Implementation Of SGD On Boston Dataset

```
In [1]: import warnings
        from scipy import stats
        warnings.filterwarnings("ignore")
        from sklearn.datasets import load boston
        from random import seed
        from random import randrange
        from csv import reader
        from math import sqrt
        from sklearn import preprocessing
        import pandas as pd
        import numpy as np
        import seaborn as sns
        import matplotlib.pyplot as plt
        from prettytable import PrettyTable
        from sklearn.linear model import SGDRegressor
        from sklearn import preprocessing
        from sklearn.metrics import mean squared error
In [2]: boston=load boston()
In [3]: print(boston.DESCR)
        Boston House Prices dataset
        Notes
        Data Set Characteristics:
            :Number of Instances: 506
            :Number of Attributes: 13 numeric/categorical predictive
            :Median Value (attribute 14) is usually the target
            :Attribute Information (in order):
                - CRIM per capita crime rate by town
                          proportion of residential land zoned for lots over 25,
        000 sq.ft.
                - INDUS proportion of non-retail business acres per town
                - CHAS
                        Charles River dummy variable (= 1 if tract bounds rive
        r; 0 otherwise)
                - NOX
                         nitric oxides concentration (parts per 10 million)
                - RM
                         average number of rooms per dwelling
                          proportion of owner-occupied units built prior to 1940
                - AGE
                - DIS
                          weighted distances to five Boston employment centres
                - RAD
                         index of accessibility to radial highways
                - TAX
                         full-value property-tax rate per $10,000
                - PTRATIO pupil-teacher ratio by town
                - В
                          1000 (Bk - 0.63) ^2 where Bk is the proportion of blacks
        by town
                - LSTAT % lower status of the population
                - MEDV
                         Median value of owner-occupied homes in $1000's
```

```
This is a copy of UCI ML housing dataset.
        http://archive.ics.uci.edu/ml/datasets/Housing
        This dataset was taken from the StatLib library which is maintained at Ca
        rnegie Mellon University.
        The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic
        prices and the demand for clean air', J. Environ. Economics & Management,
        vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnos
        tics
        ...', Wiley, 1980. N.B. Various transformations are used in the table o
        pages 244-261 of the latter.
        The Boston house-price data has been used in many machine learning papers
        that address regression
        problems.
        **References**
           - Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influent
        ial Data and Sources of Collinearity', Wiley, 1980. 244-261.
           - Quinlan, R. (1993). Combining Instance-Based and Model-Based Learnin
        q. In Proceedings on the Tenth International Conference of Machine Learni
        ng, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.
           - many more! (see http://archive.ics.uci.edu/ml/datasets/Housing)
In [4]: X = load boston().data
        Y = load boston().target
In [5]: print(X.shape)
        print(Y.shape)
        (506, 13)
        (506,)
In [6]: print(type(X))
        print(type(Y))
        <class 'numpy.ndarray'>
        <class 'numpy.ndarray'>
In [7]: boston.feature names
Out[7]: array(['CRIM', 'ZN', 'INDUS', 'CHAS', 'NOX', 'RM', 'AGE', 'DIS', 'RAD',
               'TAX', 'PTRATIO', 'B', 'LSTAT'], dtype='<U7')
        CREATING A DATAFRAME :
In [8]: | boston load=pd.DataFrame(X,columns=boston.feature names)
In [9]: y=pd.DataFrame(Y,columns=['Output'])
```

:Missing Attribute Values: None

:Creator: Harrison, D. and Rubinfeld, D.L.

Out[12]:

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE
count	506.000000	506.000000	506.000000	506.000000	506.000000	506.000000	506.000000
mean	3.593761	11.363636	11.136779	0.069170	0.554695	6.284634	68.574901
std	8.596783	23.322453	6.860353	0.253994	0.115878	0.702617	28.148861
min	0.006320	0.000000	0.460000	0.000000	0.385000	3.561000	2.900000
25%	0.082045	0.000000	5.190000	0.000000	0.449000	5.885500	45.025000
50%	0.256510	0.000000	9.690000	0.000000	0.538000	6.208500	77.500000
75%	3.647423	12.500000	18.100000	0.000000	0.624000	6.623500	94.075000
max	88.976200	100.000000	27.740000	1.000000	0.871000	8.780000	100.000000

In [13]: boston_data.head(5)

Out[13]:

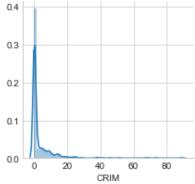
	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LS
0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.9
1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.1
2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.(
3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.9
4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.3

Analysis Of Various Features

CRIM

```
In [14]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"CRIM").add_legend();
    plt.title('PLOTTING PDFS OF CRIM')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```

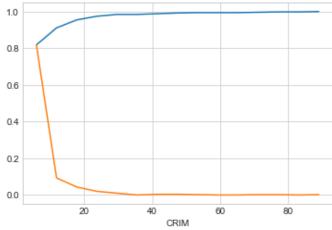


vve observe that the distribution is almost like a Power Law Distribution. So we need to apply boxcox transform to convert it into gaussian distribution

```
counts,binedges=np.histogram(boston data['CRIM'],bins=15,density=True)
In [15]:
         pdf=counts/(sum(counts))
         print(pdf);
         print(binedges)
         cdf=np.cumsum(pdf)
         plt.plot(binedges[1:],cdf)
         plt.plot(binedges[1:],pdf)
         plt.title('PLOTTING PDF & CDF OF CRIM')
         plt.xlabel('CRIM')
         plt.show();
         [0.81818182 0.09288538 0.04347826 0.01976285 0.00988142 0.
          0.00395257 0.00395257 0.00197628 0.
                                                        0.
                                                                   0.00197628
          0.00197628 0.
                                 0.001976281
         [6.32000000e-03 5.93764533e+00 1.18689707e+01 1.78002960e+01
```

2.37316213e+01 2.96629467e+01 3.55942720e+01 4.15255973e+01 4.74569227e+01 5.33882480e+01 5.93195733e+01 6.52508987e+01 7.11822240e+01 7.71135493e+01 8.30448747e+01 8.89762000e+01]

PLOTTING PDF & CDF OF CRIM

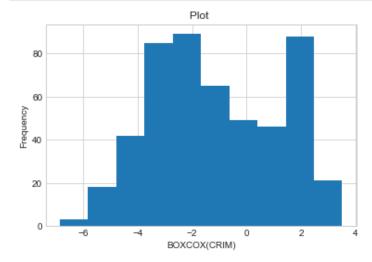


