor The number of modelled vapors (if GR are modelled).

p.vaporName Names of the modelled vapors (if GR are modelled).

p.vaporConc0 Initial concentrations [$\mu\text{g}/\text{m}^3$] of the modelled vapors (if GR are modelled).

p.molarMass Molar masses [kg/mol] of the modelled vapors (if GR are modelled).

p.dMolec Molecule diameters [m] of the modelled vapors (if GR are modelled).

p.diffMolec Diffusion coefficients [m^2/s] of the modelled vapors in air (if GR are modelled).

p.CSat Saturation concentrations [$\mu\text{g}/\text{m}^3$] of the modelled vapors (if GR are modelled).

p.surfaceTension Surface tensions [N/m] of the modelled vapors (if GR are modelled).

p.accommodationCoefficient Accommodation coefficients of the modelled vapors (if GR are modelled).

p.nucleationExponent Nucleation exponents of the modelled vapors (if GR are modelled).

p.nucleationCoefficient Nucleation coefficients of the modelled vapors (if GR are modelled).

- p.vaporWallLossRates** Wall loss rates [1/s] of the modelled vapors (if GR are modelled).
- p.vaporsTransportEquation** Transport equations the modelled vapors (if GR are modelled), denoting the interactions between the vapors (not including dilution, wall losses, or gas-to-particle conversion).
- p.condensationalTransfer** Is the condensational transfer on with the PL+LN model? Is [Eq. 2.27](#) calculated? 1 (on, default) or 0 (off). In the most cases, it should be on.
- p.condensationalTransferFactor** The condensational transfer factor, γ , in [Eq. 2.27](#) with the PL+LN model. The range is 0 ... 1 and the default value is 0.5. You can add log-normal features to the output distribution by increasing the value towards unity. More guidelines to choose the value can be found in [Olin et al. \(2016\)](#).
- p.coag** Is coagulation on? 1 (on, default) or 0 (off).
- p.coagulationTransfer** Is the coagulation transfer on with the PL+LN model? Are [Eq. 2.23](#) – [Eq. 2.25](#) calculated? 1 (on, default) or 0 (off). Either the condensational transfer or the coagulation transfer must be on for the LN distribution to form with the PL+LN model. If γ is high, the coagulation transfer can be neglected to save some computing time.
- p.binsInCoagulation** Size bins in the numeric integration of coagulation terms with the modal method. The default values is 20. Integrals in calculating coagulation terms are double integral; thus, increasing the number of size bins increases the associated computing time squarely.
- p.numericCoagulation** Are integrals in the coagulation terms always calculated numerically with the modal method? 1 (on) or 0 (off, default). If you experience numerical problems, you can try to set this on.
- p.T** Temperature [K] of the carrier gas. The default value is 300 K. It can also be a time dependent function, as in the case of **p.JMatrix**. However, coagulation equations use only the mean temperature.
- p.visc** Dynamic viscosity [Pa s] of the carrier gas. The default value is $1.85 \cdot 10^{-5}$ Pa s which is calculated through **viscosity** function. The size is the same as the size of **p.T**.
- p.rho** Particle bulk density [kg/m³]. The default value is 1000 kg/m³.
- p.sizeDependentGR** Is a size-dependent function, $g(t, D_p)$, used for the condensational growth? It is not yet supported in this version; thus, the value must be 0.
- p.coagSink** Are the coagulation losses to the background distribution included? Is [Eq. 2.21](#) or [Eq. 2.32](#) calculated? 1 (on, default) or 0 (off).

p.coagSinkCMD CMD [m] of the background distribution causing the coagulation losses. The default value is 100 nm.

p.coagSinkExponent The exponent for the coagulation losses, l_{bg} . The range is -2 ... -1 and the default value is -1.6 that corresponds to the CMD of 100 nm. Refer, e.g., [Lehtinen et al. \(2007\)](#) to choose the appropriate value.

p.coagSinkN The number concentration [cm^{-3}] of the background distribution causing the coagulation losses. The default value is 1000 cm^{-3} .

p.losses Are the depositional losses included? Is [Eq. 2.21](#) or [Eq. 2.33](#) calculated? 1 (on, default) or 0 (off).

p.lossesMethod The method for simulating depositional losses of particles. It can be 'exponent', 'vector', or 'equation'. With the 'exponent' method, the losses are based on [Eq. 2.33](#) if p.lossesExponent is -1. With the 'vector' method, the losses are given separately for each modelled particle size. With the 'equation' method, the losses are calculated using a custom equation (depending on dp).

p.lossesCoeff The deposition coefficient (value, vector, or equation), k_{dep} [m/s if the exponent method is used and the exponent is -1] [1/s otherwise].

p.lossesExponent The exponent for the depositional losses. The default value is -1 that works well with particles smaller than 100 nm.

p.dilutionRateMatrix Dilution rate [1/s], in a matrix form. The default matrix

$$\begin{bmatrix} 0 & 3600 \\ 0 & 0 \end{bmatrix} \quad (3.6)$$

denotes the following function

$$dilu(t) = \begin{cases} 0 \text{ s}^{-1}, & t \leq 0 \text{ s} \\ 0 \text{ s}^{-1}, & t \leq 3600 \text{ s} \end{cases}. \quad (3.7)$$

p.timeVec Time [s] vector to be simulated with the model. The default value is 0:3600 which denotes that the time domain to be simulated is from the time of 0 s to the time of 3600 s and that the simulation result is output with 1-second time resolution.

p.initialPSDMethod How the initial particle size distribution is given. For FS models, it can be either **parameters** or **vector**. For PLLN model, it can be either **parameters** or **moments**.

p.initialPSDMethod p.initialPSDParameters Parameters for initial particle size distribution if given as parameters.

p.initialMomentVec The vector of the moments or the concentrations of the size sections, initially. The vector must be in the size of $1 \times n$ where n is 6 with the modal method, and the number of size sections with the sectional method. The meanings of the cells in the vector are, with the modal method, $[M_{PL,0}, M_{PL,2}, M_{PL,3}, M_{LN,0}, M_{LN,2}, M_{LN,3}]$.

p.solverName The name of the ODE-solver. The default value is 'ode45'. Refer Matlab documentation to choose the solver.

p.relativeTolerance The relative tolerance for the ODE solver. The default value is 10^{-3} .

p.plotDistrDuringSim Are distributions plotted during the simulation? 1 (on, default) or 0 (off). Plotting slows down the simulation.

p.plotWaitbarDuringSim Is waitbar shown during the simulation? 1 (on, default) or 0 (off). Showing the waitbar slows down the simulation.

p.plotOutputAfterSim Is the model output plotted after the simulation? 1 (on, default) or 0 (off).

3.2 Running a simulation

The simulation can be run by typing the command **simulate**. After the simulation is complete, **out** struct is created to the workspace. It contains the time series of the output variables, depending on the time vector, **p.timeVec**. The contents of **out** struct are described next.

out.t Time [s] vector. Same as **p.timeVec** but transposed.

out.Y Time series of the moments (modal method) or the number concentrations of the size sections (sectional method). The meanings of the cells are the same as with **p.initialMomentVec**.

out.p The input parameter set used in the simulation. Some additional variables for the internal usage of the model are also included in that.

out.N_LN The number concentrations [cm^{-3}] of the log-normal distribution with the modal method.

out.CMD Count median diameters [m] of the log-normal distribution with the modal method.

out.sigma Geometric standard deviations σ [m] of the log-normal distribution with the modal method.

out.N_PL The number concentrations $[\text{cm}^{-3}]$ of the power law distribution with the modal method.

out.alpha The slope parameters α of the power law distribution with the modal method.

out.D2 The largest particle diameters D_2 $[\text{m}]$ of the power law distribution with the modal method.

out.N The total number concentrations N $[\text{cm}^{-3}]$.

out.M_2 The total 2nd moments M_2 $[\text{nm}^2 \text{ cm}^{-3}]$.

out.M_3 The total 3rd moments M_3 $[\mu\text{g m}^{-3}]$.

out.GMD Geometric mean diameters $[\text{m}]$ of the total distribution.

out.GSD Geometric standard deviations of the total distribution.

3.3 Running another simulation

Once `p` struct exist, a simulation can be run with different parameter set (1) by changing the variables directly in the Matlab's workspace, (2) by changing the variables through the Matlab's command line, or (3) by loading another setup file by typing the command `initialize`. After that, type the command `simulate`.

If you want to run the model in a batch process, make a script that alters the parameter set struct `p`, runs a simulation with the command `simulate`, and stores the output from `out` struct to another variable.

3.4 Plotting results

If `p.plotDistrDuringSim` is set to 1, the distribution at the end of the simulation is seen when the simulation is finished. If `p.plotOutputAfterSim` is set to 1, the time series of the outputs are plotted when the simulation is finished. You can plot the time series after the simulation by typing the command `plotOutput(out)`. The output plotted contains the time series of number concentration and 2nd and 3rd moments. In the case of the modal method, the parameters of the distributions are also plotted.

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