# Digital messages

is a digital message as shown in Figure 1.

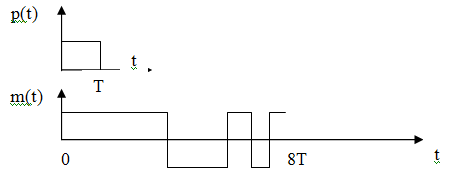


Figure Digital Message

In Figure 1, is chosen to be a so-called square pulse, where we can write . We send one such pulse for each data bit, a positive pulse for logic 1 and a negative pulse for logic 0. In the figure, the message is shown in the interval and the data bits are 11100101.

For the period , and the data is logic 1. For the next period , , and the data is logic 1. In the example figure above, the message is shown in the interval and the information bits are 11100101

We can write where the real constants  depending on whether a logic 1 or a logic 0 was sent.

In the figure above, 

# BPSK Transmitter

A general signal

,

where the complex envelope



and are obtained from the message signal.

Recall that for DSB-SC, we choose and , so that 

For DSB-SC , i.e. the complex envelope is equal to the (real) message.

For binary phase shift keying (BPSK), we also choose and  and we choose



The BPSK signal is written



The signal constellation for BPSK consists of two points located at , one at +1 and one at -1, as shown in Figure 2.



Figure BPSK Constellation

For BPSK, , i.e. the complex envelope is equal to the message.

## Real BPSK signal

To create a real BPSK signal in GRC at intermediate frequency  using these equations, we:

Generate the real baseband signal 

Upconvert it to the desired carrier frequency by multiplying by  to yield

The spectrum of  will be centered at  and has both positive and negative frequency components.

## Complex BPSK signal

To create a complex (analytic) BPSK signal in GRC at intermediate frequency  using these equations, we:

Generate the real baseband signal 

Upconvert it to the desired carrier frequency by multiplying by  . The results is a complex (analytic) signal .



The spectrum of will be centered at . Since the signal is analytic, there is no negative frequency component at .

## BPSK at radio frequency (RF)

The USRP sink block with complex input is used to transmit the BPSK signal near a radio frequency (RF) . The USRP transmitter multiplies  by  and takes the real part to generate a real RF signal centered at .

.

We can get the same result using the exponentials instead of the sine and cosines



The real signal  is centered at . Since the signal is real, there are both positive and negative frequency components.

The USRP sink block could also have used the complex input from section 2.2.

with the imaginary part set to zero to transmit the BPSK signal at  In this case the USRP transmitter multiplies  by  and takes the real part to generate a real RF signal centered at . However, this practice is not recommended, since  may contain DC, and the USRP does not pass DC.

# BPSK Receiver

To receive the BPSK signal, the USRP source block is used to downconvert the RF signal to complex baseband 

We can also simulate the BPSK receiver within GNU Radio without using the USRP source block.

The simulation is done by using the BPSK signal generated at intermediate frequency 

## Real BPSK signal

We first work with the real BPSK signal 

We use a standard IQ receiver set up for with complex output 

If there is no frequency or phase offset, then 

The IQ receiver can be implemented with real cosines and sines and low pass filters.

With a suitable low pass filter, the received data at sampling times  is  (real), where  is adjusted to sample in the middle of the pulse .

 is a timing offset to sample the data away from the transitions between different bits.

## Complex BPSK signal

We can also work with the complex BPSK signal



Again, we use a standard IQ receiver. In this case, we can use the complex IQ receiver that multiplies by (note the minus sign for downconversion).

# QPSK Transmitter

Recall that we can send separate messages on the I and Q channels, i.e. 

We can choose to be separate digital messages with the same kind of waveform as shown in Section 2.1 above. When we use both the I and Q channels, the modulation is called Quadrature Phase Shift Keying (QPSK).

To write an expression for QPSK, we can use the same general form as for BPSK above, except that the constants representing the data are now complex instead of real.

A digital message can be written as a complex envelope



where

 is a complex message waveform, is the digital data, where 

From the expression for , we see that for the period , is a complex constant. For the next period , , etc. In general, for the time period is a fixed amplitude and phase.



and



For QPSK, we choose , so that .

There are 4 possible values of depending on whether a logic 00, 01, 10 or 11 was sent.

The signal constellation for QPSK is shown in Figure 3 and consists of the 4 points located at 



Figure QPSK Constellation

In polar form , so that with , are the 4 possible phases of a QPSK signal.

## Real QPSK signal

To create a real QPSK signal in GRC at intermediate frequency  using these equations, we (1) generate the complex baseband signal  and (2) upconvert it to the desired carrier frequency with a standard IQ transmitter to yield 

The spectrum of  will be centered at  and has both positive and negative frequency components.

## Complex QPSK signal

To create an complex QPSK signal in GRC at intermediate frequency  using these equations, we (1) create the complex baseband signal  and (2) upconvert it to the desired carrier frequency by multiplying by  . The results is another complex signal 

We can create a second QPSK signal at a different intermediate frequency in the same way to yield



We can create a composite signal consisting of several QPSK signals at  etc.

## QPSK at radio frequency (RF)

The upconversion of a QPSK signal to a radio frequency (RF) wave at is the function of the USRP sink block (standard IQ transmitter) with inputs  .The USRP transmitter accepts a complex baseband signal  and multiplies it by  and takes the real part to generate a real RF signal .

The entire group of QPSK signals  can be upconverted to RF by the USRP sink block.

The USRP sink block could also have used the complex input from section 3.1.

to transmit the QPSK signal at  In this case The USRP transmitter multiplies  by  and takes the real part to generate a real RF signal centered at . However, this practice is not recommended, since  may contain DC, and the USRP does not pass DC.

# QPSK Receiver

To receive the QPSK signal, the USRP source block is used to downconvert the RF signal to complex baseband 

We can also simulate the QPSK receiver within GNU Radio without using the USRP source block.

The simulation is done by using the QPSK signal generated at intermediate frequency 

## Real QPSK signal

We first work with the real QPSK signal



We use a standard IQ receiver set up for with complex output 

This IQ receiver can be implemented with real cosines and sines and low pass filters.

With a suitable low pass filter, the received data  at sampling times  is  and the received data is , where  is adjusted to sample in the middle of the pulse 

In the complex domain, the received data at sampling times  is 

## Complex QPSK signal

We can also work with the complex QPSK signal



Again, we use a standard IQ receiver. In this case, we can use the complex IQ receiver that multiplies by (note the minus sign for downconversion). The received data at sampling times  is 

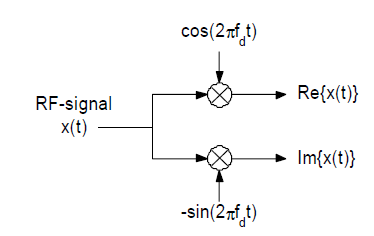
## QPSK signal at radio frequency (RF)

To receive a QPSK signal at RF, we use the USRP source block. The USRP receiver multiplies the real valued radio frequency signal by  to generate . This is called *complex downmixing* and is equivalent to the standard IQ receiver, where in the figure below and is the frequency of the USRP source block.

The USRP source block has a complex output with real and imaginary components ,

Thus the USRP source block with frequency set to  will have outputs

, .



The complex signal output from the USRP source block  is bandlimited to the sampling rate of the USRP source block. The USRP source block output can be recorded to a file and used again at a later time. This file source will have the same sampling rate and bandwidth as the USRP source block used to record it.

With a sampling rate of 200 kHz and complex samples, the bandwidth will be 200 kHz (because the complex signal spectrum is not symmetric and does not have redundant mirror-image positive and negative frequencies)

We can “tune in” (receive) any of the QPSK signals in this bandwidth by shifting the spectrum of the USRP source output. We shift by e.g  Hz by multiplying the USRP source output (complex signal) by , so that the signal that first appeared at Hz now appears at zero Hz. With a suitable low pass filter, the received data at sampling times  is , where  is adjusted to sample in the middle of the pulse 