```
In [16]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    crim, _ = stats.boxcox(boston_data["CRIM"])
    prob = stats.probplot(crim, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[16]: Text(0.5,1,'Probplot after Box-Cox transformation')

```
-3 -2 -1 0 1 2 3
Theoretical quantiles
```

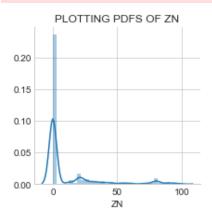
```
In [17]: plt.hist(crim)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(CRIM)")
    plt.ylabel("Frequency")
    plt.show()
```



ZN:

```
In [18]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"ZN").add_legend();
    plt.title('PLOTTING PDFS OF ZN')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



```
In [19]: counts,binedges=np.histogram(boston_data['ZN'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
```

```
cdf=np.cumsum(pdf)
plt.plot(binedges[1:],cdf)
plt.plot(binedges[1:],pdf)
plt.title('PLOTTING PDF & CDF OF ZN')
plt.xlabel('ZN')
plt.show();
[0.73517787 0.01976285 0.00395257 0.08893281 0.0256917 0.01185771
```

```
[0.73517787 0.01976285 0.00395257 0.08893281 0.0256917 0.01185771 0.0256917 0.00592885 0.00592885 0.00790514 0.00592885 0.00592885 0.03754941 0.00988142 0.00988142]
[0. 6.66666667 13.33333333 20. 26.66666667 33.33333333 40. 46.66666667 53.33333333 60. 66.66666667 73.333333333 80. 86.66666667 93.33333333 100. ]
```

PLOTTING PDF & CDF OF ZN 1.0 0.8 0.6 0.4 0.2 0.0 20 40 80 100

Here Data Is negative so box-cox transformation is having error here. So not getting any proper distribution

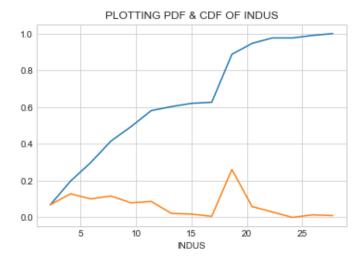
INDUS

```
In [20]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"INDUS").add_legend();
    plt.title('PLOTTING PDFS OF INDUS')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```

```
0.08
0.06
0.04
0.02
0.00
0 10 20 30
```

```
[0.06916996 0.1284585 0.10079051 0.11660079 0.07905138 0.08695652 0.02173913 0.01778656 0.00592885 0.26086957 0.05928854 0.02964427 0. 0.01383399 0.00988142] [0.46 2.27866667 4.09733333 5.916 7.73466667 9.55333333 11.372 13.19066667 15.00933333 16.828 18.64666667 20.46533333 22.284 24.10266667 25.92133333 27.74
```

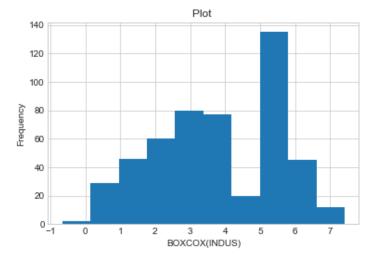


```
In [22]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    indus,_ = stats.boxcox(boston_data["INDUS"])
    prob = stats.probplot(indus, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[22]: Text(0.5,1,'Probplot after Box-Cox transformation')

```
5 -3 -2 -1 0 1 2 3
Theoretical quantiles
```

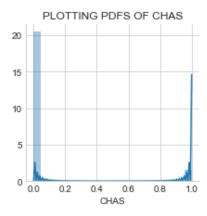
```
In [23]: plt.hist(indus)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(INDUS)")
    plt.ylabel("Frequency")
    plt.show()
```



CHAS

```
In [24]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"CHAS").add_legend();
    plt.title('PLOTTING PDFS OF CHAS')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



```
In [25]: counts,binedges=np.histogram(boston_data['CHAS'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
```

```
cdf=np.cumsum(pdf)
plt.plot(binedges[1:],cdf)
plt.plot(binedges[1:],pdf)
plt.title('PLOTTING PDF & CDF OF CHAS')
plt.xlabel('INDUS')
plt.show();
[0.93083004 0.
                        0.
                                    0.
                                                           0.
                                               0.
                                               0.
0.
            0.
                        0.
                                    0.
                                                           0.
0.
            0.
                        0.06916996]
            0.06666667 0.13333333 0.2
                                               0.26666667 0.333333333
[0.
            0.46666667 0.53333333 0.6
                                               0.66666667 0.73333333
0.4
0.8
            0.86666667 0.93333333 1.
                                              1
            PLOTTING PDF & CDF OF CHAS
1.0
```

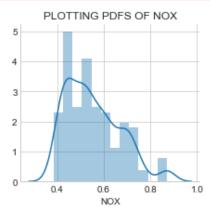
0.8 0.6 0.4 0.2 0.0 0.2 0.4 0.6 0.8 1.0 NDUS

CHAS is a binary categorical feature which has very less 1.0 class features.

NOX

```
In [26]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"NOX").add_legend();
    plt.title('PLOTTING PDFS OF NOX')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



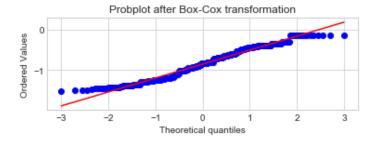
```
pdf=counts/(sum(counts))
print(pdf);
print(binedges)
cdf=np.cumsum(pdf)
plt.plot(binedges[1:],cdf)
plt.plot(binedges[1:],pdf)
plt.title('PLOTTING PDF & CDF OF NOX')
plt.xlabel('INDUS')
plt.show();
```

```
[0.09090909 0.16403162 0.0513834 0.12252964 0.13241107 0.03952569 0.11067194 0.05335968 0.04940711 0.06521739 0.07312253 0.01581028 0. 0. 0.03162055]
[0.385 0.4174 0.4498 0.4822 0.5146 0.547 0.5794 0.6118 0.6442 0.6766 0.709 0.7414 0.7738 0.8062 0.8386 0.871 ]
```

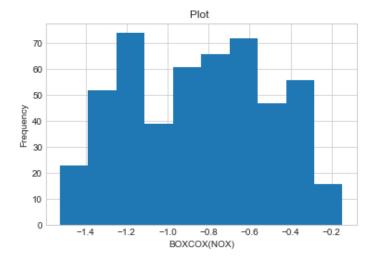


```
In [28]: fig = plt.figure()
   ax2 = fig.add_subplot(212)
   nox,_ = stats.boxcox(boston_data["NOX"])
   prob = stats.probplot(nox, dist=stats.norm, plot=ax2)
   ax2.set_title('Probplot after Box-Cox transformation')
```

Out[28]: Text(0.5,1,'Probplot after Box-Cox transformation')



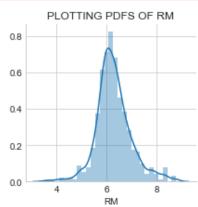
```
In [29]: plt.hist(nox)
   plt.title("Plot ")
   plt.xlabel("BOXCOX(NOX)")
   plt.ylabel("Frequency")
   plt.show()
```



RM

```
In [30]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"RM").add_legend();
    plt.title('PLOTTING PDFS OF RM')
    plt.show();

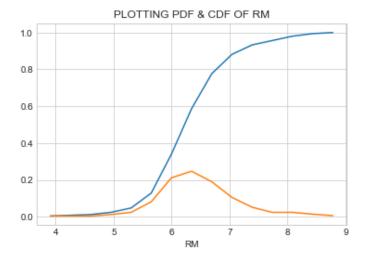
F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



```
In [31]: counts,binedges=np.histogram(boston_data['RM'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF RM')
    plt.xlabel('RM')
    plt.show();
```

```
[0.00395257 0.00395257 0.00395257 0.01185771 0.02371542 0.08102767 0.21146245 0.24703557 0.18972332 0.10474308 0.0513834 0.02371542 0.02371542 0.01383399 0.00592885]
[3.561 3.90893333 4.25686667 4.6048 4.95273333 5.30066667 5.6486 5.99653333 6.34446667 6.6924 7.04033333 7.38826667
```



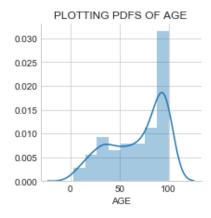


THIS DISTRIBUTION SEEMS TO BE ALMOST GAUSSIAN DISTRIBUTION

AGE

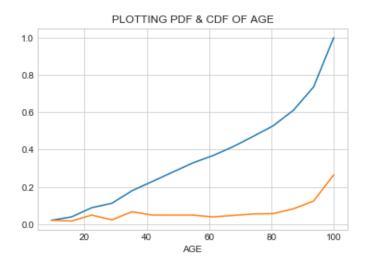
```
In [32]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot, "AGE").add_legend();
    plt.title('PLOTTING PDFS OF AGE')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
    warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



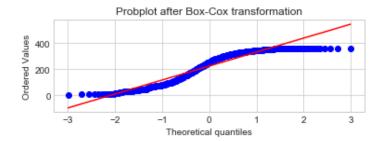
```
In [33]: counts,binedges=np.histogram(boston_data['AGE'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF AGE')
    plt.xlabel('AGE')
    plt.show();
```

[0.02173913 0.01778656 0.04940711 0.02371542 0.06719368 0.04940711 0.04940711 0.04940711 0.03952569 0.04743083 0.05533597 0.05731225

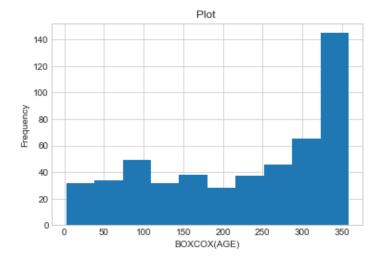


```
In [34]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    age,_ = stats.boxcox(boston_data["AGE"])
    prob = stats.probplot(age, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[34]: Text(0.5,1,'Probplot after Box-Cox transformation')



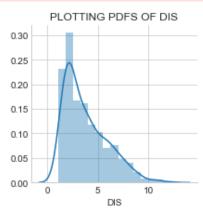
```
In [35]: plt.hist(age)
  plt.title("Plot ")
  plt.xlabel("BOXCOX(AGE)")
  plt.ylabel("Frequency")
  plt.show()
```



DIS

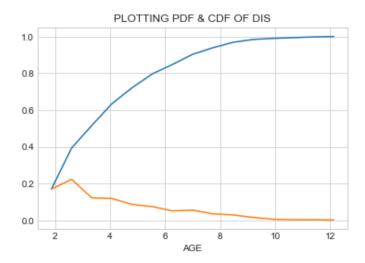
```
In [36]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"DIS").add_legend();
    plt.title('PLOTTING PDFS OF DIS')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



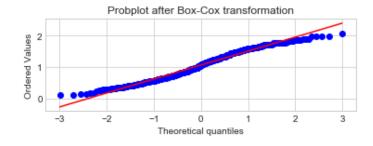
```
In [37]: counts,binedges=np.histogram(boston_data['DIS'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF DIS')
    plt.xlabel('AGE')
    plt.show();
```

```
[0.16996047 0.22332016 0.12252964 0.11857708 0.08695652 0.07509881 0.0513834 0.05533597 0.03557312 0.02964427 0.01581028 0.00592885 0.00395257 0.00197628] [1.1296 1.86272667 2.59585333 3.32898 4.06210667 4.79523333 5.52836 6.26148667 6.99461333 7.72774 8.46086667 9.19399333
```

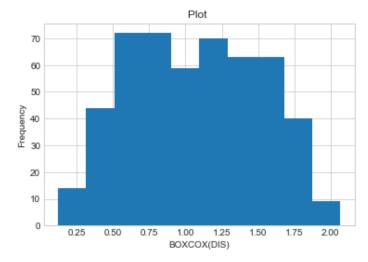


```
In [38]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    dis,_ = stats.boxcox(boston_data["DIS"])
    prob = stats.probplot(dis, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[38]: Text(0.5,1,'Probplot after Box-Cox transformation')



```
In [39]: plt.hist(dis)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(DIS)")
    plt.ylabel("Frequency")
    plt.show()
```

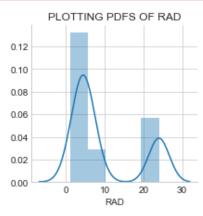


WE APPLY BOX COX TRANSFORM HERE AND SEE ALMOST GETTING LIKE A GAUSSIAN PATTERN

RAD

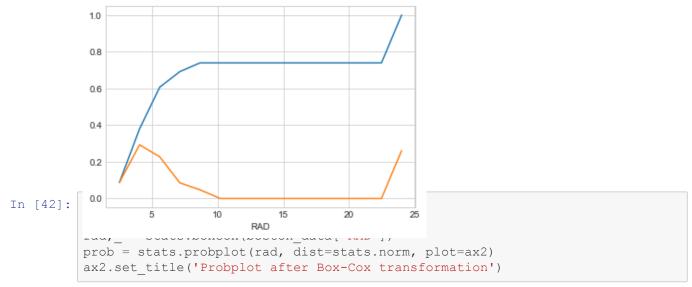
```
In [40]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot, "RAD").add_legend();
    plt.title('PLOTTING PDFS OF RAD')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```

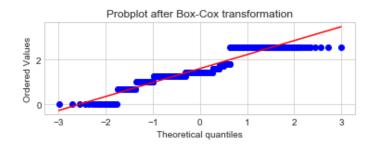


```
In [41]: counts,binedges=np.histogram(boston_data['RAD'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF RAD')
    plt.xlabel('RAD')
    plt.show();
```

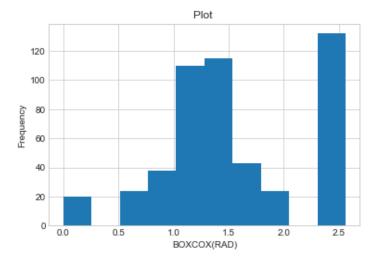
```
[0.08695652 0.29249012 0.22727273 0.08498024 0.04743083 0.
0.
        0.
                                     0. 0.
                   0.
                           0.
0.
          0.
                   0.260869571
          2.53333333 4.06666667 5.6
[ 1.
                                         7.13333333 8.66666667
                                        16.33333333 17.86666667
10.2
          11.73333333 13.26666667 14.8
19.4
          20.93333333 22.46666667 24.
                                       1
```



Out[42]: Text(0.5,1,'Probplot after Box-Cox transformation')



```
In [43]: plt.hist(rad)
   plt.title("Plot ")
   plt.xlabel("BOXCOX(RAD)")
   plt.ylabel("Frequency")
   plt.show()
```



NOT SO USEFUL IN APPLYING BOX-COX TRANSFORM

TAX

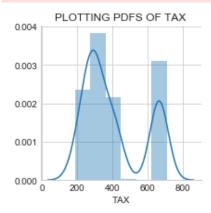
```
In [44]: sns.set_style("whitegrid")
sns.FacetGrid(boston_data).map(sns.distplot,"TAX").add_legend();
```

```
plt.title('PLOTTING PDFS OF TAX')
plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
```

F:\Anaconda3\lib\site-packages\matplotlib\axes_axes.py:6462: UserWarnin g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit y' kwarg.

warnings.warn("The 'normed' kwarg is deprecated, and has been "



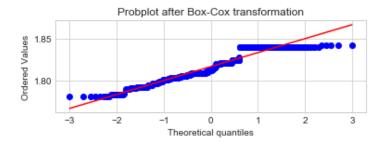
```
In [45]: counts,binedges=np.histogram(boston_data['TAX'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF TAX')
    plt.xlabel('TAX')
    plt.show();
```

PLOTTING PDF & CDF OF TAX 1.0 0.8 0.6 0.4 0.2 0.0 200 300 400 500 600 700

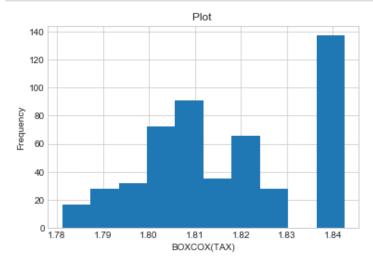
```
In [46]: fig = plt.figure()
ax2 = fig.add_subplot(212)
tax,_ = stats.boxcox(boston_data["TAX"])
```

```
prob = stats.probplot(tax, dist=stats.norm, plot=ax2)
ax2.set_title('Probplot after Box-Cox transformation')
```

Out[46]: Text(0.5,1,'Probplot after Box-Cox transformation')



```
In [47]: plt.hist(tax)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(TAX)")
    plt.ylabel("Frequency")
    plt.show()
```



NOT SO USEFUL IN APPLYING BOX COX TRANSFORM

PTRATIO

```
In [48]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot, "PTRATIO").add_legend();
    plt.title('PLOTTING PDFS OF PTRATIO')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```

```
0.4
0.3
0.2
0.1
0.0 12.5 15.0 17.5 20.0 22.5
PTRATIO
```

```
[0.02964427 0.00197628 0.00197628 0.08300395 0.03754941 0.02371542 0.06126482 0.05928854 0.08498024 0.1027668 0.08498024 0.04150198 0.27667984 0.10671937 0.00395257]
[12.6 13.22666667 13.85333333 14.48 15.10666667 15.73333333 16.36 16.98666667 17.61333333 18.24 18.86666667 19.49333333 20.12 20.74666667 21.373333333 22.
```

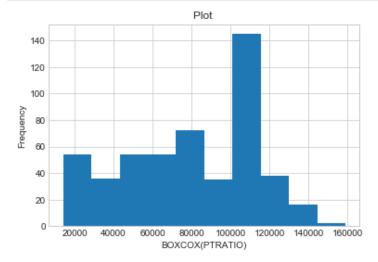
PLOTTING PDF & CDF OF PTRATIO 1.0 0.8 0.6 0.4 0.2 0.0 14 16 18 20 22 PTRATIO

```
In [50]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    ptratio,_ = stats.boxcox(boston_data["PTRATIO"])
    prob = stats.probplot(ptratio, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[50]: Text(0.5,1,'Probplot after Box-Cox transformation')

```
7 100000 0 -3 -2 -1 0 1 2 3 Theoretical quantiles
```

```
In [51]: plt.hist(ptratio)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(PTRATIO)")
    plt.ylabel("Frequency")
    plt.show()
```

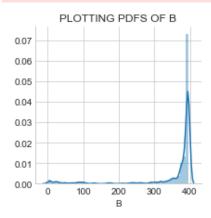


NOT MUCH USEFUL WE CAN CLEARLY SEE RIGHT SKEWED DISTRIBUTION

В

```
In [52]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"B").add_legend();
    plt.title('PLOTTING PDFS OF B')
    plt.show();

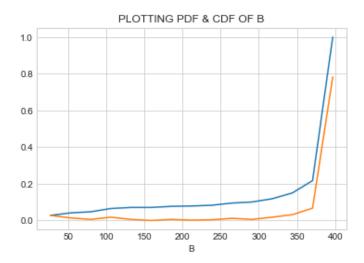
F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```



```
In [53]: counts,binedges=np.histogram(boston_data['B'],bins=15,density=True)
```

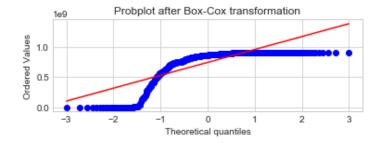
```
pdf=counts/(sum(counts))
print(pdf);
print(binedges)
cdf=np.cumsum(pdf)
plt.plot(binedges[1:],cdf)
plt.plot(binedges[1:],pdf)
plt.title('PLOTTING PDF & CDF OF B')
plt.xlabel('B')
plt.show();
```

```
[0.02766798 0.01383399 0.00592885 0.01778656 0.00592885 0.  
0.00592885 0.00197628 0.00395257 0.01185771 0.00592885 0.01778656  
0.03162055 0.06719368 0.7826087 ]
[3.20000000e-01 2.67586667e+01 5.31973333e+01 7.96360000e+01  
1.06074667e+02 1.32513333e+02 1.58952000e+02 1.85390667e+02  
2.11829333e+02 2.38268000e+02 2.64706667e+02 2.91145333e+02  
3.17584000e+02 3.44022667e+02 3.70461333e+02 3.96900000e+02]
```

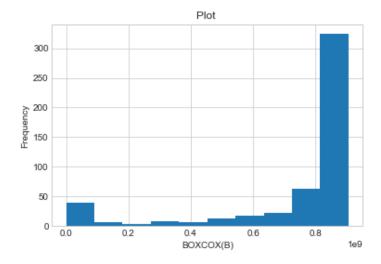


```
In [54]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    b,_ = stats.boxcox(boston_data["B"])
    prob = stats.probplot(b, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[54]: Text(0.5,1,'Probplot after Box-Cox transformation')



```
In [55]: plt.hist(b)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(B)")
    plt.ylabel("Frequency")
    plt.show()
```

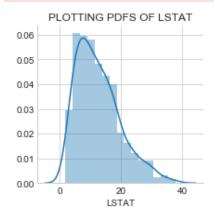


RIGHT SKEWED DISTRIBUTION. SO NOT MUCH USEFUL PERFORMING BOX COX TRANSFORM

LSTAT

```
In [56]: sns.set_style("whitegrid")
    sns.FacetGrid(boston_data).map(sns.distplot,"LSTAT").add_legend();
    plt.title('PLOTTING PDFS OF LSTAT')
    plt.show();

F:\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py:6462: UserWarnin
    g: The 'normed' kwarg is deprecated, and has been replaced by the 'densit
    y' kwarg.
        warnings.warn("The 'normed' kwarg is deprecated, and has been "
```

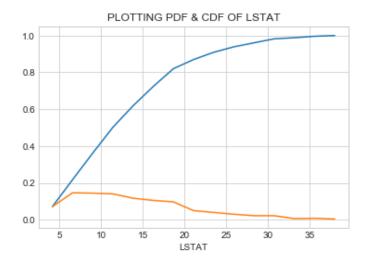


0.00592885 0.00790514 0.00395257]

```
In [57]: counts,binedges=np.histogram(boston_data['LSTAT'],bins=15,density=True)
    pdf=counts/(sum(counts))
    print(pdf);
    print(binedges)
    cdf=np.cumsum(pdf)
    plt.plot(binedges[1:],cdf)
    plt.plot(binedges[1:],pdf)
    plt.title('PLOTTING PDF & CDF OF LSTAT')
    plt.xlabel('LSTAT')
    plt.show();

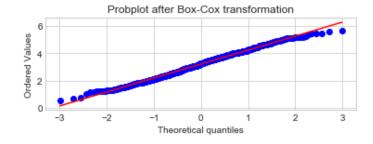
[0.07114625 0.14624506 0.14426877 0.14031621 0.11660079 0.10474308
    0.09683794 0.04940711 0.03952569 0.02964427 0.02173913 0.02173913
```

4.146 6.562 8.978 11.394 13.81 16.226 18.642 21.058 23.474

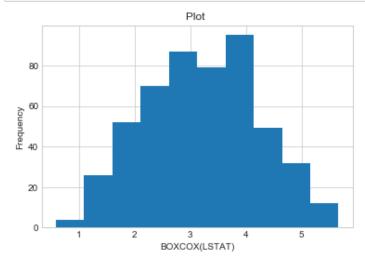


```
In [58]: fig = plt.figure()
    ax2 = fig.add_subplot(212)
    lstat,_ = stats.boxcox(boston_data["LSTAT"])
    prob = stats.probplot(lstat, dist=stats.norm, plot=ax2)
    ax2.set_title('Probplot after Box-Cox transformation')
```

Out[58]: Text(0.5,1,'Probplot after Box-Cox transformation')



```
In [59]: plt.hist(lstat)
    plt.title("Plot ")
    plt.xlabel("BOXCOX(LSTAT)")
    plt.ylabel("Frequency")
    plt.show()
```



TRANSFORMING THE REQUIRED FEATURES: LSTAT, DIS, CRIM:

```
In [60]: boston data['CRIM']=crim
In [61]: boston data['DIS']=dis
In [62]: boston data['LSTAT']=lstat
In [63]: boston data.head()
```

Out[631:

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	E
0	-6.857264	18.0	2.31	0.0	0.538	6.575	65.2	1.264870	1.0	296.0	15.3	396.90
1	-4.453811	0.0	7.07	0.0	0.469	6.421	78.9	1.418585	2.0	242.0	17.8	396.90
2	-4.454917	0.0	7.07	0.0	0.469	7.185	61.1	1.418585	2.0	242.0	17.8	392.83
3	-4.199825	0.0	2.18	0.0	0.458	6.998	45.8	1.571460	3.0	222.0	18.7	394.63
4	-3.125902	0.0	2.18	0.0	0.458	7.147	54.2	1.571460	3.0	222.0	18.7	396.90

STANDARD SCALING OF THE FEATURES:

print(crim test.shape, Y test.shape)

