STAT 200 revised/Linguistics Question Q9

- 1. It is thought that approximately 1 out of every 600 babies will be born with an orofacial cleft (cleft lip or cleft palate; see Little et al. 2004). Suppose a study is done of 10,000 newborns whose mothers who smoked regularly during their pregnancy, and it is found that there are m babies with an orofacial cleft. The researchers believe that smoking during pregnancy may increase the chance of the mother giving birth to a baby with an orofacial cleft.
 - (a) What is a parameter of interest in this study?
 - i. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy.
 - ii. All babies born with an orofacial cleft.
 - iii. The proportion of babies born with an orofacial cleft.
 - iv. Whether a baby is born with an orofacial cleft.
 - v. The number of babies born with an orofacial cleft in the sample.
 - (b) In testing a hypothesis here, what would the null hypothesis be?
 - i. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy equals 1/600.
 - ii. The proportion of the 10,000 babies chosen that are born with an orofacial cleft is phat.
 - iii. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is greater than 1/600.
 - iv. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is equal to phat.
 - v. The proportion of the 10,000 babies chosen that are born with an orofacial cleft does not equal 1/600.
 - (c) What would the alternative hypothesis be?
 - i. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is greater than 1/600.

- ii. The proportion of the 10,000 babies chosen that are born with an orofacial cleft is phat.
- iii. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is less than 1/600.
- iv. The proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is not equal to phat.
- v. The proportion of the 10,000 babies chosen that are born with an orofacial cleft does not equal 1/600.
- (d) Under the null hypothesis, what is the approximate sampling distribution of the sample proportion?

$$\begin{split} &\text{i. } N\left(\mathtt{phat}, \sqrt{1/600 \times 599/600/10,000}\right) \\ &\text{ii. } N\left(\mathtt{phat}, \sqrt{\mathtt{phat}\left(1-\mathtt{phat}\right)/10,000}\right) \\ &\text{iii. } N\left(1/600, \sqrt{1/600 \times 599/600/10,000}\right) \\ &\text{iv. } N\left(1/600, \sqrt{1/600 \times 599/600/\mathtt{m}}\right) \\ &\text{v. } N\left(1/600, \sqrt{\mathtt{phat}\left(1-\mathtt{phat}\right)/10,000}\right) \end{split}$$

- (e) Find the z-score for the sample proportion assuming the null hypothesis is true. Give your answer to four decimal places.
- (f) Use software to compute the P-value for this test. Your answer must be rounded to four decimal places.
- (g) What is an appropriate conclusion for the hypothesis test at the 5% significance level?
 - i. There is no evidence to reject the hypothesis that the proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is less than 1/600.
 - ii. There is evidence to reject the hypothesis that the proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is greater than 1/600.
 - iii. There is reason to believe the proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is greater than 1/600.

iv. There is no evidence to reject the hypothesis that the proportion of babies born with an orofacial cleft whose mothers smoked regularly during their pregnancy is equal to 1/600. Little, Julian, Amanda Cardy, and Ronald G. Munger (2004): Tobacco smoking and oral clefts: A meta-analysis. Bulletin of the World Health Organization 82, 213-218.

The following information is not visible to a student. Randomisation:

```
m <- round(runif(1, min=20, max=28))
phat <- (m/10000)</pre>
```

Attempts: Five attempts should be permitted, with any incorrect parts indicated to students after each attempt.

Solution: Available in WeBWorK

Keywords: sample proportion, hypothesis tests, P-value; identify a parameter of interest for a study, select appropriate null and alternative hypotheses, identify the approximate sampling distribution of the sample proportion, compute the z score for the test, use software to find the P-value for the test, select the appropriate conclusion for the test.

```
## DBsubject('Statistics')
## DBchapter('Hypothesis tests')
## DBsection('One sample proportion')
## Level(3)
```

Below is a screenshot showing how the question appears in WeBWorK's library browser:

