

Searching Algorithms are specific **Algorithms** a computer can use to **search** for **data** in an **array** (list).

Binary Search	Linear Search																																																																																																							
<p>Used to efficiently search large sorted lists of data for a specific item.</p> <p>Example: Binary Search for 51</p> <div><p>Binary Search for 50 in 7 elements Array</p><div><div>Given Array</div><table><tr><td>1</td><td>5</td><td>20</td><td>35</td><td>50</td><td>65</td><td>70</td></tr><tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td colspan="2">start</td><td colspan="3"></td><td colspan="2">end</td></tr></table><div><div>mid=$\frac{0+6}{2}$ =3</div><table><tr><td>1</td><td>5</td><td>20</td><td>35</td><td>50</td><td>65</td><td>70</td></tr><tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td colspan="2"></td><td colspan="3">start</td><td colspan="2">end</td></tr></table><div><div>mid=$\frac{4+6}{2}$ =5</div><table><tr><td>1</td><td>5</td><td>20</td><td>35</td><td>50</td><td>65</td><td>70</td></tr><tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td colspan="4"></td><td colspan="3">start</td></tr></table><div><div>mid=$\frac{4+4}{2}$ =4</div><table><tr><td>1</td><td>5</td><td>20</td><td>35</td><td>50</td><td>65</td><td>70</td></tr><tr><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td colspan="4"></td><td colspan="3">start</td></tr></table></div><div><div>35 < 50 Take 2nd Half</div><div>65 > 50 Take 1st Half</div><div>50 Found Return 50</div></div></div></div></div><p>Advantages Binary searches are more suitable for large lists. In general takes less steps than a linear search.</p><p>Disadvantages Not suitable for small lists. They can only be used on ordered lists</p></div>	1	5	20	35	50	65	70	0	1	2	3	4	5	6	start					end		1	5	20	35	50	65	70	0	1	2	3	4	5	6			start			end		1	5	20	35	50	65	70	0	1	2	3	4	5	6					start			1	5	20	35	50	65	70	0	1	2	3	4	5	6					start			<p>Algorithm:</p> <pre>mylist = [1,2,5,7,11,14] item= input() found = False first = 0 last = len(mylist) - 1 WHILE found = False AND first <= last midPoint = (first + last) DIV 2 IF item ==mylist[midpoint] then PRINT "item found at location", midpoint found = True ELSE IF item < mylist[midpoint] then last = midpoint - 1 ELSE first = midpoint + 1 END IF END IF END WHILE</pre> <p>Complexity: O(log N) logarithmic</p>	<p>Linear search is an algorithm that can used on any list to find a specific item. To complete a linear search you simply start with the first item and compare it to the search item. This process is repeated till the search item has been found.</p> <div><p>go through these positions, until element found and then stop</p><div><div>index</div><div>begin here</div><table><tr><td>10</td><td>8</td><td>1</td><td>21</td><td>7</td><td>32</td><td>5</td><td>11</td><td>0</td></tr><tr><td>arr[0]</td><td>arr[1]</td><td>arr[2]</td><td>arr[3]</td><td>arr[4]</td><td>arr[5]</td><td>arr[6]</td><td>arr[7]</td><td>arr[8]</td></tr></table><div>Stop</div></div><p>Element to search : 5</p></div> <p>Algorithm</p> <pre>letters_list = ['A', 'F', 'B', 'E', 'D','G','C'] position =0 found = False search_item =input() WHILE position < len(letters_list) AND found == False IF search_item == letters_list[position]: PRINT "Item found at position", position + 1 found = True ELSE: position = position + 1 ENDIF If found == False: print("Item not found") END WHILE</pre> <p>Advantages Linear search can be used on any list. Very efficient on small lists.</p> <p>Disadvantages: This algorithm is not very efficient on large lists. Usually takes more steps than a Binary search.</p> <p>Complexity: O(N) – Linear</p>	10	8	1	21	7	32	5	11	0	arr[0]	arr[1]	arr[2]	arr[3]	arr[4]	arr[5]	arr[6]	arr[7]	arr[8]
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Bubble sort

To complete this sort you must compare the first and second item of the list, if the right item is the smallest swap the items around.

65	40	30	10	100	6	Swapping Performed
40	65	30	10	100	6	Swapping Performed
40	30	65	10	100	6	Swapping Performed
40	30	10	65	100	6	No Swapping
40	30	10	65	100	6	Swapping Performed
40	30	10	65	6	100	Largest Element Found

Advantages

This algorithm works very well for small lists.

Disadvantages:

Even when the list is sorted each number still needs comparing to check. This is very slow to run as the algorithm has to do multiple passes of the data.

This algorithm is very inefficient for large sets of data.

Algorithm

```
swapMade = True
```

```
WHILE swapMade
```

```
    swapMade = False
```

```
    position = 0
```

```
    FOR position=0 to listLength-2
```

```
        IF list[position]>list[position+1] then
```

```
            temp = list[position]
```

```
            list[position] = list[position+1]
```

```
            list[position+1] = temp
```

```
            swapMade = True
```

```
        ENDIF
```

```
    END FOR
```

```
END WHILE
```

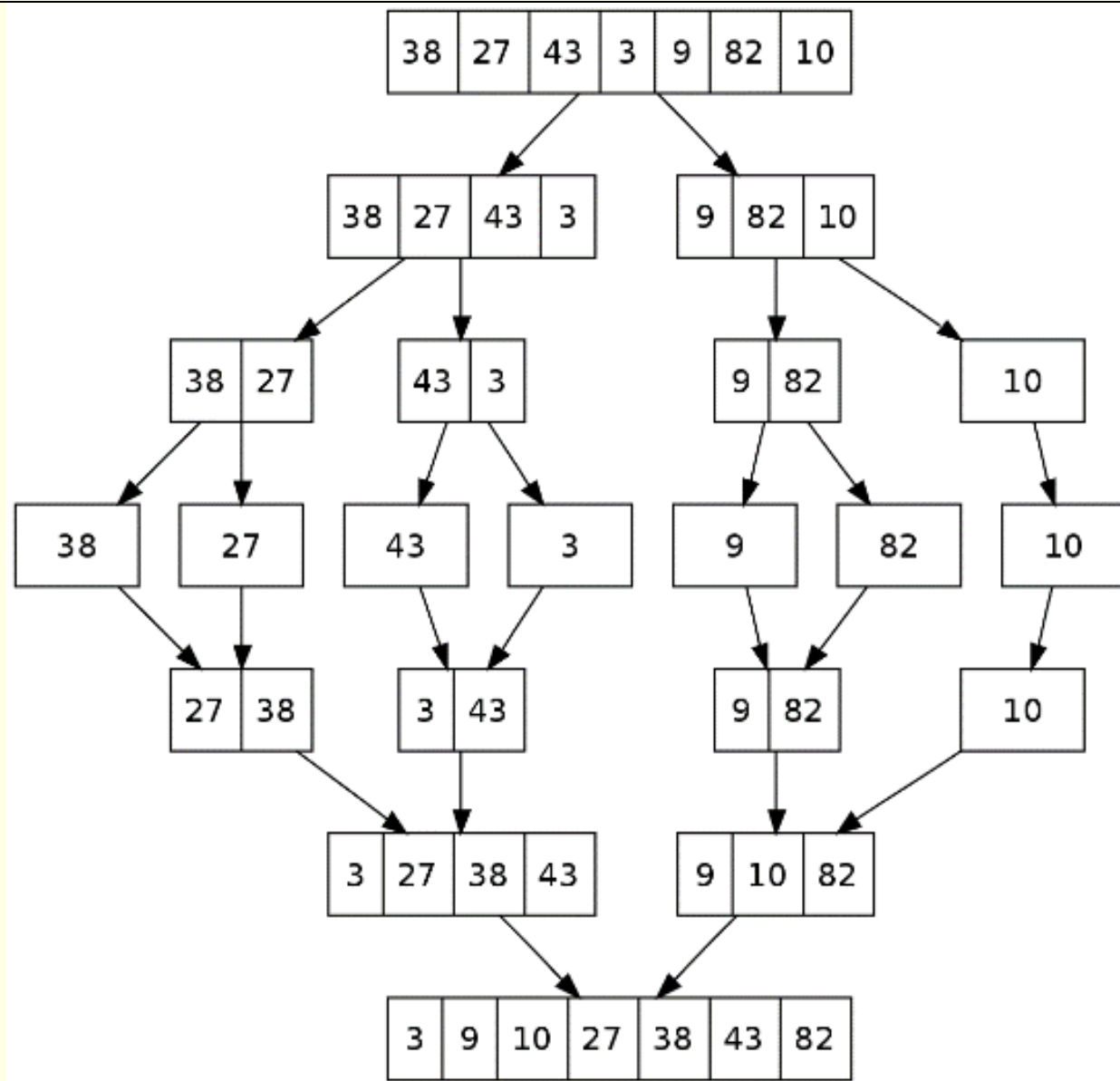
It will continue to pass through the data until it has no swaps

Loops through the elements in the list

Compare the first and second item and makes a swap if first item is greater than second item.

Complexity: $O(n^2)$ polynomial

Merge Sort Can be used efficiently on very large lists of data.



Algorithm

Step 1: Split the arrays into sub-arrays of 1 element.

Step 2: Take each sub-array and merge into a new, sorted array.

Step 3: Repeat this process until a final, sorted array is produced.

Output: A sorted array

Advantages

Very high performance on any list.

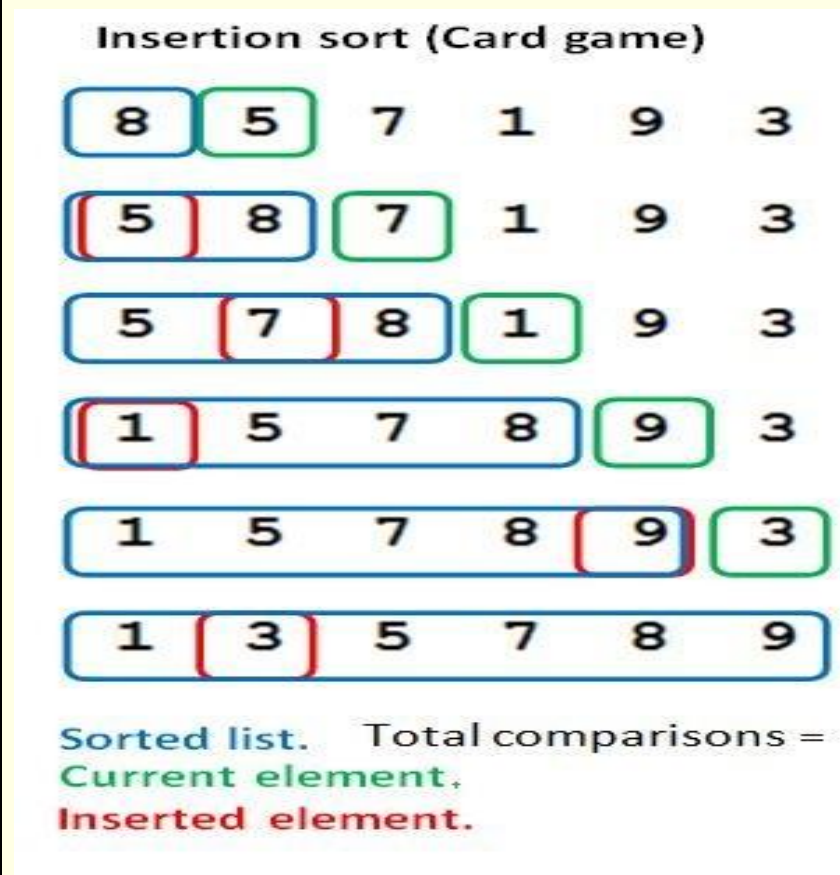
Disadvantages:

Uses a lot of memory space to run the algorithm.

Complexity

$O(n \log n)$ —logarithmic. This shows Merge Sort to be substantially faster than the Bubble and Selection Sort.

Insertion Sort - used to **sort** a live list of data.



Advantages

Very high performance in small lists.

This algorithm can work on live list where the data is still coming in.

Disadvantages:

Poor performance with large lists. Not as fast as a merge sort.

Algorithm

1. Look at the second item in the list
2. Compare it to all items before and insert the item in the correct place
3. Repeat step 2 until you get the end by moving to the next number and placing it into the correct place.

FOR position 1 to len(array -1)

currentValue = array[position]
pos = position

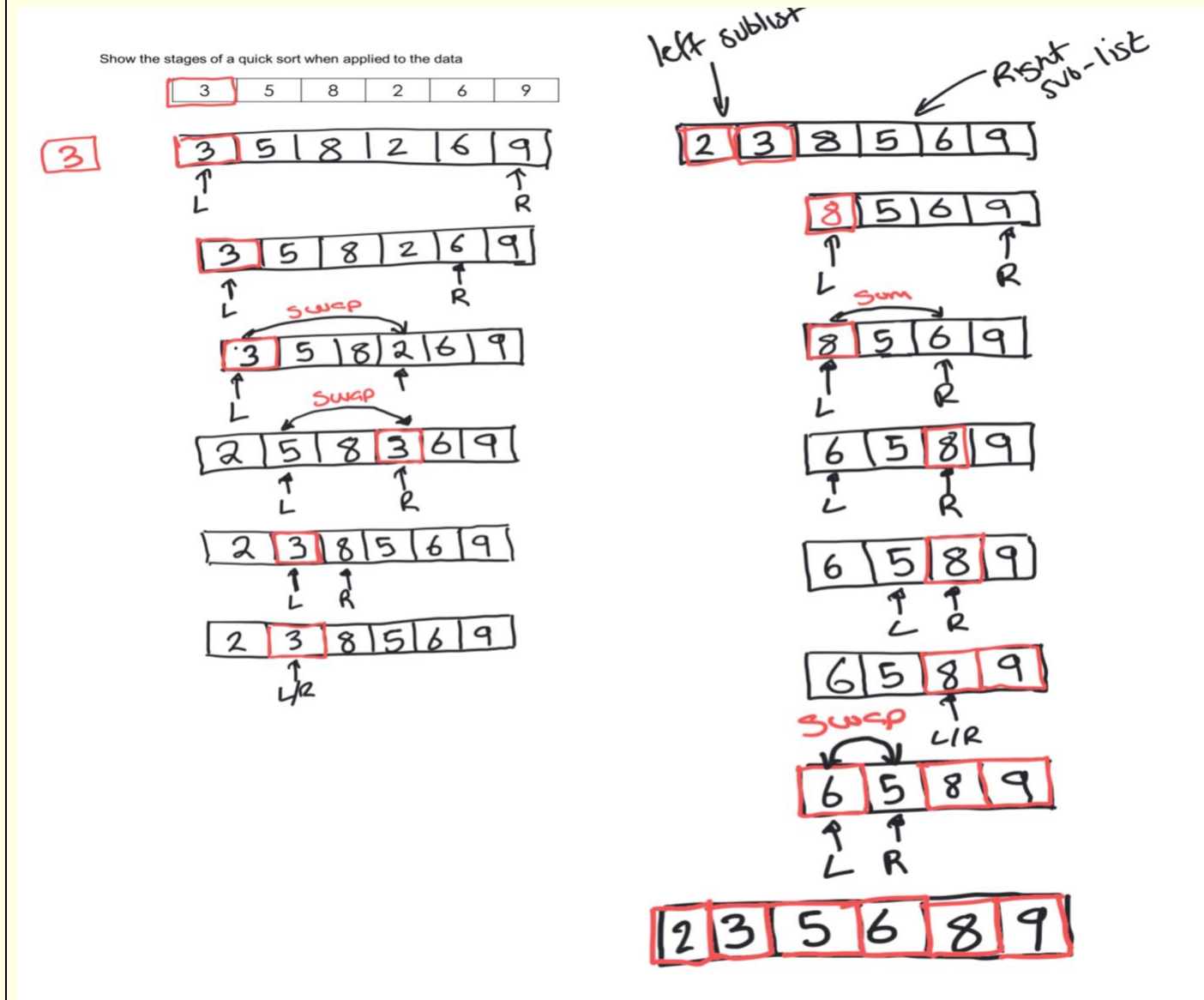
WHILE pos > 0 AND array[pos-1] > currentValue:
array[pos] = array[pos-1]
pos = pos - 1

array[pos] = currentValue

Complexity : $O(n^2)$ Polynomial

Quick Sort

Uses divide-and-conquer



Advantages can be much faster than bubble sort and insertion sort.

Disadvantage: inefficient in terms of memory for very large lists due to recursion (the stack can grow large with all the return addresses, variables etc that have to be stored for each recursive call). Sometimes it can grow too large causing a stack overflow (out of stack memory) error.

Complexity: $O(n \log(n))$ —logarithmic.