```
In [64]: X=boston data.drop("Output", axis =1)
         Y=boston data["Output"]
In [65]: from sklearn.model selection import train test split
         X train, X test, Y train, Y test = train test split(X, Y, test size = 0.21, random
          state=100)
         X train, X cv, Y train, Y cv = train test split(X train, Y train, test size=0.25,
         random state=100)
         print('Train - Predictors shape', X train.shape)
         print('CV - Predictors shape', X cv.shape)
         print('Test - Predictors shape', X test.shape)
         print('Train - Target shape', Y train.shape)
         print('CV - Target shape', Y cv.shape)
         print('Test - Target shape', Y test.shape)
         Train - Predictors shape (299, 13)
         CV - Predictors shape (100, 13)
         Test - Predictors shape (107, 13)
         Train - Target shape (299,)
         CV - Target shape (100,)
         Test - Target shape (107,)
In [66]: from sklearn.preprocessing import StandardScaler
         crim = StandardScaler()
         crim.fit(X train['CRIM'].values.reshape(-1,1))
         crim train = crim.transform(X train['CRIM'].values.reshape(-1,1))
         crim cv = crim.transform(X cv['CRIM'].values.reshape(-1,1))
         crim test = crim.transform(X test['CRIM'].values.reshape(-1,1))
         print(crim train.shape, Y train.shape)
         print(crim cv.shape, Y_cv.shape)
```

```
zn = StandardScaler()
zn.fit(X train['ZN'].values.reshape(-1,1))
zn train = zn.transform(X train['ZN'].values.reshape(-1,1))
zn cv = zn.transform(X cv['ZN'].values.reshape(-1,1))
zn test = zn.transform(X test['ZN'].values.reshape(-1,1))
print(zn train.shape, Y train.shape)
print(zn cv.shape, Y cv.shape)
print(zn test.shape, Y test.shape)
indus = StandardScaler()
indus.fit(X train['INDUS'].values.reshape(-1,1))
indus train = indus.transform(X train['INDUS'].values.reshape(-1,1))
indus cv = indus.transform(X cv['INDUS'].values.reshape(-1,1))
indus test = indus.transform(X test['INDUS'].values.reshape(-1,1))
print(indus train.shape, Y train.shape)
print(indus cv.shape, Y cv.shape)
print(indus test.shape, Y test.shape)
nox = StandardScaler()
nox.fit(X train['NOX'].values.reshape(-1,1))
nox train = nox.transform(X train['NOX'].values.reshape(-1,1))
nox cv = nox.transform(X cv['NOX'].values.reshape(-1,1))
nox test = nox.transform(X test['NOX'].values.reshape(-1,1))
print(nox train.shape, Y train.shape)
print(nox_cv.shape, Y_cv.shape)
print(nox test.shape, Y test.shape)
rm = StandardScaler()
rm.fit(X train['RM'].values.reshape(-1,1))
rm_train = rm.transform(X train['RM'].values.reshape(-1,1))
rm cv = rm.transform(X cv['RM'].values.reshape(-1,1))
rm test = rm.transform(X test['RM'].values.reshape(-1,1))
print(rm_train.shape, Y_train.shape)
print(rm cv.shape, Y cv.shape)
print(rm test.shape, Y test.shape)
age = StandardScaler()
age.fit(X train['AGE'].values.reshape(-1,1))
age train = age.transform(X train['AGE'].values.reshape(-1,1))
age cv = age.transform(X cv['AGE'].values.reshape(-1,1))
age test = age.transform(X test['AGE'].values.reshape(-1,1))
print(age train.shape, Y train.shape)
print(age cv.shape, Y cv.shape)
print(age test.shape, Y test.shape)
dis = StandardScaler()
dis.fit(X train['DIS'].values.reshape(-1,1))
dis train = dis.transform(X train['DIS'].values.reshape(-1,1))
dis cv = dis.transform(X cv['DIS'].values.reshape(-1,1))
dis test = dis.transform(X test['DIS'].values.reshape(-1,1))
print(dis train.shape, Y train.shape)
print(dis cv.shape, Y cv.shape)
print(dis_test.shape, Y_test.shape)
rad = StandardScaler()
rad.fit(X train['RAD'].values.reshape(-1,1))
rad train = rad.transform(X train['RAD'].values.reshape(-1,1))
rad_cv = rad.transform(X cv['RAD'].values.reshape(-1,1))
rad test = rad.transform(X test['RAD'].values.reshape(-1,1))
print(rad train.shape, Y train.shape)
print(rad cv.shape, Y cv.shape)
print(rad test.shape, Y test.shape)
```

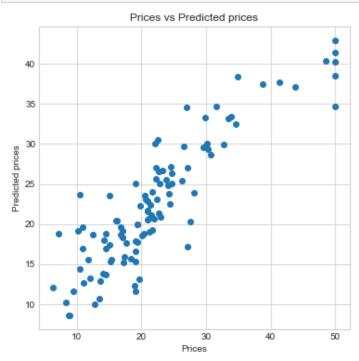
```
tax = StandardScaler()
tax.fit(X train['TAX'].values.reshape(-1,1))
tax train = tax.transform(X train['TAX'].values.reshape(-1,1))
tax cv = tax.transform(X cv['TAX'].values.reshape(-1,1))
tax test = tax.transform(X test['TAX'].values.reshape(-1,1))
print(tax train.shape, Y train.shape)
print(tax cv.shape, Y cv.shape)
print(tax test.shape, Y test.shape)
ptratio = StandardScaler()
ptratio.fit(X train['PTRATIO'].values.reshape(-1,1))
ptratio train = ptratio.transform(X train['PTRATIO'].values.reshape(-1,1))
ptratio cv = ptratio.transform(X cv['PTRATIO'].values.reshape(-1,1))
ptratio test = ptratio.transform(X test['PTRATIO'].values.reshape(-1,1))
print(ptratio train.shape, Y train.shape)
print(ptratio cv.shape, Y cv.shape)
print(ptratio test.shape, Y test.shape)
b = StandardScaler()
b.fit(X train['B'].values.reshape(-1,1))
b train = b.transform(X train['B'].values.reshape(-1,1))
b cv = b.transform(X cv['B'].values.reshape(-1,1))
b test = b.transform(X test['B'].values.reshape(-1,1))
print(b_train.shape, Y_train.shape)
print(b cv.shape, Y cv.shape)
print(b test.shape, Y test.shape)
lstat = StandardScaler()
lstat.fit(X train['LSTAT'].values.reshape(-1,1))
lstat train = lstat.transform(X train['LSTAT'].values.reshape(-1,1))
lstat cv = lstat.transform(X cv['LSTAT'].values.reshape(-1,1))
lstat test = lstat.transform(X test['LSTAT'].values.reshape(-1,1))
print(lstat train.shape, Y train.shape)
print(lstat cv.shape, Y cv.shape)
print(lstat test.shape, Y test.shape)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100, 1) (100,)
(107, 1) (107,)
(299, 1) (299,)
(100 1) (100 )
```

```
(100, 1) (100,)
         (107, 1) (107,)
         (299, 1) (299,)
         (100, 1) (100,)
         (107, 1) (107,)
         (299, 1) (299,)
         (100, 1) (100,)
         (107, 1) (107,)
In [67]: import scipy
         crim train = scipy.sparse.coo matrix(crim train)
         crim cv = scipy.sparse.coo matrix(crim cv)
         crim test = scipy.sparse.coo matrix(crim test)
         zn train = scipy.sparse.coo matrix(zn train)
         zn cv = scipy.sparse.coo matrix(zn cv)
         zn test = scipy.sparse.coo matrix(zn test)
         indus train = scipy.sparse.coo matrix(indus train)
         indus cv = scipy.sparse.coo matrix(indus cv)
         indus test = scipy.sparse.coo matrix(indus test)
         nox train = scipy.sparse.coo matrix(nox train)
         nox cv = scipy.sparse.coo matrix(nox cv)
         nox test = scipy.sparse.coo matrix(nox test)
         rm train = scipy.sparse.coo matrix(rm train)
         rm cv = scipy.sparse.coo matrix(rm cv)
         rm test = scipy.sparse.coo matrix(rm test)
         age train = scipy.sparse.coo matrix(age train)
         age cv = scipy.sparse.coo matrix(age cv)
         age test = scipy.sparse.coo matrix(age test)
         dis train = scipy.sparse.coo matrix(dis train)
         dis cv = scipy.sparse.coo matrix(dis cv)
         dis test = scipy.sparse.coo matrix(dis test)
         rad_train = scipy.sparse.coo_matrix(rad_train)
         rad cv = scipy.sparse.coo matrix(rad cv)
         rad test = scipy.sparse.coo matrix(rad test)
         tax train = scipy.sparse.coo matrix(tax train)
         tax cv = scipy.sparse.coo matrix(tax cv)
         tax test = scipy.sparse.coo matrix(tax test)
         ptratio train = scipy.sparse.coo matrix(ptratio train)
         ptratio cv = scipy.sparse.coo matrix(ptratio cv)
         ptratio test = scipy.sparse.coo matrix(ptratio test)
         b train = scipy.sparse.coo matrix(b train)
         b cv = scipy.sparse.coo matrix(b cv)
         b test = scipy.sparse.coo matrix(b test)
         lstat train = scipy.sparse.coo matrix(lstat train)
         lstat cv = scipy.sparse.coo matrix(lstat cv)
         lstat test = scipy.sparse.coo matrix(lstat test)
In [68]: from scipy.sparse import hstack
         X tr = hstack([crim train,zn train,indus train,nox train,rm train,age train,
         dis_train,rad_train,tax_train,ptratio_train,b_train,lstat_train])
         X cv = hstack([crim cv,zn cv,indus cv,nox cv,rm cv,age cv,dis cv,rad cv,tax
         cv,ptratio cv,b cv,lstat cv])
         X te = hstack([crim test,zn test,indus test,nox test,rm test,age test,dis te
         st,rad test,tax test,ptratio test,b test,lstat test])
         X tr = X tr.todense()
         X cv = X cv.todense()
         X te = X te.todense()
         print("Final Data matrix")
```

(107, 1) (107,) (299, 1) (299,)

```
print(X tr.shape, Y train.shape)
         print(X cv.shape, Y cv.shape)
         print(X te.shape, Y test.shape)
         Final Data matrix
         (299, 12) (299,)
         (100, 12) (100,)
         (107, 12) (107,)
         LINEAR REGRESSION
In [69]: from sklearn.linear model import LinearRegression
         linear = LinearRegression(fit intercept = True ,normalize=False,n jobs = -1)
         linear.fit(X tr, Y train)
         Y pred = linear.predict(X te)
In [70]: linear coeff=linear.coef
In [71]: from prettytable import PrettyTable
         x=PrettyTable()
         x.field_names=["Weights"]
         for i in linear coeff:
             x.add row([round(i,2)])
         print(x)
         +----+
         | Weights |
         +----+
           1.05
         0.49
         | -0.01 |
         | -2.39 |
            1.5
         0.56
         | -3.22 |
           1.76
         | -2.16 |
            -1.7 I
         0.96
         | -5.61 |
         +----+
In [72]: from sklearn.metrics import mean squared error
         mse = mean squared error(Y test, Y pred)
         rmse = np.sqrt(mean squared error(Y test, Y pred))
         R squared= linear.score(X te,Y test)
         print("Mean squared error : ", mse)
         print("Root Mean Squared Error: ", rmse)
         print("Coefficient of Determination: ",R_squared)
         Mean squared error : 21.410761337697338
         Root Mean Squared Error: 4.627176389300211
         Coefficient of Determination: 0.7794783877320747
In [73]: #ploting
         plt.figure(figsize=(6,6))
         sns.set style('whitegrid')
         plt.scatter(Y test, Y pred)
         plt.xlabel("Prices")
```

```
plt.ylabel("Predicted prices")
plt.title("Prices vs Predicted prices")
plt.grid(True)
plt.show()
```



USING SCHOTASTIC GRADIENT DESCENT:

```
In [74]: import tqdm
    from sklearn.linear_model import SGDRegressor
    train_rmse = []
    cv_rmse = []
    alphas = [0.00001, 0.00005, 0.0001, 0.0005, 0.001, 0.005, 0.01,
    0.5, 1, 5, 10]
```

