MATH S1202: Calculus IV Quiz 4 June 16, 2016

Define curves in the following way.

- Let D be the region above the line y = x between the circles $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$.
- ullet Let C denote the boundary of D with the positive orientation. (Note that C consists of 4 arcs.)
- Let C_1 denote the piece of C lying along the circle $x^2 + y^2 = 1$.
- 1. Determine whether the vector field is conservative on its domain and if it is conservative, find a potential function.

(a)
$$\vec{F}(x,y) = (x^4, y^4)$$

(b)
$$\vec{G}(x,y) = \frac{1}{x^2+y^2}(-y,x)$$

2. Compute the line integral of the vector field over the curve C_1 .

(a)
$$\vec{F}(x,y) = (x^4, y^4)$$

(b)
$$\vec{G}(x,y) = \frac{1}{x^2+y^2}(-y,x)$$

3. Compute the line integral of the vector field over the closed curve C.

(a)
$$\vec{F}(x,y) = (x^4, y^4)$$

(b)
$$\vec{G}(x,y) = \frac{1}{x^2 + y^2}(-y,x)$$