Algorithm

- Choose a pivot
- Set a left pointer and right pointer
- If current pointer is the right pointer
 - If right pointer data is less than pivot
 - Swap with right pointer data with left pointer data
 - Move left pointer along by 1
 - Set left pointer as current
 - Otherwise
 - Move right pointer back by one
- If current pointer is the left pointer
 - If leftpointer data is greater than pivot
 - Swap with right pointer data with left pointer data
 - Move right pointer back by 1
 - Set right pointer as current
 - Otherwise
 - Move left pointer along by 1
- Continue until leftpointer == RightPointer
- Slot the pivot data into the leftpointer
- Repeat steps on the left half and the right half of the list till the entire list is sorted.

Mark scheme Example:

- Uses divide-and-conquer (1)
- Highlight first list element as start pointer, and last list element as end pointer
- Repeatedly compare numbers being pointed to...
- ...if incorrect, swap and move end pointer
- ...else move start pointer
- Split list into 2 sublists
- Quick sort each sublist
- Repeat until all sublists have only 1 number
- Combine sublists

Big O notation

What is Big O

Evaluate the complexity of the algorithm

Show how the time / memory / resources increase as the data size increases

Evaluate worst case scenario for the algorithm

Time Complexity - How the time scales as data size increases

Space Complexity – how much memory is required

	Notation	Description	Example code	Example use
	$O(1)$	Constant. An algorithm that always executes in the same time regardless of the size of the data set. Efficient with any data set.	random_num = data_set(x)	Extracting data from any element from an array. Hashing algorithm.
	$O(\log N)$	Logarithmic. Logarithmic time complexities usually apply to algorithms that divide problems in half every time, like any Divide and conquer algorithms. This is for algorithms that halves each time and scales well (meaning increasing the data size will only result in a slight increase in time) Because the algorithm halves each time from a large data it starts off with a really large search time then flattens out over time.	While Found = False And LowerBound <= UpperBound MidPoint = LowerBound + (UpperBound - LowerBound) \ 2 If data_set (MidPoint) = searchedFor Then Found = True Elseif data_set (MidPoint) < searchedFor Then LowerBound = MidPoint + 1 Else UpperBound = MidPoint - 1 End If End While	Binary search.
	$O(N)$	Linear. An algorithm whose performance declines as the data set grows. Reduces efficiency with increasingly large data sets.	For x = 1 To y data_set(x) = counter Next	A loop iterating through a single dimension array. Linear search.
	$O(n \log N)$	Linearithmic: n means the algorithm has to look at every item at least once. log n means it also splits or repeats something fewer times (like dividing into halves each time).		Quick sort. Merge sort.
	$O(N^2)$	Polynomial. An algorithm whose performance is proportional to the square of the size of the data set. Significantly reduces efficiency with increasingly large data sets. Deeper nested iterations result in $O(N^3)$, $O(N^4)$ etc. depending on the number of dimensions.	For x = 1 To w For y = 1 To z data_set(x, y) = 0 Next Next	A nested loop iterating through a two dimension array. Bubble sort.
	$O(2^N)$	Exponential. An algorithm that doubles with each addition to the data set in each pass. Opposite to logarithmic. Inefficient.	Function fib(x) If x <= 1 Then Return x Return fib(x - 2) + fib(x - 1) End Function	Recursive functions with two calls. Fibonacci number calculation with recursion.

Big O notation

Searching algorithms	Time complexity		
	Best	Average	Worst
Linear search	$O(1)$	$O(n)$	$O(n)$
Binary search array	$O(1)$	$O(\log n)$	$O(\log n)$
Binary search tree	$O(1)$	$O(\log n)$	$O(n)$
Hashing	$O(1)$	$O(1)$	$O(n)$
Breadth/Depth first of graph	$O(1)$	$O(V+E)$ No. vertices + No. edges	$O(V^2)$

Sorting algorithms	Time complexity			Space complexity
	Best	Average	Worst	
Bubble sort	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$
Insertion sort	$O(n)$	$O(n^2)$	$O(n^2)$	$O(1)$
Merge sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n)$
Quick sort	$O(n \log n)$	$O(n \log n)$	$O(n^2)$	$O(\log n)$

n	n^2 (Polynomial)	2^n (Exponential)
1	1	2
10	100	1,024
20	400	1,048,576
30	900	1,073,741,824