```
In [75]: for i in alphas:
    sgd = SGDRegressor(loss='squared_loss',penalty='ll',alpha=i)
    sgd.fit(X_tr, Y_train)
    Y_predtrain = sgd.predict(X_tr)
    Y_predcv = sgd.predict(X_cv)
    rmsetrain = np.sqrt(mean_squared_error(Y_train, Y_predtrain))
    train_rmse.append(rmsetrain)
    rmsecv = np.sqrt(mean_squared_error(Y_cv, Y_predcv))
    cv_rmse.append(rmsecv)
```

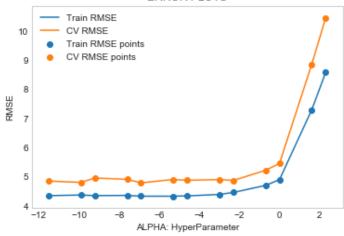
```
In [76]: import numpy
    plt.plot(numpy.log(alphas), train_rmse, label='Train RMSE')
    plt.plot(numpy.log(alphas), cv_rmse, label='CV RMSE')

plt.scatter(numpy.log(alphas), train_rmse, label='Train RMSE points')
    plt.scatter(numpy.log(alphas), cv_rmse, label='CV RMSE points')

plt.legend()
    plt.xlabel("ALPHA: HyperParameter")
    plt.ylabel("RMSE")
    plt.title("ERROR PLOTS")
```

```
plt.grid()
plt.show()
```

ERROR PLOTS



```
In [77]: sgd = SGDRegressor(loss='squared_loss',penalty='l1',alpha=0.0001)
sgd.fit(X_tr, Y_train)
Y_pred= sgd.predict(X_te)
sgd_coeff=sgd.coef_
```

```
In [78]: from prettytable import PrettyTable
    x=PrettyTable()
    x.field_names=["Weights"]
    for i in sgd_coeff:
        x.add_row([round(i,2)])
    print(x)
```

```
+-----+
| Weights |
+------+
| 0.4 |
0.3 |
-0.6 |
-0.62 |
2.41 |
-0.03 |
-2.04 |
0.57 |
-0.62 |
-1.58 |
1.12 |
-4.12 |
+------+
```

```
In [79]: from sklearn.metrics import mean_squared_error
    mse = mean_squared_error(Y_test, Y_pred)
    rmse = np.sqrt(mean_squared_error(Y_test, Y_pred))
    R_squared= sgd.score(X_te,Y_test)
    print("Mean squared error: ",mse)
    print("Root Mean Squared Error: ",rmse)
    print("Coefficient of Determination: ",R_squared)
```

Mean squared error: 23.176867753650995
Root Mean Squared Error: 4.814235947027419
Coefficient of Determination: 0.7612882529610562

```
In [80]: #ploting
   plt.figure(figsize=(6,6))
   sns.set_style('whitegrid')
   plt.scatter(Y_test,Y_pred)
   plt.xlabel("Prices")
   plt.ylabel("Predicted prices")
   plt.title("Prices vs Predicted prices")
   plt.grid(True)
   plt.show()
```



MANUAL SGD:

In [82]: W.shape

```
In [81]:
          W,B,iteration,lr rate,k=np.zeros(shape=(1,12)),0,750,0.01,299 #intialise W a
          nd B to zero
          while iteration>=0:
              w,b,temp vectors,temp intercept=W,B,np.zeros(shape=(1,12)),0
              x=np.array(X tr)
              y=np.array(Y train)
              for i in range(k):
                   temp vectors+=(-2)*x[i]*(y[i]-(np.dot(w,x[i])+b))*partial differenti
          ation wrt w d1/dw=1/k(-2x)*(y-wTx-b)
                   \texttt{temp\_intercept+=(-2)*(y[i]-(np.dot(w,x[i])+b))} \\ \textit{\#partial differentiati}
          on wrt b d1/db=1/k(-2)*(y-wTx-b)
              W=(w-lr rate*(temp vectors)/k)
              B=(b-lr rate*(temp intercept)/k)
              iteration-=1
          print(W)
          print(B)
           [[\ 1.01749806 \quad 0.41132651 \quad -0.27180488 \quad -2.11330295 \quad 1.59508463 \quad 0.48735389 ] 
                          1.22786145 -1.55280306 -1.65623543 0.98137146 -5.5160784
            -3.0880859
          [22.26220163]
```

```
Out[82]: (1, 12)
In [83]: X te.T.shape
Out[83]: (12, 107)
In [84]: | #prediction on x_test
          #https://www.geeksforgeeks.org/numpy-asscalar-in-python/
         y predic lr=[]
         for i in range(len(X te)):
             val=(np.dot(W,X_te[i].T))+B #val=wTx+b
              y predic lr.append(np.asscalar(val))
In [85]: | #Scatter plot of actual price vs predicted price
         plt.scatter(Y test, y predic lr)
         plt.xlabel('Actual price')
         plt.ylabel('Predictd price')
         plt.title('Actual price vs Predicted price')
         plt.show()
                         Actual price vs Predicted price
            40
            35
          Predictd price
            30
            25
            20
            15
            10
                           20
                                    30
                                            40
                                                     50
                               Actual price
In [86]: MSE lr=mean squared error(Y test, y predic lr)
         print('mean squared error =',MSE lr)
         mean squared error = 21.369335685761953
In [87]: from prettytable import PrettyTable
         x = PrettyTable()
         W=np.ravel(W)
         x.field names=['Weight vector manual']
Out[87]: array([ 1.01749806,  0.41132651, -0.27180488, -2.11330295,  1.59508463,
                  0.48735389, -3.0880859, 1.22786145, -1.55280306, -1.65623543,
                  0.98137146, -5.5160784 ])
In [88]: for i in range(len(W)):
             x.add row([W[i]])
         print(x)
         +----+
          | Weight vector manual |
            1.0174980637590862
```

CONCLUSION:

```
In [89]: from prettytable import PrettyTable
#If you get a ModuleNotFoundError error , install prettytable using: pip3 in
stall prettytable
x=PrettyTable()
x.field_names=["Model","Metric","Value"]
x.add_row(["Linear Regression","MSE",21.410761337697338])
x.add_row(["Linear Regression","RMSE",4.627176389300211])
x.add_row(["SGD Regression(SKLEARN)","MSE",22.580122026939538])
x.add_row(["SGD Regression(SKLEARN)","RMSE",4.751854588151824])
x.add_row(["SGD Regression(MANUAL)","MSE",21.369335685761953])
print(x)
```